

Computer algebra independent integration tests

5-Inverse-trig-functions/5.1-Inverse-sine/5.1.2-d-x^m-a+b-arcsin-c-xⁿ

Nasser M. Abbasi

May 23, 2020

Compiled on May 23, 2020 at 9:07am

Contents

1	Introduction	3
1.1	Listing of CAS systems tested	3
1.2	Results	3
1.3	Performance	5
1.4	list of integrals that has no closed form antiderivative	6
1.5	list of integrals solved by CAS but has no known antiderivative	6
1.6	list of integrals solved by CAS but failed verification	6
1.7	Timing	7
1.8	Verification	7
1.9	Important notes about some of the results	7
1.10	Design of the test system	8
2	detailed summary tables of results	11
2.1	List of integrals sorted by grade for each CAS	11
2.2	Detailed conclusion table per each integral for all CAS systems	13
2.3	Detailed conclusion table specific for Rubi results	46
3	Listing of integrals	53
3.1	$\int x^4 \sin^{-1}(ax) dx$	53
3.2	$\int x^3 \sin^{-1}(ax) dx$	56
3.3	$\int x^2 \sin^{-1}(ax) dx$	59
3.4	$\int x \sin^{-1}(ax) dx$	62
3.5	$\int \sin^{-1}(ax) dx$	65
3.6	$\int \frac{\sin^{-1}(ax)}{x} dx$	68
3.7	$\int \frac{\sin^{-1}(ax)}{x^2} dx$	71
3.8	$\int \frac{\sin^{-1}(ax)}{x^3} dx$	74
3.9	$\int \frac{\sin^{-1}(ax)}{x^4} dx$	77
3.10	$\int \frac{\sin^{-1}(ax)}{x^5} dx$	80
3.11	$\int \frac{\sin^{-1}(ax)}{x^6} dx$	83
3.12	$\int x^4 \sin^{-1}(ax)^2 dx$	86
3.13	$\int x^3 \sin^{-1}(ax)^2 dx$	89
3.14	$\int x^2 \sin^{-1}(ax)^2 dx$	92
3.15	$\int x \sin^{-1}(ax)^2 dx$	95

3.16	$\int \sin^{-1}(ax)^2 dx$	98
3.17	$\int \frac{\sin^{-1}(ax)^2}{x} dx$	101
3.18	$\int \frac{\sin^{-1}(ax)^2}{x^2} dx$	104
3.19	$\int \frac{\sin^{-1}(ax)^2}{x^3} dx$	107
3.20	$\int \frac{\sin^{-1}(ax)^2}{x^4} dx$	110
3.21	$\int \frac{\sin^{-1}(ax)^2}{x^5} dx$	114
3.22	$\int x^4 \sin^{-1}(ax)^3 dx$	117
3.23	$\int x^3 \sin^{-1}(ax)^3 dx$	121
3.24	$\int x^2 \sin^{-1}(ax)^3 dx$	125
3.25	$\int x \sin^{-1}(ax)^3 dx$	129
3.26	$\int \sin^{-1}(ax)^3 dx$	132
3.27	$\int \frac{\sin^{-1}(ax)^3}{x} dx$	135
3.28	$\int \frac{\sin^{-1}(ax)^3}{x^2} dx$	139
3.29	$\int \frac{\sin^{-1}(ax)^3}{x^3} dx$	142
3.30	$\int \frac{\sin^{-1}(ax)^3}{x^4} dx$	146
3.31	$\int \frac{\sin^{-1}(ax)^3}{x^5} dx$	150
3.32	$\int x^5 \sin^{-1}(ax)^4 dx$	154
3.33	$\int x^4 \sin^{-1}(ax)^4 dx$	158
3.34	$\int x^3 \sin^{-1}(ax)^4 dx$	162
3.35	$\int x^2 \sin^{-1}(ax)^4 dx$	166
3.36	$\int x \sin^{-1}(ax)^4 dx$	170
3.37	$\int \sin^{-1}(ax)^4 dx$	173
3.38	$\int \frac{\sin^{-1}(ax)^4}{x} dx$	176
3.39	$\int \frac{\sin^{-1}(ax)^4}{x^2} dx$	180
3.40	$\int \frac{\sin^{-1}(ax)^4}{x^3} dx$	184
3.41	$\int \frac{\sin^{-1}(ax)^4}{x^4} dx$	188
3.42	$\int \frac{x^6}{\sin^{-1}(ax)} dx$	193
3.43	$\int \frac{x^5}{\sin^{-1}(ax)} dx$	196
3.44	$\int \frac{x^4}{\sin^{-1}(ax)} dx$	199
3.45	$\int \frac{x^3}{\sin^{-1}(ax)} dx$	202
3.46	$\int \frac{x^2}{\sin^{-1}(ax)} dx$	205
3.47	$\int \frac{x}{\sin^{-1}(ax)} dx$	208
3.48	$\int \frac{1}{\sin^{-1}(ax)} dx$	211
3.49	$\int \frac{1}{x \sin^{-1}(ax)} dx$	214
3.50	$\int \frac{1}{x^2 \sin^{-1}(ax)} dx$	216
3.51	$\int \frac{x^6}{\sin^{-1}(ax)^2} dx$	218
3.52	$\int \frac{x^5}{\sin^{-1}(ax)^2} dx$	221
3.53	$\int \frac{x^4}{\sin^{-1}(ax)^2} dx$	224
3.54	$\int \frac{x^3}{\sin^{-1}(ax)^2} dx$	227
3.55	$\int \frac{x^2}{\sin^{-1}(ax)^2} dx$	230
3.56	$\int \frac{x}{\sin^{-1}(ax)^2} dx$	233

3.57	$\int \frac{1}{\sin^{-1}(ax)^2} dx$	236
3.58	$\int \frac{1}{x \sin^{-1}(ax)^2} dx$	239
3.59	$\int \frac{1}{x^2 \sin^{-1}(ax)^2} dx$	241
3.60	$\int \frac{x^4}{\sin^{-1}(ax)^3} dx$	243
3.61	$\int \frac{x^3}{\sin^{-1}(ax)^3} dx$	247
3.62	$\int \frac{x^2}{\sin^{-1}(ax)^3} dx$	251
3.63	$\int \frac{x}{\sin^{-1}(ax)^3} dx$	255
3.64	$\int \frac{1}{\sin^{-1}(ax)^3} dx$	258
3.65	$\int \frac{1}{x \sin^{-1}(ax)^3} dx$	261
3.66	$\int \frac{1}{x^2 \sin^{-1}(ax)^3} dx$	263
3.67	$\int \frac{x^4}{\sin^{-1}(ax)^4} dx$	265
3.68	$\int \frac{x^3}{\sin^{-1}(ax)^4} dx$	269
3.69	$\int \frac{x^2}{\sin^{-1}(ax)^4} dx$	273
3.70	$\int \frac{x}{\sin^{-1}(ax)^4} dx$	277
3.71	$\int \frac{1}{\sin^{-1}(ax)^4} dx$	280
3.72	$\int \frac{1}{x \sin^{-1}(ax)^4} dx$	283
3.73	$\int \frac{1}{x^2 \sin^{-1}(ax)^4} dx$	285
3.74	$\int x^4 \sqrt{\sin^{-1}(ax)} dx$	287
3.75	$\int x^3 \sqrt{\sin^{-1}(ax)} dx$	291
3.76	$\int x^2 \sqrt{\sin^{-1}(ax)} dx$	294
3.77	$\int x \sqrt{\sin^{-1}(ax)} dx$	297
3.78	$\int \sqrt{\sin^{-1}(ax)} dx$	300
3.79	$\int \frac{\sqrt{\sin^{-1}(ax)}}{x} dx$	303
3.80	$\int x^4 \sin^{-1}(ax)^{3/2} dx$	305
3.81	$\int x^3 \sin^{-1}(ax)^{3/2} dx$	310
3.82	$\int x^2 \sin^{-1}(ax)^{3/2} dx$	314
3.83	$\int x \sin^{-1}(ax)^{3/2} dx$	318
3.84	$\int \sin^{-1}(ax)^{3/2} dx$	322
3.85	$\int \frac{\sin^{-1}(ax)^{3/2}}{x} dx$	325
3.86	$\int x^4 \sin^{-1}(ax)^{5/2} dx$	327
3.87	$\int x^3 \sin^{-1}(ax)^{5/2} dx$	332
3.88	$\int x^2 \sin^{-1}(ax)^{5/2} dx$	336
3.89	$\int x \sin^{-1}(ax)^{5/2} dx$	341
3.90	$\int \sin^{-1}(ax)^{5/2} dx$	345
3.91	$\int \frac{\sin^{-1}(ax)^{5/2}}{x} dx$	348
3.92	$\int \frac{x^4}{\sqrt{\sin^{-1}(ax)}} dx$	350
3.93	$\int \frac{x^3}{\sqrt{\sin^{-1}(ax)}} dx$	353
3.94	$\int \frac{x^2}{\sqrt{\sin^{-1}(ax)}} dx$	356
3.95	$\int \frac{x}{\sqrt{\sin^{-1}(ax)}} dx$	359

3.96	$\int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx$	362
3.97	$\int \frac{1}{x\sqrt{\sin^{-1}(ax)}} dx$	365
3.98	$\int \frac{1}{x^2\sqrt{\sin^{-1}(ax)}} dx$	367
3.99	$\int \frac{x^6}{\sin^{-1}(ax)^{3/2}} dx$	369
3.100	$\int \frac{x^5}{\sin^{-1}(ax)^{3/2}} dx$	372
3.101	$\int \frac{x^4}{\sin^{-1}(ax)^{3/2}} dx$	375
3.102	$\int \frac{x^3}{\sin^{-1}(ax)^{3/2}} dx$	378
3.103	$\int \frac{x^2}{\sin^{-1}(ax)^{3/2}} dx$	381
3.104	$\int \frac{x}{\sin^{-1}(ax)^{3/2}} dx$	384
3.105	$\int \frac{1}{\sin^{-1}(ax)^{3/2}} dx$	387
3.106	$\int \frac{1}{x\sin^{-1}(ax)^{3/2}} dx$	390
3.107	$\int \frac{x^4}{\sin^{-1}(ax)^{5/2}} dx$	392
3.108	$\int \frac{x^3}{\sin^{-1}(ax)^{5/2}} dx$	396
3.109	$\int \frac{x^2}{\sin^{-1}(ax)^{5/2}} dx$	400
3.110	$\int \frac{x}{\sin^{-1}(ax)^{5/2}} dx$	404
3.111	$\int \frac{1}{\sin^{-1}(ax)^{5/2}} dx$	408
3.112	$\int \frac{1}{x\sin^{-1}(ax)^{5/2}} dx$	411
3.113	$\int \frac{x^4}{\sin^{-1}(ax)^{7/2}} dx$	413
3.114	$\int \frac{x^3}{\sin^{-1}(ax)^{7/2}} dx$	417
3.115	$\int \frac{x^2}{\sin^{-1}(ax)^{7/2}} dx$	421
3.116	$\int \frac{x}{\sin^{-1}(ax)^{7/2}} dx$	425
3.117	$\int \frac{1}{\sin^{-1}(ax)^{7/2}} dx$	429
3.118	$\int \frac{1}{x\sin^{-1}(ax)^{7/2}} dx$	432
3.119	$\int (bx)^m \sin^{-1}(ax)^4 dx$	434
3.120	$\int (bx)^m \sin^{-1}(ax)^3 dx$	436
3.121	$\int (bx)^m \sin^{-1}(ax)^2 dx$	438
3.122	$\int (bx)^m \sin^{-1}(ax) dx$	441
3.123	$\int \frac{(bx)^m}{\sin^{-1}(ax)} dx$	444
3.124	$\int \frac{(bx)^m}{\sin^{-1}(ax)^2} dx$	446
3.125	$\int (bx)^m \sin^{-1}(ax)^{3/2} dx$	448
3.126	$\int (bx)^m \sqrt{\sin^{-1}(ax)} dx$	450
3.127	$\int \frac{(bx)^m}{\sqrt{\sin^{-1}(ax)}} dx$	452
3.128	$\int \frac{(bx)^m}{\sin^{-1}(ax)^{3/2}} dx$	454
3.129	$\int (bx)^m \sin^{-1}(ax)^n dx$	456
3.130	$\int x^3 \sin^{-1}(ax)^n dx$	458
3.131	$\int x^2 \sin^{-1}(ax)^n dx$	461
3.132	$\int x \sin^{-1}(ax)^n dx$	464
3.133	$\int \sin^{-1}(ax)^n dx$	467
3.134	$\int \frac{\sin^{-1}(ax)^n}{x} dx$	470
3.135	$\int \frac{\sin^{-1}(ax)^n}{x^2} dx$	472

3.136	$\int (bx)^{3/2} \sin^{-1}(ax)^n dx$	474
3.137	$\int \sqrt{bx} \sin^{-1}(ax)^n dx$	476
3.138	$\int \frac{\sin^{-1}(ax)^n}{\sqrt{bx}} dx$	478
3.139	$\int \frac{\sin^{-1}(ax)^n}{(bx)^{3/2}} dx$	480
3.140	$\int x^3 (a + b \sin^{-1}(cx)) dx$	482
3.141	$\int x^2 (a + b \sin^{-1}(cx)) dx$	485
3.142	$\int x (a + b \sin^{-1}(cx)) dx$	488
3.143	$\int (a + b \sin^{-1}(cx)) dx$	491
3.144	$\int \frac{a+b \sin^{-1}(cx)}{x} dx$	494
3.145	$\int \frac{a+b \sin^{-1}(cx)}{x^2} dx$	497
3.146	$\int \frac{a+b \sin^{-1}(cx)}{x^3} dx$	500
3.147	$\int \frac{a+b \sin^{-1}(cx)}{x^4} dx$	503
3.148	$\int x^2 (a + b \sin^{-1}(cx))^2 dx$	506
3.149	$\int x (a + b \sin^{-1}(cx))^2 dx$	509
3.150	$\int (a + b \sin^{-1}(cx))^2 dx$	512
3.151	$\int \frac{(a+b \sin^{-1}(cx))^2}{x} dx$	515
3.152	$\int \frac{(a+b \sin^{-1}(cx))^2}{x^2} dx$	519
3.153	$\int x^2 (a + b \sin^{-1}(cx))^3 dx$	522
3.154	$\int x (a + b \sin^{-1}(cx))^3 dx$	526
3.155	$\int (a + b \sin^{-1}(cx))^3 dx$	530
3.156	$\int \frac{(a+b \sin^{-1}(cx))^3}{x} dx$	533
3.157	$\int \frac{(a+b \sin^{-1}(cx))^3}{x^2} dx$	537
3.158	$\int \frac{x^2}{a+b \sin^{-1}(cx)} dx$	541
3.159	$\int \frac{x}{a+b \sin^{-1}(cx)} dx$	544
3.160	$\int \frac{1}{a+b \sin^{-1}(cx)} dx$	547
3.161	$\int \frac{1}{x(a+b \sin^{-1}(cx))} dx$	550
3.162	$\int \frac{1}{x^2(a+b \sin^{-1}(cx))} dx$	552
3.163	$\int \frac{x^2}{(a+b \sin^{-1}(cx))^2} dx$	554
3.164	$\int \frac{x}{(a+b \sin^{-1}(cx))^2} dx$	557
3.165	$\int \frac{1}{(a+b \sin^{-1}(cx))^2} dx$	560
3.166	$\int \frac{1}{x(a+b \sin^{-1}(cx))^2} dx$	563
3.167	$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^2} dx$	565
3.168	$\int \frac{x^2}{(a+b \sin^{-1}(cx))^3} dx$	567
3.169	$\int \frac{x}{(a+b \sin^{-1}(cx))^3} dx$	572
3.170	$\int \frac{1}{(a+b \sin^{-1}(cx))^3} dx$	577
3.171	$\int \frac{1}{x(a+b \sin^{-1}(cx))^3} dx$	581
3.172	$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^3} dx$	584

3.173	$\int x^2 \sqrt{a + b \sin^{-1}(cx)} dx$	587
3.174	$\int x \sqrt{a + b \sin^{-1}(cx)} dx$	591
3.175	$\int \sqrt{a + b \sin^{-1}(cx)} dx$	595
3.176	$\int \frac{\sqrt{a + b \sin^{-1}(cx)}}{x} dx$	599
3.177	$\int \frac{\sqrt{a + b \sin^{-1}(cx)}}{x^2} dx$	601
3.178	$\int x^2 (a + b \sin^{-1}(cx))^{3/2} dx$	603
3.179	$\int x (a + b \sin^{-1}(cx))^{3/2} dx$	608
3.180	$\int (a + b \sin^{-1}(cx))^{3/2} dx$	613
3.181	$\int \frac{(a + b \sin^{-1}(cx))^{3/2}}{x} dx$	617
3.182	$\int \frac{(a + b \sin^{-1}(cx))^{3/2}}{x^2} dx$	619
3.183	$\int x^2 (a + b \sin^{-1}(cx))^{5/2} dx$	621
3.184	$\int x (a + b \sin^{-1}(cx))^{5/2} dx$	627
3.185	$\int (a + b \sin^{-1}(cx))^{5/2} dx$	632
3.186	$\int \frac{(a + b \sin^{-1}(cx))^{5/2}}{x} dx$	637
3.187	$\int \frac{(a + b \sin^{-1}(cx))^{5/2}}{x^2} dx$	639
3.188	$\int \frac{x^2}{\sqrt{a + b \sin^{-1}(cx)}} dx$	641
3.189	$\int \frac{x}{\sqrt{a + b \sin^{-1}(cx)}} dx$	645
3.190	$\int \frac{1}{\sqrt{a + b \sin^{-1}(cx)}} dx$	649
3.191	$\int \frac{1}{x \sqrt{a + b \sin^{-1}(cx)}} dx$	652
3.192	$\int \frac{1}{x^2 \sqrt{a + b \sin^{-1}(cx)}} dx$	654
3.193	$\int \frac{x^2}{(a + b \sin^{-1}(cx))^{3/2}} dx$	656
3.194	$\int \frac{x}{(a + b \sin^{-1}(cx))^{3/2}} dx$	660
3.195	$\int \frac{1}{(a + b \sin^{-1}(cx))^{3/2}} dx$	664
3.196	$\int \frac{1}{x (a + b \sin^{-1}(cx))^{3/2}} dx$	668
3.197	$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{3/2}} dx$	670
3.198	$\int \frac{x^2}{(a + b \sin^{-1}(cx))^{5/2}} dx$	672
3.199	$\int \frac{x}{(a + b \sin^{-1}(cx))^{5/2}} dx$	677
3.200	$\int \frac{1}{(a + b \sin^{-1}(cx))^{5/2}} dx$	682
3.201	$\int \frac{1}{x (a + b \sin^{-1}(cx))^{5/2}} dx$	686
3.202	$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{5/2}} dx$	688
3.203	$\int (dx)^{5/2} (a + b \sin^{-1}(cx)) dx$	690
3.204	$\int (dx)^{3/2} (a + b \sin^{-1}(cx)) dx$	693
3.205	$\int \sqrt{dx} (a + b \sin^{-1}(cx)) dx$	697
3.206	$\int \frac{a + b \sin^{-1}(cx)}{\sqrt{dx}} dx$	700
3.207	$\int \frac{a + b \sin^{-1}(cx)}{(dx)^{3/2}} dx$	703

3.208	$\int \frac{a+b \sin^{-1}(cx)}{(dx)^{5/2}} dx$	706
3.209	$\int (dx)^{5/2} (a + b \sin^{-1}(cx))^2 dx$	710
3.210	$\int (dx)^{3/2} (a + b \sin^{-1}(cx))^2 dx$	713
3.211	$\int \sqrt{dx} (a + b \sin^{-1}(cx))^2 dx$	716
3.212	$\int \frac{(a+b \sin^{-1}(cx))^2}{\sqrt{dx}} dx$	719
3.213	$\int \frac{(a+b \sin^{-1}(cx))^2}{(dx)^{3/2}} dx$	722
3.214	$\int \frac{(a+b \sin^{-1}(cx))^2}{(dx)^{5/2}} dx$	725
3.215	$\int (dx)^{3/2} (a + b \sin^{-1}(cx))^3 dx$	728
3.216	$\int \sqrt{dx} (a + b \sin^{-1}(cx))^3 dx$	730
3.217	$\int \frac{(a+b \sin^{-1}(cx))^3}{\sqrt{dx}} dx$	732
3.218	$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{3/2}} dx$	734
3.219	$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{5/2}} dx$	736
3.220	$\int \frac{(dx)^{3/2}}{a+b \sin^{-1}(cx)} dx$	738
3.221	$\int \frac{\sqrt{dx}}{a+b \sin^{-1}(cx)} dx$	740
3.222	$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))} dx$	742
3.223	$\int \frac{1}{(dx)^{3/2}(a+b \sin^{-1}(cx))} dx$	744
3.224	$\int \frac{(dx)^{3/2}}{(a+b \sin^{-1}(cx))^2} dx$	746
3.225	$\int \frac{\sqrt{dx}}{(a+b \sin^{-1}(cx))^2} dx$	748
3.226	$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))^2} dx$	750
3.227	$\int \frac{1}{(dx)^{3/2}(a+b \sin^{-1}(cx))^2} dx$	752

4 Listing of Grading functions

755

Chapter 1

Introduction

This report gives the result of running the computer algebra independent integration problems. The listing of the problems are maintained by and can be downloaded from <https://rulebasedintegration.org>

The number of integrals in this report is [227]. This is test number [142].

1.1 Listing of CAS systems tested

The following systems were tested at this time.

1. Mathematica 12.1 (64 bit) on windows 10.
2. Rubi 4.16.1 in Mathematica 12 on windows 10.
3. Maple 2020 (64 bit) on windows 10.
4. Maxima 5.43 on Linux. (via sagemath 8.9)
5. Fricas 1.3.6 on Linux (via sagemath 9.0)
6. Sympy 1.5 under Python 3.7.3 using Anaconda distribution.
7. Giac/Xcas 1.5 on Linux. (via sagemath 8.9)

Maxima, Fricas and Giac/Xcas were called from inside SageMath. This was done using SageMath integrate command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly using Python.

1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or Hypergeometric2F1 functions. RootSum and RootOf are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	solved	Failed
Rubi	% 100. (227)	% 0. (0)
Mathematica	% 99.56 (226)	% 0.44 (1)
Maple	% 95.59 (217)	% 4.41 (10)
Maxima	% 27.75 (63)	% 72.25 (164)
Fricas	% 34.8 (79)	% 65.2 (148)
Sympy	% 40.09 (91)	% 59.91 (136)
Giac	% 74.01 (168)	% 25.99 (59)

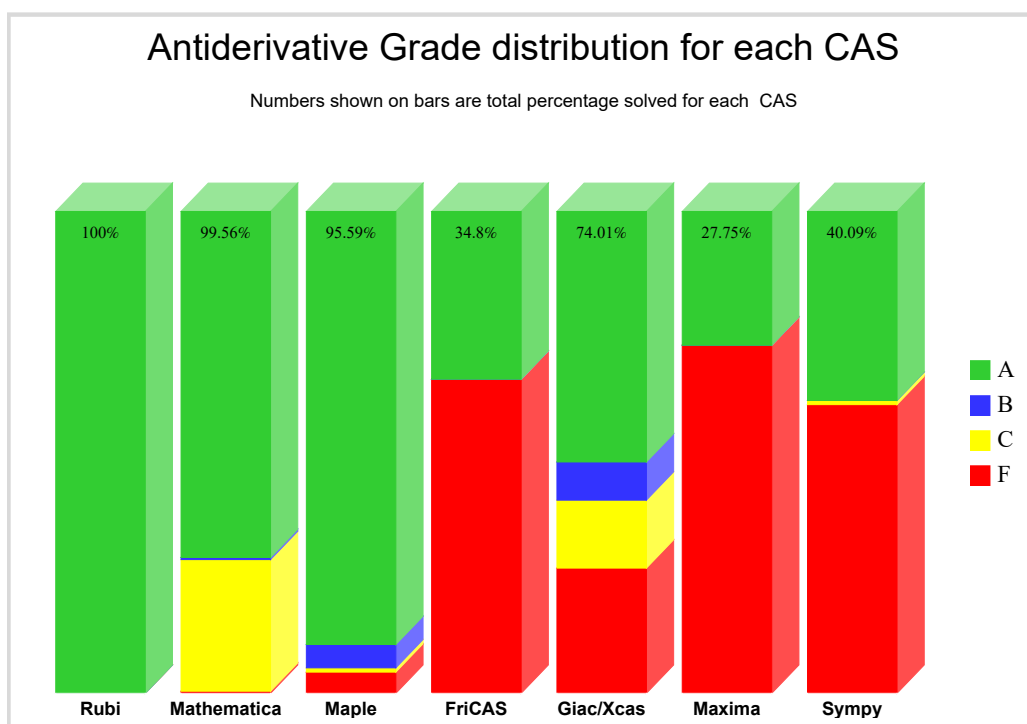
The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> 1. antiderivative contains a hypergeometric function and the optimal antiderivative does not. 2. antiderivative contains a special function and the optimal antiderivative does not. 3. antiderivative contains the imaginary unit and the optimal antiderivative does not.
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

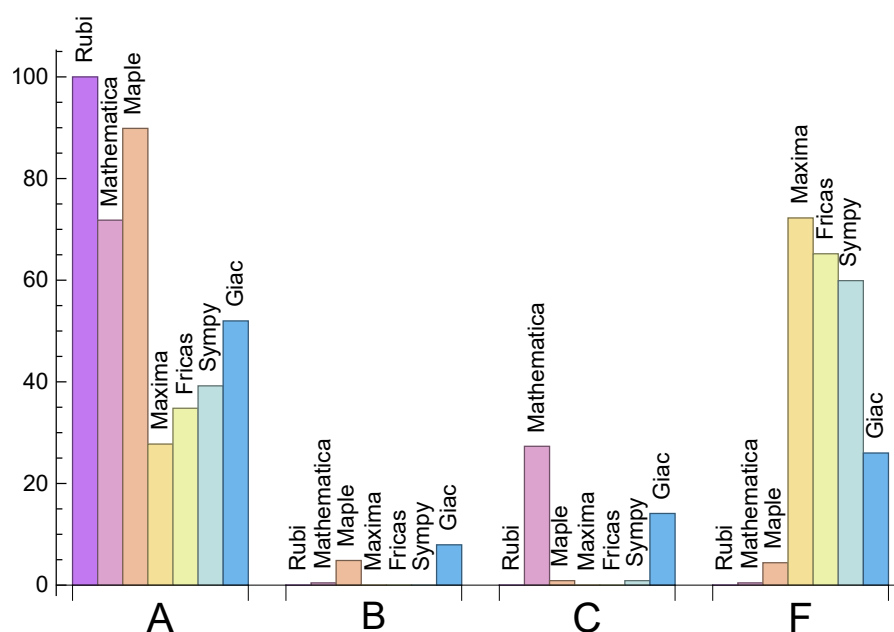
Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

System	% A grade	% B grade	% C grade	% F grade
Rubi	100.	0.	0.	0.
Mathematica	71.81	0.44	27.31	0.44
Maple	89.87	4.85	0.88	4.41
Maxima	27.75	0.	0.	72.25
Fricas	34.8	0.	0.	65.2
Sympy	39.21	0.	0.88	59.91
Giac	51.98	7.93	14.1	25.99

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



1.3 Performance

The table below summarizes the performance of each CAS system in terms of CPU time and leaf size of results.

System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.16	81.81	0.73	75.	1.
Mathematica	1.6	86.96	0.78	69.5	0.83
Maple	0.08	98.41	0.85	67.	0.89
Maxima	0.85	56.56	0.73	32.	1.12
Fricas	1.06	91.96	1.13	66.	1.36
Sympy	4.06	49.03	0.54	0.	0.
Giac	0.96	195.97	1.62	88.5	1.42

1.4 list of integrals that has no closed form antiderivative

{49, 50, 58, 59, 65, 66, 72, 73, 79, 85, 91, 97, 98, 106, 112, 118, 119, 120, 123, 124, 125, 126, 127, 128, 129, 134, 135, 136, 137, 138, 139, 161, 162, 166, 167, 171, 172, 176, 177, 181, 182, 186, 187, 191, 192, 196, 197, 201, 202, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227}

1.5 list of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

Rubi {}

Mathematica {17, 18, 20, 27, 28, 30, 38, 39, 40, 41, 74, 75, 76, 77, 78, 80, 81, 82, 83, 84, 86, 87, 88, 89, 90, 92, 93, 94, 95, 96, 99, 100, 101, 102, 103, 104, 105, 107, 108, 109, 110, 111, 113, 114, 115, 116, 117, 144, 151, 152, 156, 157, 173, 174, 175, 178, 179, 180, 183, 184, 185, 188, 189, 190, 193, 194, 195, 198, 199, 200}

Maple Verification phase not implemented yet.

Maxima Verification phase not implemented yet.

Fricas Verification phase not implemented yet.

Sympy Verification phase not implemented yet.

Giac Verification phase not implemented yet.

1.7 Timing

The command `AboluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of _int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call has completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out is not counted in the final statistics.

1.8 Verification

A verification phase was applied on the result of integration for Rubi and Mathematica. Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative produced was correct.

Verification phase has 3 minutes time out. An integral whose result was not verified could still be correct. Further investigation is needed on those integrals which failed verifications. Such integrals are marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

1.9 Important notes about some of the results

1.9.1 Important note about Maxima results

Since these integrals are run in a batch mode, using an automated script, and by using `sagemath` (SageMath uses Maxima), then any integral where Maxima needs an interactive response from the user to answer a question during evaluation of the integral in order to complete the integration, will fail and is counted as failed.

The exception raised is `ValueError`. Therefore Maxima result below is lower than what could result if Maxima was run directly and each question Maxima asks was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the Timofeev test file, there were about 30 such integrals out of total 705, or about 4 percent. This pecentage can be higher or lower depending on the specific input test file.

Such integrals can be indentified by looking at the output of the integration in each section for Maxima. If the output was an exception `ValueError` then this is most likely due to this reason.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath loading of Maxima `abs_integrate` was found to cause some problem. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

1.9.2 Important note about FriCAS and Giac/X-CAS results

There are Few integrals which failed due to SageMath not able to translate the result back to SageMath syntax and not because these CAS system were not able to do the integrations.

These will fail With error Exception raised: NotImplementedError

The number of such cases seems to be very small. About 1 or 2 percent of all integrals.

Hopefully the next version of SageMath will have complete translation of FriCAS and XCAS syntax and I will re-run all the tests again when this happens.

1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi and Maple, the builtin system function LeafSize is used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special builtin function for this purpose at this time. Therefore the leaf size is determined as follows.

For Fricas, Giac and Maxima (all called via sagemath) the following code is used

#see <https://stackoverflow.com/questions/25202346/how-to-obtain-leaf-count-expression-size-in->

```
def tree(expr):
    if expr.operator() is None:
        return expr
    else:
        return [expr.operator()+map(tree, expr.operands())
```

```
try:
    # 1.35 is a fudge factor since this estimate of leaf count is bit lower than
    #what it should be compared to Mathematica's
    leafCount = round(1.35*len(flatten(tree(anti))))
except Exception as ee:
    leafCount =1
```

For Sympy, called directly from Python, the following code is used

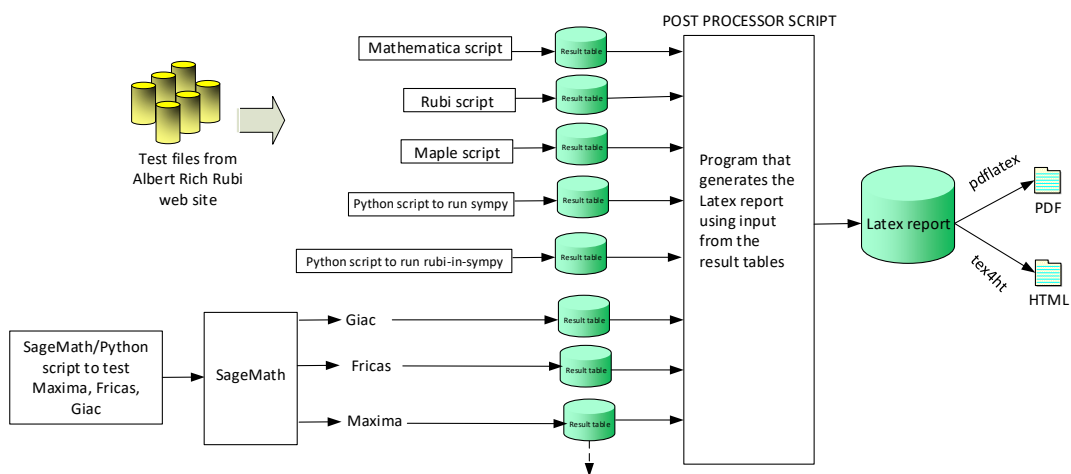
```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount =1
```

When these cas systems have a builtin function to find the leaf size of expressions, it will be used instead, and these tests run again.

1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



One record (line) per one integral result. The line is CSV comma separated. It contains 13 fields. This is description of each record (line)

1. integer, the problem number.
2. integer. 0 or 1 for failed or passed. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntax.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"
13. String. The optimal antiderivative in CAS own syntax.

High level overview of the CAS independent integration test build system

Naser M. Abbasi
June 22, 2018

Chapter 2

detailed summary tables of results

2.1 List of integrals sorted by grade for each CAS

2.1.1 Rubi

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227 }

B grade: { }

C grade: { }

F grade: { }

2.1.2 Mathematica

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 79, 85, 91, 97, 98, 106, 112, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 176, 177, 181, 182, 186, 187, 191, 192, 196, 197, 201, 202, 209, 210, 211, 212, 213, 214, 215, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227 }

B grade: { 157 }

C grade: { 11, 74, 75, 76, 77, 78, 80, 81, 82, 83, 84, 86, 87, 88, 89, 90, 92, 93, 94, 95, 96, 99, 100, 101, 102, 103, 104, 105, 107, 108, 109, 110, 111, 113, 114, 115, 116, 117, 173, 174, 175, 178, 179, 180, 183, 184, 185, 188, 189, 190, 193, 194, 195, 198, 199, 200, 203, 204, 205, 206, 207, 208 }

F grade: { 216 }

2.1.3 Maple

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81,

82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 123, 124, 125, 126, 127, 128, 129, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 152, 153, 154, 155, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 179, 181, 182, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 201, 202, 203, 204, 205, 206, 207, 208, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227 }

B grade: { 151, 156, 157, 178, 180, 183, 184, 185, 198, 199, 200 }

C grade: { 132, 133 }

F grade: { 121, 122, 130, 131, 209, 210, 211, 212, 213, 214 }

2.1.4 Maxima

A grade: { 1, 2, 3, 4, 5, 7, 8, 9, 10, 11, 12, 14, 16, 19, 21, 22, 24, 26, 33, 35, 37, 49, 50, 65, 66, 72, 73, 123, 140, 141, 142, 143, 145, 146, 147, 148, 150, 153, 155, 161, 162, 171, 172, 176, 177, 181, 182, 186, 187, 191, 192, 196, 197, 201, 202, 220, 221, 222, 223, 224, 225, 226, 227 }

B grade: { }

C grade: { }

F grade: { 6, 13, 15, 17, 18, 20, 23, 25, 27, 28, 29, 30, 31, 32, 34, 36, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 67, 68, 69, 70, 71, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 144, 149, 151, 152, 154, 156, 157, 158, 159, 160, 163, 164, 165, 166, 167, 168, 169, 170, 173, 174, 175, 178, 179, 180, 183, 184, 185, 188, 189, 190, 193, 194, 195, 198, 199, 200, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219 }

2.1.5 FriCAS

A grade: { 1, 2, 3, 4, 5, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 19, 21, 22, 23, 24, 25, 26, 32, 33, 34, 35, 36, 37, 49, 50, 58, 59, 65, 66, 72, 73, 119, 120, 123, 124, 129, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 145, 146, 147, 148, 149, 150, 153, 154, 155, 161, 162, 166, 167, 171, 172, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227 }

B grade: { }

C grade: { }

F grade: { 6, 17, 18, 20, 27, 28, 29, 30, 31, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 51, 52, 53, 54, 55, 56, 57, 60, 61, 62, 63, 64, 67, 68, 69, 70, 71, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 121, 122, 125, 126, 127, 128, 130, 131, 132, 133, 144, 151, 152, 156, 157, 158, 159, 160, 163, 164, 165, 168, 169, 170, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214 }

2.1.6 Sympy

A grade: { 1, 2, 3, 4, 5, 9, 10, 11, 12, 13, 14, 15, 16, 22, 23, 24, 25, 26, 32, 33, 34, 35, 36, 37, 49, 50, 58, 59, 65, 66, 72, 73, 79, 85, 97, 98, 106, 112, 119, 120, 123, 124, 126, 127, 128, 129, 134, 135, 137, 138, 140, 141, 142, 143, 145, 146, 147, 148, 149, 150, 153, 154, 155, 161, 162, 166, 167, 171, 172, 176, 177, 181, 182, 191, 192, 196, 197, 201, 204, 205, 216, 220, 221, 222, 223, 224, 225, 226, 227 }

B grade: { }

C grade: { 7, 8 }

F grade: { 6, 17, 18, 19, 20, 21, 27, 28, 29, 30, 31, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 51, 52, 53, 54, 55, 56, 57, 60, 61, 62, 63, 64, 67, 68, 69, 70, 71, 74, 75, 76, 77, 78, 80, 81, 82, 83, 84, 86, 87,

88, 89, 90, 91, 92, 93, 94, 95, 96, 99, 100, 101, 102, 103, 104, 105, 107, 108, 109, 110, 111, 113, 114, 115, 116, 117, 118, 121, 122, 125, 130, 131, 132, 133, 136, 139, 144, 151, 152, 156, 157, 158, 159, 160, 163, 164, 165, 168, 169, 170, 173, 174, 175, 178, 179, 180, 183, 184, 185, 186, 187, 188, 189, 190, 193, 194, 195, 198, 199, 200, 202, 203, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 217, 218, 219 }

2.1.7 Giac

A grade: { 1, 2, 3, 4, 5, 7, 9, 11, 12, 13, 14, 15, 16, 22, 23, 24, 25, 26, 32, 33, 34, 35, 36, 37, 42, 43, 44, 45, 46, 47, 48, 49, 50, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 79, 85, 91, 97, 98, 106, 112, 118, 119, 120, 123, 124, 125, 126, 127, 128, 129, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 150, 155, 158, 159, 160, 161, 162, 166, 167, 171, 172, 176, 177, 181, 182, 186, 187, 191, 192, 196, 197, 201, 202, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227 }

B grade: { 8, 10, 19, 21, 51, 145, 146, 147, 148, 149, 153, 154, 163, 164, 165, 168, 169, 170 }

C grade: { 74, 75, 76, 77, 78, 80, 81, 82, 83, 84, 86, 87, 88, 89, 90, 92, 93, 94, 95, 96, 173, 174, 175, 178, 179, 180, 183, 184, 185, 188, 189, 190 }

F grade: { 6, 17, 18, 20, 27, 28, 29, 30, 31, 38, 39, 40, 41, 99, 100, 101, 102, 103, 104, 105, 107, 108, 109, 110, 111, 113, 114, 115, 116, 117, 121, 122, 130, 131, 132, 133, 144, 151, 152, 156, 157, 193, 194, 195, 198, 199, 200, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214 }

2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table, the column **normalized size** is defined as $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$

Problem 1	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	75	75	51	72	96	113	70	153
normalized size	1	1.	0.68	0.96	1.28	1.51	0.93	2.04
time (sec)	N/A	0.049	0.032	0.032	1.686	2.134	7.083	1.222

Problem 2	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	69	69	50	60	99	109	61	113
normalized size	1	1.	0.72	0.87	1.43	1.58	0.88	1.64
time (sec)	N/A	0.029	0.019	0.004	1.727	2.026	1.645	1.448

Problem 3	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	54	54	41	52	68	92	48	86
normalized size	1	1.	0.76	0.96	1.26	1.7	0.89	1.59
time (sec)	N/A	0.035	0.025	0.003	1.709	2.138	0.82	1.303

Problem 4	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	45	45	40	40	70	86	37	62
normalized size	1	1.	0.89	0.89	1.56	1.91	0.82	1.38
time (sec)	N/A	0.016	0.011	0.004	1.671	2.2	0.346	1.239

Problem 5	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	25	25	25	25	32	57	20	32
normalized size	1	1.	1.	1.	1.28	2.28	0.8	1.28
time (sec)	N/A	0.008	0.008	0.001	1.689	2.106	0.619	1.331

Problem 6	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	51	51	46	111	0	0	0	0
normalized size	1	1.	0.9	2.18	0.	0.	0.	0.
time (sec)	N/A	0.058	0.028	0.158	0.	0.	0.	0.

Problem 7	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	C	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	28	28	28	31	53	124	32	65
normalized size	1	1.	1.	1.11	1.89	4.43	1.14	2.32
time (sec)	N/A	0.022	0.002	0.003	1.624	2.235	4.859	1.475

Problem 8	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	C	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	34	34	29	38	38	66	51	92
normalized size	1	1.	0.85	1.12	1.12	1.94	1.5	2.71
time (sec)	N/A	0.014	0.007	0.003	1.658	2.191	2.114	1.282

Problem 9	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	56	56	53	53	81	176	109	95
normalized size	1	1.	0.95	0.95	1.45	3.14	1.95	1.7
time (sec)	N/A	0.033	0.014	0.003	1.731	2.743	7.035	1.315

Problem 10	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	58	58	41	58	68	89	100	176
normalized size	1	1.	0.71	1.	1.17	1.53	1.72	3.03
time (sec)	N/A	0.022	0.019	0.003	1.656	2.535	3.911	1.354

Problem 11	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	80	80	51	73	111	204	182	120
normalized size	1	1.	0.64	0.91	1.39	2.55	2.28	1.5
time (sec)	N/A	0.045	0.013	0.004	1.764	2.794	24.051	1.302

Problem 12	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	120	120	82	76	138	189	114	228
normalized size	1	1.	0.68	0.63	1.15	1.58	0.95	1.9
time (sec)	N/A	0.194	0.034	0.126	1.67	2.428	7.614	1.344

Problem 13	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	98	98	74	93	0	162	90	180
normalized size	1	1.	0.76	0.95	0.	1.65	0.92	1.84
time (sec)	N/A	0.163	0.029	0.063	0.	2.402	4.84	1.229

Problem 14	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	82	82	64	59	97	143	76	131
normalized size	1	1.	0.78	0.72	1.18	1.74	0.93	1.6
time (sec)	N/A	0.121	0.028	0.059	1.735	2.415	2.594	1.312

Problem 15	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	60	60	55	65	0	123	51	99
normalized size	1	1.	0.92	1.08	0.	2.05	0.85	1.65
time (sec)	N/A	0.093	0.017	0.025	0.	2.339	0.77	1.215

Problem 16	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	35	35	35	37	45	89	32	45
normalized size	1	1.	1.	1.06	1.29	2.54	0.91	1.29
time (sec)	N/A	0.045	0.011	0.021	1.821	2.352	0.239	1.348

Problem 17	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	71	71	71	169	0	0	0	0
normalized size	1	1.	1.	2.38	0.	0.	0.	0.
time (sec)	N/A	0.095	0.04	0.042	0.	0.	0.	0.

Problem 18	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	66	66	87	119	0	0	0	0
normalized size	1	1.	1.32	1.8	0.	0.	0.	0.
time (sec)	N/A	0.103	0.162	0.092	0.	0.	0.	0.

Problem 19	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	44	44	44	43	54	112	0	116
normalized size	1	1.	1.	0.98	1.23	2.55	0.	2.64
time (sec)	N/A	0.08	0.025	0.026	1.628	2.568	0.	1.382

Problem 20	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	116	116	139	157	0	0	0	0
normalized size	1	1.	1.2	1.35	0.	0.	0.	0.
time (sec)	N/A	0.17	0.615	0.196	0.	0.	0.	0.

Problem 21	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	87	87	69	76	100	149	0	223
normalized size	1	1.	0.79	0.87	1.15	1.71	0.	2.56
time (sec)	N/A	0.14	0.038	0.032	1.613	2.309	0.	1.457

Problem 22	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	201	201	122	159	231	265	196	336
normalized size	1	1.	0.61	0.79	1.15	1.32	0.98	1.67
time (sec)	N/A	0.385	0.07	0.059	1.692	2.2	13.62	1.386

Problem 23	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	167	167	112	154	0	234	160	250
normalized size	1	1.	0.67	0.92	0.	1.4	0.96	1.5
time (sec)	N/A	0.297	0.048	0.06	0.	2.05	6.943	1.302

Problem 24	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	136	136	95	106	162	189	128	192
normalized size	1	1.	0.7	0.78	1.19	1.39	0.94	1.41
time (sec)	N/A	0.225	0.045	0.045	1.726	2.169	5.895	1.3

Problem 25	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	99	99	82	96	0	170	92	136
normalized size	1	1.	0.83	0.97	0.	1.72	0.93	1.37
time (sec)	N/A	0.156	0.025	0.041	0.	2.035	1.609	1.305

Problem 26	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	60	60	60	57	77	116	54	76
normalized size	1	1.	1.	0.95	1.28	1.93	0.9	1.27
time (sec)	N/A	0.08	0.011	0.024	1.681	2.047	0.832	1.36

Problem 27	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	97	97	97	229	0	0	0	0
normalized size	1	1.	1.	2.36	0.	0.	0.	0.
time (sec)	N/A	0.109	0.056	0.046	0.	0.	0.	0.

Problem 28	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	108	108	133	179	0	0	0	0
normalized size	1	1.	1.23	1.66	0.	0.	0.	0.
time (sec)	N/A	0.163	0.124	0.074	0.	0.	0.	0.

Problem 29	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	102	102	92	163	0	0	0	0
normalized size	1	1.	0.9	1.6	0.	0.	0.	0.
time (sec)	N/A	0.169	0.253	0.098	0.	0.	0.	0.

Problem 30	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	179	179	284	250	0	0	0	0
normalized size	1	1.	1.59	1.4	0.	0.	0.	0.
time (sec)	N/A	0.285	2.795	0.148	0.	0.	0.	0.

Problem 31	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	169	169	116	225	0	0	0	0
normalized size	1	1.	0.69	1.33	0.	0.	0.	0.
time (sec)	N/A	0.292	0.679	0.156	0.	0.	0.	0.

Problem 32	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	282	282	167	320	0	383	269	489
normalized size	1	1.	0.59	1.13	0.	1.36	0.95	1.73
time (sec)	N/A	0.869	0.098	0.1	0.	2.22	33.002	1.375

Problem 33	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	250	250	150	197	279	352	241	412
normalized size	1	1.	0.6	0.79	1.12	1.41	0.96	1.65
time (sec)	N/A	0.663	0.075	0.059	1.853	2.149	18.648	1.29

Problem 34	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	198	198	135	209	0	292	190	316
normalized size	1	1.	0.68	1.06	0.	1.47	0.96	1.6
time (sec)	N/A	0.516	0.059	0.059	0.	2.209	15.126	1.414

Problem 35	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	166	166	114	130	198	247	158	238
normalized size	1	1.	0.69	0.78	1.19	1.49	0.95	1.43
time (sec)	N/A	0.353	0.048	0.048	1.687	2.01	5.592	1.404

Problem 36	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	111	111	96	117	0	205	104	171
normalized size	1	1.	0.86	1.05	0.	1.85	0.94	1.54
time (sec)	N/A	0.238	0.029	0.039	0.	2.211	3.343	1.404

Problem 37	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	69	69	69	67	101	149	65	88
normalized size	1	1.	1.	0.97	1.46	2.16	0.94	1.28
time (sec)	N/A	0.118	0.016	0.026	1.768	1.926	1.988	1.39

Problem 38	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	113	113	113	287	0	0	0	0
normalized size	1	1.	1.	2.54	0.	0.	0.	0.
time (sec)	N/A	0.122	0.044	0.046	0.	0.	0.	0.

Problem 39	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	156	156	198	241	0	0	0	0
normalized size	1	1.	1.27	1.54	0.	0.	0.	0.
time (sec)	N/A	0.194	0.267	0.077	0.	0.	0.	0.

Problem 40	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	119	119	124	227	0	0	0	0
normalized size	1	1.	1.04	1.91	0.	0.	0.	0.
time (sec)	N/A	0.216	0.283	0.091	0.	0.	0.	0.

Problem 41	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	276	276	399	409	0	0	0	0
normalized size	1	1.	1.45	1.48	0.	0.	0.	0.
time (sec)	N/A	0.41	4.27	0.145	0.	0.	0.	0.

Problem 42	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	55	55	40	40	0	0	0	63
normalized size	1	1.	0.73	0.73	0.	0.	0.	1.15
time (sec)	N/A	0.097	0.016	0.039	0.	0.	0.	1.318

Problem 43	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	43	43	33	33	0	0	0	50
normalized size	1	1.	0.77	0.77	0.	0.	0.	1.16
time (sec)	N/A	0.08	0.115	0.031	0.	0.	0.	1.275

Problem 44	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	41	41	31	31	0	0	0	47
normalized size	1	1.	0.76	0.76	0.	0.	0.	1.15
time (sec)	N/A	0.081	0.009	0.023	0.	0.	0.	1.352

Problem 45	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	29	29	24	24	0	0	0	34
normalized size	1	1.	0.83	0.83	0.	0.	0.	1.17
time (sec)	N/A	0.062	0.079	0.022	0.	0.	0.	1.339

Problem 46	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	27	27	22	22	0	0	0	31
normalized size	1	1.	0.81	0.81	0.	0.	0.	1.15
time (sec)	N/A	0.063	0.006	0.021	0.	0.	0.	1.371

Problem 47	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	14	14	14	13	0	0	0	16
normalized size	1	1.	1.	0.93	0.	0.	0.	1.14
time (sec)	N/A	0.035	0.023	0.025	0.	0.	0.	1.346

Problem 48	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	9	9	9	10	0	0	0	12
normalized size	1	1.	1.	1.11	0.	0.	0.	1.33
time (sec)	N/A	0.017	0.009	0.017	0.	0.	0.	1.356

Problem 49	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	0.191	0.09	0.	0.	0.	0.

Problem 50	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.014	1.098	0.123	0.	0.	0.	0.

Problem 51	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	83	83	86	105	0	0	0	217
normalized size	1	1.	1.04	1.27	0.	0.	0.	2.61
time (sec)	N/A	0.074	0.244	0.042	0.	0.	0.	1.287

Problem 52	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	71	71	78	78	0	0	0	162
normalized size	1	1.	1.1	1.1	0.	0.	0.	2.28
time (sec)	N/A	0.063	0.045	0.033	0.	0.	0.	1.311

Problem 53	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	69	69	61	81	0	0	0	155
normalized size	1	1.	0.88	1.17	0.	0.	0.	2.25
time (sec)	N/A	0.058	0.209	0.026	0.	0.	0.	1.305

Problem 54	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	57	57	56	54	0	0	0	97
normalized size	1	1.	0.98	0.95	0.	0.	0.	1.7
time (sec)	N/A	0.049	0.017	0.021	0.	0.	0.	1.385

Problem 55	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	55	55	50	57	0	0	0	92
normalized size	1	1.	0.91	1.04	0.	0.	0.	1.67
time (sec)	N/A	0.044	0.165	0.023	0.	0.	0.	1.36

Problem 56	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	38	38	32	28	0	0	0	49
normalized size	1	1.	0.84	0.74	0.	0.	0.	1.29
time (sec)	N/A	0.025	0.003	0.024	0.	0.	0.	1.374

Problem 57	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	36	36	32	33	0	0	0	46
normalized size	1	1.	0.89	0.92	0.	0.	0.	1.28
time (sec)	N/A	0.078	0.059	0.019	0.	0.	0.	1.33

Problem 58	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-1)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.012	0.904	0.078	0.	0.	0.	0.

Problem 59	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-1)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.014	9.711	0.141	0.	0.	0.	0.

Problem 60	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	98	98	103	121	0	0	0	230
normalized size	1	1.	1.05	1.23	0.	0.	0.	2.35
time (sec)	N/A	0.343	0.185	0.042	0.	0.	0.	1.328

Problem 61	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	83	83	73	82	0	0	0	169
normalized size	1	1.	0.88	0.99	0.	0.	0.	2.04
time (sec)	N/A	0.3	0.187	0.034	0.	0.	0.	1.362

Problem 62	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	82	82	68	82	0	0	0	138
normalized size	1	1.	0.83	1.	0.	0.	0.	1.68
time (sec)	N/A	0.249	0.136	0.026	0.	0.	0.	1.371

Problem 63	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	64	64	61	45	0	0	0	90
normalized size	1	1.	0.95	0.7	0.	0.	0.	1.41
time (sec)	N/A	0.168	0.06	0.026	0.	0.	0.	1.418

Problem 64	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	51	51	48	43	0	0	0	58
normalized size	1	1.	0.94	0.84	0.	0.	0.	1.14
time (sec)	N/A	0.085	0.022	0.021	0.	0.	0.	1.339

Problem 65	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.012	0.541	0.078	0.	0.	0.	0.

Problem 66	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	6.431	0.122	0.	0.	0.	0.

Problem 67	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	158	158	159	171	0	0	0	338
normalized size	1	1.	1.01	1.08	0.	0.	0.	2.14
time (sec)	N/A	0.314	0.338	0.04	0.	0.	0.	1.271

Problem 68	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	144	144	107	114	0	0	0	235
normalized size	1	1.	0.74	0.79	0.	0.	0.	1.63
time (sec)	N/A	0.282	0.36	0.03	0.	0.	0.	1.377

Problem 69	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	141	141	102	117	0	0	0	200
normalized size	1	1.	0.72	0.83	0.	0.	0.	1.42
time (sec)	N/A	0.303	0.259	0.028	0.	0.	0.	1.329

Problem 70	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	97	97	86	60	0	0	0	124
normalized size	1	1.	0.89	0.62	0.	0.	0.	1.28
time (sec)	N/A	0.164	0.138	0.027	0.	0.	0.	1.257

Problem 71	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	78	78	70	63	0	0	0	89
normalized size	1	1.	0.9	0.81	0.	0.	0.	1.14
time (sec)	N/A	0.153	0.062	0.023	0.	0.	0.	1.245

Problem 72	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.012	2.34	0.075	0.	0.	0.	0.

Problem 73	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.014	17.869	0.118	0.	0.	0.	0.

Problem 74	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	121	121	204	143	0	0	0	333
normalized size	1	1.	1.69	1.18	0.	0.	0.	2.75
time (sec)	N/A	0.242	0.099	0.074	0.	0.	0.	1.345

Problem 75	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	95	95	138	91	0	0	0	207
normalized size	1	1.	1.45	0.96	0.	0.	0.	2.18
time (sec)	N/A	0.189	0.061	0.049	0.	0.	0.	1.432

Problem 76	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	86	86	126	96	0	0	0	223
normalized size	1	1.	1.47	1.12	0.	0.	0.	2.59
time (sec)	N/A	0.181	0.05	0.044	0.	0.	0.	1.488

Problem 77	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	59	59	81	42	0	0	0	96
normalized size	1	1.	1.37	0.71	0.	0.	0.	1.63
time (sec)	N/A	0.151	0.021	0.033	0.	0.	0.	1.378

Problem 78	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	44	44	66	49	0	0	0	112
normalized size	1	1.	1.5	1.11	0.	0.	0.	2.55
time (sec)	N/A	0.09	0.031	0.032	0.	0.	0.	1.361

Problem 79	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	0.399	0.078	0.	0.	0.	0.

Problem 80	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	214	282	202	193	0	0	0	479
normalized size	1	1.32	0.94	0.9	0.	0.	0.	2.24
time (sec)	N/A	0.533	0.065	0.079	0.	0.	0.	1.401

Problem 81	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	157	157	130	121	0	0	0	304
normalized size	1	1.	0.83	0.77	0.	0.	0.	1.94
time (sec)	N/A	0.379	0.033	0.053	0.	0.	0.	1.398

Problem 82	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	147	147	136	131	0	0	0	320
normalized size	1	1.	0.93	0.89	0.	0.	0.	2.18
time (sec)	N/A	0.303	0.059	0.05	0.	0.	0.	1.392

Problem 83	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	89	89	71	64	0	0	0	144
normalized size	1	1.	0.8	0.72	0.	0.	0.	1.62
time (sec)	N/A	0.183	0.015	0.036	0.	0.	0.	1.342

Problem 84	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	75	75	76	72	0	0	0	161
normalized size	1	1.	1.01	0.96	0.	0.	0.	2.15
time (sec)	N/A	0.099	0.043	0.036	0.	0.	0.	1.469

Problem 85	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	0.372	0.063	0.	0.	0.	0.

Problem 86	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	263	298	204	233	0	0	0	625
normalized size	1	1.13	0.78	0.89	0.	0.	0.	2.38
time (sec)	N/A	0.803	0.071	0.077	0.	0.	0.	1.475

Problem 87	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	205	205	140	154	0	0	0	401
normalized size	1	1.	0.68	0.75	0.	0.	0.	1.96
time (sec)	N/A	0.6	0.041	0.056	0.	0.	0.	1.494

Problem 88	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	178	178	125	156	0	0	0	417
normalized size	1	1.	0.7	0.88	0.	0.	0.	2.34
time (sec)	N/A	0.469	0.047	0.055	0.	0.	0.	1.436

Problem 89	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	119	119	81	79	0	0	0	193
normalized size	1	1.	0.68	0.66	0.	0.	0.	1.62
time (sec)	N/A	0.313	0.02	0.036	0.	0.	0.	1.463

Problem 90	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	88	88	68	88	0	0	0	209
normalized size	1	1.	0.77	1.	0.	0.	0.	2.38
time (sec)	N/A	0.165	0.035	0.037	0.	0.	0.	1.514

Problem 91	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	0.373	0.063	0.	0.	0.	0.

Problem 92	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	106	106	193	72	0	0	0	188
normalized size	1	1.	1.82	0.68	0.	0.	0.	1.77
time (sec)	N/A	0.112	0.057	0.055	0.	0.	0.	1.452

Problem 93	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	65	65	128	44	0	0	0	109
normalized size	1	1.	1.97	0.68	0.	0.	0.	1.68
time (sec)	N/A	0.083	0.032	0.039	0.	0.	0.	1.476

Problem 94	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	71	71	128	51	0	0	0	126
normalized size	1	1.	1.8	0.72	0.	0.	0.	1.77
time (sec)	N/A	0.089	0.051	0.039	0.	0.	0.	1.434

Problem 95	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	28	28	71	21	0	0	0	47
normalized size	1	1.	2.54	0.75	0.	0.	0.	1.68
time (sec)	N/A	0.045	0.017	0.029	0.	0.	0.	1.479

Problem 96	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	30	30	69	25	0	0	0	63
normalized size	1	1.	2.3	0.83	0.	0.	0.	2.1
time (sec)	N/A	0.024	0.026	0.028	0.	0.	0.	1.369

Problem 97	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.014	0.356	0.069	0.	0.	0.	0.

Problem 98	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	2.993	0.122	0.	0.	0.	0.

Problem 99	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	171	171	427	184	0	0	0	0
normalized size	1	1.	2.5	1.08	0.	0.	0.	0.
time (sec)	N/A	0.144	0.234	0.077	0.	0.	0.	0.

Problem 100	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	127	127	231	121	0	0	0	0
normalized size	1	1.	1.82	0.95	0.	0.	0.	0.
time (sec)	N/A	0.107	0.135	0.067	0.	0.	0.	0.

Problem 101	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	136	136	319	138	0	0	0	0
normalized size	1	1.	2.35	1.01	0.	0.	0.	0.
time (sec)	N/A	0.098	0.152	0.051	0.	0.	0.	0.

Problem 102	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	90	90	154	83	0	0	0	0
normalized size	1	1.	1.71	0.92	0.	0.	0.	0.
time (sec)	N/A	0.07	0.046	0.042	0.	0.	0.	0.

Problem 103	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	96	96	211	95	0	0	0	0
normalized size	1	1.	2.2	0.99	0.	0.	0.	0.
time (sec)	N/A	0.069	0.072	0.046	0.	0.	0.	0.

Problem 104	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	55	55	91	43	0	0	0	0
normalized size	1	1.	1.65	0.78	0.	0.	0.	0.
time (sec)	N/A	0.032	0.033	0.031	0.	0.	0.	0.

Problem 105	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	59	59	87	65	0	0	0	0
normalized size	1	1.	1.47	1.1	0.	0.	0.	0.
time (sec)	N/A	0.09	0.095	0.035	0.	0.	0.	0.

Problem 106	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.014	0.455	0.063	0.	0.	0.	0.

Problem 107	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	171	235	418	175	0	0	0	0
normalized size	1	1.37	2.44	1.02	0.	0.	0.	0.
time (sec)	N/A	0.434	0.329	0.07	0.	0.	0.	0.

Problem 108	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	126	126	200	109	0	0	0	0
normalized size	1	1.	1.59	0.87	0.	0.	0.	0.
time (sec)	N/A	0.338	0.394	0.057	0.	0.	0.	0.

Problem 109	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	125	125	277	117	0	0	0	0
normalized size	1	1.	2.22	0.94	0.	0.	0.	0.
time (sec)	N/A	0.301	0.208	0.055	0.	0.	0.	0.

Problem 110	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	89	89	112	56	0	0	0	0
normalized size	1	1.	1.26	0.63	0.	0.	0.	0.
time (sec)	N/A	0.18	0.225	0.039	0.	0.	0.	0.

Problem 111	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	76	76	138	83	0	0	0	0
normalized size	1	1.	1.82	1.09	0.	0.	0.	0.
time (sec)	N/A	0.099	0.127	0.042	0.	0.	0.	0.

Problem 112	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	0.462	0.069	0.	0.	0.	0.

Problem 113	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	264	264	417	225	0	0	0	0
normalized size	1	1.	1.58	0.85	0.	0.	0.	0.
time (sec)	N/A	0.396	0.772	0.083	0.	0.	0.	0.

Problem 114	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	190	190	272	139	0	0	0	0
normalized size	1	1.	1.43	0.73	0.	0.	0.	0.
time (sec)	N/A	0.319	1.187	0.055	0.	0.	0.	0.

Problem 115	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	191	191	280	154	0	0	0	0
normalized size	1	1.	1.47	0.81	0.	0.	0.	0.
time (sec)	N/A	0.348	0.476	0.055	0.	0.	0.	0.

Problem 116	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	119	119	146	73	0	0	0	0
normalized size	1	1.	1.23	0.61	0.	0.	0.	0.
time (sec)	N/A	0.172	0.412	0.038	0.	0.	0.	0.

Problem 117	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F(-2)	F(-1)	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	105	105	143	110	0	0	0	0
normalized size	1	1.	1.36	1.05	0.	0.	0.	0.
time (sec)	N/A	0.166	0.26	0.04	0.	0.	0.	0.

Problem 118	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.013	0.462	0.066	0.	0.	0.	0.

Problem 119	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	64	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.122	1.064	0.828	0.	0.	0.	0.

Problem 120	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	64	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.118	0.941	0.548	0.	0.	0.	0.

Problem 121	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	150	150	122	0	0	0	0	0
normalized size	1	1.	0.81	0.	0.	0.	0.	0.
time (sec)	N/A	0.114	0.043	0.525	0.	0.	0.	0.

Problem 122	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	69	69	56	0	0	0	0	0
normalized size	1	1.	0.81	0.	0.	0.	0.	0.
time (sec)	N/A	0.025	0.02	0.531	0.	0.	0.	0.

Problem 123	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.017	0.561	0.434	0.	0.	0.	0.

Problem 124	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-1)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.015	0.576	0.434	0.	0.	0.	0.

Problem 125	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.016	2.626	0.07	0.	0.	0.	0.

Problem 126	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.015	2.929	0.062	0.	0.	0.	0.

Problem 127	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.015	2.204	0.066	0.	0.	0.	0.

Problem 128	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.015	2.192	0.059	0.	0.	0.	0.

Problem 129	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.016	0.798	0.758	0.	0.	0.	0.

Problem 130	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	167	167	132	0	0	0	0	0
normalized size	1	1.	0.79	0.	0.	0.	0.	0.
time (sec)	N/A	0.177	0.088	0.144	0.	0.	0.	0.

Problem 131	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	171	171	137	0	0	0	0	0
normalized size	1	1.	0.8	0.	0.	0.	0.	0.
time (sec)	N/A	0.166	0.072	0.154	0.	0.	0.	0.

Problem 132	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	C	F(-2)	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	85	85	75	138	0	0	0	0
normalized size	1	1.	0.88	1.62	0.	0.	0.	0.
time (sec)	N/A	0.082	0.019	0.117	0.	0.	0.	0.

Problem 133	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	C	F(-2)	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	79	79	73	240	0	0	0	0
normalized size	1	1.	0.92	3.04	0.	0.	0.	0.
time (sec)	N/A	0.055	0.035	0.082	0.	0.	0.	0.

Problem 134	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.015	0.278	0.102	0.	0.	0.	0.

Problem 135	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.016	0.525	0.072	0.	0.	0.	0.

Problem 136	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.021	3.571	0.089	0.	0.	0.	0.

Problem 137	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.017	4.269	0.07	0.	0.	0.	0.

Problem 138	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.018	1.552	0.069	0.	0.	0.	0.

Problem 139	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.021	1.9	0.069	0.	0.	0.	0.

Problem 140	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	76	76	81	72	111	139	80	163
normalized size	1	1.	1.07	0.95	1.46	1.83	1.05	2.14
time (sec)	N/A	0.035	0.03	0.005	1.591	1.436	2.371	1.37

Problem 141	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	60	60	49	64	80	119	65	100
normalized size	1	1.	0.82	1.07	1.33	1.98	1.08	1.67
time (sec)	N/A	0.039	0.039	0.003	1.686	1.53	0.922	1.347

Problem 142	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	51	51	56	52	82	111	54	86
normalized size	1	1.	1.1	1.02	1.61	2.18	1.06	1.69
time (sec)	N/A	0.019	0.019	0.003	1.598	1.484	0.435	1.316

Problem 143	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	30	30	30	30	39	73	26	39
normalized size	1	1.	1.	1.	1.3	2.43	0.87	1.3
time (sec)	N/A	0.014	0.012	0.003	1.517	1.459	0.17	1.286

Problem 144	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	63	63	52	122	0	0	0	0
normalized size	1	1.	0.83	1.94	0.	0.	0.	0.
time (sec)	N/A	0.07	0.032	0.03	0.	0.	0.	0.

Problem 145	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	33	33	36	43	63	140	39	439
normalized size	1	1.	1.09	1.3	1.91	4.24	1.18	13.3
time (sec)	N/A	0.027	0.003	0.004	1.505	1.552	3.323	1.583

Problem 146	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	39	39	44	50	49	88	61	220
normalized size	1	1.	1.13	1.28	1.26	2.26	1.56	5.64
time (sec)	N/A	0.019	0.013	0.004	1.538	1.489	2.896	1.402

Problem 147	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	62	62	67	65	93	194	119	383
normalized size	1	1.	1.08	1.05	1.5	3.13	1.92	6.18
time (sec)	N/A	0.038	0.018	0.003	1.55	1.663	5.744	2.034

Problem 148	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	102	102	95	126	192	255	170	262
normalized size	1	1.	0.93	1.24	1.88	2.5	1.67	2.57
time (sec)	N/A	0.154	0.189	0.025	1.549	1.436	2.059	1.347

Problem 149	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	76	76	73	120	0	221	126	209
normalized size	1	1.	0.96	1.58	0.	2.91	1.66	2.75
time (sec)	N/A	0.119	0.073	0.023	0.	1.482	1.174	1.3

Problem 150	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	47	47	47	72	97	159	82	101
normalized size	1	1.	1.	1.53	2.06	3.38	1.74	2.15
time (sec)	N/A	0.06	0.04	0.023	1.566	1.555	0.528	1.351

Problem 151	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	B	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	90	90	143	319	0	0	0	0
normalized size	1	1.	1.59	3.54	0.	0.	0.	0.
time (sec)	N/A	0.123	0.156	0.03	0.	0.	0.	0.

Problem 152	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	81	81	126	171	0	0	0	0
normalized size	1	1.	1.56	2.11	0.	0.	0.	0.
time (sec)	N/A	0.128	0.225	0.056	0.	0.	0.	0.

Problem 153	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	178	178	163	235	369	441	328	497
normalized size	1	1.	0.92	1.32	2.07	2.48	1.84	2.79
time (sec)	N/A	0.297	0.409	0.029	1.888	1.804	3.745	1.458

Problem 154	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	125	125	114	219	0	378	264	385
normalized size	1	1.	0.91	1.75	0.	3.02	2.11	3.08
time (sec)	N/A	0.205	0.148	0.027	0.	1.681	1.893	1.478

Problem 155	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	A	A	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	82	82	77	132	190	262	160	203
normalized size	1	1.	0.94	1.61	2.32	3.2	1.95	2.48
time (sec)	N/A	0.109	0.088	0.024	1.869	1.793	1.209	1.374

Problem 156	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	B	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	123	123	244	592	0	0	0	0
normalized size	1	1.	1.98	4.81	0.	0.	0.	0.
time (sec)	N/A	0.147	0.239	0.026	0.	0.	0.	0.

Problem 157	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	B	B	F	F	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	137	137	283	378	0	0	0	0
normalized size	1	1.	2.07	2.76	0.	0.	0.	0.
time (sec)	N/A	0.213	0.314	0.042	0.	0.	0.	0.

Problem 158	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	121	117	91	102	0	0	0	234
normalized size	1	0.97	0.75	0.84	0.	0.	0.	1.93
time (sec)	N/A	0.254	0.2	0.025	0.	0.	0.	1.302

Problem 159	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	63	63	56	58	0	0	0	116
normalized size	1	1.	0.89	0.92	0.	0.	0.	1.84
time (sec)	N/A	0.132	0.079	0.023	0.	0.	0.	1.288

Problem 160	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	53	53	44	48	0	0	0	66
normalized size	1	1.	0.83	0.91	0.	0.	0.	1.25
time (sec)	N/A	0.067	0.065	0.023	0.	0.	0.	1.412

Problem 161	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.024	0.245	0.145	0.	0.	0.	0.

Problem 162	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.025	2.167	0.243	0.	0.	0.	0.

Problem 163	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	156	152	125	149	0	0	0	872
normalized size	1	0.97	0.8	0.96	0.	0.	0.	5.59
time (sec)	N/A	0.182	0.531	0.037	0.	0.	0.	1.403

Problem 164	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	90	90	79	77	0	0	0	440
normalized size	1	1.	0.88	0.86	0.	0.	0.	4.89
time (sec)	N/A	0.1	0.266	0.027	0.	0.	0.	1.413

Problem 165	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F(-1)	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	86	82	72	76	0	0	0	259
normalized size	1	0.95	0.84	0.88	0.	0.	0.	3.01
time (sec)	N/A	0.169	0.156	0.03	0.	0.	0.	1.359

Problem 166	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-1)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.023	3.985	0.184	0.	0.	0.	0.

Problem 167	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-1)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.023	33.323	0.339	0.	0.	0.	0.

Problem 168	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	197	245	168	290	0	0	0	2078
normalized size	1	1.24	0.85	1.47	0.	0.	0.	10.55
time (sec)	N/A	0.542	0.861	0.034	0.	0.	0.	1.705

Problem 169	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	130	130	108	157	0	0	0	1166
normalized size	1	1.	0.83	1.21	0.	0.	0.	8.97
time (sec)	N/A	0.323	0.33	0.027	0.	0.	0.	1.687

Problem 170	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	111	111	93	138	0	0	0	651
normalized size	1	1.	0.84	1.24	0.	0.	0.	5.86
time (sec)	N/A	0.172	0.418	0.03	0.	0.	0.	1.426

Problem 171	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.023	2.128	0.276	0.	0.	0.	0.

Problem 172	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	16	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.023	17.855	0.5	0.	0.	0.	0.

Problem 173	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	242	242	246	356	0	0	0	531
normalized size	1	1.	1.02	1.47	0.	0.	0.	2.19
time (sec)	N/A	0.756	0.304	0.083	0.	0.	0.	2.105

Problem 174	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	137	137	141	173	0	0	0	236
normalized size	1	1.	1.03	1.26	0.	0.	0.	1.72
time (sec)	N/A	0.453	0.072	0.052	0.	0.	0.	1.805

Problem 175	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	120	120	119	178	0	0	0	266
normalized size	1	1.	0.99	1.48	0.	0.	0.	2.22
time (sec)	N/A	0.331	0.089	0.043	0.	0.	0.	1.687

Problem 176	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.046	3.254	0.128	0.	0.	0.	0.

Problem 177	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.037	11.4	0.165	0.	0.	0.	0.

Problem 178	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	313	313	245	540	0	0	0	1740
normalized size	1	1.	0.78	1.73	0.	0.	0.	5.56
time (sec)	N/A	1.046	0.285	0.105	0.	0.	0.	3.5

Problem 179	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	172	172	126	267	0	0	0	757
normalized size	1	1.	0.73	1.55	0.	0.	0.	4.4
time (sec)	N/A	0.525	0.059	0.092	0.	0.	0.	2.23

Problem 180	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	159	159	291	270	0	0	0	879
normalized size	1	1.	1.83	1.7	0.	0.	0.	5.53
time (sec)	N/A	0.281	2.796	0.056	0.	0.	0.	2.469

Problem 181	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.045	2.901	0.11	0.	0.	0.	0.

Problem 182	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.042	10.143	0.169	0.	0.	0.	0.

Problem 183	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	358	358	228	792	0	0	0	3357
normalized size	1	1.	0.64	2.21	0.	0.	0.	9.38
time (sec)	N/A	1.409	0.273	0.118	0.	0.	0.	5.104

Problem 184	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	216	216	141	394	0	0	0	1570
normalized size	1	1.	0.65	1.82	0.	0.	0.	7.27
time (sec)	N/A	0.743	0.095	0.068	0.	0.	0.	2.798

Problem 185	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F(-1)	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	179	179	379	393	0	0	0	1578
normalized size	1	1.	2.12	2.2	0.	0.	0.	8.82
time (sec)	N/A	0.502	2.899	0.067	0.	0.	0.	3.193

Problem 186	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.044	3.06	0.101	0.	0.	0.	0.

Problem 187	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.043	10.216	0.161	0.	0.	0.	0.

Problem 188	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	223	223	228	168	0	0	0	428
normalized size	1	1.	1.02	0.75	0.	0.	0.	1.92
time (sec)	N/A	0.421	0.266	0.058	0.	0.	0.	2.271

Problem 189	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	99	99	123	80	0	0	0	178
normalized size	1	1.	1.24	0.81	0.	0.	0.	1.8
time (sec)	N/A	0.176	0.061	0.038	0.	0.	0.	1.992

Problem 190	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	101	101	121	83	0	0	0	215
normalized size	1	1.	1.2	0.82	0.	0.	0.	2.13
time (sec)	N/A	0.091	0.087	0.029	0.	0.	0.	1.912

Problem 191	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.037	2.866	0.082	0.	0.	0.	0.

Problem 192	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.037	11.63	0.137	0.	0.	0.	0.

Problem 193	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	250	250	343	295	0	0	0	0
normalized size	1	1.	1.37	1.18	0.	0.	0.	0.
time (sec)	N/A	0.418	0.443	0.066	0.	0.	0.	0.

Problem 194	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	130	130	155	143	0	0	0	0
normalized size	1	1.	1.19	1.1	0.	0.	0.	0.
time (sec)	N/A	0.163	0.145	0.045	0.	0.	0.	0.

Problem 195	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	137	137	167	149	0	0	0	0
normalized size	1	1.	1.22	1.09	0.	0.	0.	0.
time (sec)	N/A	0.294	0.298	0.042	0.	0.	0.	0.

Problem 196	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.044	3.458	0.079	0.	0.	0.	0.

Problem 197	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.043	11.405	0.158	0.	0.	0.	0.

Problem 198	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	291	291	370	660	0	0	0	0
normalized size	1	1.	1.27	2.27	0.	0.	0.	0.
time (sec)	N/A	1.007	1.855	0.088	0.	0.	0.	0.

Problem 199	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	180	180	173	311	0	0	0	0
normalized size	1	1.	0.96	1.73	0.	0.	0.	0.
time (sec)	N/A	0.506	1.231	0.059	0.	0.	0.	0.

Problem 200	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	163	163	214	325	0	0	0	0
normalized size	1	1.	1.31	1.99	0.	0.	0.	0.
time (sec)	N/A	0.276	0.852	0.053	0.	0.	0.	0.

Problem 201	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.045	3.613	0.073	0.	0.	0.	0.

Problem 202	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	F(-2)	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.045	11.448	0.161	0.	0.	0.	0.

Problem 203	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	120	120	100	144	0	0	0	0
normalized size	1	1.	0.83	1.2	0.	0.	0.	0.
time (sec)	N/A	0.076	0.039	0.036	0.	0.	0.	0.

Problem 204	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	124	124	66	138	0	0	82	0
normalized size	1	1.	0.53	1.11	0.	0.	0.66	0.
time (sec)	N/A	0.098	0.025	0.01	0.	0.	163.098	0.

Problem 205	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	88	88	66	119	0	0	76	0
normalized size	1	1.	0.75	1.35	0.	0.	0.86	0.
time (sec)	N/A	0.045	0.017	0.008	0.	0.	4.419	0.

Problem 206	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	89	89	45	98	0	0	0	0
normalized size	1	1.	0.51	1.1	0.	0.	0.	0.
time (sec)	N/A	0.078	0.015	0.009	0.	0.	0.	0.

Problem 207	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	55	55	40	85	0	0	0	0
normalized size	1	1.	0.73	1.55	0.	0.	0.	0.
time (sec)	N/A	0.038	0.013	0.009	0.	0.	0.	0.

Problem 208	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F(-2)	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	125	125	42	129	0	0	0	0
normalized size	1	1.	0.34	1.03	0.	0.	0.	0.
time (sec)	N/A	0.097	0.015	0.013	0.	0.	0.	0.

Problem 209	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	109	109	90	0	0	0	0	0
normalized size	1	1.	0.83	0.	0.	0.	0.	0.
time (sec)	N/A	0.141	0.061	0.158	0.	0.	0.	0.

Problem 210	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F(-1)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	109	109	90	0	0	0	0	0
normalized size	1	1.	0.83	0.	0.	0.	0.	0.
time (sec)	N/A	0.141	0.056	0.143	0.	0.	0.	0.

Problem 211	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	109	109	90	0	0	0	0	0
normalized size	1	1.	0.83	0.	0.	0.	0.	0.
time (sec)	N/A	0.143	0.052	0.184	0.	0.	0.	0.

Problem 212	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	107	107	90	0	0	0	0	0
normalized size	1	1.	0.84	0.	0.	0.	0.	0.
time (sec)	N/A	0.13	0.049	0.358	0.	0.	0.	0.

Problem 213	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	105	105	87	0	0	0	0	0
normalized size	1	1.	0.83	0.	0.	0.	0.	0.
time (sec)	N/A	0.135	0.047	0.154	0.	0.	0.	0.

Problem 214	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F(-2)	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	109	109	87	0	0	0	0	0
normalized size	1	1.	0.8	0.	0.	0.	0.	0.
time (sec)	N/A	0.145	0.054	0.144	0.	0.	0.	0.

Problem 215	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	F(-1)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	68	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.17	36.379	0.144	0.	0.	0.	0.

Problem 216	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	F	A	F(-2)	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	66	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.168	180.002	0.142	0.	0.	0.	0.

Problem 217	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	F(-2)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	64	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.16	8.126	0.199	0.	0.	0.	0.

Problem 218	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	F(-2)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	64	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.159	7.576	0.145	0.	0.	0.	0.

Problem 219	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	F(-2)	A	F(-2)	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	66	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.173	13.129	0.139	0.	0.	0.	0.

Problem 220	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.03	2.676	0.093	0.	0.	0.	0.

Problem 221	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.026	2.565	0.092	0.	0.	0.	0.

Problem 222	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.029	0.769	0.1	0.	0.	0.	0.

Problem 223	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.032	3.841	0.099	0.	0.	0.	0.

Problem 224	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.029	5.683	0.098	0.	0.	0.	0.

Problem 225	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.026	4.897	0.095	0.	0.	0.	0.

Problem 226	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.025	8.376	0.102	0.	0.	0.	0.

Problem 227	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.028	13.561	0.092	0.	0.	0.	0.

2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio $\frac{\text{number of rules}}{\text{integrand size}}$ is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [30] had the largest ratio of [1.]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	4	3	1.	8	0.375
2	A	4	3	1.	8	0.375
3	A	4	3	1.	8	0.375
4	A	3	3	1.	6	0.5
5	A	2	2	1.	4	0.5
6	A	5	5	1.	8	0.625
7	A	4	4	1.	8	0.5
8	A	2	2	1.	8	0.25
9	A	5	5	1.	8	0.625
10	A	3	3	1.	8	0.375
11	A	6	5	1.	8	0.625
12	A	7	5	1.	10	0.5
13	A	6	4	1.	10	0.4
14	A	5	5	1.	10	0.5
15	A	4	4	1.	8	0.5
16	A	3	3	1.	6	0.5
17	A	6	6	1.	10	0.6
18	A	7	5	1.	10	0.5
19	A	3	3	1.	10	0.3
20	A	9	7	1.	10	0.7
21	A	5	5	1.	10	0.5
22	A	14	7	1.	10	0.7
23	A	11	5	1.	10	0.5
24	A	9	7	1.	10	0.7
25	A	6	5	1.	8	0.625
26	A	4	3	1.	6	0.5
27	A	7	7	1.	10	0.7
28	A	9	6	1.	10	0.6
29	A	7	7	1.	10	0.7
30	A	14	10	1.	10	1.
31	A	10	9	1.	10	0.9
32	A	23	4	1.	10	0.4
33	A	19	6	1.	10	0.6
34	A	14	4	1.	10	0.4
35	A	11	6	1.	10	0.6

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
36	A	7	4	1.	8	0.5
37	A	5	3	1.	6	0.5
38	A	8	7	1.	10	0.7
39	A	11	7	1.	10	0.7
40	A	8	8	1.	10	0.8
41	A	19	10	1.	10	1.
42	A	7	3	1.	10	0.3
43	A	6	3	1.	10	0.3
44	A	6	3	1.	10	0.3
45	A	5	3	1.	10	0.3
46	A	5	3	1.	10	0.3
47	A	4	4	1.	8	0.5
48	A	2	2	1.	6	0.333
49	A	0	0	0.	0	0.
50	A	0	0	0.	0	0.
51	A	6	2	1.	10	0.2
52	A	5	2	1.	10	0.2
53	A	5	2	1.	10	0.2
54	A	4	2	1.	10	0.2
55	A	4	2	1.	10	0.2
56	A	2	2	1.	8	0.25
57	A	3	3	1.	6	0.5
58	A	0	0	0.	0	0.
59	A	0	0	0.	0	0.
60	A	14	5	1.	10	0.5
61	A	12	6	1.	10	0.6
62	A	10	6	1.	10	0.6
63	A	7	7	1.	8	0.875
64	A	4	4	1.	6	0.667
65	A	0	0	0.	0	0.
66	A	0	0	0.	0	0.
67	A	12	4	1.	10	0.4
68	A	9	4	1.	10	0.4
69	A	10	6	1.	10	0.6
70	A	5	5	1.	8	0.625
71	A	5	4	1.	6	0.667
72	A	0	0	0.	0	0.
73	A	0	0	0.	0	0.
74	A	10	5	1.	12	0.417
75	A	8	5	1.	12	0.417
76	A	8	5	1.	12	0.417
77	A	6	5	1.	10	0.5
78	A	4	4	1.	8	0.5
79	A	0	0	0.	0	0.

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
80	A	23	8	1.32	12	0.667
81	A	16	8	1.	12	0.667
82	A	13	8	1.	12	0.667
83	A	8	8	1.	10	0.8
84	A	5	5	1.	8	0.625
85	A	0	0	0.	0	0.
86	A	26	8	1.13	12	0.667
87	A	18	7	1.	12	0.583
88	A	15	8	1.	12	0.667
89	A	9	7	1.	10	0.7
90	A	6	5	1.	8	0.625
91	A	0	0	0.	0	0.
92	A	9	4	1.	12	0.333
93	A	7	4	1.	12	0.333
94	A	7	4	1.	12	0.333
95	A	5	5	1.	10	0.5
96	A	3	3	1.	8	0.375
97	A	0	0	0.	0	0.
98	A	0	0	0.	0	0.
99	A	10	3	1.	12	0.25
100	A	8	3	1.	12	0.25
101	A	8	3	1.	12	0.25
102	A	6	3	1.	12	0.25
103	A	6	3	1.	12	0.25
104	A	3	3	1.	10	0.3
105	A	4	4	1.	8	0.5
106	A	0	0	0.	0	0.
107	A	19	6	1.37	12	0.5
108	A	15	7	1.	12	0.583
109	A	13	7	1.	12	0.583
110	A	8	8	1.	10	0.8
111	A	5	5	1.	8	0.625
112	A	0	0	0.	0	0.
113	A	17	5	1.	12	0.417
114	A	12	5	1.	12	0.417
115	A	13	7	1.	12	0.583
116	A	6	6	1.	10	0.6
117	A	6	5	1.	8	0.625
118	A	0	0	0.	0	0.
119	A	0	0	0.	0	0.
120	A	0	0	0.	0	0.
121	A	2	2	1.	12	0.167
122	A	2	2	1.	10	0.2
123	A	0	0	0.	0	0.

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
124	A	0	0	0.	0	0.
125	A	0	0	0.	0	0.
126	A	0	0	0.	0	0.
127	A	0	0	0.	0	0.
128	A	0	0	0.	0	0.
129	A	0	0	0.	0	0.
130	A	9	4	1.	10	0.4
131	A	9	4	1.	10	0.4
132	A	6	5	1.	8	0.625
133	A	4	3	1.	6	0.5
134	A	0	0	0.	0	0.
135	A	0	0	0.	0	0.
136	A	0	0	0.	0	0.
137	A	0	0	0.	0	0.
138	A	0	0	0.	0	0.
139	A	0	0	0.	0	0.
140	A	4	3	1.	12	0.25
141	A	4	3	1.	12	0.25
142	A	3	3	1.	10	0.3
143	A	3	2	1.	8	0.25
144	A	5	5	1.	12	0.417
145	A	4	4	1.	12	0.333
146	A	2	2	1.	12	0.167
147	A	5	5	1.	12	0.417
148	A	5	5	1.	14	0.357
149	A	4	4	1.	12	0.333
150	A	3	3	1.	10	0.3
151	A	6	6	1.	14	0.429
152	A	7	5	1.	14	0.357
153	A	10	7	1.	14	0.5
154	A	6	5	1.	12	0.417
155	A	5	3	1.	10	0.3
156	A	7	7	1.	14	0.5
157	A	9	6	1.	14	0.429
158	A	9	5	0.97	14	0.357
159	A	6	6	1.	12	0.5
160	A	4	4	1.	10	0.4
161	A	0	0	0.	0	0.
162	A	0	0	0.	0	0.
163	A	8	4	0.97	14	0.286
164	A	4	4	1.	12	0.333
165	A	5	5	0.95	10	0.5
166	A	0	0	0.	0	0.
167	A	0	0	0.	0	0.

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
168	A	16	8	1.24	14	0.571
169	A	9	9	1.	12	0.75
170	A	6	6	1.	10	0.6
171	A	0	0	0.	0	0.
172	A	0	0	0.	0	0.
173	A	14	8	1.	16	0.5
174	A	9	8	1.	14	0.571
175	A	7	7	1.	12	0.583
176	A	0	0	0.	0	0.
177	A	0	0	0.	0	0.
178	A	22	11	1.	16	0.688
179	A	11	11	1.	14	0.786
180	A	8	8	1.	12	0.667
181	A	0	0	0.	0	0.
182	A	0	0	0.	0	0.
183	A	24	11	1.	16	0.688
184	A	12	10	1.	14	0.714
185	A	9	8	1.	12	0.667
186	A	0	0	0.	0	0.
187	A	0	0	0.	0	0.
188	A	13	7	1.	16	0.438
189	A	8	8	1.	14	0.571
190	A	6	6	1.	12	0.5
191	A	0	0	0.	0	0.
192	A	0	0	0.	0	0.
193	A	12	6	1.	16	0.375
194	A	6	6	1.	14	0.429
195	A	7	7	1.	12	0.583
196	A	0	0	0.	0	0.
197	A	0	0	0.	0	0.
198	A	22	10	1.	16	0.625
199	A	11	11	1.	14	0.786
200	A	8	8	1.	12	0.667
201	A	0	0	0.	0	0.
202	A	0	0	0.	0	0.
203	A	5	4	1.	16	0.25
204	A	7	7	1.	16	0.438
205	A	4	4	1.	16	0.25
206	A	6	6	1.	16	0.375
207	A	3	3	1.	16	0.188
208	A	7	7	1.	16	0.438
209	A	2	2	1.	18	0.111
210	A	2	2	1.	18	0.111
211	A	2	2	1.	18	0.111

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
212	A	2	2	1.	18	0.111
213	A	2	2	1.	18	0.111
214	A	2	2	1.	18	0.111
215	A	0	0	0.	0	0.
216	A	0	0	0.	0	0.
217	A	0	0	0.	0	0.
218	A	0	0	0.	0	0.
219	A	0	0	0.	0	0.
220	A	0	0	0.	0	0.
221	A	0	0	0.	0	0.
222	A	0	0	0.	0	0.
223	A	0	0	0.	0	0.
224	A	0	0	0.	0	0.
225	A	0	0	0.	0	0.
226	A	0	0	0.	0	0.
227	A	0	0	0.	0	0.

Chapter 3

Listing of integrals

3.1 $\int x^4 \sin^{-1}(ax) dx$

Optimal. Leaf size=75

$$\frac{(1-a^2x^2)^{5/2}}{25a^5} - \frac{2(1-a^2x^2)^{3/2}}{15a^5} + \frac{\sqrt{1-a^2x^2}}{5a^5} + \frac{1}{5}x^5 \sin^{-1}(ax)$$

```
[Out] Sqrt[1 - a^2*x^2]/(5*a^5) - (2*(1 - a^2*x^2)^(3/2))/(15*a^5) + (1 - a^2*x^2)^(5/2)/(25*a^5) + (x^5*ArcSin[a*x])/5
```

Rubi [A] time = 0.0489039, antiderivative size = 75, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {4627, 266, 43}

$$\frac{(1-a^2x^2)^{5/2}}{25a^5} - \frac{2(1-a^2x^2)^{3/2}}{15a^5} + \frac{\sqrt{1-a^2x^2}}{5a^5} + \frac{1}{5}x^5 \sin^{-1}(ax)$$

Antiderivative was successfully verified.

```
[In] Int[x^4*ArcSin[a*x], x]
```

```
[Out] Sqrt[1 - a^2*x^2]/(5*a^5) - (2*(1 - a^2*x^2)^(3/2))/(15*a^5) + (1 - a^2*x^2)^(5/2)/(25*a^5) + (x^5*ArcSin[a*x])/5
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 266

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol]
:> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]
```

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol]
:> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n},
```

$x] \&\& \text{NeQ}[b*c - a*d, 0] \&\& \text{IGtQ}[m, 0] \&\& (!\text{IntegerQ}[n] \ || \ (\text{EqQ}[c, 0] \ \&\& \ \text{LeQ}[7*m + 4*n + 4, 0]) \ || \ \text{LtQ}[9*m + 5*(n + 1), 0] \ || \ \text{GtQ}[m + n + 2, 0])$

Rubi steps

$$\begin{aligned} \int x^4 \sin^{-1}(ax) dx &= \frac{1}{5} x^5 \sin^{-1}(ax) - \frac{1}{5} a \int \frac{x^5}{\sqrt{1-a^2x^2}} dx \\ &= \frac{1}{5} x^5 \sin^{-1}(ax) - \frac{1}{10} a \text{Subst} \left(\int \frac{x^2}{\sqrt{1-a^2x}} dx, x, x^2 \right) \\ &= \frac{1}{5} x^5 \sin^{-1}(ax) - \frac{1}{10} a \text{Subst} \left(\int \left(\frac{1}{a^4 \sqrt{1-a^2x}} - \frac{2\sqrt{1-a^2x}}{a^4} + \frac{(1-a^2x)^{3/2}}{a^4} \right) dx, x, x^2 \right) \\ &= \frac{\sqrt{1-a^2x^2}}{5a^5} - \frac{2(1-a^2x^2)^{3/2}}{15a^5} + \frac{(1-a^2x^2)^{5/2}}{25a^5} + \frac{1}{5} x^5 \sin^{-1}(ax) \end{aligned}$$

Mathematica [A] time = 0.0320767, size = 51, normalized size = 0.68

$$\frac{\sqrt{1-a^2x^2} (3a^4x^4 + 4a^2x^2 + 8)}{75a^5} + \frac{1}{5} x^5 \sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] Integrate[x^4*ArcSin[a*x],x]

[Out] (Sqrt[1 - a^2*x^2]*(8 + 4*a^2*x^2 + 3*a^4*x^4))/(75*a^5) + (x^5*ArcSin[a*x])/5

Maple [A] time = 0.032, size = 72, normalized size = 1.

$$\frac{1}{a^5} \left(\frac{a^5 x^5 \arcsin(ax)}{5} + \frac{a^4 x^4}{25} \sqrt{-a^2 x^2 + 1} + \frac{4 a^2 x^2}{75} \sqrt{-a^2 x^2 + 1} + \frac{8}{75} \sqrt{-a^2 x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*arcsin(a*x),x)

[Out] 1/a^5*(1/5*a^5*x^5*arcsin(a*x)+1/25*a^4*x^4*(-a^2*x^2+1)^(1/2)+4/75*a^2*x^2*(-a^2*x^2+1)^(1/2)+8/75*(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.68565, size = 96, normalized size = 1.28

$$\frac{1}{5} x^5 \arcsin(ax) + \frac{1}{75} \left(\frac{3 \sqrt{-a^2 x^2 + 1} x^4}{a^2} + \frac{4 \sqrt{-a^2 x^2 + 1} x^2}{a^4} + \frac{8 \sqrt{-a^2 x^2 + 1}}{a^6} \right) a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x),x, algorithm="maxima")

[Out] $1/5*x^5*\arcsin(ax) + 1/75*(3*\sqrt{-a^2*x^2 + 1})*x^4/a^2 + 4*\sqrt{-a^2*x^2 + 1}*x^2/a^4 + 8*\sqrt{-a^2*x^2 + 1}/a^6)*a$

Fricas [A] time = 2.13446, size = 113, normalized size = 1.51

$$\frac{15a^5x^5\arcsin(ax) + (3a^4x^4 + 4a^2x^2 + 8)\sqrt{-a^2x^2 + 1}}{75a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*arcsin(a*x),x, algorithm="fricas")`

[Out] $1/75*(15*a^5*x^5*\arcsin(a*x) + (3*a^4*x^4 + 4*a^2*x^2 + 8)*\sqrt{-a^2*x^2 + 1})/a^5$

Sympy [A] time = 7.08271, size = 70, normalized size = 0.93

$$\begin{cases} \frac{x^5 \arcsin(ax)}{5} + \frac{x^4 \sqrt{-a^2x^2+1}}{25a} + \frac{4x^2 \sqrt{-a^2x^2+1}}{75a^3} + \frac{8\sqrt{-a^2x^2+1}}{75a^5} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**4*asin(a*x),x)`

[Out] `Piecewise((x**5*asin(a*x)/5 + x**4*sqrt(-a**2*x**2 + 1)/(25*a) + 4*x**2*sqrt(-a**2*x**2 + 1)/(75*a**3) + 8*sqrt(-a**2*x**2 + 1)/(75*a**5), Ne(a, 0)), (0, True))`

Giac [A] time = 1.2218, size = 153, normalized size = 2.04

$$\frac{(a^2x^2 - 1)^2 x \arcsin(ax)}{5a^4} + \frac{2(a^2x^2 - 1)x \arcsin(ax)}{5a^4} + \frac{x \arcsin(ax)}{5a^4} + \frac{(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1}}{25a^5} - \frac{2(-a^2x^2 + 1)^{\frac{3}{2}}}{15a^5} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*arcsin(a*x),x, algorithm="giac")`

[Out] $1/5*(a^2*x^2 - 1)^2*x*\arcsin(a*x)/a^4 + 2/5*(a^2*x^2 - 1)*x*\arcsin(a*x)/a^4 + 1/5*x*\arcsin(a*x)/a^4 + 1/25*(a^2*x^2 - 1)^2*\sqrt{-a^2*x^2 + 1}/a^5 - 2/15*(-a^2*x^2 + 1)^{(3/2)}/a^5 + 1/5*\sqrt{-a^2*x^2 + 1}/a^5$

3.2 $\int x^3 \sin^{-1}(ax) dx$

Optimal. Leaf size=69

$$\frac{x^3\sqrt{1-a^2x^2}}{16a} + \frac{3x\sqrt{1-a^2x^2}}{32a^3} - \frac{3\sin^{-1}(ax)}{32a^4} + \frac{1}{4}x^4\sin^{-1}(ax)$$

[Out] (3*x*Sqrt[1 - a^2*x^2])/(32*a^3) + (x^3*Sqrt[1 - a^2*x^2])/(16*a) - (3*ArcSin[a*x])/(32*a^4) + (x^4*ArcSin[a*x])/4

Rubi [A] time = 0.0285116, antiderivative size = 69, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {4627, 321, 216}

$$\frac{x^3\sqrt{1-a^2x^2}}{16a} + \frac{3x\sqrt{1-a^2x^2}}{32a^3} - \frac{3\sin^{-1}(ax)}{32a^4} + \frac{1}{4}x^4\sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] Int[x^3*ArcSin[a*x], x]

[Out] (3*x*Sqrt[1 - a^2*x^2])/(32*a^3) + (x^3*Sqrt[1 - a^2*x^2])/(16*a) - (3*ArcSin[a*x])/(32*a^4) + (x^4*ArcSin[a*x])/4

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 321

Int[((c_.)*(x_))^(m_)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(c^(n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), Int[(c*x)^(m - n)*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n - 1] && NeQ[m + n*p + 1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int x^3 \sin^{-1}(ax) dx &= \frac{1}{4}x^4 \sin^{-1}(ax) - \frac{1}{4}a \int \frac{x^4}{\sqrt{1-a^2x^2}} dx \\ &= \frac{x^3\sqrt{1-a^2x^2}}{16a} + \frac{1}{4}x^4 \sin^{-1}(ax) - \frac{3 \int \frac{x^2}{\sqrt{1-a^2x^2}} dx}{16a} \\ &= \frac{3x\sqrt{1-a^2x^2}}{32a^3} + \frac{x^3\sqrt{1-a^2x^2}}{16a} + \frac{1}{4}x^4 \sin^{-1}(ax) - \frac{3 \int \frac{1}{\sqrt{1-a^2x^2}} dx}{32a^3} \\ &= \frac{3x\sqrt{1-a^2x^2}}{32a^3} + \frac{x^3\sqrt{1-a^2x^2}}{16a} - \frac{3\sin^{-1}(ax)}{32a^4} + \frac{1}{4}x^4 \sin^{-1}(ax) \end{aligned}$$

Mathematica [A] time = 0.0185745, size = 50, normalized size = 0.72

$$\frac{ax\sqrt{1-a^2x^2}(2a^2x^2+3)+(8a^4x^4-3)\sin^{-1}(ax)}{32a^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*ArcSin[a*x],x]

[Out] (a*x*Sqrt[1 - a^2*x^2]*(3 + 2*a^2*x^2) + (-3 + 8*a^4*x^4)*ArcSin[a*x])/(32*a^4)

Maple [A] time = 0.004, size = 60, normalized size = 0.9

$$\frac{1}{a^4} \left(\frac{a^4 x^4 \arcsin(ax)}{4} + \frac{a^3 x^3 \sqrt{-a^2 x^2 + 1}}{16} + \frac{3 ax \sqrt{-a^2 x^2 + 1}}{32} - \frac{3 \arcsin(ax)}{32} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x),x)

[Out] 1/a^4*(1/4*a^4*x^4*arcsin(a*x)+1/16*a^3*x^3*(-a^2*x^2+1)^(1/2)+3/32*a*x*(-a^2*x^2+1)^(1/2)-3/32*arcsin(a*x))

Maxima [A] time = 1.7267, size = 99, normalized size = 1.43

$$\frac{1}{4} x^4 \arcsin(ax) + \frac{1}{32} \left(\frac{2 \sqrt{-a^2 x^2 + 1} x^3}{a^2} + \frac{3 \sqrt{-a^2 x^2 + 1} x}{a^4} - \frac{3 \arcsin\left(\frac{a^2 x}{\sqrt{a^2}}\right)}{\sqrt{a^2} a^4} \right) a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x),x, algorithm="maxima")

[Out] 1/4*x^4*arcsin(a*x) + 1/32*(2*sqrt(-a^2*x^2 + 1)*x^3/a^2 + 3*sqrt(-a^2*x^2 + 1)*x/a^4 - 3*arcsin(a^2*x/sqrt(a^2))/(sqrt(a^2)*a^4))*a

Fricas [A] time = 2.02599, size = 109, normalized size = 1.58

$$\frac{(8a^4x^4-3)\arcsin(ax)+(2a^3x^3+3ax)\sqrt{-a^2x^2+1}}{32a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x),x, algorithm="fricas")

[Out] 1/32*((8*a^4*x^4 - 3)*arcsin(a*x) + (2*a^3*x^3 + 3*a*x)*sqrt(-a^2*x^2 + 1))/a^4

Sympy [A] time = 1.64484, size = 61, normalized size = 0.88

$$\begin{cases} \frac{x^4 \operatorname{asin}(ax)}{4} + \frac{x^3 \sqrt{-a^2 x^2 + 1}}{16a} + \frac{3x \sqrt{-a^2 x^2 + 1}}{32a^3} - \frac{3 \operatorname{asin}(ax)}{32a^4} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x),x)

[Out] Piecewise((x**4*asin(a*x)/4 + x**3*sqrt(-a**2*x**2 + 1)/(16*a) + 3*x*sqrt(-a**2*x**2 + 1)/(32*a**3) - 3*asin(a*x)/(32*a**4), Ne(a, 0)), (0, True))

Giac [A] time = 1.44762, size = 113, normalized size = 1.64

$$-\frac{(-a^2 x^2 + 1)^{\frac{3}{2}} x}{16 a^3} + \frac{(a^2 x^2 - 1)^2 \operatorname{arcsin}(ax)}{4 a^4} + \frac{5 \sqrt{-a^2 x^2 + 1} x}{32 a^3} + \frac{(a^2 x^2 - 1) \operatorname{arcsin}(ax)}{2 a^4} + \frac{5 \operatorname{arcsin}(ax)}{32 a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x),x, algorithm="giac")

[Out] -1/16*(-a^2*x^2 + 1)^(3/2)*x/a^3 + 1/4*(a^2*x^2 - 1)^2*arcsin(a*x)/a^4 + 5/32*sqrt(-a^2*x^2 + 1)*x/a^3 + 1/2*(a^2*x^2 - 1)*arcsin(a*x)/a^4 + 5/32*arcsin(a*x)/a^4

3.3 $\int x^2 \sin^{-1}(ax) dx$

Optimal. Leaf size=54

$$-\frac{(1-a^2x^2)^{3/2}}{9a^3} + \frac{\sqrt{1-a^2x^2}}{3a^3} + \frac{1}{3}x^3 \sin^{-1}(ax)$$

[Out] Sqrt[1 - a^2*x^2]/(3*a^3) - (1 - a^2*x^2)^(3/2)/(9*a^3) + (x^3*ArcSin[a*x])/3

Rubi [A] time = 0.034606, antiderivative size = 54, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {4627, 266, 43}

$$-\frac{(1-a^2x^2)^{3/2}}{9a^3} + \frac{\sqrt{1-a^2x^2}}{3a^3} + \frac{1}{3}x^3 \sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] Int[x^2*ArcSin[a*x],x]

[Out] Sqrt[1 - a^2*x^2]/(3*a^3) - (1 - a^2*x^2)^(3/2)/(9*a^3) + (x^3*ArcSin[a*x])/3

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 266

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned}
\int x^2 \sin^{-1}(ax) dx &= \frac{1}{3}x^3 \sin^{-1}(ax) - \frac{1}{3}a \int \frac{x^3}{\sqrt{1-a^2x^2}} dx \\
&= \frac{1}{3}x^3 \sin^{-1}(ax) - \frac{1}{6}a \operatorname{Subst} \left(\int \frac{x}{\sqrt{1-a^2x}} dx, x, x^2 \right) \\
&= \frac{1}{3}x^3 \sin^{-1}(ax) - \frac{1}{6}a \operatorname{Subst} \left(\int \left(\frac{1}{a^2\sqrt{1-a^2x}} - \frac{\sqrt{1-a^2x}}{a^2} \right) dx, x, x^2 \right) \\
&= \frac{\sqrt{1-a^2x^2}}{3a^3} - \frac{(1-a^2x^2)^{3/2}}{9a^3} + \frac{1}{3}x^3 \sin^{-1}(ax)
\end{aligned}$$

Mathematica [A] time = 0.0249748, size = 41, normalized size = 0.76

$$\frac{1}{9} \left(\frac{\sqrt{1-a^2x^2}(a^2x^2+2)}{a^3} + 3x^3 \sin^{-1}(ax) \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*ArcSin[a*x],x]

[Out] ((Sqrt[1 - a^2*x^2]*(2 + a^2*x^2))/a^3 + 3*x^3*ArcSin[a*x])/9

Maple [A] time = 0.003, size = 52, normalized size = 1.

$$\frac{1}{a^3} \left(\frac{a^3 x^3 \arcsin(ax)}{3} + \frac{a^2 x^2}{9} \sqrt{-a^2 x^2 + 1} + \frac{2}{9} \sqrt{-a^2 x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*arcsin(a*x),x)

[Out] 1/a^3*(1/3*a^3*x^3*arcsin(a*x)+1/9*a^2*x^2*(-a^2*x^2+1)^(1/2)+2/9*(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.70877, size = 68, normalized size = 1.26

$$\frac{1}{3}x^3 \arcsin(ax) + \frac{1}{9}a \left(\frac{\sqrt{-a^2x^2+1}x^2}{a^2} + \frac{2\sqrt{-a^2x^2+1}}{a^4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x),x, algorithm="maxima")

[Out] 1/3*x^3*arcsin(a*x) + 1/9*a*(sqrt(-a^2*x^2 + 1)*x^2/a^2 + 2*sqrt(-a^2*x^2 + 1)/a^4)

Fricas [A] time = 2.13791, size = 92, normalized size = 1.7

$$\frac{3a^3x^3 \arcsin(ax) + (a^2x^2 + 2)\sqrt{-a^2x^2 + 1}}{9a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x²*arcsin(a*x),x, algorithm="fricas")

[Out] 1/9*(3*a³*x³*arcsin(a*x) + (a²*x² + 2)*sqrt(-a²*x² + 1))/a³

Sympy [A] time = 0.819754, size = 48, normalized size = 0.89

$$\begin{cases} \frac{x^3 \operatorname{asin}(ax)}{3} + \frac{x^2 \sqrt{-a^2 x^2 + 1}}{9a} + \frac{2\sqrt{-a^2 x^2 + 1}}{9a^3} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*asin(a*x),x)

[Out] Piecewise((x**3*asin(a*x)/3 + x**2*sqrt(-a**2*x**2 + 1)/(9*a) + 2*sqrt(-a**2*x**2 + 1)/(9*a**3), Ne(a, 0)), (0, True))

Giac [A] time = 1.30279, size = 86, normalized size = 1.59

$$\frac{(a^2 x^2 - 1)x \arcsin(ax)}{3a^2} + \frac{x \arcsin(ax)}{3a^2} - \frac{(-a^2 x^2 + 1)^{\frac{3}{2}}}{9a^3} + \frac{\sqrt{-a^2 x^2 + 1}}{3a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x²*arcsin(a*x),x, algorithm="giac")

[Out] 1/3*(a²*x² - 1)*x*arcsin(a*x)/a² + 1/3*x*arcsin(a*x)/a² - 1/9*(-a²*x² + 1)^(3/2)/a³ + 1/3*sqrt(-a²*x² + 1)/a³

3.4 $\int x \sin^{-1}(ax) dx$

Optimal. Leaf size=45

$$\frac{x\sqrt{1-a^2x^2}}{4a} - \frac{\sin^{-1}(ax)}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)$$

[Out] (x*Sqrt[1 - a^2*x^2])/(4*a) - ArcSin[a*x]/(4*a^2) + (x^2*ArcSin[a*x])/2

Rubi [A] time = 0.0158949, antiderivative size = 45, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 321, 216}

$$\frac{x\sqrt{1-a^2x^2}}{4a} - \frac{\sin^{-1}(ax)}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] Int[x*ArcSin[a*x], x]

[Out] (x*Sqrt[1 - a^2*x^2])/(4*a) - ArcSin[a*x]/(4*a^2) + (x^2*ArcSin[a*x])/2

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^n_.]*((d_.)*(x_.))^m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 321

Int[((c_.)*(x_.))^m_.]*((a_.) + (b_.)*(x_.)^n_)^p_.), x_Symbol] :> Simp[(c^(n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), Int[(c*x)^(m - n)*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n - 1] && NeQ[m + n*p + 1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int x \sin^{-1}(ax) dx &= \frac{1}{2}x^2 \sin^{-1}(ax) - \frac{1}{2}a \int \frac{x^2}{\sqrt{1-a^2x^2}} dx \\ &= \frac{x\sqrt{1-a^2x^2}}{4a} + \frac{1}{2}x^2 \sin^{-1}(ax) - \frac{\int \frac{1}{\sqrt{1-a^2x^2}} dx}{4a} \\ &= \frac{x\sqrt{1-a^2x^2}}{4a} - \frac{\sin^{-1}(ax)}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax) \end{aligned}$$

Mathematica [A] time = 0.0112639, size = 40, normalized size = 0.89

$$\frac{ax\sqrt{1-a^2x^2} + (2a^2x^2 - 1)\sin^{-1}(ax)}{4a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*ArcSin[a*x],x]

[Out] (a*x*Sqrt[1 - a^2*x^2] + (-1 + 2*a^2*x^2)*ArcSin[a*x])/(4*a^2)

Maple [A] time = 0.004, size = 40, normalized size = 0.9

$$\frac{1}{a^2} \left(\frac{a^2 x^2 \arcsin(ax)}{2} + \frac{ax}{4} \sqrt{-a^2 x^2 + 1} - \frac{\arcsin(ax)}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*arcsin(a*x),x)

[Out] 1/a^2*(1/2*a^2*x^2*arcsin(a*x)+1/4*a*x*(-a^2*x^2+1)^(1/2)-1/4*arcsin(a*x))

Maxima [A] time = 1.67149, size = 70, normalized size = 1.56

$$\frac{1}{2} x^2 \arcsin(ax) + \frac{1}{4} a \left(\frac{\sqrt{-a^2 x^2 + 1} x}{a^2} - \frac{\arcsin\left(\frac{a^2 x}{\sqrt{a^2}}\right)}{\sqrt{a^2} a^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x),x, algorithm="maxima")

[Out] 1/2*x^2*arcsin(a*x) + 1/4*a*(sqrt(-a^2*x^2 + 1)*x/a^2 - arcsin(a^2*x/sqrt(a^2)))/(sqrt(a^2)*a^2)

Fricas [A] time = 2.20046, size = 86, normalized size = 1.91

$$\frac{\sqrt{-a^2 x^2 + 1} a x + (2 a^2 x^2 - 1) \arcsin(ax)}{4 a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x),x, algorithm="fricas")

[Out] 1/4*(sqrt(-a^2*x^2 + 1)*a*x + (2*a^2*x^2 - 1)*arcsin(a*x))/a^2

Sympy [A] time = 0.345889, size = 37, normalized size = 0.82

$$\begin{cases} \frac{x^2 \operatorname{asin}(ax)}{2} + \frac{x\sqrt{-a^2 x^2 + 1}}{4a} - \frac{\operatorname{asin}(ax)}{4a^2} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*asin(a*x),x)

[Out] Piecewise((x**2*asin(a*x)/2 + x*sqrt(-a**2*x**2 + 1)/(4*a) - asin(a*x)/(4*a**2), Ne(a, 0)), (0, True))

Giac [A] time = 1.23908, size = 62, normalized size = 1.38

$$\frac{\sqrt{-a^2x^2 + 1}x}{4a} + \frac{(a^2x^2 - 1)\arcsin(ax)}{2a^2} + \frac{\arcsin(ax)}{4a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x),x, algorithm="giac")

[Out] 1/4*sqrt(-a^2*x^2 + 1)*x/a + 1/2*(a^2*x^2 - 1)*arcsin(a*x)/a^2 + 1/4*arcsin(a*x)/a^2

3.5 $\int \sin^{-1}(ax) dx$

Optimal. Leaf size=25

$$\frac{\sqrt{1-a^2x^2}}{a} + x \sin^{-1}(ax)$$

[Out] Sqrt[1 - a^2*x^2]/a + x*ArcSin[a*x]

Rubi [A] time = 0.0075506, antiderivative size = 25, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 4, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4619, 261}

$$\frac{\sqrt{1-a^2x^2}}{a} + x \sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x],x]

[Out] Sqrt[1 - a^2*x^2]/a + x*ArcSin[a*x]

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.), x_Symbol] :> Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 261

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(a + b*x^n)^(p + 1)/(b*n*(p + 1)), x] /; FreeQ[{a, b, m, n, p}, x] && EqQ[m, n - 1] && NeQ[p, -1]

Rubi steps

$$\begin{aligned} \int \sin^{-1}(ax) dx &= x \sin^{-1}(ax) - a \int \frac{x}{\sqrt{1-a^2x^2}} dx \\ &= \frac{\sqrt{1-a^2x^2}}{a} + x \sin^{-1}(ax) \end{aligned}$$

Mathematica [A] time = 0.0075927, size = 25, normalized size = 1.

$$\frac{\sqrt{1-a^2x^2}}{a} + x \sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x],x]

[Out] Sqrt[1 - a^2*x^2]/a + x*ArcSin[a*x]

Maple [A] time = 0.001, size = 25, normalized size = 1.

$$\frac{1}{a} \left(ax \arcsin(ax) + \sqrt{-a^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x),x)

[Out] 1/a*(a*x*arcsin(a*x)+(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.68877, size = 32, normalized size = 1.28

$$\frac{ax \arcsin(ax) + \sqrt{-a^2x^2 + 1}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x),x, algorithm="maxima")

[Out] (a*x*arcsin(a*x) + sqrt(-a^2*x^2 + 1))/a

Fricas [A] time = 2.10614, size = 57, normalized size = 2.28

$$\frac{ax \arcsin(ax) + \sqrt{-a^2x^2 + 1}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x),x, algorithm="fricas")

[Out] (a*x*arcsin(a*x) + sqrt(-a^2*x^2 + 1))/a

Sympy [A] time = 0.618542, size = 20, normalized size = 0.8

$$\begin{cases} x \arcsin(ax) + \frac{\sqrt{-a^2x^2+1}}{a} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x),x)

[Out] Piecewise((x*asin(a*x) + sqrt(-a**2*x**2 + 1))/a, Ne(a, 0)), (0, True))

Giac [A] time = 1.33051, size = 32, normalized size = 1.28

$$\frac{ax \arcsin(ax) + \sqrt{-a^2x^2 + 1}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x),x, algorithm="giac")
```

```
[Out] (a*x*arcsin(a*x) + sqrt(-a^2*x^2 + 1))/a
```

3.6 $\int \frac{\sin^{-1}(ax)}{x} dx$

Optimal. Leaf size=51

$$-\frac{1}{2}i\text{PolyLog}\left(2, e^{2i\sin^{-1}(ax)}\right) - \frac{1}{2}i\sin^{-1}(ax)^2 + \sin^{-1}(ax)\log\left(1 - e^{2i\sin^{-1}(ax)}\right)$$

[Out] $(-I/2)*\text{ArcSin}[a*x]^2 + \text{ArcSin}[a*x]*\text{Log}[1 - E^{\{(2*I)*\text{ArcSin}[a*x]\}}] - (I/2)*\text{PolyLog}[2, E^{\{(2*I)*\text{ArcSin}[a*x]\}}]$

Rubi [A] time = 0.0584378, antiderivative size = 51, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4625, 3717, 2190, 2279, 2391}

$$-\frac{1}{2}i\text{PolyLog}\left(2, e^{2i\sin^{-1}(ax)}\right) - \frac{1}{2}i\sin^{-1}(ax)^2 + \sin^{-1}(ax)\log\left(1 - e^{2i\sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]/x, x]$

[Out] $(-I/2)*\text{ArcSin}[a*x]^2 + \text{ArcSin}[a*x]*\text{Log}[1 - E^{\{(2*I)*\text{ArcSin}[a*x]\}}] - (I/2)*\text{PolyLog}[2, E^{\{(2*I)*\text{ArcSin}[a*x]\}}]$

Rule 4625

$\text{Int}[\{(a_.) + \text{ArcSin}[(c_.)*(x_.)]*(b_.)\}^{(n_.)}/(x_.), x_Symbol] \rightarrow \text{Subst}[\text{Int}[(a + b*x)^n/\text{Tan}[x], x], x, \text{ArcSin}[c*x]] \text{ /; FreeQ}\{a, b, c\}, x\} \&\& \text{IGtQ}[n, 0]$

Rule 3717

$\text{Int}[\{(c_.) + (d_.)*(x_.)\}^{(m_.)}*\text{tan}[(e_.) + \text{Pi}*(k_.) + (f_.)*(x_.)], x_Symbol] \rightarrow \text{Simp}[(I*(c + d*x)^{(m + 1)})/(d*(m + 1)), x] - \text{Dist}[2*I, \text{Int}[\{(c + d*x)^m * E^{\{(2*I*k*Pi) + 2*I*(e + f*x)\}}\}}/(1 + E^{\{(2*I*k*Pi) + 2*I*(e + f*x)\}}), x], x] \text{ /; FreeQ}\{c, d, e, f\}, x\} \&\& \text{IntegerQ}[4*k] \&\& \text{IGtQ}[m, 0]$

Rule 2190

$\text{Int}[\{(F_.)^{\{(g_.)*((e_.) + (f_.)*(x_.))\}}\}^{(n_.)}*\{(c_.) + (d_.)*(x_.)\}^{(m_.)}/\{(a_.) + (b_.)*\{(F_.)^{\{(g_.)*((e_.) + (f_.)*(x_.))\}}\}^{(n_.)}\}, x_Symbol] \rightarrow \text{Simp}[\{(c + d*x)^m * \text{Log}[1 + (b*(F^{\{(g*(e + f*x)\}})^n)/a)]/(b*f*g*n*\text{Log}[F]), x] - \text{Dist}[(d*m)/(b*f*g*n*\text{Log}[F]), \text{Int}[(c + d*x)^{(m - 1)}*\text{Log}[1 + (b*(F^{\{(g*(e + f*x)\}})^n)/a)], x], x] \text{ /; FreeQ}\{F, a, b, c, d, e, f, g, n\}, x\} \&\& \text{IGtQ}[m, 0]$

Rule 2279

$\text{Int}[\text{Log}[(a_.) + (b_.)*\{(F_.)^{\{(e_.)*((c_.) + (d_.)*(x_.))\}}\}^{(n_.)}], x_Symbol] \rightarrow \text{Dist}[1/(d*e*n*\text{Log}[F]), \text{Subst}[\text{Int}[\text{Log}[a + b*x]/x, x], x, (F^{\{(e*(c + d*x)\}})^n], x] \text{ /; FreeQ}\{F, a, b, c, d, e, n\}, x\} \&\& \text{GtQ}[a, 0]$

Rule 2391

$\text{Int}[\text{Log}[(c_.)*\{(d_.) + (e_.)*(x_.)^{(n_.)}\}]/(x_.), x_Symbol] \rightarrow -\text{Simp}[\text{PolyLog}[2, -(c*e*x^n)]/n, x] \text{ /; FreeQ}\{c, d, e, n\}, x\} \&\& \text{EqQ}[c*d, 1]$

Rubi steps

$$\begin{aligned}
\int \frac{\sin^{-1}(ax)}{x} dx &= \text{Subst} \left(\int x \cot(x) dx, x, \sin^{-1}(ax) \right) \\
&= -\frac{1}{2}i \sin^{-1}(ax)^2 - 2i \text{Subst} \left(\int \frac{e^{2ix}}{1 - e^{2ix}} dx, x, \sin^{-1}(ax) \right) \\
&= -\frac{1}{2}i \sin^{-1}(ax)^2 + \sin^{-1}(ax) \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - \text{Subst} \left(\int \log(1 - e^{2ix}) dx, x, \sin^{-1}(ax) \right) \\
&= -\frac{1}{2}i \sin^{-1}(ax)^2 + \sin^{-1}(ax) \log \left(1 - e^{2i \sin^{-1}(ax)} \right) + \frac{1}{2}i \text{Subst} \left(\int \frac{\log(1 - x)}{x} dx, x, e^{2i \sin^{-1}(ax)} \right) \\
&= -\frac{1}{2}i \sin^{-1}(ax)^2 + \sin^{-1}(ax) \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - \frac{1}{2}i \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right)
\end{aligned}$$

Mathematica [A] time = 0.0278319, size = 46, normalized size = 0.9

$$\sin^{-1}(ax) \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - \frac{1}{2}i \left(\sin^{-1}(ax)^2 + \text{PolyLog} \left(2, e^{2i \sin^{-1}(ax)} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]/x,x]

[Out] ArcSin[a*x]*Log[1 - E^((2*I)*ArcSin[a*x])] - (I/2)*(ArcSin[a*x]^2 + PolyLog[2, E^((2*I)*ArcSin[a*x])])

Maple [A] time = 0.158, size = 111, normalized size = 2.2

$$-\frac{i}{2} (\arcsin(ax))^2 + \arcsin(ax) \ln \left(1 - iax - \sqrt{-a^2x^2 + 1} \right) + \arcsin(ax) \ln \left(1 + iax + \sqrt{-a^2x^2 + 1} \right) - i \text{polylog} \left(2, -iax - \sqrt{-a^2x^2 + 1} \right) - i \text{polylog} \left(2, iax + \sqrt{-a^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)/x,x)

[Out] -1/2*I*arcsin(a*x)^2+arcsin(a*x)*ln(1-I*a*x-(-a^2*x^2+1)^(1/2))+arcsin(a*x)*ln(1+I*a*x+(-a^2*x^2+1)^(1/2))-I*polylog(2,-I*a*x-(-a^2*x^2+1)^(1/2))-I*polylog(2,I*a*x+(-a^2*x^2+1)^(1/2))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x,x, algorithm="maxima")

[Out] integrate(arcsin(a*x)/x, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{\arcsin(ax)}{x}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x,x, algorithm="fricas")

[Out] integral(arcsin(a*x)/x, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)/x,x)

[Out] Integral(asin(a*x)/x, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x,x, algorithm="giac")

[Out] integrate(arcsin(a*x)/x, x)

3.7 $\int \frac{\sin^{-1}(ax)}{x^2} dx$

Optimal. Leaf size=28

$$-a \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) - \frac{\sin^{-1}(ax)}{x}$$

[Out] -(ArcSin[a*x]/x) - a*ArcTanh[Sqrt[1 - a^2*x^2]]

Rubi [A] time = 0.0218774, antiderivative size = 28, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 266, 63, 208}

$$-a \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) - \frac{\sin^{-1}(ax)}{x}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]/x^2,x]

[Out] -(ArcSin[a*x]/x) - a*ArcTanh[Sqrt[1 - a^2*x^2]]

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 266

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[1/n, Subst[
Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b
, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sin^{-1}(ax)}{x^2} dx &= -\frac{\sin^{-1}(ax)}{x} + a \int \frac{1}{x\sqrt{1-a^2x^2}} dx \\
&= -\frac{\sin^{-1}(ax)}{x} + \frac{1}{2}a \operatorname{Subst}\left(\int \frac{1}{x\sqrt{1-a^2x}} dx, x, x^2\right) \\
&= -\frac{\sin^{-1}(ax)}{x} - \frac{\operatorname{Subst}\left(\int \frac{1}{\frac{1}{a^2} - \frac{x^2}{a^2}} dx, x, \sqrt{1-a^2x^2}\right)}{a} \\
&= -\frac{\sin^{-1}(ax)}{x} - a \tanh^{-1}\left(\sqrt{1-a^2x^2}\right)
\end{aligned}$$

Mathematica [A] time = 0.0023416, size = 28, normalized size = 1.

$$-a \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) - \frac{\sin^{-1}(ax)}{x}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]/x^2,x]

[Out] -(ArcSin[a*x]/x) - a*ArcTanh[Sqrt[1 - a^2*x^2]]

Maple [A] time = 0.003, size = 31, normalized size = 1.1

$$a\left(-\frac{\arcsin(ax)}{ax} - \operatorname{Artanh}\left(\frac{1}{\sqrt{-a^2x^2+1}}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)/x^2,x)

[Out] a*(-arcsin(a*x)/a/x-arctanh(1/(-a^2*x^2+1)^(1/2)))

Maxima [A] time = 1.62401, size = 53, normalized size = 1.89

$$-a \log\left(\frac{2\sqrt{-a^2x^2+1}}{|x|} + \frac{2}{|x|}\right) - \frac{\arcsin(ax)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^2,x, algorithm="maxima")

[Out] -a*log(2*sqrt(-a^2*x^2 + 1)/abs(x) + 2/abs(x)) - arcsin(a*x)/x

Fricas [A] time = 2.23544, size = 124, normalized size = 4.43

$$-\frac{ax \log\left(\sqrt{-a^2x^2+1}+1\right) - ax \log\left(\sqrt{-a^2x^2+1}-1\right) + 2 \arcsin(ax)}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)/x^2,x, algorithm="fricas")
```

```
[Out] -1/2*(a*x*log(sqrt(-a^2*x^2 + 1) + 1) - a*x*log(sqrt(-a^2*x^2 + 1) - 1) + 2*arcsin(a*x))/x
```

Sympy [C] time = 4.85904, size = 32, normalized size = 1.14

$$a \left(\begin{cases} -\operatorname{acosh}\left(\frac{1}{ax}\right) & \text{for } \frac{1}{|a^2x^2|} > 1 \\ i \operatorname{asin}\left(\frac{1}{ax}\right) & \text{otherwise} \end{cases} \right) - \frac{\operatorname{asin}(ax)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(asin(a*x)/x**2,x)
```

```
[Out] a*Piecewise((-acosh(1/(a*x)), 1/Abs(a**2*x**2) > 1), (I*asin(1/(a*x)), True)) - asin(a*x)/x
```

Giac [A] time = 1.47518, size = 65, normalized size = 2.32

$$-\frac{1}{2}a \left(\log\left(\sqrt{-a^2x^2 + 1} + 1\right) - \log\left(-\sqrt{-a^2x^2 + 1} + 1\right) \right) - \frac{\operatorname{arcsin}(ax)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)/x^2,x, algorithm="giac")
```

```
[Out] -1/2*a*(log(sqrt(-a^2*x^2 + 1) + 1) - log(-sqrt(-a^2*x^2 + 1) + 1)) - arcsin(a*x)/x
```

3.8 $\int \frac{\sin^{-1}(ax)}{x^3} dx$

Optimal. Leaf size=34

$$-\frac{a\sqrt{1-a^2x^2}}{2x} - \frac{\sin^{-1}(ax)}{2x^2}$$

[Out] $-(a\sqrt{1-a^2x^2})/(2x) - \text{ArcSin}[a*x]/(2*x^2)$

Rubi [A] time = 0.01436, antiderivative size = 34, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4627, 264}

$$-\frac{a\sqrt{1-a^2x^2}}{2x} - \frac{\sin^{-1}(ax)}{2x^2}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]/x^3,x]

[Out] $-(a\sqrt{1-a^2x^2})/(2x) - \text{ArcSin}[a*x]/(2*x^2)$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m+1)*(a + b*ArcSin[c*x])^n)/(d*(m+1)), x] - Dist[(b*c*n)/(d*(m+1)), Int[((d*x)^(m+1)*(a + b*ArcSin[c*x])^(n-1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 264

Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[((c*x)^(m+1)*(a + b*x^n)^(p+1))/(a*c*(m+1)), x] /; FreeQ[{a, b, c, m, n, p}, x] && EqQ[(m+1)/n + p + 1, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)}{x^3} dx &= -\frac{\sin^{-1}(ax)}{2x^2} + \frac{1}{2}a \int \frac{1}{x^2\sqrt{1-a^2x^2}} dx \\ &= -\frac{a\sqrt{1-a^2x^2}}{2x} - \frac{\sin^{-1}(ax)}{2x^2} \end{aligned}$$

Mathematica [A] time = 0.0071846, size = 29, normalized size = 0.85

$$-\frac{ax\sqrt{1-a^2x^2} + \sin^{-1}(ax)}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]/x^3,x]

[Out] $-(a*x*\sqrt{1-a^2*x^2} + \text{ArcSin}[a*x])/(2*x^2)$

Maple [A] time = 0.003, size = 38, normalized size = 1.1

$$a^2 \left(-\frac{\arcsin(ax)}{2a^2x^2} - \frac{1}{2ax} \sqrt{-a^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)/x^3,x)

[Out] a^2*(-1/2*arcsin(a*x)/a^2/x^2-1/2/a/x*(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.65813, size = 38, normalized size = 1.12

$$-\frac{\sqrt{-a^2x^2 + 1}a}{2x} - \frac{\arcsin(ax)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^3,x, algorithm="maxima")

[Out] -1/2*sqrt(-a^2*x^2 + 1)*a/x - 1/2*arcsin(a*x)/x^2

Fricas [A] time = 2.1906, size = 66, normalized size = 1.94

$$-\frac{\sqrt{-a^2x^2 + 1}ax + \arcsin(ax)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^3,x, algorithm="fricas")

[Out] -1/2*(sqrt(-a^2*x^2 + 1)*a*x + arcsin(a*x))/x^2

Sympy [C] time = 2.11402, size = 51, normalized size = 1.5

$$\frac{a \left(\begin{cases} -\frac{i\sqrt{a^2x^2-1}}{x} & \text{for } |a^2x^2| > 1 \\ -\frac{\sqrt{-a^2x^2+1}}{x} & \text{otherwise} \end{cases} \right)}{2} - \frac{\operatorname{asin}(ax)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)/x**3,x)

[Out] a*Piecewise((-I*sqrt(a**2*x**2 - 1)/x, Abs(a**2*x**2) > 1), (-sqrt(-a**2*x**2 + 1)/x, True))/2 - asin(a*x)/(2*x**2)

Giac [B] time = 1.28193, size = 92, normalized size = 2.71

$$\frac{1}{4} \left(\frac{a^4 x}{\left(\sqrt{-a^2 x^2 + 1} |a| + a \right) |a|} - \frac{\sqrt{-a^2 x^2 + 1} |a| + a}{x |a|} \right) a - \frac{\arcsin(ax)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^3,x, algorithm="giac")

[Out] 1/4*(a^4*x/((sqrt(-a^2*x^2 + 1)*abs(a) + a)*abs(a)) - (sqrt(-a^2*x^2 + 1)*abs(a) + a)/(x*abs(a)))*a - 1/2*arcsin(a*x)/x^2

3.9 $\int \frac{\sin^{-1}(ax)}{x^4} dx$

Optimal. Leaf size=56

$$-\frac{a\sqrt{1-a^2x^2}}{6x^2} - \frac{1}{6}a^3 \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) - \frac{\sin^{-1}(ax)}{3x^3}$$

[Out] $-(a\sqrt{1-a^2x^2})/(6x^2) - \text{ArcSin}[a*x]/(3x^3) - (a^3\text{ArcTanh}[\text{Sqrt}[1-a^2x^2]])/6$

Rubi [A] time = 0.0328187, antiderivative size = 56, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4627, 266, 51, 63, 208}

$$-\frac{a\sqrt{1-a^2x^2}}{6x^2} - \frac{1}{6}a^3 \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) - \frac{\sin^{-1}(ax)}{3x^3}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]/x^4,x]

[Out] $-(a\sqrt{1-a^2x^2})/(6x^2) - \text{ArcSin}[a*x]/(3x^3) - (a^3\text{ArcTanh}[\text{Sqrt}[1-a^2x^2]])/6$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m+1)*(a + b*ArcSin[c*x])^n)/(d*(m+1)), x] - Dist[(b*c*n)/(d*(m+1)), Int[((d*x)^(m+1)*(a + b*ArcSin[c*x])^(n-1))/Sqrt[1-c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 266

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Dist[1/n, Subst[Int[x^(Simplify[(m+1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m+1)/n]]

Rule 51

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[((a + b*x)^(m+1)*(c + d*x)^(n+1))/((b*c - a*d)*(m+1)), x] - Dist[(d*(m+n+2))/((b*c - a*d)*(m+1)), Int[(a + b*x)^(m+1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m-n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m+1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sin^{-1}(ax)}{x^4} dx &= -\frac{\sin^{-1}(ax)}{3x^3} + \frac{1}{3}a \int \frac{1}{x^3\sqrt{1-a^2x^2}} dx \\
&= -\frac{\sin^{-1}(ax)}{3x^3} + \frac{1}{6}a \operatorname{Subst}\left(\int \frac{1}{x^2\sqrt{1-a^2x}} dx, x, x^2\right) \\
&= -\frac{a\sqrt{1-a^2x^2}}{6x^2} - \frac{\sin^{-1}(ax)}{3x^3} + \frac{1}{12}a^3 \operatorname{Subst}\left(\int \frac{1}{x\sqrt{1-a^2x}} dx, x, x^2\right) \\
&= -\frac{a\sqrt{1-a^2x^2}}{6x^2} - \frac{\sin^{-1}(ax)}{3x^3} - \frac{1}{6}a \operatorname{Subst}\left(\int \frac{1}{\frac{1}{a^2} - \frac{x^2}{a^2}} dx, x, \sqrt{1-a^2x^2}\right) \\
&= -\frac{a\sqrt{1-a^2x^2}}{6x^2} - \frac{\sin^{-1}(ax)}{3x^3} - \frac{1}{6}a^3 \tanh^{-1}\left(\sqrt{1-a^2x^2}\right)
\end{aligned}$$

Mathematica [A] time = 0.0136419, size = 53, normalized size = 0.95

$$\frac{ax\sqrt{1-a^2x^2} + a^3x^3 \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) + 2 \sin^{-1}(ax)}{6x^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[ArcSin[a*x]/x^4, x]
```

```
[Out] -(a*x*Sqrt[1 - a^2*x^2] + 2*ArcSin[a*x] + a^3*x^3*ArcTanh[Sqrt[1 - a^2*x^2]
])/ (6*x^3)
```

Maple [A] time = 0.003, size = 53, normalized size = 1.

$$a^3 \left(-\frac{\arcsin(ax)}{3a^3x^3} - \frac{1}{6a^2x^2} \sqrt{-a^2x^2 + 1} - \frac{1}{6} \operatorname{Arctanh}\left(\frac{1}{\sqrt{-a^2x^2 + 1}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(arcsin(a*x)/x^4, x)
```

```
[Out] a^3*(-1/3*arcsin(a*x)/a^3/x^3-1/6/a^2/x^2*(-a^2*x^2+1)^(1/2)-1/6*arctanh(1/
(-a^2*x^2+1)^(1/2)))
```

Maxima [A] time = 1.73144, size = 81, normalized size = 1.45

$$-\frac{1}{6} \left(a^2 \log\left(\frac{2\sqrt{-a^2x^2+1}}{|x|} + \frac{2}{|x|}\right) + \frac{\sqrt{-a^2x^2+1}}{x^2} \right) a - \frac{\arcsin(ax)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)/x^4, x, algorithm="maxima")
```

[Out] $-1/6*(a^2*\log(2*\sqrt{-a^2*x^2 + 1})/abs(x) + 2/abs(x)) + \sqrt{-a^2*x^2 + 1}/x^2*a - 1/3*\arcsin(ax)/x^3$

Fricas [A] time = 2.74306, size = 176, normalized size = 3.14

$$\frac{a^3 x^3 \log\left(\sqrt{-a^2 x^2 + 1} + 1\right) - a^3 x^3 \log\left(\sqrt{-a^2 x^2 + 1} - 1\right) + 2\sqrt{-a^2 x^2 + 1} a x + 4 \arcsin(ax)}{12 x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)/x^4,x, algorithm="fricas")`

[Out] $-1/12*(a^3*x^3*\log(\sqrt{-a^2*x^2 + 1} + 1) - a^3*x^3*\log(\sqrt{-a^2*x^2 + 1} - 1) + 2*\sqrt{-a^2*x^2 + 1}*a*x + 4*\arcsin(ax))/x^3$

Sympy [A] time = 7.03483, size = 109, normalized size = 1.95

$$a \left(\begin{array}{l} \frac{a^2 \operatorname{acosh}\left(\frac{1}{ax}\right)}{2} - \frac{a\sqrt{-1+\frac{1}{a^2x^2}}}{2x} \quad \text{for } \frac{1}{|a^2x^2|} > 1 \\ \frac{ia^2 \operatorname{asin}\left(\frac{1}{ax}\right)}{2} - \frac{ia}{2x\sqrt{1-\frac{1}{a^2x^2}}} + \frac{i}{2ax^3\sqrt{1-\frac{1}{a^2x^2}}} \quad \text{otherwise} \end{array} \right) - \frac{\operatorname{asin}(ax)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(asin(a*x)/x**4,x)`

[Out] $a*\operatorname{Piecewise}\left(\left(-a**2*\operatorname{acosh}(1/(a*x))/2 - a*\sqrt{-1 + 1/(a**2*x**2)}\right)/(2*x), 1/\operatorname{Abs}(a**2*x**2) > 1\right), \left(I*a**2*\operatorname{asin}(1/(a*x))/2 - I*a/(2*x*\sqrt{1 - 1/(a**2*x**2)})\right) + I/(2*a*x**3*\sqrt{1 - 1/(a**2*x**2)})\right), \operatorname{True})/3 - \operatorname{asin}(a*x)/(3*x**3)$

Giac [A] time = 1.31479, size = 95, normalized size = 1.7

$$-\frac{1}{12} a^3 \left(\frac{2\sqrt{-a^2x^2 + 1}}{a^2x^2} + \log\left(\sqrt{-a^2x^2 + 1} + 1\right) - \log\left(-\sqrt{-a^2x^2 + 1} + 1\right) \right) - \frac{\arcsin(ax)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)/x^4,x, algorithm="giac")`

[Out] $-1/12*a^3*(2*\sqrt{-a^2*x^2 + 1}/(a^2*x^2) + \log(\sqrt{-a^2*x^2 + 1} + 1) - \log(-\sqrt{-a^2*x^2 + 1} + 1)) - 1/3*\arcsin(a*x)/x^3$

3.10 $\int \frac{\sin^{-1}(ax)}{x^5} dx$

Optimal. Leaf size=58

$$-\frac{a^3\sqrt{1-a^2x^2}}{6x} - \frac{a\sqrt{1-a^2x^2}}{12x^3} - \frac{\sin^{-1}(ax)}{4x^4}$$

[Out] $-(a*\text{Sqrt}[1 - a^2*x^2])/(12*x^3) - (a^3*\text{Sqrt}[1 - a^2*x^2])/(6*x) - \text{ArcSin}[a*x]/(4*x^4)$

Rubi [A] time = 0.0224819, antiderivative size = 58, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {4627, 271, 264}

$$-\frac{a^3\sqrt{1-a^2x^2}}{6x} - \frac{a\sqrt{1-a^2x^2}}{12x^3} - \frac{\sin^{-1}(ax)}{4x^4}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]/x^5,x]

[Out] $-(a*\text{Sqrt}[1 - a^2*x^2])/(12*x^3) - (a^3*\text{Sqrt}[1 - a^2*x^2])/(6*x) - \text{ArcSin}[a*x]/(4*x^4)$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((d_.)*(x_.))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 271

Int[(x_)^(m_)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(x^(m + 1)*(a + b*x^n)^(p + 1))/(a*(m + 1)), x] - Dist[(b*(m + n*(p + 1) + 1))/(a*(m + 1)), Int[x^(m + n)*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, m, n, p}, x] && ILtQ[Simplify[(m + 1)/n + p + 1], 0] && NeQ[m, -1]

Rule 264

Int[((c_.)*(x_.))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[((c*x)^(m + 1)*(a + b*x^n)^(p + 1))/(a*c*(m + 1)), x] /; FreeQ[{a, b, c, m, n, p}, x] && EqQ[(m + 1)/n + p + 1, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)}{x^5} dx &= -\frac{\sin^{-1}(ax)}{4x^4} + \frac{1}{4}a \int \frac{1}{x^4\sqrt{1-a^2x^2}} dx \\ &= -\frac{a\sqrt{1-a^2x^2}}{12x^3} - \frac{\sin^{-1}(ax)}{4x^4} + \frac{1}{6}a^3 \int \frac{1}{x^2\sqrt{1-a^2x^2}} dx \\ &= -\frac{a\sqrt{1-a^2x^2}}{12x^3} - \frac{a^3\sqrt{1-a^2x^2}}{6x} - \frac{\sin^{-1}(ax)}{4x^4} \end{aligned}$$

Mathematica [A] time = 0.0186953, size = 41, normalized size = 0.71

$$\frac{ax\sqrt{1-a^2x^2}(2a^2x^2+1)+3\sin^{-1}(ax)}{12x^4}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]/x^5,x]

[Out] -(a*x*Sqrt[1 - a^2*x^2]*(1 + 2*a^2*x^2) + 3*ArcSin[a*x])/(12*x^4)

Maple [A] time = 0.003, size = 58, normalized size = 1.

$$a^4 \left(-\frac{\arcsin(ax)}{4a^4x^4} - \frac{1}{12a^3x^3} \sqrt{-a^2x^2+1} - \frac{1}{6ax} \sqrt{-a^2x^2+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)/x^5,x)

[Out] a^4*(-1/4*arcsin(a*x)/a^4/x^4-1/12/a^3/x^3*(-a^2*x^2+1)^(1/2)-1/6/a/x*(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.65557, size = 68, normalized size = 1.17

$$-\frac{1}{12} \left(\frac{2\sqrt{-a^2x^2+1}a^2}{x} + \frac{\sqrt{-a^2x^2+1}}{x^3} \right) a - \frac{\arcsin(ax)}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^5,x, algorithm="maxima")

[Out] -1/12*(2*sqrt(-a^2*x^2 + 1)*a^2/x + sqrt(-a^2*x^2 + 1)/x^3)*a - 1/4*arcsin(a*x)/x^4

Fricas [A] time = 2.53501, size = 89, normalized size = 1.53

$$\frac{(2a^3x^3+ax)\sqrt{-a^2x^2+1}+3\arcsin(ax)}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^5,x, algorithm="fricas")

[Out] -1/12*((2*a^3*x^3 + a*x)*sqrt(-a^2*x^2 + 1) + 3*arcsin(a*x))/x^4

Sympy [A] time = 3.91116, size = 100, normalized size = 1.72

$$a \left(\begin{cases} \frac{-\frac{2ia^2\sqrt{a^2x^2-1}}{3x} - \frac{i\sqrt{a^2x^2-1}}{3x^3}}{\frac{3x}{3x} - \frac{\sqrt{-a^2x^2+1}}{3x^3}} & \text{for } |a^2x^2| > 1 \\ \frac{-\frac{2a^2\sqrt{-a^2x^2+1}}{3x} - \frac{\sqrt{-a^2x^2+1}}{3x^3}}{\frac{3x}{3x} - \frac{\sqrt{-a^2x^2+1}}{3x^3}} & \text{otherwise} \end{cases} \right) - \frac{\operatorname{asin}(ax)}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)/x**5,x)

[Out] a*Piecewise((-2*I*a**2*sqrt(a**2*x**2 - 1)/(3*x) - I*sqrt(a**2*x**2 - 1)/(3*x**3), Abs(a**2*x**2) > 1), (-2*a**2*sqrt(-a**2*x**2 + 1)/(3*x) - sqrt(-a**2*x**2 + 1)/(3*x**3), True))/4 - asin(a*x)/(4*x**4)

Giac [B] time = 1.35443, size = 176, normalized size = 3.03

$$\frac{1}{96} \left(\frac{\left(a^4 + \frac{9(\sqrt{-a^2x^2+1}|a|+a)^2}{x^2} \right) a^6 x^3}{\left(\sqrt{-a^2x^2+1}|a|+a \right)^3 |a|} - \frac{9(\sqrt{-a^2x^2+1}|a|+a)^4}{x} + \frac{(\sqrt{-a^2x^2+1}|a|+a)^3}{x^3} \right) a - \frac{\arcsin(ax)}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^5,x, algorithm="giac")

[Out] 1/96*((a^4 + 9*(sqrt(-a^2*x^2 + 1)*abs(a) + a)^2/x^2)*a^6*x^3/((sqrt(-a^2*x^2 + 1)*abs(a) + a)^3*abs(a)) - (9*(sqrt(-a^2*x^2 + 1)*abs(a) + a)*a^4/x + (sqrt(-a^2*x^2 + 1)*abs(a) + a)^3/x^3)/(a^2*abs(a)))*a - 1/4*arcsin(a*x)/x^4

3.11 $\int \frac{\sin^{-1}(ax)}{x^6} dx$

Optimal. Leaf size=80

$$-\frac{3a^3\sqrt{1-a^2x^2}}{40x^2} - \frac{a\sqrt{1-a^2x^2}}{20x^4} - \frac{3}{40}a^5 \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) - \frac{\sin^{-1}(ax)}{5x^5}$$

[Out] $-(a\sqrt{1-a^2x^2})/(20x^4) - (3a^3\sqrt{1-a^2x^2})/(40x^2) - \text{ArcSin}[a*x]/(5x^5) - (3a^5\text{ArcTanh}[\sqrt{1-a^2x^2}])/40$

Rubi [A] time = 0.0454824, antiderivative size = 80, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4627, 266, 51, 63, 208}

$$-\frac{3a^3\sqrt{1-a^2x^2}}{40x^2} - \frac{a\sqrt{1-a^2x^2}}{20x^4} - \frac{3}{40}a^5 \tanh^{-1}\left(\sqrt{1-a^2x^2}\right) - \frac{\sin^{-1}(ax)}{5x^5}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]/x^6,x]

[Out] $-(a\sqrt{1-a^2x^2})/(20x^4) - (3a^3\sqrt{1-a^2x^2})/(40x^2) - \text{ArcSin}[a*x]/(5x^5) - (3a^5\text{ArcTanh}[\sqrt{1-a^2x^2}])/40$

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 266

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Dist[1/n, Subst[
Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b
, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]
```

Rule 51

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> Simp[
((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(
m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x
] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ
[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && I
ntLinearQ[a, b, c, d, m, n, x]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] :> With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]

Rubi steps

$$\begin{aligned}
 \int \frac{\sin^{-1}(ax)}{x^6} dx &= -\frac{\sin^{-1}(ax)}{5x^5} + \frac{1}{5}a \int \frac{1}{x^5\sqrt{1-a^2x^2}} dx \\
 &= -\frac{\sin^{-1}(ax)}{5x^5} + \frac{1}{10}a \operatorname{Subst}\left(\int \frac{1}{x^3\sqrt{1-a^2x}} dx, x, x^2\right) \\
 &= -\frac{a\sqrt{1-a^2x^2}}{20x^4} - \frac{\sin^{-1}(ax)}{5x^5} + \frac{1}{40}(3a^3) \operatorname{Subst}\left(\int \frac{1}{x^2\sqrt{1-a^2x}} dx, x, x^2\right) \\
 &= -\frac{a\sqrt{1-a^2x^2}}{20x^4} - \frac{3a^3\sqrt{1-a^2x^2}}{40x^2} - \frac{\sin^{-1}(ax)}{5x^5} + \frac{1}{80}(3a^5) \operatorname{Subst}\left(\int \frac{1}{x\sqrt{1-a^2x}} dx, x, x^2\right) \\
 &= -\frac{a\sqrt{1-a^2x^2}}{20x^4} - \frac{3a^3\sqrt{1-a^2x^2}}{40x^2} - \frac{\sin^{-1}(ax)}{5x^5} - \frac{1}{40}(3a^3) \operatorname{Subst}\left(\int \frac{1}{\frac{1}{a^2} - \frac{x^2}{a^2}} dx, x, \sqrt{1-a^2x^2}\right) \\
 &= -\frac{a\sqrt{1-a^2x^2}}{20x^4} - \frac{3a^3\sqrt{1-a^2x^2}}{40x^2} - \frac{\sin^{-1}(ax)}{5x^5} - \frac{3}{40}a^5 \tanh^{-1}\left(\sqrt{1-a^2x^2}\right)
 \end{aligned}$$

Mathematica [C] time = 0.0126055, size = 51, normalized size = 0.64

$$-\frac{1}{5}a^5\sqrt{1-a^2x^2}\operatorname{Hypergeometric2F1}\left(\frac{1}{2}, 3, \frac{3}{2}, 1-a^2x^2\right) - \frac{\sin^{-1}(ax)}{5x^5}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]/x^6, x]

[Out] -ArcSin[a*x]/(5*x^5) - (a^5*Sqrt[1 - a^2*x^2]*Hypergeometric2F1[1/2, 3, 3/2, 1 - a^2*x^2])/5

Maple [A] time = 0.004, size = 73, normalized size = 0.9

$$a^5\left(-\frac{\arcsin(ax)}{5a^5x^5} - \frac{1}{20a^4x^4}\sqrt{-a^2x^2+1} - \frac{3}{40a^2x^2}\sqrt{-a^2x^2+1} - \frac{3}{40}\operatorname{Arctanh}\left(\frac{1}{\sqrt{-a^2x^2+1}}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)/x^6, x)

[Out] a^5*(-1/5*arcsin(a*x)/a^5/x^5-1/20/a^4/x^4*(-a^2*x^2+1)^(1/2)-3/40/a^2/x^2*(-a^2*x^2+1)^(1/2)-3/40*arctanh(1/(-a^2*x^2+1)^(1/2)))

Maxima [A] time = 1.76392, size = 111, normalized size = 1.39

$$-\frac{1}{40}\left(3a^4\log\left(\frac{2\sqrt{-a^2x^2+1}}{|x|} + \frac{2}{|x|}\right) + \frac{3\sqrt{-a^2x^2+1}a^2}{x^2} + \frac{2\sqrt{-a^2x^2+1}}{x^4}\right)a - \frac{\arcsin(ax)}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^6,x, algorithm="maxima")

[Out] $-1/40*(3*a^4*\log(2*\sqrt{-a^2*x^2 + 1})/abs(x) + 2/abs(x)) + 3*\sqrt{-a^2*x^2 + 1}*a^2/x^2 + 2*\sqrt{-a^2*x^2 + 1}/x^4)*a - 1/5*arcsin(a*x)/x^5$

Fricas [A] time = 2.79369, size = 204, normalized size = 2.55

$$\frac{3a^5x^5 \log\left(\sqrt{-a^2x^2 + 1} + 1\right) - 3a^5x^5 \log\left(\sqrt{-a^2x^2 + 1} - 1\right) + 2\left(3a^3x^3 + 2ax\right)\sqrt{-a^2x^2 + 1} + 16 \arcsin(ax)}{80x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^6,x, algorithm="fricas")

[Out] $-1/80*(3*a^5*x^5*\log(\sqrt{-a^2*x^2 + 1} + 1) - 3*a^5*x^5*\log(\sqrt{-a^2*x^2 + 1} - 1) - 1) + 2*(3*a^3*x^3 + 2*a*x)*\sqrt{-a^2*x^2 + 1} + 16*arcsin(a*x))/x^5$

Sympy [A] time = 24.0507, size = 182, normalized size = 2.28

$$a \left(\begin{array}{l} \left(\frac{3a^4 \operatorname{acosh}\left(\frac{1}{ax}\right)}{8} + \frac{3a^3}{8x\sqrt{-1+\frac{1}{a^2x^2}}} - \frac{a}{8x^3\sqrt{-1+\frac{1}{a^2x^2}}} - \frac{1}{4ax^5\sqrt{-1+\frac{1}{a^2x^2}}} \right) \text{ for } \frac{1}{|a^2x^2|} > 1 \\ \left(\frac{3ia^4 \operatorname{asin}\left(\frac{1}{ax}\right)}{8} - \frac{3ia^3}{8x\sqrt{1-\frac{1}{a^2x^2}}} + \frac{ia}{8x^3\sqrt{1-\frac{1}{a^2x^2}}} + \frac{i}{4ax^5\sqrt{1-\frac{1}{a^2x^2}}} \right) \text{ otherwise} \end{array} \right) - \frac{\operatorname{asin}(ax)}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)/x**6,x)

[Out] $a*\operatorname{Piecewise}\left(\left(-3*a**4*\operatorname{acosh}\left(1/\left(a*x\right)\right)/8 + 3*a**3/\left(8*x*\sqrt{-1 + 1/\left(a**2*x**2\right)}\right) - a/\left(8*x**3*\sqrt{-1 + 1/\left(a**2*x**2\right)}\right) - 1/\left(4*a*x**5*\sqrt{-1 + 1/\left(a**2*x**2\right)}\right)\right), 1/\operatorname{Abs}\left(a**2*x**2\right) > 1\right), \left(3*I*a**4*\operatorname{asin}\left(1/\left(a*x\right)\right)/8 - 3*I*a**3/\left(8*x*\sqrt{1 - 1/\left(a**2*x**2\right)}\right) + I*a/\left(8*x**3*\sqrt{1 - 1/\left(a**2*x**2\right)}\right) + I/\left(4*a*x**5*\sqrt{1 - 1/\left(a**2*x**2\right)}\right)\right), \operatorname{True}\right)/5 - \operatorname{asin}\left(a*x\right)/\left(5*x**5\right)$

Giac [A] time = 1.30165, size = 120, normalized size = 1.5

$$\frac{1}{80} a^5 \left(\frac{2 \left(3 \left(-a^2 x^2 + 1 \right)^{\frac{3}{2}} - 5 \sqrt{-a^2 x^2 + 1} \right)}{a^4 x^4} - 3 \log \left(\sqrt{-a^2 x^2 + 1} + 1 \right) + 3 \log \left(-\sqrt{-a^2 x^2 + 1} + 1 \right) \right) - \frac{\arcsin(ax)}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)/x^6,x, algorithm="giac")

[Out] $1/80*a^5*(2*(3*(-a^2*x^2 + 1)^(3/2) - 5*\sqrt{-a^2*x^2 + 1})/(a^4*x^4) - 3*\log(\sqrt{-a^2*x^2 + 1} + 1) + 3*\log(-\sqrt{-a^2*x^2 + 1} + 1)) - 1/5*arcsin(a*x)/x^5$

3.12 $\int x^4 \sin^{-1}(ax)^2 dx$

Optimal. Leaf size=120

$$-\frac{8x^3}{225a^2} + \frac{2x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)}{25a} + \frac{8x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{75a^3} + \frac{16\sqrt{1-a^2x^2}\sin^{-1}(ax)}{75a^5} - \frac{16x}{75a^4} + \frac{1}{5}x^5\sin^{-1}(ax)^2 - \frac{2x^5}{125}$$

[Out] $(-16*x)/(75*a^4) - (8*x^3)/(225*a^2) - (2*x^5)/125 + (16*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(75*a^5) + (8*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(75*a^3) + (2*x^4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(25*a) + (x^5*\text{ArcSin}[a*x]^2)/5$

Rubi [A] time = 0.193986, antiderivative size = 120, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4707, 4677, 8, 30}

$$-\frac{8x^3}{225a^2} + \frac{2x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)}{25a} + \frac{8x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{75a^3} + \frac{16\sqrt{1-a^2x^2}\sin^{-1}(ax)}{75a^5} - \frac{16x}{75a^4} + \frac{1}{5}x^5\sin^{-1}(ax)^2 - \frac{2x^5}{125}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^4*\text{ArcSin}[a*x]^2, x]$

[Out] $(-16*x)/(75*a^4) - (8*x^3)/(225*a^2) - (2*x^5)/125 + (16*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(75*a^5) + (8*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(75*a^3) + (2*x^4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(25*a) + (x^5*\text{ArcSin}[a*x]^2)/5$

Rule 4627

$\text{Int}[(a_.) + \text{ArcSin}[c_.*(x_.)]*(b_.)]^{(n_.)}*((d_.)*(x_.))^{(m_.)}, x_Symbol]$
 $:= \text{Simp}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}]/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

$\text{Int}[(a_.) + \text{ArcSin}[c_.*(x_.)]*(b_.)]^{(n_.)}*((f_.)*(x_.))^{(m_.)}/\text{Sqrt}[(d_.) + (e_.)*(x_.)^2], x_Symbol]$
 $:= \text{Simp}[(f*(f*x))^{(m-1)}*\text{Sqrt}[d + e*x^2]*(a + b*\text{ArcSin}[c*x])^n/(e*m), x] + (\text{Dist}[(f^2*(m-1))/(c^2*m), \text{Int}[(f*x)^{(m-2)}*(a + b*\text{ArcSin}[c*x])^n]/\text{Sqrt}[d + e*x^2], x], x] + \text{Dist}[(b*f*n*\text{Sqrt}[1 - c^2*x^2])/(c*m*\text{Sqrt}[d + e*x^2]), \text{Int}[(f*x)^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}, x], x]) /;$ FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

$\text{Int}[(a_.) + \text{ArcSin}[c_.*(x_.)]*(b_.)]^{(n_.)}*(x_.)*((d_.) + (e_.)*(x_.)^2)^{(p_.)}, x_Symbol]$
 $:= \text{Simp}[(d + e*x^2)^{(p+1)}*(a + b*\text{ArcSin}[c*x])^n/(2*e*(p+1)), x] + \text{Dist}[(b*n*d*\text{IntPart}[p]*(d + e*x^2)^{\text{FracPart}[p]})/(2*c*(p+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(1 - c^2*x^2)^{(p+1/2)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 8

$\text{Int}[a_, x_Symbol] := \text{Simp}[a*x, x] /;$ FreeQ[a, x]

Rule 30

`Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]`

Rubi steps

$$\begin{aligned}
 \int x^4 \sin^{-1}(ax)^2 dx &= \frac{1}{5}x^5 \sin^{-1}(ax)^2 - \frac{1}{5}(2a) \int \frac{x^5 \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\
 &= \frac{2x^4 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^2 - \frac{2 \int x^4 dx}{25} - \frac{8 \int \frac{x^3 \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx}{25a} \\
 &= -\frac{2x^5}{125} + \frac{8x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{75a^3} + \frac{2x^4 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^2 - \frac{16 \int \frac{x \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx}{75a^3} \\
 &= -\frac{8x^3}{225a^2} - \frac{2x^5}{125} + \frac{16\sqrt{1-a^2x^2} \sin^{-1}(ax)}{75a^5} + \frac{8x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{75a^3} + \frac{2x^4 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^2 \\
 &= -\frac{16x}{75a^4} - \frac{8x^3}{225a^2} - \frac{2x^5}{125} + \frac{16\sqrt{1-a^2x^2} \sin^{-1}(ax)}{75a^5} + \frac{8x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{75a^3} + \frac{2x^4 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^2
 \end{aligned}$$

Mathematica [A] time = 0.0336199, size = 82, normalized size = 0.68

$$\frac{-2ax(9a^4x^4 + 20a^2x^2 + 120) + 225a^5x^5 \sin^{-1}(ax)^2 + 30\sqrt{1-a^2x^2}(3a^4x^4 + 4a^2x^2 + 8) \sin^{-1}(ax)}{1125a^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*ArcSin[a*x]^2,x]

[Out] (-2*a*x*(120 + 20*a^2*x^2 + 9*a^4*x^4) + 30*Sqrt[1 - a^2*x^2]*(8 + 4*a^2*x^2 + 3*a^4*x^4)*ArcSin[a*x] + 225*a^5*x^5*ArcSin[a*x]^2)/(1125*a^5)

Maple [A] time = 0.126, size = 76, normalized size = 0.6

$$\frac{1}{a^5} \left(\frac{a^5 x^5 (\arcsin(ax))^2}{5} + \frac{2 \arcsin(ax) (3a^4 x^4 + 4a^2 x^2 + 8)}{75} \sqrt{-a^2 x^2 + 1} - \frac{2a^5 x^5}{125} - \frac{8a^3 x^3}{225} - \frac{16ax}{75} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*arcsin(a*x)^2,x)

[Out] 1/a^5*(1/5*a^5*x^5*arcsin(a*x)^2+2/75*arcsin(a*x)*(3*a^4*x^4+4*a^2*x^2+8)*(-a^2*x^2+1)^(1/2)-2/125*a^5*x^5-8/225*a^3*x^3-16/75*a*x)

Maxima [A] time = 1.67013, size = 138, normalized size = 1.15

$$\frac{1}{5}x^5 \arcsin(ax)^2 + \frac{2}{75} \left(\frac{3\sqrt{-a^2x^2+1}x^4}{a^2} + \frac{4\sqrt{-a^2x^2+1}x^2}{a^4} + \frac{8\sqrt{-a^2x^2+1}}{a^6} \right) a \arcsin(ax) - \frac{2(9a^4x^5 + 20a^2x^3 + 120ax)}{1125a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^2,x, algorithm="maxima")

[Out] $\frac{1}{5}x^5\arcsin(ax)^2 + \frac{2}{75}(3\sqrt{-a^2x^2 + 1})x^4/a^2 + 4\sqrt{-a^2x^2 + 1}x^2/a^4 + 8\sqrt{-a^2x^2 + 1}/a^6)a\arcsin(ax) - \frac{2}{1125}(9a^4x^5 + 20a^2x^3 + 120x)/a^4$

Fricas [A] time = 2.42754, size = 189, normalized size = 1.58

$$\frac{225 a^5 x^5 \arcsin(ax)^2 - 18 a^5 x^5 - 40 a^3 x^3 + 30 (3 a^4 x^4 + 4 a^2 x^2 + 8) \sqrt{-a^2 x^2 + 1} \arcsin(ax) - 240 a x}{1125 a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^2,x, algorithm="fricas")

[Out] $\frac{1}{1125}(225a^5x^5\arcsin(ax)^2 - 18a^5x^5 - 40a^3x^3 + 30(3a^4x^4 + 4a^2x^2 + 8)\sqrt{-a^2x^2 + 1}\arcsin(ax) - 240ax)/a^5$

Sympy [A] time = 7.61404, size = 114, normalized size = 0.95

$$\begin{cases} \frac{x^5 \arcsin^2(ax)}{5} - \frac{2x^5}{125} + \frac{2x^4 \sqrt{-a^2x^2+1} \arcsin(ax)}{25a} - \frac{8x^3}{225a^2} + \frac{8x^2 \sqrt{-a^2x^2+1} \arcsin(ax)}{75a^3} - \frac{16x}{75a^4} + \frac{16 \sqrt{-a^2x^2+1} \arcsin(ax)}{75a^5} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4*asin(a*x)**2,x)

[Out] Piecewise((x**5*asin(a*x)**2/5 - 2*x**5/125 + 2*x**4*sqrt(-a**2*x**2 + 1)*asin(a*x)/(25*a) - 8*x**3/(225*a**2) + 8*x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)/(75*a**3) - 16*x/(75*a**4) + 16*sqrt(-a**2*x**2 + 1)*asin(a*x)/(75*a**5), Ne(a, 0)), (0, True))

Giac [A] time = 1.34402, size = 228, normalized size = 1.9

$$\frac{(a^2x^2 - 1)^2 x \arcsin(ax)^2}{5a^4} + \frac{2(a^2x^2 - 1)x \arcsin(ax)^2}{5a^4} - \frac{2(a^2x^2 - 1)^2 x}{125a^4} + \frac{x \arcsin(ax)^2}{5a^4} + \frac{2(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1} \arcsin(ax)}{25a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^2,x, algorithm="giac")

[Out] $\frac{1}{5}(a^2x^2 - 1)^2x\arcsin(ax)^2/a^4 + \frac{2}{5}(a^2x^2 - 1)x\arcsin(ax)^2/a^4 - \frac{2}{125}(a^2x^2 - 1)^2x/a^4 + \frac{1}{5}x\arcsin(ax)^2/a^4 + \frac{2}{25}(a^2x^2 - 1)^2\sqrt{-a^2x^2 + 1}\arcsin(ax)/a^5 - \frac{76}{1125}(a^2x^2 - 1)x/a^4 - \frac{4}{15}(-a^2x^2 + 1)^{3/2}\arcsin(ax)/a^5 - \frac{298}{1125}x/a^4 + \frac{2}{5}\sqrt{-a^2x^2 + 1}\arcsin(ax)/a^5$

3.13 $\int x^3 \sin^{-1}(ax)^2 dx$

Optimal. Leaf size=98

$$-\frac{3x^2}{32a^2} + \frac{x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{8a} + \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)}{16a^3} - \frac{3\sin^{-1}(ax)^2}{32a^4} + \frac{1}{4}x^4\sin^{-1}(ax)^2 - \frac{x^4}{32}$$

[Out] $(-3*x^2)/(32*a^2) - x^4/32 + (3*x*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(16*a^3) + (x^3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(8*a) - (3*\text{ArcSin}[a*x]^2)/(32*a^4) + (x^4*\text{ArcSin}[a*x]^2)/4$

Rubi [A] time = 0.162577, antiderivative size = 98, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4627, 4707, 4641, 30}

$$-\frac{3x^2}{32a^2} + \frac{x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{8a} + \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)}{16a^3} - \frac{3\sin^{-1}(ax)^2}{32a^4} + \frac{1}{4}x^4\sin^{-1}(ax)^2 - \frac{x^4}{32}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*\text{ArcSin}[a*x]^2, x]$

[Out] $(-3*x^2)/(32*a^2) - x^4/32 + (3*x*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(16*a^3) + (x^3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(8*a) - (3*\text{ArcSin}[a*x]^2)/(32*a^4) + (x^4*\text{ArcSin}[a*x]^2)/4$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(d*x)^m, x_Symbol] \rightarrow \text{Simp}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}]/\text{Sqrt}[1 - c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 4707

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(f*x)^m/\text{Sqrt}[d + e*x^2] + (e*x)^2, x_Symbol] \rightarrow \text{Simp}[(f*(f*x)^{m-1}*\text{Sqrt}[d + e*x^2]*(a + b*\text{ArcSin}[c*x])^n)/(e*m), x] + (\text{Dist}[(f^2*(m-1))/(c^2*m), \text{Int}[(f*x)^{m-2}*(a + b*\text{ArcSin}[c*x])^n]/\text{Sqrt}[d + e*x^2], x], x] + \text{Dist}[(b*f*n*\text{Sqrt}[1 - c^2*x^2])/(c*m*\text{Sqrt}[d + e*x^2]), \text{Int}[(f*x)^{m-1}*(a + b*\text{ArcSin}[c*x])^{n-1}], x], x) /; \text{FreeQ}\{a, b, c, d, e, f\}, x \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{GtQ}[m, 1] \ \&\& \ \text{IntegerQ}[m]$

Rule 4641

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n/\text{Sqrt}[d + (e*x)^2], x_Symbol] \rightarrow \text{Simp}[(a + b*\text{ArcSin}[c*x])^{n+1}/(b*c*\text{Sqrt}[d]*(n+1)), x] /; \text{FreeQ}\{a, b, c, d, e, n\}, x \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[d, 0] \ \&\& \ \text{NeQ}[n, -1]$

Rule 30

$\text{Int}[x^m, x_Symbol] \rightarrow \text{Simp}[x^{m+1}/(m+1), x] /; \text{FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned}
\int x^3 \sin^{-1}(ax)^2 dx &= \frac{1}{4}x^4 \sin^{-1}(ax)^2 - \frac{1}{2}a \int \frac{x^4 \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\
&= \frac{x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{8a} + \frac{1}{4}x^4 \sin^{-1}(ax)^2 - \frac{\int x^3 dx}{8} - \frac{3 \int \frac{x^2 \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx}{8a} \\
&= -\frac{x^4}{32} + \frac{3x \sqrt{1-a^2x^2} \sin^{-1}(ax)}{16a^3} + \frac{x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{8a} + \frac{1}{4}x^4 \sin^{-1}(ax)^2 - \frac{3 \int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx}{16a^3} - \frac{3 \int x}{16a^3} \\
&= -\frac{3x^2}{32a^2} - \frac{x^4}{32} + \frac{3x \sqrt{1-a^2x^2} \sin^{-1}(ax)}{16a^3} + \frac{x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{8a} - \frac{3 \sin^{-1}(ax)^2}{32a^4} + \frac{1}{4}x^4 \sin^{-1}(ax)^2
\end{aligned}$$

Mathematica [A] time = 0.0289285, size = 74, normalized size = 0.76

$$\frac{-a^2x^2(a^2x^2+3)+2ax\sqrt{1-a^2x^2}(2a^2x^2+3)\sin^{-1}(ax)+(8a^4x^4-3)\sin^{-1}(ax)^2}{32a^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*ArcSin[a*x]^2,x]

[Out] $(-a^2x^2(3+a^2x^2)+2ax\sqrt{1-a^2x^2}(3+2a^2x^2)\text{ArcSin}[ax]+(-3+8a^4x^4)\text{ArcSin}[ax]^2)/(32a^4)$

Maple [A] time = 0.063, size = 93, normalized size = 1.

$$\frac{1}{a^4} \left(\frac{a^4x^4(\arcsin(ax))^2}{4} - \frac{\arcsin(ax)}{16} \left(-2a^3x^3\sqrt{-a^2x^2+1} - 3ax\sqrt{-a^2x^2+1} + 3\arcsin(ax) \right) + \frac{3(\arcsin(ax))^2}{32} - \frac{a^4x^4}{32} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x)^2,x)

[Out] $1/a^4*(1/4*a^4*x^4*arcsin(a*x)^2-1/16*arcsin(a*x)*(-2*a^3*x^3*(-a^2*x^2+1)^(1/2)-3*a*x*(-a^2*x^2+1)^(1/2)+3*arcsin(a*x))+3/32*arcsin(a*x)^2-1/32*a^4*x^4-3/32*a^2*x^2)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{4}x^4 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right) + a \int \frac{\sqrt{ax+1}\sqrt{-ax+1}x^4 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)}{2(a^2x^2-1)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^2,x, algorithm="maxima")

[Out] $1/4*x^4*arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1})^2 + a*integrate(1/2*\sqrt{a*x+1}*\sqrt{-a*x+1}*x^4*arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1})/(a^2*x^2-1), x)$

Fricas [A] time = 2.40165, size = 162, normalized size = 1.65

$$\frac{a^4 x^4 + 3 a^2 x^2 - (8 a^4 x^4 - 3) \arcsin(ax)^2 - 2(2 a^3 x^3 + 3 a x) \sqrt{-a^2 x^2 + 1} \arcsin(ax)}{32 a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^2,x, algorithm="fricas")

[Out] -1/32*(a^4*x^4 + 3*a^2*x^2 - (8*a^4*x^4 - 3)*arcsin(a*x)^2 - 2*(2*a^3*x^3 + 3*a*x)*sqrt(-a^2*x^2 + 1)*arcsin(a*x))/a^4

Sympy [A] time = 4.84024, size = 90, normalized size = 0.92

$$\begin{cases} \frac{x^4 \operatorname{asin}^2(ax)}{4} - \frac{x^4}{32} + \frac{x^3 \sqrt{-a^2 x^2 + 1} \operatorname{asin}(ax)}{8a} - \frac{3x^2}{32a^2} + \frac{3x \sqrt{-a^2 x^2 + 1} \operatorname{asin}(ax)}{16a^3} - \frac{3 \operatorname{asin}^2(ax)}{32a^4} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x)**2,x)

[Out] Piecewise((x**4*asin(a*x)**2/4 - x**4/32 + x**3*sqrt(-a**2*x**2 + 1)*asin(a*x)/(8*a) - 3*x**2/(32*a**2) + 3*x*sqrt(-a**2*x**2 + 1)*asin(a*x)/(16*a**3) - 3*asin(a*x)**2/(32*a**4), Ne(a, 0)), (0, True))

Giac [A] time = 1.22945, size = 180, normalized size = 1.84

$$-\frac{(-a^2 x^2 + 1)^{\frac{3}{2}} x \arcsin(ax)}{8 a^3} + \frac{(a^2 x^2 - 1)^2 \arcsin(ax)^2}{4 a^4} + \frac{5 \sqrt{-a^2 x^2 + 1} x \arcsin(ax)}{16 a^3} + \frac{(a^2 x^2 - 1) \arcsin(ax)^2}{2 a^4} - \frac{(a^2 x^2 - 1) \arcsin(ax)}{32 a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^2,x, algorithm="giac")

[Out] -1/8*(-a^2*x^2 + 1)^(3/2)*x*arcsin(a*x)/a^3 + 1/4*(a^2*x^2 - 1)^2*arcsin(a*x)^2/a^4 + 5/16*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)/a^3 + 1/2*(a^2*x^2 - 1)*arcsin(a*x)^2/a^4 - 1/32*(a^2*x^2 - 1)^2/a^4 + 5/32*arcsin(a*x)^2/a^4 - 5/32*(a^2*x^2 - 1)/a^4 - 17/256/a^4

3.14 $\int x^2 \sin^{-1}(ax)^2 dx$

Optimal. Leaf size=82

$$\frac{2x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{9a} + \frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)}{9a^3} - \frac{4x}{9a^2} + \frac{1}{3}x^3\sin^{-1}(ax)^2 - \frac{2x^3}{27}$$

[Out] $(-4*x)/(9*a^2) - (2*x^3)/27 + (4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(9*a^3) + (2*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(9*a) + (x^3*\text{ArcSin}[a*x]^2)/3$

Rubi [A] time = 0.121434, antiderivative size = 82, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4707, 4677, 8, 30}

$$\frac{2x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{9a} + \frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)}{9a^3} - \frac{4x}{9a^2} + \frac{1}{3}x^3\sin^{-1}(ax)^2 - \frac{2x^3}{27}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{ArcSin}[a*x]^2, x]$

[Out] $(-4*x)/(9*a^2) - (2*x^3)/27 + (4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(9*a^3) + (2*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(9*a) + (x^3*\text{ArcSin}[a*x]^2)/3$

Rule 4627

$\text{Int}[(a_.) + \text{ArcSin}[c_.*(x_.)]*(b_.)]^{(n_.)}*((d_.)*(x_.))^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c^n)/(d*(m+1)), \text{Int}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}]/\text{Sqrt}[1 - c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \&\& \text{IGtQ}[n, 0] \&\& \text{NeQ}[m, -1]$

Rule 4707

$\text{Int}[(a_.) + \text{ArcSin}[c_.*(x_.)]*(b_.)]^{(n_.)}*((f_.)*(x_.))^{(m_.)}/\text{Sqrt}[(d_.) + (e_.)*(x_.)^2], x_Symbol] \rightarrow \text{Simp}[(f*(f*x))^{(m-1)}*\text{Sqrt}[d + e*x^2]*(a + b*\text{ArcSin}[c*x])^n/(e*m), x] + (\text{Dist}[(f^2*(m-1))/(c^2*m), \text{Int}[(f*x)^{(m-2)}*(a + b*\text{ArcSin}[c*x])^n]/\text{Sqrt}[d + e*x^2], x], x] + \text{Dist}[(b*f*n*\text{Sqrt}[1 - c^2*x^2])/(c*m*\text{Sqrt}[d + e*x^2]), \text{Int}[(f*x)^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}, x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{GtQ}[n, 0] \&\& \text{GtQ}[m, 1] \&\& \text{IntegerQ}[m]$

Rule 4677

$\text{Int}[(a_.) + \text{ArcSin}[c_.*(x_.)]*(b_.)]^{(n_.)}*(x_.)*((d_.) + (e_.)*(x_.)^2)^{(p_.)}, x_Symbol] \rightarrow \text{Simp}[(d + e*x^2)^{(p+1)}*(a + b*\text{ArcSin}[c*x])^n/(2*e*(p+1)), x] + \text{Dist}[(b*n*d^{\text{IntPart}[p]}*(d + e*x^2)^{\text{FracPart}[p]})/(2*c*(p+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(1 - c^2*x^2)^{(p+1/2)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, p\}, x \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{GtQ}[n, 0] \&\& \text{NeQ}[p, -1]$

Rule 8

$\text{Int}[a_, x_Symbol] \rightarrow \text{Simp}[a*x, x] /; \text{FreeQ}[a, x]$

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int x^2 \sin^{-1}(ax)^2 dx &= \frac{1}{3} x^3 \sin^{-1}(ax)^2 - \frac{1}{3} (2a) \int \frac{x^3 \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\ &= \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{9a} + \frac{1}{3} x^3 \sin^{-1}(ax)^2 - \frac{2 \int x^2 dx}{9} - \frac{4 \int \frac{x \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx}{9a} \\ &= -\frac{2x^3}{27} + \frac{4\sqrt{1-a^2x^2} \sin^{-1}(ax)}{9a^3} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{9a} + \frac{1}{3} x^3 \sin^{-1}(ax)^2 - \frac{4 \int 1 dx}{9a^2} \\ &= -\frac{4x}{9a^2} - \frac{2x^3}{27} + \frac{4\sqrt{1-a^2x^2} \sin^{-1}(ax)}{9a^3} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{9a} + \frac{1}{3} x^3 \sin^{-1}(ax)^2 \end{aligned}$$

Mathematica [A] time = 0.0280522, size = 64, normalized size = 0.78

$$\frac{-2ax(a^2x^2 + 6) + 9a^3x^3 \sin^{-1}(ax)^2 + 6\sqrt{1-a^2x^2}(a^2x^2 + 2) \sin^{-1}(ax)}{27a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*ArcSin[a*x]^2,x]

[Out] (-2*a*x*(6 + a^2*x^2) + 6*Sqrt[1 - a^2*x^2]*(2 + a^2*x^2)*ArcSin[a*x] + 9*a^3*x^3*ArcSin[a*x]^2)/(27*a^3)

Maple [A] time = 0.059, size = 59, normalized size = 0.7

$$\frac{1}{a^3} \left(\frac{a^3 x^3 (\arcsin(ax))^2}{3} + \frac{2 \arcsin(ax) (a^2 x^2 + 2)}{9} \sqrt{-a^2 x^2 + 1} - \frac{2 a^3 x^3}{27} - \frac{4 ax}{9} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*arcsin(a*x)^2,x)

[Out] 1/a^3*(1/3*a^3*x^3*arcsin(a*x)^2+2/9*arcsin(a*x)*(a^2*x^2+2)*(-a^2*x^2+1)^(1/2)-2/27*a^3*x^3-4/9*a*x)

Maxima [A] time = 1.73538, size = 97, normalized size = 1.18

$$\frac{1}{3} x^3 \arcsin(ax)^2 + \frac{2}{9} a \left(\frac{\sqrt{-a^2x^2+1}x^2}{a^2} + \frac{2\sqrt{-a^2x^2+1}}{a^4} \right) \arcsin(ax) - \frac{2(a^2x^3+6x)}{27a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^2,x, algorithm="maxima")

[Out] 1/3*x^3*arcsin(a*x)^2 + 2/9*a*(sqrt(-a^2*x^2 + 1)*x^2/a^2 + 2*sqrt(-a^2*x^2 + 1)/a^4)*arcsin(a*x) - 2/27*(a^2*x^3 + 6*x)/a^2

Fricas [A] time = 2.41462, size = 143, normalized size = 1.74

$$\frac{9a^3x^3 \arcsin(ax)^2 - 2a^3x^3 + 6(a^2x^2 + 2)\sqrt{-a^2x^2 + 1} \arcsin(ax) - 12ax}{27a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^2,x, algorithm="fricas")

[Out] 1/27*(9*a^3*x^3*arcsin(a*x)^2 - 2*a^3*x^3 + 6*(a^2*x^2 + 2)*sqrt(-a^2*x^2 + 1)*arcsin(a*x) - 12*a*x)/a^3

Sympy [A] time = 2.59436, size = 76, normalized size = 0.93

$$\begin{cases} \frac{x^3 \operatorname{asin}^2(ax)}{3} - \frac{2x^3}{27} + \frac{2x^2\sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{9a} - \frac{4x}{9a^2} + \frac{4\sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{9a^3} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*asin(a*x)**2,x)

[Out] Piecewise((x**3*asin(a*x)**2/3 - 2*x**3/27 + 2*x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)/(9*a) - 4*x/(9*a**2) + 4*sqrt(-a**2*x**2 + 1)*asin(a*x)/(9*a**3), Ne(a, 0)), (0, True))

Giac [A] time = 1.31157, size = 131, normalized size = 1.6

$$\frac{(a^2x^2 - 1)x \arcsin(ax)^2}{3a^2} + \frac{x \arcsin(ax)^2}{3a^2} - \frac{2(a^2x^2 - 1)x}{27a^2} - \frac{2(-a^2x^2 + 1)^{\frac{3}{2}} \arcsin(ax)}{9a^3} - \frac{14x}{27a^2} + \frac{2\sqrt{-a^2x^2 + 1} \arcsin(ax)}{3a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^2,x, algorithm="giac")

[Out] 1/3*(a^2*x^2 - 1)*x*arcsin(a*x)^2/a^2 + 1/3*x*arcsin(a*x)^2/a^2 - 2/27*(a^2*x^2 - 1)*x/a^2 - 2/9*(-a^2*x^2 + 1)^(3/2)*arcsin(a*x)/a^3 - 14/27*x/a^2 + 2/3*sqrt(-a^2*x^2 + 1)*arcsin(a*x)/a^3

3.15 $\int x \sin^{-1}(ax)^2 dx$

Optimal. Leaf size=60

$$\frac{x\sqrt{1-a^2x^2}\sin^{-1}(ax)}{2a} - \frac{\sin^{-1}(ax)^2}{4a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^2 - \frac{x^2}{4}$$

[Out] $-x^2/4 + (x\sqrt{1 - a^2*x^2}*\text{ArcSin}[a*x])/(2*a) - \text{ArcSin}[a*x]^2/(4*a^2) + (x^2*\text{ArcSin}[a*x]^2)/2$

Rubi [A] time = 0.0932273, antiderivative size = 60, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4707, 4641, 30}

$$\frac{x\sqrt{1-a^2x^2}\sin^{-1}(ax)}{2a} - \frac{\sin^{-1}(ax)^2}{4a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^2 - \frac{x^2}{4}$$

Antiderivative was successfully verified.

[In] Int[x*ArcSin[a*x]^2,x]

[Out] $-x^2/4 + (x\sqrt{1 - a^2*x^2}*\text{ArcSin}[a*x])/(2*a) - \text{ArcSin}[a*x]^2/(4*a^2) + (x^2*\text{ArcSin}[a*x]^2)/2$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned} \int x \sin^{-1}(ax)^2 dx &= \frac{1}{2}x^2 \sin^{-1}(ax)^2 - a \int \frac{x^2 \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\ &= \frac{x\sqrt{1-a^2x^2} \sin^{-1}(ax)}{2a} + \frac{1}{2}x^2 \sin^{-1}(ax)^2 - \frac{\int x dx}{2} - \frac{\int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx}{2a} \\ &= -\frac{x^2}{4} + \frac{x\sqrt{1-a^2x^2} \sin^{-1}(ax)}{2a} - \frac{\sin^{-1}(ax)^2}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^2 \end{aligned}$$

Mathematica [A] time = 0.016981, size = 55, normalized size = 0.92

$$\frac{-a^2x^2 + 2ax\sqrt{1-a^2x^2} \sin^{-1}(ax) + (2a^2x^2 - 1) \sin^{-1}(ax)^2}{4a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*ArcSin[a*x]^2,x]

[Out] $(-(a^2x^2) + 2a*x*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x] + (-1 + 2*a^2*x^2)*\text{ArcSin}[a*x]^2)/(4*a^2)$

Maple [A] time = 0.025, size = 65, normalized size = 1.1

$$\frac{1}{a^2} \left(\frac{(a^2x^2 - 1) (\arcsin(ax))^2}{2} + \frac{\arcsin(ax)}{2} \left(ax\sqrt{-a^2x^2 + 1} + \arcsin(ax) \right) - \frac{(\arcsin(ax))^2}{4} - \frac{a^2x^2}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*arcsin(a*x)^2,x)

[Out] $1/a^2*(1/2*(a^2*x^2-1)*\arcsin(a*x)^2+1/2*\arcsin(a*x)*(a*x*(-a^2*x^2+1)^(1/2)+\arcsin(a*x))-1/4*\arcsin(a*x)^2-1/4*a^2*x^2)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{2}x^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2 + a \int \frac{\sqrt{ax+1}\sqrt{-ax+1}x^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)}{a^2x^2-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^2,x, algorithm="maxima")

[Out] $1/2*x^2*\arctan2(a*x, \text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1))^2 + a*\text{integrate}(\text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1)*x^2*\arctan2(a*x, \text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1))/(a^2*x^2 - 1), x)$

Fricas [A] time = 2.33855, size = 123, normalized size = 2.05

$$\frac{a^2x^2 - 2\sqrt{-a^2x^2 + 1}ax \arcsin(ax) - (2a^2x^2 - 1) \arcsin(ax)^2}{4a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^2,x, algorithm="fricas")

[Out] $-1/4*(a^2*x^2 - 2*\sqrt{-a^2*x^2 + 1})*a*x*\arcsin(a*x) - (2*a^2*x^2 - 1)*\arcsin(a*x)^2/a^2$

Sympy [A] time = 0.769838, size = 51, normalized size = 0.85

$$\begin{cases} \frac{x^2 \operatorname{asin}^2(ax)}{2} - \frac{x^2}{4} + \frac{x\sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{2a} - \frac{\operatorname{asin}^2(ax)}{4a^2} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*asin(a*x)**2,x)

[Out] Piecewise((x**2*asin(a*x)**2/2 - x**2/4 + x*sqrt(-a**2*x**2 + 1)*asin(a*x)/(2*a) - asin(a*x)**2/(4*a**2), Ne(a, 0)), (0, True))

Giac [A] time = 1.21496, size = 99, normalized size = 1.65

$$\frac{\sqrt{-a^2x^2+1}x \operatorname{arcsin}(ax)}{2a} + \frac{(a^2x^2-1) \operatorname{arcsin}(ax)^2}{2a^2} + \frac{\operatorname{arcsin}(ax)^2}{4a^2} - \frac{a^2x^2-1}{4a^2} - \frac{1}{8a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^2,x, algorithm="giac")

[Out] $1/2*\sqrt{-a^2*x^2 + 1})*x*\arcsin(a*x)/a + 1/2*(a^2*x^2 - 1)*\arcsin(a*x)^2/a^2 + 1/4*\arcsin(a*x)^2/a^2 - 1/4*(a^2*x^2 - 1)/a^2 - 1/8/a^2$

3.16 $\int \sin^{-1}(ax)^2 dx$

Optimal. Leaf size=35

$$\frac{2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^2 - 2x$$

[Out] $-2*x + (2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/a + x*\text{ArcSin}[a*x]^2$

Rubi [A] time = 0.0449068, antiderivative size = 35, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4619, 4677, 8}

$$\frac{2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^2 - 2x$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^2, x]$

[Out] $-2*x + (2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/a + x*\text{ArcSin}[a*x]^2$

Rule 4619

$\text{Int}[(a_. + \text{ArcSin}[(c_.)(x_)](b_.))^n, x_Symbol] \rightarrow \text{Simp}[x*(a + b*\text{ArcSin}[c*x])^n, x] - \text{Dist}[b*c*n, \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{n-1})/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ $\text{FreeQ}\{a, b, c, x\} \ \&\& \ \text{GtQ}[n, 0]$

Rule 4677

$\text{Int}[(a_. + \text{ArcSin}[(c_.)(x_)](b_.))^n(x_)((d_. + (e_.)(x_)^2)^p, x_Symbol] \rightarrow \text{Simp}[(d + e*x^2)^{p+1}(a + b*\text{ArcSin}[c*x])^n/(2*e*(p+1)), x] + \text{Dist}[(b*n*d^{\text{IntPart}[p]}(d + e*x^2)^{\text{FracPart}[p]})/(2*c*(p+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(1 - c^2*x^2)^{p+1/2}(a + b*\text{ArcSin}[c*x])^{n-1}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, e, p, x\} \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{NeQ}[p, -1]$

Rule 8

$\text{Int}[a_, x_Symbol] \rightarrow \text{Simp}[a*x, x] /;$ $\text{FreeQ}[a, x]$

Rubi steps

$$\begin{aligned} \int \sin^{-1}(ax)^2 dx &= x\sin^{-1}(ax)^2 - (2a) \int \frac{x\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\ &= \frac{2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^2 - 2 \int 1 dx \\ &= -2x + \frac{2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^2 \end{aligned}$$

Mathematica [A] time = 0.0109879, size = 35, normalized size = 1.

$$\frac{2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^2 - 2x$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^2,x]

[Out] $-2*x + (2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/a + x*\text{ArcSin}[a*x]^2$

Maple [A] time = 0.021, size = 37, normalized size = 1.1

$$\frac{1}{a} \left(ax (\arcsin(ax))^2 - 2ax + 2 \arcsin(ax) \sqrt{-a^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^2,x)

[Out] $1/a*(a*x*\arcsin(a*x)^2-2*a*x+2*\arcsin(a*x)*(-a^2*x^2+1)^{(1/2)})$

Maxima [A] time = 1.82134, size = 45, normalized size = 1.29

$$x \arcsin(ax)^2 - 2x + \frac{2\sqrt{-a^2x^2 + 1} \arcsin(ax)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2,x, algorithm="maxima")

[Out] $x*\arcsin(a*x)^2 - 2*x + 2*\text{sqrt}(-a^2*x^2 + 1)*\arcsin(a*x)/a$

Fricas [A] time = 2.35201, size = 89, normalized size = 2.54

$$\frac{ax \arcsin(ax)^2 - 2ax + 2\sqrt{-a^2x^2 + 1} \arcsin(ax)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2,x, algorithm="fricas")

[Out] $(a*x*\arcsin(a*x)^2 - 2*a*x + 2*\text{sqrt}(-a^2*x^2 + 1)*\arcsin(a*x))/a$

Sympy [A] time = 0.23858, size = 32, normalized size = 0.91

$$\begin{cases} x \operatorname{asin}^2(ax) - 2x + \frac{2\sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{a} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**2,x)

```
[Out] Piecewise((x*asin(a*x)**2 - 2*x + 2*sqrt(-a**2*x**2 + 1)*asin(a*x)/a, Ne(a, 0)), (0, True))
```

Giac [A] time = 1.34824, size = 45, normalized size = 1.29

$$x \arcsin(ax)^2 - 2x + \frac{2\sqrt{-a^2x^2 + 1} \arcsin(ax)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^2,x, algorithm="giac")
```

```
[Out] x*arcsin(a*x)^2 - 2*x + 2*sqrt(-a^2*x^2 + 1)*arcsin(a*x)/a
```

$$3.17 \quad \int \frac{\sin^{-1}(ax)^2}{x} dx$$

Optimal. Leaf size=71

$$-i \sin^{-1}(ax) \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + \frac{1}{2} \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) - \frac{1}{3} i \sin^{-1}(ax)^3 + \sin^{-1}(ax)^2 \log\left(1 - e^{2i \sin^{-1}(ax)}\right)$$

[Out] $(-I/3)*\text{ArcSin}[a*x]^3 + \text{ArcSin}[a*x]^2*\text{Log}[1 - E^{((2*I)*\text{ArcSin}[a*x])}] - I*\text{ArcSin}[a*x]*\text{PolyLog}[2, E^{((2*I)*\text{ArcSin}[a*x])}] + \text{PolyLog}[3, E^{((2*I)*\text{ArcSin}[a*x])}]]/2$

Rubi [A] time = 0.0945688, antiderivative size = 71, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4625, 3717, 2190, 2531, 2282, 6589}

$$-i \sin^{-1}(ax) \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + \frac{1}{2} \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) - \frac{1}{3} i \sin^{-1}(ax)^3 + \sin^{-1}(ax)^2 \log\left(1 - e^{2i \sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^2/x, x]$

[Out] $(-I/3)*\text{ArcSin}[a*x]^3 + \text{ArcSin}[a*x]^2*\text{Log}[1 - E^{((2*I)*\text{ArcSin}[a*x])}] - I*\text{ArcSin}[a*x]*\text{PolyLog}[2, E^{((2*I)*\text{ArcSin}[a*x])}] + \text{PolyLog}[3, E^{((2*I)*\text{ArcSin}[a*x])}]]/2$

Rule 4625

$\text{Int}[(a + \text{ArcSin}[c*x])^n/\text{Tan}[x], x, \text{ArcSin}[c*x]] \rightarrow \text{Subst}[\text{Int}[a + b*x]^n/\text{Tan}[x], x, \text{ArcSin}[c*x]] \text{ ; FreeQ}\{a, b, c, x\} \ \&\& \ \text{IGtQ}[n, 0]$

Rule 3717

$\text{Int}[(c + (d*x)^m*\text{tan}[(e + \text{Pi}*k) + (f*x)]), x_Symbol] \rightarrow \text{Simp}[(I*(c + d*x)^{(m+1)})/(d*(m+1)), x] - \text{Dist}[2*I, \text{Int}[(c + d*x)^m * E^{(2*I*k*\text{Pi})} * E^{(2*I*(e + f*x))}]/(1 + E^{(2*I*k*\text{Pi})} * E^{(2*I*(e + f*x))}), x], x] \text{ ; FreeQ}\{c, d, e, f, x\} \ \&\& \ \text{IntegerQ}[4*k] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2190

$\text{Int}[(F^{((g_*)*((e_*) + (f_*)*(x_)))})^{(n_*)}*((c_*) + (d_*)*(x_))^{(m_*)}]/((a_*) + (b_*)*(F^{((g_*)*((e_*) + (f_*)*(x_)))})^{(n_*)}), x_Symbol] \rightarrow \text{Simp}[(c + d*x)^m*\text{Log}[1 + (b*(F^{(g*(e + f*x))})^n)/a]/(b*f*g*n*\text{Log}[F]), x] - \text{Dist}[(d*m)/(b*f*g*n*\text{Log}[F]), \text{Int}[(c + d*x)^{(m-1)}*\text{Log}[1 + (b*(F^{(g*(e + f*x))})^n)/a], x], x] \text{ ; FreeQ}\{F, a, b, c, d, e, f, g, n, x\} \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2531

$\text{Int}[\text{Log}[1 + (e_*)*(F^{((c_*)*((a_*) + (b_*)*(x_)))})^{(n_*)}]]*((f_*) + (g_*)*(x_))^{(m_*)}, x_Symbol] \rightarrow -\text{Simp}[(f + g*x)^m*\text{PolyLog}[2, -(e*(F^{(c*(a + b*x))})^n)]/(b*c*n*\text{Log}[F]), x] + \text{Dist}[(g*m)/(b*c*n*\text{Log}[F]), \text{Int}[(f + g*x)^{(m-1)}*\text{PolyLog}[2, -(e*(F^{(c*(a + b*x))})^n)], x], x] \text{ ; FreeQ}\{F, a, b, c, e, f, g, n, x\} \ \&\& \ \text{GtQ}[m, 0]$

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^2}{x} dx &= \text{Subst} \left(\int x^2 \cot(x) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{3} i \sin^{-1}(ax)^3 - 2i \text{Subst} \left(\int \frac{e^{2ix} x^2}{1 - e^{2ix}} dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{3} i \sin^{-1}(ax)^3 + \sin^{-1}(ax)^2 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 2 \text{Subst} \left(\int x \log \left(1 - e^{2ix} \right) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{3} i \sin^{-1}(ax)^3 + \sin^{-1}(ax)^2 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - i \sin^{-1}(ax) \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + i \text{Subst} \left(\int \text{Li}_2 \left(e^{2ix} \right) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{3} i \sin^{-1}(ax)^3 + \sin^{-1}(ax)^2 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - i \sin^{-1}(ax) \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + \frac{1}{2} \text{Subst} \left(\int \frac{\text{Li}_2(x)}{x} dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{3} i \sin^{-1}(ax)^3 + \sin^{-1}(ax)^2 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - i \sin^{-1}(ax) \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + \frac{1}{2} \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \end{aligned}$$

Mathematica [A] time = 0.0397966, size = 71, normalized size = 1.

$$i \sin^{-1}(ax) \text{PolyLog} \left(2, e^{-2i \sin^{-1}(ax)} \right) + \frac{1}{2} \text{PolyLog} \left(3, e^{-2i \sin^{-1}(ax)} \right) + \frac{1}{3} i \sin^{-1}(ax)^3 + \sin^{-1}(ax)^2 \log \left(1 - e^{-2i \sin^{-1}(ax)} \right)$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[ArcSin[a*x]^2/x, x]
```

```
[Out] (I/3)*ArcSin[a*x]^3 + ArcSin[a*x]^2*Log[1 - E^((-2*I)*ArcSin[a*x])] + I*Arc
Sin[a*x]*PolyLog[2, E^((-2*I)*ArcSin[a*x])] + PolyLog[3, E^((-2*I)*ArcSin[a
*x])]/2
```

Maple [A] time = 0.042, size = 169, normalized size = 2.4

$$-\frac{i}{3} (\arcsin(ax))^3 + (\arcsin(ax))^2 \ln \left(1 + iax + \sqrt{-a^2x^2 + 1} \right) - 2i \arcsin(ax) \text{polylog} \left(2, -iax - \sqrt{-a^2x^2 + 1} \right) + 2 \text{polylog} \left(3, -iax - \sqrt{-a^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(arcsin(a*x)^2/x, x)
```

```
[Out] -1/3*I*arcsin(a*x)^3+arcsin(a*x)^2*ln(1+I*a*x+(-a^2*x^2+1)^(1/2))-2*I*arcsi
n(a*x)*polylog(2,-I*a*x-(-a^2*x^2+1)^(1/2))+2*polylog(3,-I*a*x-(-a^2*x^2+1)
^(1/2))+arcsin(a*x)^2*ln(1-I*a*x-(-a^2*x^2+1)^(1/2))-2*I*arcsin(a*x)*polylo
g(2,I*a*x+(-a^2*x^2+1)^(1/2))+2*polylog(3,I*a*x+(-a^2*x^2+1)^(1/2))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x,x, algorithm="maxima")

[Out] integrate(arcsin(a*x)^2/x, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^2}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^2/x, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{asin}^2(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**2/x,x)

[Out] Integral(asin(a*x)**2/x, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^2/x, x)

3.18 $\int \frac{\sin^{-1}(ax)^2}{x^2} dx$

Optimal. Leaf size=66

$$2ia\text{PolyLog}\left(2, -e^{i\sin^{-1}(ax)}\right) - 2ia\text{PolyLog}\left(2, e^{i\sin^{-1}(ax)}\right) - \frac{\sin^{-1}(ax)^2}{x} - 4a\sin^{-1}(ax)\tanh^{-1}\left(e^{i\sin^{-1}(ax)}\right)$$

[Out] $-(\text{ArcSin}[a*x]^2/x) - 4*a*\text{ArcSin}[a*x]*\text{ArcTanh}[E^{(I*\text{ArcSin}[a*x])}] + (2*I)*a*\text{PolyLog}[2, -E^{(I*\text{ArcSin}[a*x])}] - (2*I)*a*\text{PolyLog}[2, E^{(I*\text{ArcSin}[a*x])}]$

Rubi [A] time = 0.102522, antiderivative size = 66, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4709, 4183, 2279, 2391}

$$2ia\text{PolyLog}\left(2, -e^{i\sin^{-1}(ax)}\right) - 2ia\text{PolyLog}\left(2, e^{i\sin^{-1}(ax)}\right) - \frac{\sin^{-1}(ax)^2}{x} - 4a\sin^{-1}(ax)\tanh^{-1}\left(e^{i\sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^2/x^2, x]$

[Out] $-(\text{ArcSin}[a*x]^2/x) - 4*a*\text{ArcSin}[a*x]*\text{ArcTanh}[E^{(I*\text{ArcSin}[a*x])}] + (2*I)*a*\text{PolyLog}[2, -E^{(I*\text{ArcSin}[a*x])}] - (2*I)*a*\text{PolyLog}[2, E^{(I*\text{ArcSin}[a*x])}]$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + (d*x)^m)^n, x_Symbol] \rightarrow \text{Simp}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4709

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + (d*x)^m)/\text{Sqrt}[d + (e*x)^2], x_Symbol] \rightarrow \text{Dist}[1/(c^{m+1}*\text{Sqrt}[d]), \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m, x, \text{ArcSin}[c*x]], x] /;$ FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && IGtQ[n, 0] && IntegerQ[m]

Rule 4183

$\text{Int}[\text{csc}[e + (f*x)]*(c + (d*x)^m), x_Symbol] \rightarrow \text{Simp}[-2*(c + d*x)^m*\text{ArcTanh}[E^{(I*(e + f*x))}]/f, x] + (-\text{Dist}[(d*m)/f, \text{Int}[(c + d*x)^{m-1}*\text{Log}[1 - E^{(I*(e + f*x))}], x], x] + \text{Dist}[(d*m)/f, \text{Int}[(c + d*x)^{m-1}*\text{Log}[1 + E^{(I*(e + f*x))}], x], x) /;$ FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 2279

$\text{Int}[\text{Log}[a + (b*x)]*(F^{(e + (c + d*x)^n))}, x_Symbol] \rightarrow \text{Dist}[1/(d*e*n*\text{Log}[F]), \text{Subst}[\text{Int}[\text{Log}[a + b*x]/x, x], x, (F^{(e + (c + d*x)^n))}] /;$ FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

$\text{Int}[\text{Log}[(c + (d*x)^n)/(e + (f*x)^n)], x_Symbol] \rightarrow -\text{Simp}[\text{PolyLog}[2, -(c*e*x^n)/n], x] /;$ FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rubi steps

$$\begin{aligned}
\int \frac{\sin^{-1}(ax)^2}{x^2} dx &= -\frac{\sin^{-1}(ax)^2}{x} + (2a) \int \frac{\sin^{-1}(ax)}{x\sqrt{1-a^2x^2}} dx \\
&= -\frac{\sin^{-1}(ax)^2}{x} + (2a) \text{Subst} \left(\int x \csc(x) dx, x, \sin^{-1}(ax) \right) \\
&= -\frac{\sin^{-1}(ax)^2}{x} - 4a \sin^{-1}(ax) \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) - (2a) \text{Subst} \left(\int \log(1 - e^{ix}) dx, x, \sin^{-1}(ax) \right) + (2ia) \text{Subst} \left(\int \log(1 - e^{-ix}) dx, x, \sin^{-1}(ax) \right) \\
&= -\frac{\sin^{-1}(ax)^2}{x} - 4a \sin^{-1}(ax) \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) + (2ia) \text{Subst} \left(\int \frac{\log(1 - x)}{x} dx, x, e^{i \sin^{-1}(ax)} \right) - (2ia) \text{Subst} \left(\int \frac{\log(1 - x)}{x} dx, x, e^{-i \sin^{-1}(ax)} \right) \\
&= -\frac{\sin^{-1}(ax)^2}{x} - 4a \sin^{-1}(ax) \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) + 2ia \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) - 2ia \text{Li}_2 \left(e^{i \sin^{-1}(ax)} \right)
\end{aligned}$$

Mathematica [A] time = 0.161989, size = 87, normalized size = 1.32

$$a \left(2i \text{PolyLog} \left(2, -e^{i \sin^{-1}(ax)} \right) - 2i \text{PolyLog} \left(2, e^{i \sin^{-1}(ax)} \right) - \sin^{-1}(ax) \left(\frac{\sin^{-1}(ax)}{ax} - 2 \log \left(1 - e^{i \sin^{-1}(ax)} \right) + 2 \log \left(1 + e^{i \sin^{-1}(ax)} \right) \right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^2/x^2,x]

[Out] a*(-(ArcSin[a*x]*(ArcSin[a*x]/(a*x) - 2*Log[1 - E^(I*ArcSin[a*x])]) + 2*Log[1 + E^(I*ArcSin[a*x])])) + (2*I)*PolyLog[2, -E^(I*ArcSin[a*x])] - (2*I)*PolyLog[2, E^(I*ArcSin[a*x])]

Maple [A] time = 0.092, size = 119, normalized size = 1.8

$$-\frac{(\arcsin(ax))^2}{x} - 2a \arcsin(ax) \ln \left(1 + iax + \sqrt{-a^2x^2 + 1} \right) + 2a \arcsin(ax) \ln \left(1 - iax - \sqrt{-a^2x^2 + 1} \right) + 2iapolylog(2, -1 - iax - \sqrt{-a^2x^2 + 1}) - 2iapolylog(2, -1 + iax + \sqrt{-a^2x^2 + 1})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^2/x^2,x)

[Out] -arcsin(a*x)^2/x-2*a*arcsin(a*x)*ln(1+I*a*x+(-a^2*x^2+1)^(1/2))+2*a*arcsin(a*x)*ln(1-I*a*x-(-a^2*x^2+1)^(1/2))+2*I*a*polylog(2,-I*a*x-(-a^2*x^2+1)^(1/2))-2*I*a*polylog(2,I*a*x+(-a^2*x^2+1)^(1/2))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{2ax \int \frac{\sqrt{-ax+1} \arctan(ax, \sqrt{ax+1} \sqrt{-ax+1})}{\sqrt{ax+1}(ax-1)x} dx + \arctan(ax, \sqrt{ax+1} \sqrt{-ax+1})^2}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x^2,x, algorithm="maxima")

[Out] -(2*a*x*integrate(sqrt(a*x + 1)*sqrt(-a*x + 1)*arctan2(a*x, sqrt(a*x + 1))*sqrt(-a*x + 1))/(a^2*x^3 - x), x) + arctan2(a*x, sqrt(a*x + 1))*sqrt(-a*x + 1)

)^2)/x

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^2}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x^2,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^2/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin^2(ax)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**2/x**2,x)

[Out] Integral(asin(a*x)**2/x**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x^2,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^2/x^2, x)

3.19 $\int \frac{\sin^{-1}(ax)^2}{x^3} dx$

Optimal. Leaf size=44

$$-\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{x} + a^2\log(x) - \frac{\sin^{-1}(ax)^2}{2x^2}$$

[Out] $-\left(\frac{a\sqrt{1-a^2x^2}\text{ArcSin}[a*x]}{x}\right) - \frac{\text{ArcSin}[a*x]^2}{2*x^2} + a^2*\text{Log}[x]$

Rubi [A] time = 0.0798736, antiderivative size = 44, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4627, 4681, 29}

$$-\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{x} + a^2\log(x) - \frac{\sin^{-1}(ax)^2}{2x^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^2/x^3, x]$

[Out] $-\left(\frac{a\sqrt{1-a^2x^2}\text{ArcSin}[a*x]}{x}\right) - \frac{\text{ArcSin}[a*x]^2}{2*x^2} + a^2*\text{Log}[x]$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(d*x)^m, x_Symbol]$
 $:\> \text{Simp}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}]/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ $\text{FreeQ}\{a, b, c, d, m\}, x] \&\& \text{IGtQ}[n, 0] \&\& \text{NeQ}[m, -1]$

Rule 4681

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(f*x)^m*(d + e*x^2)^p, x_Symbol]$
 $:\> \text{Simp}[(f*x)^{m+1}*(d + e*x^2)^{p+1}*(a + b*\text{ArcSin}[c*x])^n/(d*f*(m+1)), x] - \text{Dist}[(b*c*n*d*\text{IntPart}[p]*(d + e*x^2)^{\text{FracPart}[p]})/(f*(m+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(f*x)^{m+1}*(1 - c^2*x^2)^{p+1/2}*(a + b*\text{ArcSin}[c*x])^{n-1}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, e, f, m, p\}, x] \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{GtQ}[n, 0] \&\& \text{EqQ}[m + 2*p + 3, 0] \&\& \text{NeQ}[m, -1]$

Rule 29

$\text{Int}[(x)^{-1}, x_Symbol] :\> \text{Simp}[\text{Log}[x], x]$

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^2}{x^3} dx &= -\frac{\sin^{-1}(ax)^2}{2x^2} + a \int \frac{\sin^{-1}(ax)}{x^2\sqrt{1-a^2x^2}} dx \\ &= -\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{x} - \frac{\sin^{-1}(ax)^2}{2x^2} + a^2 \int \frac{1}{x} dx \\ &= -\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{x} - \frac{\sin^{-1}(ax)^2}{2x^2} + a^2 \log(x) \end{aligned}$$

Mathematica [A] time = 0.0254089, size = 44, normalized size = 1.

$$-\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{x} + a^2\log(x) - \frac{\sin^{-1}(ax)^2}{2x^2}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^2/x^3,x]

[Out] -((a*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/x) - ArcSin[a*x]^2/(2*x^2) + a^2*Log[x]

Maple [A] time = 0.026, size = 43, normalized size = 1.

$$-\frac{(\arcsin(ax))^2}{2x^2} - \frac{a\arcsin(ax)}{x}\sqrt{-a^2x^2+1} + a^2\ln(ax)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^2/x^3,x)

[Out] -1/2*arcsin(a*x)^2/x^2-a*arcsin(a*x)*(-a^2*x^2+1)^(1/2)/x+a^2*ln(a*x)

Maxima [A] time = 1.62754, size = 54, normalized size = 1.23

$$a^2\log(x) - \frac{\sqrt{-a^2x^2+1}a\arcsin(ax)}{x} - \frac{\arcsin(ax)^2}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x^3,x, algorithm="maxima")

[Out] a^2*log(x) - sqrt(-a^2*x^2 + 1)*a*arcsin(a*x)/x - 1/2*arcsin(a*x)^2/x^2

Fricas [A] time = 2.56778, size = 112, normalized size = 2.55

$$\frac{2a^2x^2\log(x) - 2\sqrt{-a^2x^2+1}ax\arcsin(ax) - \arcsin(ax)^2}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x^3,x, algorithm="fricas")

[Out] 1/2*(2*a^2*x^2*log(x) - 2*sqrt(-a^2*x^2 + 1)*a*x*arcsin(a*x) - arcsin(a*x)^2)/x^2

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin^2(ax)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**2/x**3,x)

[Out] Integral(asin(a*x)**2/x**3, x)

Giac [B] time = 1.38224, size = 116, normalized size = 2.64

$$\frac{1}{2} \left(\left(\frac{a^4 x}{\left(\sqrt{-a^2 x^2 + 1} |a| + a \right) |a|} - \frac{\sqrt{-a^2 x^2 + 1} |a| + a}{x |a|} \right) \arcsin(ax) + a \log(a^2 x^2) \right) a - \frac{\arcsin(ax)^2}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x^3,x, algorithm="giac")

[Out] 1/2*((a^4*x/((sqrt(-a^2*x^2 + 1)*abs(a) + a)*abs(a)) - (sqrt(-a^2*x^2 + 1)*abs(a) + a)/(x*abs(a)))*arcsin(a*x) + a*log(a^2*x^2))*a - 1/2*arcsin(a*x)^2/x^2

3.20 $\int \frac{\sin^{-1}(ax)^2}{x^4} dx$

Optimal. Leaf size=116

$$\frac{1}{3}ia^3\text{PolyLog}\left(2, -e^{i\sin^{-1}(ax)}\right) - \frac{1}{3}ia^3\text{PolyLog}\left(2, e^{i\sin^{-1}(ax)}\right) - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x^2} - \frac{a^2}{3x} - \frac{2}{3}a^3\sin^{-1}(ax)\tanh^{-1}\left(e^{i\sin^{-1}(ax)}\right)$$

[Out] $-a^2/(3*x) - (a*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(3*x^2) - \text{ArcSin}[a*x]^2/(3*x^3) - (2*a^3*\text{ArcSin}[a*x]*\text{ArcTanh}[E^{(I*\text{ArcSin}[a*x])}])/3 + (I/3)*a^3*\text{PolyLog}[2, -E^{(I*\text{ArcSin}[a*x])}] - (I/3)*a^3*\text{PolyLog}[2, E^{(I*\text{ArcSin}[a*x])}]$

Rubi [A] time = 0.169508, antiderivative size = 116, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4627, 4701, 4709, 4183, 2279, 2391, 30}

$$\frac{1}{3}ia^3\text{PolyLog}\left(2, -e^{i\sin^{-1}(ax)}\right) - \frac{1}{3}ia^3\text{PolyLog}\left(2, e^{i\sin^{-1}(ax)}\right) - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x^2} - \frac{a^2}{3x} - \frac{2}{3}a^3\sin^{-1}(ax)\tanh^{-1}\left(e^{i\sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^2/x^4, x]$

[Out] $-a^2/(3*x) - (a*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(3*x^2) - \text{ArcSin}[a*x]^2/(3*x^3) - (2*a^3*\text{ArcSin}[a*x]*\text{ArcTanh}[E^{(I*\text{ArcSin}[a*x])}])/3 + (I/3)*a^3*\text{PolyLog}[2, -E^{(I*\text{ArcSin}[a*x])}] - (I/3)*a^3*\text{PolyLog}[2, E^{(I*\text{ArcSin}[a*x])}]$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*((d*x)^m), x_Symbol] \rightarrow \text{Simp}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c^n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}]/\text{Sqrt}[1 - c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 4701

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*((f*x)^m)*((d + e*x^2)^p), x_Symbol] \rightarrow \text{Simp}[(f*x)^{m+1}*(d + e*x^2)^{p+1}*(a + b*\text{ArcSin}[c*x])^n/(d*f*(m+1)), x] + (\text{Dist}[(c^2*(m+2*p+3))/(f^2*(m+1)), \text{Int}[(f*x)^{m+2}*(d + e*x^2)^p*(a + b*\text{ArcSin}[c*x])^n, x], x] - \text{Dist}[(b*c^n*d*\text{IntPart}[p]*(d + e*x^2)^{\text{FracPart}[p]}]/(f*(m+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(f*x)^{m+1}*(1 - c^2*x^2)^{p+1/2}*(a + b*\text{ArcSin}[c*x])^{n-1}, x], x]) /; \text{FreeQ}\{a, b, c, d, e, f, p\}, x \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{LtQ}[m, -1] \ \&\& \ \text{IntegerQ}[m]$

Rule 4709

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n/(d + e*x^2), x_Symbol] \rightarrow \text{Dist}[1/(c^{m+1}*\text{Sqrt}[d]), \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m, x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c, d, e\}, x \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[d, 0] \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{IntegerQ}[m]$

Rule 4183

$\text{Int}[\text{csc}[e*x + f*x]*((c + d*x)^m), x_Symbol] \rightarrow \text{Simp}[(c + d*x)^m*\text{ArcTanh}[E^{(I*(e + f*x))}]/f, x] + (-\text{Dist}[(d*m)/f, \text{Int}[(c + d*x)^{m-1}*\text{Log}[1 - E^{(I*(e + f*x))}], x], x] + \text{Dist}[(d*m)/f, \text{Int}[(c + d*x)^m, x], x]$

$(m - 1) \cdot \text{Log}[1 + E^{(I*(e + f*x))}] , x , x] / ; \text{FreeQ}\{c, d, e, f, x\} \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2279

$\text{Int}[\text{Log}[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_)))^((n_))], x_Symbol]$
 $:\> \text{Dist}[1/(d*e*n*\text{Log}[F]), \text{Subst}[\text{Int}[\text{Log}[a + b*x]/x, x], x, (F^{(e*(c + d*x))})^n], x] / ; \text{FreeQ}\{F, a, b, c, d, e, n, x\} \ \&\& \ \text{GtQ}[a, 0]$

Rule 2391

$\text{Int}[\text{Log}[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] :\> -\text{Simp}[\text{PolyLog}[2, -(c*e*x^n)]/n, x] / ; \text{FreeQ}\{c, d, e, n, x\} \ \&\& \ \text{EqQ}[c*d, 1]$

Rule 30

$\text{Int}[(x_)^(m_), x_Symbol] :\> \text{Simp}[x^(m + 1)/(m + 1), x] / ; \text{FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^2}{x^4} dx &= -\frac{\sin^{-1}(ax)^2}{3x^3} + \frac{1}{3}(2a) \int \frac{\sin^{-1}(ax)}{x^3\sqrt{1-a^2x^2}} dx \\ &= -\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x^2} - \frac{\sin^{-1}(ax)^2}{3x^3} + \frac{1}{3}a^2 \int \frac{1}{x^2} dx + \frac{1}{3}a^3 \int \frac{\sin^{-1}(ax)}{x\sqrt{1-a^2x^2}} dx \\ &= -\frac{a^2}{3x} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x^2} - \frac{\sin^{-1}(ax)^2}{3x^3} + \frac{1}{3}a^3 \text{Subst}\left(\int x \csc(x) dx, x, \sin^{-1}(ax)\right) \\ &= -\frac{a^2}{3x} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x^2} - \frac{\sin^{-1}(ax)^2}{3x^3} - \frac{2}{3}a^3 \sin^{-1}(ax) \tanh^{-1}\left(e^{i\sin^{-1}(ax)}\right) - \frac{1}{3}a^3 \text{Subst}\left(\int \log\right) \\ &= -\frac{a^2}{3x} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x^2} - \frac{\sin^{-1}(ax)^2}{3x^3} - \frac{2}{3}a^3 \sin^{-1}(ax) \tanh^{-1}\left(e^{i\sin^{-1}(ax)}\right) + \frac{1}{3}(ia^3) \text{Subst}\left(\int \log\right) \\ &= -\frac{a^2}{3x} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x^2} - \frac{\sin^{-1}(ax)^2}{3x^3} - \frac{2}{3}a^3 \sin^{-1}(ax) \tanh^{-1}\left(e^{i\sin^{-1}(ax)}\right) + \frac{1}{3}ia^3 \text{Li}_2\left(-e^{i\sin^{-1}(ax)}\right) \end{aligned}$$

Mathematica [A] time = 0.615219, size = 139, normalized size = 1.2

$$\frac{-ia^3x^3\text{PolyLog}\left(2, -e^{i\sin^{-1}(ax)}\right) + ia^3x^3\text{PolyLog}\left(2, e^{i\sin^{-1}(ax)}\right) + a^2x^2 + ax\sqrt{1-a^2x^2}\sin^{-1}(ax) - a^3x^3\sin^{-1}(ax)\log}{3x^3}$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^2/x^4, x]

[Out] $-(a^2*x^2 + a*x*\text{Sqrt}[1 - a^2*x^2])*ArcSin[a*x] + ArcSin[a*x]^2 - a^3*x^3*ArcSin[a*x]*\text{Log}[1 - E^{(I*ArcSin[a*x])}] + a^3*x^3*ArcSin[a*x]*\text{Log}[1 + E^{(I*ArcSin[a*x])}] - I*a^3*x^3*\text{PolyLog}[2, -E^{(I*ArcSin[a*x])}] + I*a^3*x^3*\text{PolyLog}[2, E^{(I*ArcSin[a*x])}]/(3*x^3)$

Maple [A] time = 0.196, size = 157, normalized size = 1.4

$$-\frac{a \arcsin(ax)}{3x^2} \sqrt{-a^2x^2 + 1} - \frac{a^2}{3x} - \frac{(\arcsin(ax))^2}{3x^3} - \frac{a^3 \arcsin(ax)}{3} \ln\left(1 + iax + \sqrt{-a^2x^2 + 1}\right) + \frac{i}{3}a^3 \text{polylog}\left(2, -iax\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(arcsin(a*x)^2/x^4,x)`

[Out] $-1/3*a*\arcsin(a*x)*(-a^2*x^2+1)^{(1/2)}/x^2-1/3*a^2/x-1/3*\arcsin(a*x)^2/x^3-1/3*a^3*\arcsin(a*x)*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)})+1/3*I*a^3*\text{polylog}(2,-I*a*x-(-a^2*x^2+1)^{(1/2)})+1/3*a^3*\arcsin(a*x)*\ln(1-I*a*x-(-a^2*x^2+1)^{(1/2)})-1/3*I*a^3*\text{polylog}(2,I*a*x+(-a^2*x^2+1)^{(1/2)})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$-\frac{2ax^3 \int \frac{\sqrt{ax+1}\sqrt{-ax+1} \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})}{a^2x^5-x^3} dx + \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^2/x^4,x, algorithm="maxima")`

[Out] $-1/3*(6*a*x^3*\text{integrate}(1/3*\text{sqrt}(a*x+1)*\text{sqrt}(-a*x+1)*\text{arctan2}(a*x, \text{sqrt}(a*x+1)*\text{sqrt}(-a*x+1))/(a^2*x^5-x^3), x) + \text{arctan2}(a*x, \text{sqrt}(a*x+1)*\text{sqrt}(-a*x+1))^2)/x^3$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^2}{x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^2/x^4,x, algorithm="fricas")`

[Out] `integral(arcsin(a*x)^2/x^4, x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{asin}^2(ax)}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(asin(a*x)**2/x**4,x)`

[Out] `Integral(asin(a*x)**2/x**4, x)`

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^2}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^2/x^4,x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^2/x^4, x)
```

3.21 $\int \frac{\sin^{-1}(ax)^2}{x^5} dx$

Optimal. Leaf size=87

$$-\frac{a^2}{12x^2} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{6x^3} + \frac{1}{3}a^4\log(x) - \frac{\sin^{-1}(ax)^2}{4x^4}$$

[Out] $-a^2/(12*x^2) - (a*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(6*x^3) - (a^3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(3*x) - \text{ArcSin}[a*x]^2/(4*x^4) + (a^4*\text{Log}[x])/3$

Rubi [A] time = 0.140384, antiderivative size = 87, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4701, 4681, 29, 30}

$$-\frac{a^2}{12x^2} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{6x^3} + \frac{1}{3}a^4\log(x) - \frac{\sin^{-1}(ax)^2}{4x^4}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^2/x^5, x]$

[Out] $-a^2/(12*x^2) - (a*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(6*x^3) - (a^3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/(3*x) - \text{ArcSin}[a*x]^2/(4*x^4) + (a^4*\text{Log}[x])/3$

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4701

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_.)*((d_) + (e_.
)*(x_)^2)^(p_), x_Symbol] :> Simp[((f*x)^(m + 1)*(d + e*x^2)^(p + 1)*(a + b
*ArcSin[c*x])^n)/(d*f*(m + 1)), x] + (Dist[(c^2*(m + 2*p + 3))/(f^2*(m + 1)
), Int[(f*x)^(m + 2)*(d + e*x^2)^p*(a + b*ArcSin[c*x])^n, x], x] - Dist[(b*
c*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(f*(m + 1)*(1 - c^2*x^2)^FracPart
[p]), Int[(f*x)^(m + 1)*(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1)
, x], x]) /; FreeQ[{a, b, c, d, e, f, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n,
0] && LtQ[m, -1] && IntegerQ[m]
```

Rule 4681

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_.)*((d_) + (e_.
)*(x_)^2)^(p_), x_Symbol] :> Simp[((f*x)^(m + 1)*(d + e*x^2)^(p + 1)*(a + b
*ArcSin[c*x])^n)/(d*f*(m + 1)), x] - Dist[(b*c*n*d^IntPart[p]*(d + e*x^2)^F
racPart[p])/(f*(m + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(f*x)^(m + 1)*(1 - c
^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d,
e, f, m, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && EqQ[m + 2*p + 3, 0] &
& NeQ[m, -1]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```


Rule 30

$\text{Int}[(x_)^{(m_.)}, x_Symbol] \text{ :> Simp}[x^{(m + 1)}/(m + 1), x] \text{ /; FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^2}{x^5} dx &= -\frac{\sin^{-1}(ax)^2}{4x^4} + \frac{1}{2}a \int \frac{\sin^{-1}(ax)}{x^4\sqrt{1-a^2x^2}} dx \\ &= -\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{6x^3} - \frac{\sin^{-1}(ax)^2}{4x^4} + \frac{1}{6}a^2 \int \frac{1}{x^3} dx + \frac{1}{3}a^3 \int \frac{\sin^{-1}(ax)}{x^2\sqrt{1-a^2x^2}} dx \\ &= -\frac{a^2}{12x^2} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{6x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x} - \frac{\sin^{-1}(ax)^2}{4x^4} + \frac{1}{3}a^4 \int \frac{1}{x} dx \\ &= -\frac{a^2}{12x^2} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)}{6x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{3x} - \frac{\sin^{-1}(ax)^2}{4x^4} + \frac{1}{3}a^4 \log(x) \end{aligned}$$

Mathematica [A] time = 0.0380599, size = 69, normalized size = 0.79

$$-\frac{a^2}{12x^2} - \frac{a\sqrt{1-a^2x^2}(2a^2x^2+1)\sin^{-1}(ax)}{6x^3} + \frac{1}{3}a^4 \log(x) - \frac{\sin^{-1}(ax)^2}{4x^4}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^2/x^5,x]

[Out] -a^2/(12*x^2) - (a*Sqrt[1 - a^2*x^2]*(1 + 2*a^2*x^2)*ArcSin[a*x])/(6*x^3) - ArcSin[a*x]^2/(4*x^4) + (a^4*Log[x])/3

Maple [A] time = 0.032, size = 76, normalized size = 0.9

$$-\frac{(\arcsin(ax))^2}{4x^4} - \frac{a \arcsin(ax)}{6x^3} \sqrt{-a^2x^2+1} - \frac{a^2}{12x^2} - \frac{a^3 \arcsin(ax)}{3x} \sqrt{-a^2x^2+1} + \frac{a^4 \ln(ax)}{3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^2/x^5,x)

[Out] -1/4*arcsin(a*x)^2/x^4-1/6*a*arcsin(a*x)*(-a^2*x^2+1)^(1/2)/x^3-1/12*a^2/x^2-1/3*a^3*arcsin(a*x)*(-a^2*x^2+1)^(1/2)/x+1/3*a^4*ln(a*x)

Maxima [A] time = 1.61304, size = 100, normalized size = 1.15

$$\frac{1}{12} \left(4a^2 \log(x) - \frac{1}{x^2} \right) a^2 - \frac{1}{6} \left(\frac{2\sqrt{-a^2x^2+1}a^2}{x} + \frac{\sqrt{-a^2x^2+1}}{x^3} \right) a \arcsin(ax) - \frac{\arcsin(ax)^2}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^2/x^5,x, algorithm="maxima")

[Out] $1/12*(4*a^2*\log(x) - 1/x^2)*a^2 - 1/6*(2*\sqrt{-a^2*x^2 + 1})*a^2/x + \sqrt{-a^2*x^2 + 1}/x^3)*a*\arcsin(ax) - 1/4*\arcsin(ax)^2/x^4$

Fricas [A] time = 2.30886, size = 149, normalized size = 1.71

$$\frac{4a^4x^4 \log(x) - a^2x^2 - 2(2a^3x^3 + ax)\sqrt{-a^2x^2 + 1} \arcsin(ax) - 3 \arcsin(ax)^2}{12x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^2/x^5,x, algorithm="fricas")`

[Out] $1/12*(4*a^4*x^4*\log(x) - a^2*x^2 - 2*(2*a^3*x^3 + a*x)*\sqrt{-a^2*x^2 + 1}*\arcsin(ax) - 3*\arcsin(ax)^2)/x^4$

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin^2(ax)}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(asin(a*x)**2/x**5,x)`

[Out] `Integral(asin(a*x)**2/x**5, x)`

Giac [B] time = 1.4574, size = 223, normalized size = 2.56

$$\frac{1}{48} \left(\left(\frac{\left(a^4 + \frac{9(\sqrt{-a^2x^2+1}|a|+a)^2}{x^2} \right) a^6 x^3}{(\sqrt{-a^2x^2+1}|a|+a)^3 |a|} - \frac{9(\sqrt{-a^2x^2+1}|a|+a) a^4}{x} + \frac{(\sqrt{-a^2x^2+1}|a|+a)^3}{x^3} \right) \arcsin(ax) + \frac{4 \left(2a^4 \log(a^2x^2) - \frac{a^2}{x^2} \right)}{a} \right) a - \frac{\arcsin(ax)}{4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^2/x^5,x, algorithm="giac")`

[Out] $1/48*(((a^4 + 9*(\sqrt{-a^2*x^2 + 1})*\text{abs}(a) + a)^2/x^2)*a^6*x^3/((\sqrt{-a^2*x^2 + 1})*\text{abs}(a) + a)^3*\text{abs}(a)) - (9*(\sqrt{-a^2*x^2 + 1})*\text{abs}(a) + a)*a^4/x + (\sqrt{-a^2*x^2 + 1})*\text{abs}(a) + a)^3/x^3)/(a^2*\text{abs}(a)))*\arcsin(ax) + 4*(2*a^4*\log(a^2*x^2) - a^2/x^2)/a)*a - 1/4*\arcsin(a*x)^2/x^4$

3.22 $\int x^4 \sin^{-1}(ax)^3 dx$

Optimal. Leaf size=201

$$-\frac{6(1-a^2x^2)^{5/2}}{625a^5} + \frac{76(1-a^2x^2)^{3/2}}{1125a^5} - \frac{298\sqrt{1-a^2x^2}}{375a^5} + \frac{3x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{25a} - \frac{8x^3\sin^{-1}(ax)}{75a^2} + \frac{4x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{25a^3}$$

[Out] $(-298*\text{Sqrt}[1 - a^2*x^2])/(375*a^5) + (76*(1 - a^2*x^2)^{(3/2)})/(1125*a^5) - (6*(1 - a^2*x^2)^{(5/2)})/(625*a^5) - (16*x*\text{ArcSin}[a*x])/(25*a^4) - (8*x^3*\text{ArcSin}[a*x])/(75*a^2) - (6*x^5*\text{ArcSin}[a*x])/125 + (8*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(25*a^5) + (4*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(25*a^3) + (3*x^4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(25*a) + (x^5*\text{ArcSin}[a*x]^3)/5$

Rubi [A] time = 0.384514, antiderivative size = 201, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4627, 4707, 4677, 4619, 261, 266, 43}

$$-\frac{6(1-a^2x^2)^{5/2}}{625a^5} + \frac{76(1-a^2x^2)^{3/2}}{1125a^5} - \frac{298\sqrt{1-a^2x^2}}{375a^5} + \frac{3x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{25a} - \frac{8x^3\sin^{-1}(ax)}{75a^2} + \frac{4x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{25a^3}$$

Antiderivative was successfully verified.

[In] Int[x^4*ArcSin[a*x]^3,x]

[Out] $(-298*\text{Sqrt}[1 - a^2*x^2])/(375*a^5) + (76*(1 - a^2*x^2)^{(3/2)})/(1125*a^5) - (6*(1 - a^2*x^2)^{(5/2)})/(625*a^5) - (16*x*\text{ArcSin}[a*x])/(25*a^4) - (8*x^3*\text{ArcSin}[a*x])/(75*a^2) - (6*x^5*\text{ArcSin}[a*x])/125 + (8*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(25*a^5) + (4*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(25*a^3) + (3*x^4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(25*a) + (x^5*\text{ArcSin}[a*x]^3)/5$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*(x_)^p*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d*IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4619

```
Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^n, x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]
```

Rule 261

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_.))^p, x_Symbol] := Simp[(a + b*x^n)^(p + 1)/(b*n*(p + 1)), x] /; FreeQ[{a, b, m, n, p}, x] && EqQ[m, n - 1] && NeQ[p, -1]
```

Rule 266

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_.))^p, x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]
```

Rule 43

```
Int[((a_.) + (b_.)*(x_.))^m*((c_.) + (d_.)*(x_.))^n, x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int x^4 \sin^{-1}(ax)^3 dx &= \frac{1}{5}x^5 \sin^{-1}(ax)^3 - \frac{1}{5}(3a) \int \frac{x^5 \sin^{-1}(ax)^2}{\sqrt{1-a^2x^2}} dx \\ &= \frac{3x^4\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^3 - \frac{6}{25} \int x^4 \sin^{-1}(ax) dx - \frac{12}{25a} \int \frac{x^3 \sin^{-1}(ax)^2}{\sqrt{1-a^2x^2}} dx \\ &= -\frac{6}{125}x^5 \sin^{-1}(ax) + \frac{4x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a^3} + \frac{3x^4\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^3 - \frac{8}{125} \int x^3 \sin^{-1}(ax) dx \\ &= -\frac{8x^3 \sin^{-1}(ax)}{75a^2} - \frac{6}{125}x^5 \sin^{-1}(ax) + \frac{8\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a^5} + \frac{4x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a^3} + \frac{3x^4\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a} \\ &= -\frac{16x \sin^{-1}(ax)}{25a^4} - \frac{8x^3 \sin^{-1}(ax)}{75a^2} - \frac{6}{125}x^5 \sin^{-1}(ax) + \frac{8\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a^5} + \frac{4x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{25a^3} \\ &= -\frac{86\sqrt{1-a^2x^2}}{125a^5} + \frac{4(1-a^2x^2)^{3/2}}{125a^5} - \frac{6(1-a^2x^2)^{5/2}}{625a^5} - \frac{16x \sin^{-1}(ax)}{25a^4} - \frac{8x^3 \sin^{-1}(ax)}{75a^2} - \frac{6}{125}x^5 \sin^{-1}(ax) \\ &= -\frac{298\sqrt{1-a^2x^2}}{375a^5} + \frac{76(1-a^2x^2)^{3/2}}{1125a^5} - \frac{6(1-a^2x^2)^{5/2}}{625a^5} - \frac{16x \sin^{-1}(ax)}{25a^4} - \frac{8x^3 \sin^{-1}(ax)}{75a^2} - \frac{6}{125}x^5 \sin^{-1}(ax) \end{aligned}$$

Mathematica [A] time = 0.0700747, size = 122, normalized size = 0.61

$$\frac{-2\sqrt{1-a^2x^2}(27a^4x^4 + 136a^2x^2 + 2072) + 1125a^5x^5 \sin^{-1}(ax)^3 - 30ax(9a^4x^4 + 20a^2x^2 + 120) \sin^{-1}(ax) + 225\sqrt{1-a^2x^2}}{5625a^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*ArcSin[a*x]^3, x]

[Out] $(-2\sqrt{1 - a^2x^2})(2072 + 136a^2x^2 + 27a^4x^4) - 30ax(120 + 20a^2x^2 + 9a^4x^4)\text{ArcSin}[ax] + 225\sqrt{1 - a^2x^2}(8 + 4a^2x^2 + 3a^4x^4)\text{ArcSin}[ax]^2 + 1125a^5x^5\text{ArcSin}[ax]^3)/(5625a^5)$

Maple [A] time = 0.059, size = 159, normalized size = 0.8

$$\frac{1}{a^5} \left(\frac{a^5 x^5 (\arcsin(ax))^3}{5} + \frac{(\arcsin(ax))^2 (3a^4 x^4 + 4a^2 x^2 + 8)}{25} \sqrt{-a^2 x^2 + 1} - \frac{16}{25} \sqrt{-a^2 x^2 + 1} - \frac{16ax \arcsin(ax)}{25} - \frac{6a^5}{25} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^4*arcsin(a*x)^3,x)`

[Out] $1/a^5*(1/5*a^5*x^5*\arcsin(a*x)^3+1/25*\arcsin(a*x)^2*(3*a^4*x^4+4*a^2*x^2+8)*(-a^2*x^2+1)^{(1/2)}-16/25*(-a^2*x^2+1)^{(1/2)}-16/25*a*x*\arcsin(a*x)-6/125*a^5*x^5*\arcsin(a*x)-2/625*(3*a^4*x^4+4*a^2*x^2+8)*(-a^2*x^2+1)^{(1/2)}-8/75*a^3*x^3*\arcsin(a*x)-8/225*(a^2*x^2+2)*(-a^2*x^2+1)^{(1/2)})$

Maxima [A] time = 1.69177, size = 231, normalized size = 1.15

$$\frac{1}{5} x^5 \arcsin(ax)^3 + \frac{1}{25} \left(\frac{3\sqrt{-a^2x^2+1}x^4}{a^2} + \frac{4\sqrt{-a^2x^2+1}x^2}{a^4} + \frac{8\sqrt{-a^2x^2+1}}{a^6} \right) a \arcsin(ax)^2 - \frac{2}{5625} a \left(\frac{27\sqrt{-a^2x^2+1}}{a^5} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*arcsin(a*x)^3,x, algorithm="maxima")`

[Out] $1/5*x^5*\arcsin(a*x)^3 + 1/25*(3*\sqrt{-a^2*x^2 + 1}*x^4/a^2 + 4*\sqrt{-a^2*x^2 + 1}*x^2/a^4 + 8*\sqrt{-a^2*x^2 + 1}/a^6)*a*\arcsin(a*x)^2 - 2/5625*a*((27*\sqrt{-a^2*x^2 + 1}*a^2*x^4 + 136*\sqrt{-a^2*x^2 + 1}*x^2 + 2072*\sqrt{-a^2*x^2 + 1}/a^2)/a^4 + 15*(9*a^4*x^5 + 20*a^2*x^3 + 120*x)*\arcsin(a*x)/a^5)$

Fricas [A] time = 2.19976, size = 265, normalized size = 1.32

$$\frac{1125a^5x^5 \arcsin(ax)^3 - 30(9a^5x^5 + 20a^3x^3 + 120ax) \arcsin(ax) - (54a^4x^4 + 272a^2x^2 - 225(3a^4x^4 + 4a^2x^2 + 8)) \arcsin(ax)^2 + 4144\sqrt{-a^2x^2+1}}{5625a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^4*arcsin(a*x)^3,x, algorithm="fricas")`

[Out] $1/5625*(1125*a^5*x^5*\arcsin(a*x)^3 - 30*(9*a^5*x^5 + 20*a^3*x^3 + 120*a*x)*\arcsin(a*x) - (54*a^4*x^4 + 272*a^2*x^2 - 225*(3*a^4*x^4 + 4*a^2*x^2 + 8))*\arcsin(a*x)^2 + 4144*\sqrt{-a^2*x^2 + 1})/a^5$

Sympy [A] time = 13.6204, size = 196, normalized size = 0.98

$$\left\{ \begin{array}{l} \frac{x^5 \operatorname{asin}^3(ax)}{5} - \frac{6x^5 \operatorname{asin}(ax)}{125} + \frac{3x^4 \sqrt{-a^2x^2+1} \operatorname{asin}^2(ax)}{25a} - \frac{6x^4 \sqrt{-a^2x^2+1}}{625a} - \frac{8x^3 \operatorname{asin}(ax)}{75a^2} + \frac{4x^2 \sqrt{-a^2x^2+1} \operatorname{asin}^2(ax)}{25a^3} - \frac{272x^2 \sqrt{-a^2x^2+1}}{5625a^3} - \frac{16x \operatorname{asin}(ax)}{25a^4} - \frac{2}{5625a^5} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4*asin(a*x)**3,x)

[Out] Piecewise((x**5*asin(a*x)**3/5 - 6*x**5*asin(a*x)/125 + 3*x**4*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(25*a) - 6*x**4*sqrt(-a**2*x**2 + 1)/(625*a) - 8*x**3*asin(a*x)/(75*a**2) + 4*x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(25*a**3) - 272*x**2*sqrt(-a**2*x**2 + 1)/(5625*a**3) - 16*x*asin(a*x)/(25*a**4) + 8*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(25*a**5) - 4144*sqrt(-a**2*x**2 + 1)/(5625*a**5), Ne(a, 0)), (0, True))

Giac [A] time = 1.38628, size = 336, normalized size = 1.67

$$\frac{(a^2x^2 - 1)^2 x \arcsin(ax)^3}{5a^4} + \frac{2(a^2x^2 - 1)x \arcsin(ax)^3}{5a^4} - \frac{6(a^2x^2 - 1)^2 x \arcsin(ax)}{125a^4} + \frac{x \arcsin(ax)^3}{5a^4} + \frac{3(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1}}{25a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^3,x, algorithm="giac")

[Out] 1/5*(a^2*x^2 - 1)^2*x*arcsin(a*x)^3/a^4 + 2/5*(a^2*x^2 - 1)*x*arcsin(a*x)^3/a^4 - 6/125*(a^2*x^2 - 1)^2*x*arcsin(a*x)/a^4 + 1/5*x*arcsin(a*x)^3/a^4 + 3/25*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^2/a^5 - 76/375*(a^2*x^2 - 1)*x*arcsin(a*x)/a^4 - 2/5*(-a^2*x^2 + 1)^(3/2)*arcsin(a*x)^2/a^5 - 298/375*x*arcsin(a*x)/a^4 - 6/625*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)/a^5 + 3/5*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^2/a^5 + 76/1125*(-a^2*x^2 + 1)^(3/2)/a^5 - 298/375*sqrt(-a^2*x^2 + 1)/a^5

3.23 $\int x^3 \sin^{-1}(ax)^3 dx$

Optimal. Leaf size=167

$$-\frac{3x^3\sqrt{1-a^2x^2}}{128a} - \frac{45x\sqrt{1-a^2x^2}}{256a^3} + \frac{3x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{16a} - \frac{9x^2\sin^{-1}(ax)}{32a^2} + \frac{9x\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{32a^3} - \frac{3\sin^{-1}(ax)}{32a^4}$$

[Out] $(-45*x*\text{Sqrt}[1 - a^2*x^2])/(256*a^3) - (3*x^3*\text{Sqrt}[1 - a^2*x^2])/(128*a) + (45*\text{ArcSin}[a*x])/(256*a^4) - (9*x^2*\text{ArcSin}[a*x])/(32*a^2) - (3*x^4*\text{ArcSin}[a*x])/32 + (9*x*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(32*a^3) + (3*x^3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(16*a) - (3*\text{ArcSin}[a*x]^3)/(32*a^4) + (x^4*\text{ArcSin}[a*x]^3)/4$

Rubi [A] time = 0.297097, antiderivative size = 167, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4707, 4641, 321, 216}

$$-\frac{3x^3\sqrt{1-a^2x^2}}{128a} - \frac{45x\sqrt{1-a^2x^2}}{256a^3} + \frac{3x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{16a} - \frac{9x^2\sin^{-1}(ax)}{32a^2} + \frac{9x\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{32a^3} - \frac{3\sin^{-1}(ax)}{32a^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*ArcSin[a*x]^3,x]

[Out] $(-45*x*\text{Sqrt}[1 - a^2*x^2])/(256*a^3) - (3*x^3*\text{Sqrt}[1 - a^2*x^2])/(128*a) + (45*\text{ArcSin}[a*x])/(256*a^4) - (9*x^2*\text{ArcSin}[a*x])/(32*a^2) - (3*x^4*\text{ArcSin}[a*x])/32 + (9*x*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(32*a^3) + (3*x^3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(16*a) - (3*\text{ArcSin}[a*x]^3)/(32*a^4) + (x^4*\text{ArcSin}[a*x]^3)/4$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 321

Int[((c_.)*(x_))^(m_)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(c^(n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[

$(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), \text{Int}[(c*x)^{(m - n)}*(a + b*x^n)^p, x], x] /; \text{FreeQ}\{a, b, c, p\}, x\} \&\& \text{IGtQ}\{n, 0\} \&\& \text{GtQ}\{m, n - 1\} \&\& \text{NeQ}\{m + n*p + 1, 0\} \&\& \text{IntBinomialQ}\{a, b, c, n, m, p, x\}$

Rule 216

$\text{Int}[1/\text{Sqrt}[(a_) + (b_)*(x_)^2], x_Symbol] \rightarrow \text{Simp}[\text{ArcSin}[(\text{Rt}[-b, 2]*x)/\text{Sqrt}[a]]/\text{Rt}[-b, 2], x] /; \text{FreeQ}\{a, b\}, x\} \&\& \text{GtQ}\{a, 0\} \&\& \text{NegQ}\{b\}$

Rubi steps

$$\begin{aligned} \int x^3 \sin^{-1}(ax)^3 dx &= \frac{1}{4}x^4 \sin^{-1}(ax)^3 - \frac{1}{4}(3a) \int \frac{x^4 \sin^{-1}(ax)^2}{\sqrt{1 - a^2x^2}} dx \\ &= \frac{3x^3 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{16a} + \frac{1}{4}x^4 \sin^{-1}(ax)^3 - \frac{3}{8} \int x^3 \sin^{-1}(ax) dx - \frac{9 \int \frac{x^2 \sin^{-1}(ax)^2}{\sqrt{1 - a^2x^2}} dx}{16a} \\ &= -\frac{3}{32}x^4 \sin^{-1}(ax) + \frac{9x \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{32a^3} + \frac{3x^3 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{16a} + \frac{1}{4}x^4 \sin^{-1}(ax)^3 - \frac{9 \int \frac{\sin^{-1}(ax)^2}{\sqrt{1 - a^2x^2}} dx}{32a} \\ &= -\frac{3x^3 \sqrt{1 - a^2x^2}}{128a} - \frac{9x^2 \sin^{-1}(ax)}{32a^2} - \frac{3}{32}x^4 \sin^{-1}(ax) + \frac{9x \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{32a^3} + \frac{3x^3 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{16a} \\ &= -\frac{45x \sqrt{1 - a^2x^2}}{256a^3} - \frac{3x^3 \sqrt{1 - a^2x^2}}{128a} - \frac{9x^2 \sin^{-1}(ax)}{32a^2} - \frac{3}{32}x^4 \sin^{-1}(ax) + \frac{9x \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{32a^3} + \frac{3x^3 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{16a} \\ &= -\frac{45x \sqrt{1 - a^2x^2}}{256a^3} - \frac{3x^3 \sqrt{1 - a^2x^2}}{128a} + \frac{45 \sin^{-1}(ax)}{256a^4} - \frac{9x^2 \sin^{-1}(ax)}{32a^2} - \frac{3}{32}x^4 \sin^{-1}(ax) + \frac{9x \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{32a^3} + \frac{3x^3 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{16a} \end{aligned}$$

Mathematica [A] time = 0.0483489, size = 112, normalized size = 0.67

$$\frac{-3ax\sqrt{1 - a^2x^2}(2a^2x^2 + 15) + 8(8a^4x^4 - 3)\sin^{-1}(ax)^3 + 24ax\sqrt{1 - a^2x^2}(2a^2x^2 + 3)\sin^{-1}(ax)^2 - 3(8a^4x^4 + 24a^2x^2 - 15)\sin^{-1}(ax)}{256a^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*ArcSin[a*x]^3,x]

[Out] $(-3*a*x*\text{Sqrt}[1 - a^2*x^2]*(15 + 2*a^2*x^2) - 3*(-15 + 24*a^2*x^2 + 8*a^4*x^4)*\text{ArcSin}[a*x] + 24*a*x*\text{Sqrt}[1 - a^2*x^2]*(3 + 2*a^2*x^2)*\text{ArcSin}[a*x]^2 + 8*(-3 + 8*a^4*x^4)*\text{ArcSin}[a*x]^3)/(256*a^4)$

Maple [A] time = 0.06, size = 154, normalized size = 0.9

$$\frac{1}{a^4} \left(\frac{a^4 x^4 (\arcsin(ax))^3}{4} - \frac{3 (\arcsin(ax))^2}{32} \left(-2 a^3 x^3 \sqrt{-a^2 x^2 + 1} - 3 a x \sqrt{-a^2 x^2 + 1} + 3 \arcsin(ax) \right) - \frac{3 a^4 x^4 \arcsin(ax)}{32} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x)^3,x)

[Out] $1/a^4*(1/4*a^4*x^4*\arcsin(a*x)^3 - 3/32*\arcsin(a*x)^2*(-2*a^3*x^3*(-a^2*x^2+1)^{(1/2)} - 3*a*x*(-a^2*x^2+1)^{(1/2)} + 3*\arcsin(a*x)) - 3/32*a^4*x^4*\arcsin(a*x) - 3/256*a*x*(2*a^2*x^2+3)*(-a^2*x^2+1)^{(1/2)} - 27/256*\arcsin(a*x) - 9/32*(a^2*x^2-15)*\arcsin(a*x))$

) * arcsin(a*x) - 9/64 * a * x * (-a^2 * x^2 + 1)^(1/2) + 3/16 * arcsin(a*x)^3

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{4} x^4 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3 + 3a \int \frac{\sqrt{ax+1}\sqrt{-ax+1} x^4 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2}{4(a^2x^2-1)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^3,x, algorithm="maxima")

[Out] 1/4*x^4*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3 + 3*a*integrate(1/4*sqrt(a*x + 1)*sqrt(-a*x + 1)*x^4*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2/(a^2*x^2 - 1), x)

Fricas [A] time = 2.05025, size = 234, normalized size = 1.4

$$\frac{8(8a^4x^4 - 3)\arcsin(ax)^3 - 3(8a^4x^4 + 24a^2x^2 - 15)\arcsin(ax) - 3(2a^3x^3 - 8(2a^3x^3 + 3ax)\arcsin(ax)^2 + 15ax)}{256a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^3,x, algorithm="fricas")

[Out] 1/256*(8*(8*a^4*x^4 - 3)*arcsin(a*x)^3 - 3*(8*a^4*x^4 + 24*a^2*x^2 - 15)*arcsin(a*x) - 3*(2*a^3*x^3 - 8*(2*a^3*x^3 + 3*a*x)*arcsin(a*x)^2 + 15*a*x)*sqrt(-a^2*x^2 + 1))/a^4

Sympy [A] time = 6.94277, size = 160, normalized size = 0.96

$$\begin{cases} \frac{x^4 \operatorname{asin}^3(ax)}{4} - \frac{3x^4 \operatorname{asin}(ax)}{32} + \frac{3x^3 \sqrt{-a^2x^2+1} \operatorname{asin}^2(ax)}{16a} - \frac{3x^3 \sqrt{-a^2x^2+1}}{128a} - \frac{9x^2 \operatorname{asin}(ax)}{32a^2} + \frac{9x \sqrt{-a^2x^2+1} \operatorname{asin}^2(ax)}{32a^3} - \frac{45x \sqrt{-a^2x^2+1}}{256a^3} - \frac{3 \operatorname{asin}^3(ax)}{32a^4} \\ 0 \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x)**3,x)

[Out] Piecewise((x**4*asin(a*x)**3/4 - 3*x**4*asin(a*x)/32 + 3*x**3*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(16*a) - 3*x**3*sqrt(-a**2*x**2 + 1)/(128*a) - 9*x**2*asin(a*x)/(32*a**2) + 9*x*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(32*a**3) - 45*x*sqrt(-a**2*x**2 + 1)/(256*a**3) - 3*asin(a*x)**3/(32*a**4) + 45*asin(a*x)/(256*a**4), Ne(a, 0)), (0, True))

Giac [A] time = 1.30246, size = 250, normalized size = 1.5

$$-\frac{3(-a^2x^2+1)^{\frac{3}{2}}x\arcsin(ax)^2}{16a^3} + \frac{(a^2x^2-1)^2\arcsin(ax)^3}{4a^4} + \frac{15\sqrt{-a^2x^2+1}x\arcsin(ax)^2}{32a^3} + \frac{(a^2x^2-1)\arcsin(ax)^3}{2a^4} +$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*arcsin(a*x)^3,x, algorithm="giac")
```

```
[Out] -3/16*(-a^2*x^2 + 1)^(3/2)*x*arcsin(a*x)^2/a^3 + 1/4*(a^2*x^2 - 1)^2*arcsin
(a*x)^3/a^4 + 15/32*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)^2/a^3 + 1/2*(a^2*x^2 -
1)*arcsin(a*x)^3/a^4 + 3/128*(-a^2*x^2 + 1)^(3/2)*x/a^3 - 3/32*(a^2*x^2 -
1)^2*arcsin(a*x)/a^4 + 5/32*arcsin(a*x)^3/a^4 - 51/256*sqrt(-a^2*x^2 + 1)*x
/a^3 - 15/32*(a^2*x^2 - 1)*arcsin(a*x)/a^4 - 51/256*arcsin(a*x)/a^4
```

3.24 $\int x^2 \sin^{-1}(ax)^3 dx$

Optimal. Leaf size=136

$$\frac{2(1-a^2x^2)^{3/2}}{27a^3} - \frac{14\sqrt{1-a^2x^2}}{9a^3} + \frac{x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{3a} + \frac{2\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{3a^3} - \frac{4x\sin^{-1}(ax)}{3a^2} + \frac{1}{3}x^3\sin^{-1}(ax)^3 -$$

[Out] (-14*Sqrt[1 - a^2*x^2])/(9*a^3) + (2*(1 - a^2*x^2)^(3/2))/(27*a^3) - (4*x*ArcSin[a*x])/(3*a^2) - (2*x^3*ArcSin[a*x])/9 + (2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(3*a^3) + (x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(3*a) + (x^3*ArcSin[a*x]^3)/3

Rubi [A] time = 0.224747, antiderivative size = 136, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4627, 4707, 4677, 4619, 261, 266, 43}

$$\frac{2(1-a^2x^2)^{3/2}}{27a^3} - \frac{14\sqrt{1-a^2x^2}}{9a^3} + \frac{x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{3a} + \frac{2\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{3a^3} - \frac{4x\sin^{-1}(ax)}{3a^2} + \frac{1}{3}x^3\sin^{-1}(ax)^3 -$$

Antiderivative was successfully verified.

[In] Int[x^2*ArcSin[a*x]^3,x]

[Out] (-14*Sqrt[1 - a^2*x^2])/(9*a^3) + (2*(1 - a^2*x^2)^(3/2))/(27*a^3) - (4*x*ArcSin[a*x])/(3*a^2) - (2*x^3*ArcSin[a*x])/9 + (2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(3*a^3) + (x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(3*a) + (x^3*ArcSin[a*x]^3)/3

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((f_.)*(x_))^(m_.)/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)*((d_.) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4619

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x]))^(n - 1)]/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]
```

Rule 261

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[(a + b*x^n)^(p + 1)/(b*n*(p + 1)), x] /; FreeQ[{a, b, m, n, p}, x] && EqQ[m, n - 1] && NeQ[p, -1]
```

Rule 266

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]
```

Rule 43

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])
```

Rubi steps

$$\begin{aligned} \int x^2 \sin^{-1}(ax)^3 dx &= \frac{1}{3}x^3 \sin^{-1}(ax)^3 - a \int \frac{x^3 \sin^{-1}(ax)^2}{\sqrt{1 - a^2x^2}} dx \\ &= \frac{x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a} + \frac{1}{3}x^3 \sin^{-1}(ax)^3 - \frac{2}{3} \int x^2 \sin^{-1}(ax) dx - \frac{2 \int \frac{x \sin^{-1}(ax)^2}{\sqrt{1 - a^2x^2}} dx}{3a} \\ &= -\frac{2}{9}x^3 \sin^{-1}(ax) + \frac{2\sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a^3} + \frac{x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a} + \frac{1}{3}x^3 \sin^{-1}(ax)^3 - \frac{4 \int \sin^{-1}(ax) dx}{3a^2} \\ &= -\frac{4x \sin^{-1}(ax)}{3a^2} - \frac{2}{9}x^3 \sin^{-1}(ax) + \frac{2\sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a^3} + \frac{x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a} + \frac{1}{3}x^3 \sin^{-1}(ax)^3 \\ &= -\frac{4\sqrt{1 - a^2x^2}}{3a^3} - \frac{4x \sin^{-1}(ax)}{3a^2} - \frac{2}{9}x^3 \sin^{-1}(ax) + \frac{2\sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a^3} + \frac{x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a} + \frac{1}{3}x^3 \sin^{-1}(ax)^3 \\ &= -\frac{14\sqrt{1 - a^2x^2}}{9a^3} + \frac{2(1 - a^2x^2)^{3/2}}{27a^3} - \frac{4x \sin^{-1}(ax)}{3a^2} - \frac{2}{9}x^3 \sin^{-1}(ax) + \frac{2\sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a^3} + \frac{x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^2}{3a} + \frac{1}{3}x^3 \sin^{-1}(ax)^3 \end{aligned}$$

Mathematica [A] time = 0.0446312, size = 95, normalized size = 0.7

$$\frac{-2\sqrt{1 - a^2x^2}(a^2x^2 + 20) + 9a^3x^3 \sin^{-1}(ax)^3 + 9\sqrt{1 - a^2x^2}(a^2x^2 + 2) \sin^{-1}(ax)^2 - 6ax(a^2x^2 + 6) \sin^{-1}(ax)}{27a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*ArcSin[a*x]^3,x]
```

```
[Out] (-2*Sqrt[1 - a^2*x^2]*(20 + a^2*x^2) - 6*a*x*(6 + a^2*x^2)*ArcSin[a*x] + 9*Sqrt[1 - a^2*x^2]*(2 + a^2*x^2)*ArcSin[a*x]^2 + 9*a^3*x^3*ArcSin[a*x]^3)/(27*a^3)
```

Maple [A] time = 0.045, size = 106, normalized size = 0.8

$$\frac{1}{a^3} \left(\frac{a^3 x^3 (\arcsin(ax))^3}{3} + \frac{(\arcsin(ax))^2 (a^2 x^2 + 2)}{3} \sqrt{-a^2 x^2 + 1} - \frac{4}{3} \sqrt{-a^2 x^2 + 1} - \frac{4ax \arcsin(ax)}{3} - \frac{2a^3 x^3 \arcsin(ax)}{9} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*arcsin(a*x)^3,x)

[Out] 1/a^3*(1/3*a^3*x^3*arcsin(a*x)^3+1/3*arcsin(a*x)^2*(a^2*x^2+2)*(-a^2*x^2+1)^(1/2)-4/3*(-a^2*x^2+1)^(1/2)-4/3*a*x*arcsin(a*x)-2/9*a^3*x^3*arcsin(a*x)-2/27*(a^2*x^2+2)*(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.72559, size = 162, normalized size = 1.19

$$\frac{1}{3} x^3 \arcsin(ax)^3 + \frac{1}{3} a \left(\frac{\sqrt{-a^2 x^2 + 1} x^2}{a^2} + \frac{2\sqrt{-a^2 x^2 + 1}}{a^4} \right) \arcsin(ax)^2 - \frac{2}{27} a \left(\frac{\sqrt{-a^2 x^2 + 1} x^2 + \frac{20\sqrt{-a^2 x^2 + 1}}{a^2}}{a^2} + \frac{3(a^2 x^3 + \dots)}{a^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^3,x, algorithm="maxima")

[Out] 1/3*x^3*arcsin(a*x)^3 + 1/3*a*(sqrt(-a^2*x^2 + 1)*x^2/a^2 + 2*sqrt(-a^2*x^2 + 1)/a^4)*arcsin(a*x)^2 - 2/27*a*((sqrt(-a^2*x^2 + 1)*x^2 + 20*sqrt(-a^2*x^2 + 1)/a^2)/a^2 + 3*(a^2*x^3 + 6*x)*arcsin(a*x)/a^3)

Fricas [A] time = 2.16897, size = 189, normalized size = 1.39

$$\frac{9a^3 x^3 \arcsin(ax)^3 - 6(a^3 x^3 + 6ax) \arcsin(ax) - (2a^2 x^2 - 9(a^2 x^2 + 2) \arcsin(ax)^2 + 40) \sqrt{-a^2 x^2 + 1}}{27a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^3,x, algorithm="fricas")

[Out] 1/27*(9*a^3*x^3*arcsin(a*x)^3 - 6*(a^3*x^3 + 6*a*x)*arcsin(a*x) - (2*a^2*x^2 + 2 - 9*(a^2*x^2 + 2)*arcsin(a*x)^2 + 40)*sqrt(-a^2*x^2 + 1))/a^3

Sympy [A] time = 5.89492, size = 128, normalized size = 0.94

$$\begin{cases} \frac{x^3 \operatorname{asin}^3(ax)}{3} - \frac{2x^3 \operatorname{asin}(ax)}{9} + \frac{x^2 \sqrt{-a^2 x^2 + 1} \operatorname{asin}^2(ax)}{3a} - \frac{2x^2 \sqrt{-a^2 x^2 + 1}}{27a} - \frac{4x \operatorname{asin}(ax)}{3a^2} + \frac{2\sqrt{-a^2 x^2 + 1} \operatorname{asin}^2(ax)}{3a^3} - \frac{40\sqrt{-a^2 x^2 + 1}}{27a^3} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*asin(a*x)**3,x)

[Out] Piecewise((x**3*asin(a*x)**3/3 - 2*x**3*asin(a*x)/9 + x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(3*a) - 2*x**2*sqrt(-a**2*x**2 + 1)/(27*a) - 4*x*asin(a*x

```
)/(3*a**2) + 2*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(3*a**3) - 40*sqrt(-a**2*x**2 + 1)/(27*a**3), Ne(a, 0)), (0, True))
```

Giac [A] time = 1.29957, size = 192, normalized size = 1.41

$$\frac{(a^2x^2 - 1)x \arcsin(ax)^3}{3a^2} + \frac{x \arcsin(ax)^3}{3a^2} - \frac{2(a^2x^2 - 1)x \arcsin(ax)}{9a^2} - \frac{(-a^2x^2 + 1)^{\frac{3}{2}} \arcsin(ax)^2}{3a^3} - \frac{14x \arcsin(ax)}{9a^2} +$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*arcsin(a*x)^3,x, algorithm="giac")
```

```
[Out] 1/3*(a^2*x^2 - 1)*x*arcsin(a*x)^3/a^2 + 1/3*x*arcsin(a*x)^3/a^2 - 2/9*(a^2*x^2 - 1)*x*arcsin(a*x)/a^2 - 1/3*(-a^2*x^2 + 1)^(3/2)*arcsin(a*x)^2/a^3 - 14/9*x*arcsin(a*x)/a^2 + sqrt(-a^2*x^2 + 1)*arcsin(a*x)^2/a^3 + 2/27*(-a^2*x^2 + 1)^(3/2)/a^3 - 14/9*sqrt(-a^2*x^2 + 1)/a^3
```

3.25 $\int x \sin^{-1}(ax)^3 dx$

Optimal. Leaf size=99

$$-\frac{3x\sqrt{1-a^2x^2}}{8a} + \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4a} - \frac{\sin^{-1}(ax)^3}{4a^2} + \frac{3\sin^{-1}(ax)}{8a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^3 - \frac{3}{4}x^2\sin^{-1}(ax)$$

[Out] $(-3*x*\text{Sqrt}[1 - a^2*x^2])/(8*a) + (3*\text{ArcSin}[a*x])/(8*a^2) - (3*x^2*\text{ArcSin}[a*x])/4 + (3*x*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(4*a) - \text{ArcSin}[a*x]^3/(4*a^2) + (x^2*\text{ArcSin}[a*x]^3)/2$

Rubi [A] time = 0.155988, antiderivative size = 99, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4627, 4707, 4641, 321, 216}

$$-\frac{3x\sqrt{1-a^2x^2}}{8a} + \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4a} - \frac{\sin^{-1}(ax)^3}{4a^2} + \frac{3\sin^{-1}(ax)}{8a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^3 - \frac{3}{4}x^2\sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{ArcSin}[a*x]^3, x]$

[Out] $(-3*x*\text{Sqrt}[1 - a^2*x^2])/(8*a) + (3*\text{ArcSin}[a*x])/(8*a^2) - (3*x^2*\text{ArcSin}[a*x])/4 + (3*x*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/(4*a) - \text{ArcSin}[a*x]^3/(4*a^2) + (x^2*\text{ArcSin}[a*x]^3)/2$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + (d*x)^m)^n, x_Symbol] \rightarrow \text{Simp}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}]/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + (f*x)^m)/\text{Sqrt}[d + (e*x)^2], x_Symbol] \rightarrow \text{Simp}[(f*(f*x)^{m-1}*\text{Sqrt}[d + e*x^2]*(a + b*\text{ArcSin}[c*x])^n)/(e*m), x] + (\text{Dist}[(f^2*(m-1))/(c^2*m), \text{Int}[(f*x)^{m-2}*(a + b*\text{ArcSin}[c*x])^n]/\text{Sqrt}[d + e*x^2], x], x] + \text{Dist}[(b*f*n*\text{Sqrt}[1 - c^2*x^2])/(c*m*\text{Sqrt}[d + e*x^2]), \text{Int}[(f*x)^{m-1}*(a + b*\text{ArcSin}[c*x])^{n-1}], x], x] /;$ FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + (d + (e*x)^2))^n, x_Symbol] \rightarrow \text{Simp}[(a + b*\text{ArcSin}[c*x])^{n+1}/(b*c*\text{Sqrt}[d + e*x^2]), x] /;$ FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 321

$\text{Int}[(c*x)^m*(a + (b*x)^n)^p, x_Symbol] \rightarrow \text{Simp}[(c^{n-1}*(c*x)^{m-n+1}*(a + b*x^n)^{p+1})/(b*(m+n*p+1)), x] - \text{Dist}[(a*c^n*(m-n+1))/(b*(m+n*p+1)), \text{Int}[(c*x)^{m-n}*(a + b*x^n)^p, x], x] /;$ FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n-1] && NeQ[m+n*p+1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 216

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]
```

Rubi steps

$$\begin{aligned} \int x \sin^{-1}(ax)^3 dx &= \frac{1}{2}x^2 \sin^{-1}(ax)^3 - \frac{1}{2}(3a) \int \frac{x^2 \sin^{-1}(ax)^2}{\sqrt{1-a^2x^2}} dx \\ &= \frac{3x\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{4a} + \frac{1}{2}x^2 \sin^{-1}(ax)^3 - \frac{3}{2} \int x \sin^{-1}(ax) dx - \frac{3 \int \frac{\sin^{-1}(ax)^2}{\sqrt{1-a^2x^2}} dx}{4a} \\ &= -\frac{3}{4}x^2 \sin^{-1}(ax) + \frac{3x\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{4a} - \frac{\sin^{-1}(ax)^3}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^3 + \frac{1}{4}(3a) \int \frac{x^2}{\sqrt{1-a^2x^2}} dx \\ &= -\frac{3x\sqrt{1-a^2x^2}}{8a} - \frac{3}{4}x^2 \sin^{-1}(ax) + \frac{3x\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{4a} - \frac{\sin^{-1}(ax)^3}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^3 + \frac{3 \int \frac{1}{\sqrt{1-a^2x^2}} dx}{8a} \\ &= -\frac{3x\sqrt{1-a^2x^2}}{8a} + \frac{3 \sin^{-1}(ax)}{8a^2} - \frac{3}{4}x^2 \sin^{-1}(ax) + \frac{3x\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{4a} - \frac{\sin^{-1}(ax)^3}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^3 \end{aligned}$$

Mathematica [A] time = 0.025192, size = 82, normalized size = 0.83

$$\frac{-3ax\sqrt{1-a^2x^2} + (4a^2x^2 - 2) \sin^{-1}(ax)^3 + 6ax\sqrt{1-a^2x^2} \sin^{-1}(ax)^2 + (3 - 6a^2x^2) \sin^{-1}(ax)}{8a^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*ArcSin[a*x]^3,x]
```

```
[Out] (-3*a*x*Sqrt[1 - a^2*x^2] + (3 - 6*a^2*x^2)*ArcSin[a*x] + 6*a*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2 + (-2 + 4*a^2*x^2)*ArcSin[a*x]^3)/(8*a^2)
```

Maple [A] time = 0.041, size = 96, normalized size = 1.

$$\frac{1}{a^2} \left(\frac{(a^2x^2 - 1)(\arcsin(ax))^3}{2} + \frac{3(\arcsin(ax))^2}{4} \left(ax\sqrt{-a^2x^2 + 1} + \arcsin(ax) \right) - \frac{(3a^2x^2 - 3)\arcsin(ax)}{4} - \frac{3ax}{8}\sqrt{-a^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*arcsin(a*x)^3,x)
```

```
[Out] 1/a^2*(1/2*(a^2*x^2-1)*arcsin(a*x)^3+3/4*arcsin(a*x)^2*(a*x*(-a^2*x^2+1)^(1/2)+arcsin(a*x))-3/4*(a^2*x^2-1)*arcsin(a*x)-3/8*a*x*(-a^2*x^2+1)^(1/2)-3/8*arcsin(a*x)-1/2*arcsin(a*x)^3)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{2}x^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3 + 3a \int \frac{\sqrt{ax+1}\sqrt{-ax+1}x^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2}{2(a^2x^2-1)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^3,x, algorithm="maxima")

[Out] $\frac{1}{2}x^2 \arctan 2(a*x, \sqrt{a*x+1} \sqrt{-a*x+1})^3 + 3*a \int \frac{1}{2} \sqrt{a*x+1} \sqrt{-a*x+1} x^2 \arctan 2(a*x, \sqrt{a*x+1} \sqrt{-a*x+1})^2}{(a^2*x^2-1), x}$

Fricas [A] time = 2.03548, size = 170, normalized size = 1.72

$$\frac{2(2a^2x^2-1)\arcsin(ax)^3 - 3(2a^2x^2-1)\arcsin(ax) + 3\sqrt{-a^2x^2+1}(2ax\arcsin(ax)^2 - ax)}{8a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^3,x, algorithm="fricas")

[Out] $\frac{1}{8}*(2*(2*a^2*x^2-1)*\arcsin(a*x)^3 - 3*(2*a^2*x^2-1)*\arcsin(a*x) + 3*\sqrt{-a^2*x^2+1}*(2*a*x*\arcsin(a*x)^2 - a*x))/a^2$

Sympy [A] time = 1.60898, size = 92, normalized size = 0.93

$$\begin{cases} \frac{x^2 \operatorname{asin}^3(ax)}{2} - \frac{3x^2 \operatorname{asin}(ax)}{4} + \frac{3x\sqrt{-a^2x^2+1} \operatorname{asin}^2(ax)}{4a} - \frac{3x\sqrt{-a^2x^2+1}}{8a} - \frac{\operatorname{asin}^3(ax)}{4a^2} + \frac{3 \operatorname{asin}(ax)}{8a^2} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*asin(a*x)**3,x)

[Out] Piecewise((x**2*asin(a*x)**3/2 - 3*x**2*asin(a*x)/4 + 3*x*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/(4*a) - 3*x*sqrt(-a**2*x**2 + 1)/(8*a) - asin(a*x)**3/(4*a**2) + 3*asin(a*x)/(8*a**2), Ne(a, 0)), (0, True))

Giac [A] time = 1.30534, size = 136, normalized size = 1.37

$$\frac{3\sqrt{-a^2x^2+1}x\arcsin(ax)^2}{4a} + \frac{(a^2x^2-1)\arcsin(ax)^3}{2a^2} + \frac{\arcsin(ax)^3}{4a^2} - \frac{3\sqrt{-a^2x^2+1}x}{8a} - \frac{3(a^2x^2-1)\arcsin(ax)}{4a^2} - \frac{3}{4a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^3,x, algorithm="giac")

[Out] $\frac{3}{4} \sqrt{-a^2*x^2+1} * x * \arcsin(a*x)^2 / a + \frac{1}{2} * (a^2*x^2-1) * \arcsin(a*x)^3 / a^2 + \frac{1}{4} * \arcsin(a*x)^3 / a^2 - \frac{3}{8} * \sqrt{-a^2*x^2+1} * x / a - \frac{3}{4} * (a^2*x^2-1) * \arcsin(a*x) / a^2 - \frac{3}{8} * \arcsin(a*x) / a^2$

3.26 $\int \sin^{-1}(ax)^3 dx$

Optimal. Leaf size=60

$$-\frac{6\sqrt{1-a^2x^2}}{a} + \frac{3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{a} + x\sin^{-1}(ax)^3 - 6x\sin^{-1}(ax)$$

[Out] $(-6*\text{Sqrt}[1 - a^2*x^2])/a - 6*x*\text{ArcSin}[a*x] + (3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/a + x*\text{ArcSin}[a*x]^3$

Rubi [A] time = 0.0801758, antiderivative size = 60, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4619, 4677, 261}

$$-\frac{6\sqrt{1-a^2x^2}}{a} + \frac{3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{a} + x\sin^{-1}(ax)^3 - 6x\sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^3, x]$

[Out] $(-6*\text{Sqrt}[1 - a^2*x^2])/a - 6*x*\text{ArcSin}[a*x] + (3*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^2)/a + x*\text{ArcSin}[a*x]^3$

Rule 4619

```
Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.), x_Symbol] :> Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]
```

Rule 4677

```
Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_.)*((d_.) + (e_.)*(x_.)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]
```

Rule 261

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_.))^(p_.), x_Symbol] :> Simp[(a + b*x^n)^(p + 1)/(b*n*(p + 1)), x] /; FreeQ[{a, b, m, n, p}, x] && EqQ[m, n - 1] && NeQ[p, -1]
```

Rubi steps

$$\begin{aligned}
\int \sin^{-1}(ax)^3 dx &= x \sin^{-1}(ax)^3 - (3a) \int \frac{x \sin^{-1}(ax)^2}{\sqrt{1-a^2x^2}} dx \\
&= \frac{3\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{a} + x \sin^{-1}(ax)^3 - 6 \int \sin^{-1}(ax) dx \\
&= -6x \sin^{-1}(ax) + \frac{3\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{a} + x \sin^{-1}(ax)^3 + (6a) \int \frac{x}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{6\sqrt{1-a^2x^2}}{a} - 6x \sin^{-1}(ax) + \frac{3\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{a} + x \sin^{-1}(ax)^3
\end{aligned}$$

Mathematica [A] time = 0.0112293, size = 60, normalized size = 1.

$$-\frac{6\sqrt{1-a^2x^2}}{a} + \frac{3\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{a} + x \sin^{-1}(ax)^3 - 6x \sin^{-1}(ax)$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^3,x]

[Out] (-6*Sqrt[1 - a^2*x^2])/a - 6*x*ArcSin[a*x] + (3*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/a + x*ArcSin[a*x]^3

Maple [A] time = 0.024, size = 57, normalized size = 1.

$$\frac{1}{a} \left(ax (\arcsin(ax))^3 + 3 (\arcsin(ax))^2 \sqrt{-a^2x^2 + 1} - 6 \sqrt{-a^2x^2 + 1} - 6 ax \arcsin(ax) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^3,x)

[Out] 1/a*(a*x*arcsin(a*x)^3+3*arcsin(a*x)^2*(-a^2*x^2+1)^(1/2)-6*(-a^2*x^2+1)^(1/2)-6*a*x*arcsin(a*x))

Maxima [A] time = 1.68067, size = 77, normalized size = 1.28

$$x \arcsin(ax)^3 + \frac{3\sqrt{-a^2x^2+1} \arcsin(ax)^2}{a} - \frac{6(ax \arcsin(ax) + \sqrt{-a^2x^2+1})}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3,x, algorithm="maxima")

[Out] x*arcsin(a*x)^3 + 3*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^2/a - 6*(a*x*arcsin(a*x) + sqrt(-a^2*x^2 + 1))/a

Fricas [A] time = 2.04743, size = 116, normalized size = 1.93

$$\frac{ax \arcsin(ax)^3 - 6ax \arcsin(ax) + 3\sqrt{-a^2x^2+1}(\arcsin(ax)^2 - 2)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3,x, algorithm="fricas")

[Out] (a*x*arcsin(a*x)^3 - 6*a*x*arcsin(a*x) + 3*sqrt(-a^2*x^2 + 1)*(arcsin(a*x)^2 - 2))/a

Sympy [A] time = 0.832359, size = 54, normalized size = 0.9

$$\begin{cases} x \operatorname{asin}^3(ax) - 6x \operatorname{asin}(ax) + \frac{3\sqrt{-a^2x^2+1} \operatorname{asin}^2(ax)}{a} - \frac{6\sqrt{-a^2x^2+1}}{a} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**3,x)

[Out] Piecewise((x*asin(a*x)**3 - 6*x*asin(a*x) + 3*sqrt(-a**2*x**2 + 1)*asin(a*x)**2/a - 6*sqrt(-a**2*x**2 + 1)/a, Ne(a, 0)), (0, True))

Giac [A] time = 1.36035, size = 76, normalized size = 1.27

$$x \operatorname{arcsin}(ax)^3 - 6x \operatorname{arcsin}(ax) + \frac{3\sqrt{-a^2x^2+1} \operatorname{arcsin}(ax)^2}{a} - \frac{6\sqrt{-a^2x^2+1}}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3,x, algorithm="giac")

[Out] x*arcsin(a*x)^3 - 6*x*arcsin(a*x) + 3*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^2/a - 6*sqrt(-a^2*x^2 + 1)/a

$$3.27 \quad \int \frac{\sin^{-1}(ax)^3}{x} dx$$

Optimal. Leaf size=97

$$-\frac{3}{2}i \sin^{-1}(ax)^2 \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + \frac{3}{2} \sin^{-1}(ax) \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) + \frac{3}{4}i \text{PolyLog}\left(4, e^{2i \sin^{-1}(ax)}\right) - \frac{1}{4}i \sin^{-1}$$

```
[Out] (-I/4)*ArcSin[a*x]^4 + ArcSin[a*x]^3*Log[1 - E^((2*I)*ArcSin[a*x])] - ((3*I)/2)*ArcSin[a*x]^2*PolyLog[2, E^((2*I)*ArcSin[a*x])] + (3*ArcSin[a*x]*PolyLog[3, E^((2*I)*ArcSin[a*x])])/2 + ((3*I)/4)*PolyLog[4, E^((2*I)*ArcSin[a*x])]
```

Rubi [A] time = 0.108999, antiderivative size = 97, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4625, 3717, 2190, 2531, 6609, 2282, 6589}

$$-\frac{3}{2}i \sin^{-1}(ax)^2 \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + \frac{3}{2} \sin^{-1}(ax) \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) + \frac{3}{4}i \text{PolyLog}\left(4, e^{2i \sin^{-1}(ax)}\right) - \frac{1}{4}i \sin^{-1}$$

Antiderivative was successfully verified.

```
[In] Int[ArcSin[a*x]^3/x, x]
```

```
[Out] (-I/4)*ArcSin[a*x]^4 + ArcSin[a*x]^3*Log[1 - E^((2*I)*ArcSin[a*x])] - ((3*I)/2)*ArcSin[a*x]^2*PolyLog[2, E^((2*I)*ArcSin[a*x])] + (3*ArcSin[a*x]*PolyLog[3, E^((2*I)*ArcSin[a*x])])/2 + ((3*I)/4)*PolyLog[4, E^((2*I)*ArcSin[a*x])]
```

Rule 4625

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/(x_), x_Symbol] :> Subst[Int[(a + b*x)^n/Tan[x], x], x, ArcSin[c*x]] /; FreeQ[{a, b, c}, x] && IGtQ[n, 0]
```

Rule 3717

```
Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + Pi*(k_.) + (f_.)*(x_)], x_Symbol] :> Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m * E^(2*I*k*Pi) * E^(2*I*(e + f*x)))/(1 + E^(2*I*k*Pi) * E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IntegerQ[4*k] && IGtQ[m, 0]
```

Rule 2190

```
Int[(((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)*((c_.) + (d_.)*(x_))^(m_.))/((a_.) + (b_.)*(F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.), x_Symbol] :> Simp[((c + d*x)^m * Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1) * Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*((f_.) + (g_.)*(x_))^(m_.), x_Symbol] :> -Simp[((f + g*x)^m * PolyLog[2, -(e*(F^(c*(a + b*x))))^n])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1) * PolyLog[2, -(e*(F^(c*(a + b*x))))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]
```

Rule 6609

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_)))^(p_.)], x_Symbol] :> Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p])/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rule 2282

```
Int[u_, x_Symbol] :> With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_)^v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] :> Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^3}{x} dx &= \text{Subst} \left(\int x^3 \cot(x) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{4}i \sin^{-1}(ax)^4 - 2i \text{Subst} \left(\int \frac{e^{2ix} x^3}{1 - e^{2ix}} dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{4}i \sin^{-1}(ax)^4 + \sin^{-1}(ax)^3 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 3 \text{Subst} \left(\int x^2 \log \left(1 - e^{2ix} \right) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{4}i \sin^{-1}(ax)^4 + \sin^{-1}(ax)^3 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - \frac{3}{2}i \sin^{-1}(ax)^2 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + 3i \text{Subst} \left(\int x \text{Li}_2 \left(e^{2ix} \right) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{4}i \sin^{-1}(ax)^4 + \sin^{-1}(ax)^3 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - \frac{3}{2}i \sin^{-1}(ax)^2 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + \frac{3}{2} \sin^{-1}(ax) \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \\ &= -\frac{1}{4}i \sin^{-1}(ax)^4 + \sin^{-1}(ax)^3 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - \frac{3}{2}i \sin^{-1}(ax)^2 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + \frac{3}{2} \sin^{-1}(ax) \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \\ &= -\frac{1}{4}i \sin^{-1}(ax)^4 + \sin^{-1}(ax)^3 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - \frac{3}{2}i \sin^{-1}(ax)^2 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + \frac{3}{2} \sin^{-1}(ax) \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \end{aligned}$$

Mathematica [A] time = 0.0556827, size = 97, normalized size = 1.

$$-\frac{1}{64}i \left(-96 \sin^{-1}(ax)^2 \text{PolyLog} \left(2, e^{-2i \sin^{-1}(ax)} \right) + 96i \sin^{-1}(ax) \text{PolyLog} \left(3, e^{-2i \sin^{-1}(ax)} \right) + 48 \text{PolyLog} \left(4, e^{-2i \sin^{-1}(ax)} \right) \right) -$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^3/x, x]

[Out] (-I/64)*(Pi^4 - 16*ArcSin[a*x]^4 + (64*I)*ArcSin[a*x]^3*Log[1 - E^((-2*I)*ArcSin[a*x])] - 96*ArcSin[a*x]^2*PolyLog[2, E^((-2*I)*ArcSin[a*x])] + (96*I)*ArcSin[a*x]*PolyLog[3, E^((-2*I)*ArcSin[a*x])] + 48*PolyLog[4, E^((-2*I)*ArcSin[a*x])])

Maple [A] time = 0.046, size = 229, normalized size = 2.4

$$-\frac{i}{4} (\arcsin(ax))^4 + (\arcsin(ax))^3 \ln \left(1 + iax + \sqrt{-a^2x^2 + 1} \right) - 3i (\arcsin(ax))^2 \text{polylog} \left(2, -iax - \sqrt{-a^2x^2 + 1} \right) + 6 \arcsin(ax) \text{Li}_3 \left(e^{2i \arcsin(ax)} \right) - \frac{3}{2}i \arcsin(ax)^2 \text{Li}_2 \left(e^{2i \arcsin(ax)} \right) - \frac{1}{4}i \arcsin(ax)^4 - 2i \text{Subst} \left(\int \frac{e^{2ix} x^3}{1 - e^{2ix}} dx, x, \arcsin(ax) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^3/x,x)

[Out] $-1/4*I*\arcsin(a*x)^4+\arcsin(a*x)^3*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)})-3*I*\arcsin(a*x)^2*\operatorname{polylog}(2,-I*a*x-(-a^2*x^2+1)^{(1/2)})+6*\arcsin(a*x)*\operatorname{polylog}(3,-I*a*x-(-a^2*x^2+1)^{(1/2)})+6*I*\operatorname{polylog}(4,-I*a*x-(-a^2*x^2+1)^{(1/2)})+\arcsin(a*x)^3*\ln(1-I*a*x-(-a^2*x^2+1)^{(1/2)})-3*I*\arcsin(a*x)^2*\operatorname{polylog}(2,I*a*x+(-a^2*x^2+1)^{(1/2)})+6*\arcsin(a*x)*\operatorname{polylog}(3,I*a*x+(-a^2*x^2+1)^{(1/2)})+6*I*\operatorname{polylog}(4,I*a*x+(-a^2*x^2+1)^{(1/2)})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^3}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x,x, algorithm="maxima")

[Out] integrate(arcsin(a*x)^3/x, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\arcsin(ax)^3}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^3/x, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{asin}^3(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**3/x,x)

[Out] Integral(asin(a*x)**3/x, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^3}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^3/x,x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^3/x, x)
```


$$3.28 \quad \int \frac{\sin^{-1}(ax)^3}{x^2} dx$$

Optimal. Leaf size=108

$$6ia \sin^{-1}(ax) \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 6ia \sin^{-1}(ax) \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 6a \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right) + 6a \text{PolyLog}\left(3, e^{i \sin^{-1}(ax)}\right)$$

```
[Out] -(ArcSin[a*x]^3/x) - 6*a*ArcSin[a*x]^2*ArcTanh[E^(I*ArcSin[a*x])] + (6*I)*a
*ArcSin[a*x]*PolyLog[2, -E^(I*ArcSin[a*x])] - (6*I)*a*ArcSin[a*x]*PolyLog[2
, E^(I*ArcSin[a*x])] - 6*a*PolyLog[3, -E^(I*ArcSin[a*x])] + 6*a*PolyLog[3,
E^(I*ArcSin[a*x])]
```

Rubi [A] time = 0.1632, antiderivative size = 108, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4627, 4709, 4183, 2531, 2282, 6589}

$$6ia \sin^{-1}(ax) \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 6ia \sin^{-1}(ax) \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 6a \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right) + 6a \text{PolyLog}\left(3, e^{i \sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

```
[In] Int[ArcSin[a*x]^3/x^2,x]
```

```
[Out] -(ArcSin[a*x]^3/x) - 6*a*ArcSin[a*x]^2*ArcTanh[E^(I*ArcSin[a*x])] + (6*I)*a
*ArcSin[a*x]*PolyLog[2, -E^(I*ArcSin[a*x])] - (6*I)*a*ArcSin[a*x]*PolyLog[2
, E^(I*ArcSin[a*x])] - 6*a*PolyLog[3, -E^(I*ArcSin[a*x])] + 6*a*PolyLog[3,
E^(I*ArcSin[a*x])]
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4709

```
Int((((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*(x_)^(m_))/Sqrt[(d_) + (e_.)*
(x_)^2], x_Symbol] :> Dist[1/(c^(m + 1)*Sqrt[d]), Subst[Int[(a + b*x)^n*Sin
[x]^m, x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d +
e, 0] && GtQ[d, 0] && IGtQ[n, 0] && IntegerQ[m]
```

Rule 4183

```
Int[csc[(e_.) + (f_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(-
2*(c + d*x)^m*ArcTanh[E^(I*(e + f*x))])/f, x] + (-Dist[(d*m)/f, Int[(c + d
*x)^(m - 1)*Log[1 - E^(I*(e + f*x))], x], x] + Dist[(d*m)/f, Int[(c + d*x)^(
m - 1)*Log[1 + E^(I*(e + f*x))], x], x]) /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*((f_.) + (g_.)
*(x_))^(m_.), x_Symbol] :> -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x
))))^n])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m -
1)*PolyLog[2, -(e*(F^(c*(a + b*x))))^n], x], x] /; FreeQ[{F, a, b, c, e, f
```

, g, n}, x] && GtQ[m, 0]

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^3}{x^2} dx &= -\frac{\sin^{-1}(ax)^3}{x} + (3a) \int \frac{\sin^{-1}(ax)^2}{x\sqrt{1-a^2x^2}} dx \\ &= -\frac{\sin^{-1}(ax)^3}{x} + (3a) \operatorname{Subst}\left(\int x^2 \csc(x) dx, x, \sin^{-1}(ax)\right) \\ &= -\frac{\sin^{-1}(ax)^3}{x} - 6a \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) - (6a) \operatorname{Subst}\left(\int x \log(1 - e^{ix}) dx, x, \sin^{-1}(ax)\right) + (6a) \operatorname{Subst}\left(\int x \log(1 + e^{ix}) dx, x, \sin^{-1}(ax)\right) \\ &= -\frac{\sin^{-1}(ax)^3}{x} - 6a \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) + 6ia \sin^{-1}(ax) \operatorname{Li}_2\left(-e^{i \sin^{-1}(ax)}\right) - 6ia \sin^{-1}(ax) \operatorname{Li}_2\left(e^{i \sin^{-1}(ax)}\right) \\ &= -\frac{\sin^{-1}(ax)^3}{x} - 6a \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) + 6ia \sin^{-1}(ax) \operatorname{Li}_2\left(-e^{i \sin^{-1}(ax)}\right) - 6ia \sin^{-1}(ax) \operatorname{Li}_2\left(e^{i \sin^{-1}(ax)}\right) \\ &= -\frac{\sin^{-1}(ax)^3}{x} - 6a \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) + 6ia \sin^{-1}(ax) \operatorname{Li}_2\left(-e^{i \sin^{-1}(ax)}\right) - 6ia \sin^{-1}(ax) \operatorname{Li}_2\left(e^{i \sin^{-1}(ax)}\right) \end{aligned}$$

Mathematica [A] time = 0.12395, size = 133, normalized size = 1.23

$$a \left(6i \sin^{-1}(ax) \operatorname{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 6i \sin^{-1}(ax) \operatorname{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 6 \operatorname{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right) + 6 \operatorname{PolyLog}\left(3, e^{i \sin^{-1}(ax)}\right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^3/x^2, x]

[Out] a*(-(ArcSin[a*x]^3/(a*x)) + 3*ArcSin[a*x]^2*Log[1 - E^(I*ArcSin[a*x])] - 3*ArcSin[a*x]^2*Log[1 + E^(I*ArcSin[a*x])] + (6*I)*ArcSin[a*x]*PolyLog[2, -E^(I*ArcSin[a*x])] - (6*I)*ArcSin[a*x]*PolyLog[2, E^(I*ArcSin[a*x])] - 6*PolyLog[3, -E^(I*ArcSin[a*x])] + 6*PolyLog[3, E^(I*ArcSin[a*x])])

Maple [A] time = 0.074, size = 179, normalized size = 1.7

$$-\frac{(\arcsin(ax))^3}{x} - 3a(\arcsin(ax))^2 \ln\left(1 + iax + \sqrt{-a^2x^2 + 1}\right) + 6ia \arcsin(ax) \operatorname{polylog}\left(2, -iax - \sqrt{-a^2x^2 + 1}\right) - 6a \operatorname{polylog}\left(2, iax - \sqrt{-a^2x^2 + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^3/x^2, x)

```
[Out] -arcsin(a*x)^3/x-3*a*arcsin(a*x)^2*ln(1+I*a*x+(-a^2*x^2+1)^(1/2))+6*I*a*arcsin(a*x)*polylog(2,-I*a*x-(-a^2*x^2+1)^(1/2))-6*a*polylog(3,-I*a*x-(-a^2*x^2+1)^(1/2))+3*a*arcsin(a*x)^2*ln(1-I*a*x-(-a^2*x^2+1)^(1/2))-6*I*a*arcsin(a*x)*polylog(2,I*a*x+(-a^2*x^2+1)^(1/2))+6*a*polylog(3,I*a*x+(-a^2*x^2+1)^(1/2))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{\arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3 + 3ax \int \frac{\sqrt{-ax+1} \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2}{\sqrt{ax+1}(ax-1)x} dx}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^3/x^2,x, algorithm="maxima")
```

```
[Out] -(arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3 + 3*a*x*integrate(sqrt(a*x + 1)*sqrt(-a*x + 1)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2/(a^2*x^3 - x), x))/x
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^3}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^3/x^2,x, algorithm="fricas")
```

```
[Out] integral(arcsin(a*x)^3/x^2, x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{asin}^3(ax)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(asin(a*x)**3/x**2,x)
```

```
[Out] Integral(asin(a*x)**3/x**2, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^3}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^3/x^2,x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^3/x^2, x)
```

3.29 $\int \frac{\sin^{-1}(ax)^3}{x^3} dx$

Optimal. Leaf size=102

$$-\frac{3}{2}ia^2\text{PolyLog}\left(2, e^{2i\sin^{-1}(ax)}\right) - \frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{3}{2}ia^2\sin^{-1}(ax)^2 + 3a^2\sin^{-1}(ax)\log\left(1 - e^{2i\sin^{-1}(ax)}\right) - \frac{\sin^{-1}(ax)^3}{2x^2}$$

```
[Out] ((-3*I)/2)*a^2*ArcSin[a*x]^2 - (3*a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(2*x)
- ArcSin[a*x]^3/(2*x^2) + 3*a^2*ArcSin[a*x]*Log[1 - E^((2*I)*ArcSin[a*x])]
- ((3*I)/2)*a^2*PolyLog[2, E^((2*I)*ArcSin[a*x])]
```

Rubi [A] time = 0.169331, antiderivative size = 102, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4627, 4681, 4625, 3717, 2190, 2279, 2391}

$$-\frac{3}{2}ia^2\text{PolyLog}\left(2, e^{2i\sin^{-1}(ax)}\right) - \frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{3}{2}ia^2\sin^{-1}(ax)^2 + 3a^2\sin^{-1}(ax)\log\left(1 - e^{2i\sin^{-1}(ax)}\right) - \frac{\sin^{-1}(ax)^3}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[ArcSin[a*x]^3/x^3, x]
```

```
[Out] ((-3*I)/2)*a^2*ArcSin[a*x]^2 - (3*a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(2*x)
- ArcSin[a*x]^3/(2*x^2) + 3*a^2*ArcSin[a*x]*Log[1 - E^((2*I)*ArcSin[a*x])]
- ((3*I)/2)*a^2*PolyLog[2, E^((2*I)*ArcSin[a*x])]
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4681

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_.)*((d_) + (e_.
)*(x_)^2)^(p_), x_Symbol] :> Simp[((f*x)^(m + 1)*(d + e*x^2)^(p + 1)*(a + b
*ArcSin[c*x])^n)/(d*f*(m + 1)), x] - Dist[(b*c*n*d^IntPart[p]*(d + e*x^2)^F
racPart[p])/(f*(m + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(f*x)^(m + 1)*(1 - c
^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d,
e, f, m, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && EqQ[m + 2*p + 3, 0] &
& NeQ[m, -1]
```

Rule 4625

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)/(x_), x_Symbol] :> Subst[Int[(
a + b*x)^n/Tan[x], x], x, ArcSin[c*x]] /; FreeQ[{a, b, c}, x] && IGtQ[n, 0]
```

Rule 3717

```
Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + Pi*(k_.) + (f_.)*(x_)], x_Symbol]
:> Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^
m*E^(2*I*k*Pi)*E^(2*I*(e + f*x)))/(1 + E^(2*I*k*Pi)*E^(2*I*(e + f*x))), x],
x] /; FreeQ[{c, d, e, f}, x] && IntegerQ[4*k] && IGtQ[m, 0]
```

Rule 2190

```
Int[(((F_)^((g_)*(e_) + (f_)*(x_)))^(n_))*((c_) + (d_)*(x_))^(m_)]/
((a_) + (b_)*((F_)^((g_)*(e_) + (f_)*(x_)))^(n_)), x_Symbol] := Simp
[((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a]/(b*f*g*n*Log[F]), x] - Di
st[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)
))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2279

```
Int[Log[(a_) + (b_)*((F_)^((e_)*((c_) + (d_)*(x_)))^(n_))], x_Symbol]
:= Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)
))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2391

```
Int[Log[(c_)*((d_) + (e_)*(x_)^(n_))]/(x_), x_Symbol] := -Simp[PolyLog[2
, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^3}{x^3} dx &= -\frac{\sin^{-1}(ax)^3}{2x^2} + \frac{1}{2}(3a) \int \frac{\sin^{-1}(ax)^2}{x^2\sqrt{1-a^2x^2}} dx \\ &= -\frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{2x^2} + (3a^2) \int \frac{\sin^{-1}(ax)}{x} dx \\ &= -\frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{2x^2} + (3a^2) \text{Subst} \left(\int x \cot(x) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{3}{2}ia^2 \sin^{-1}(ax)^2 - \frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{2x^2} - (6ia^2) \text{Subst} \left(\int \frac{e^{2ix}}{1-e^{2ix}} dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{3}{2}ia^2 \sin^{-1}(ax)^2 - \frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{2x^2} + 3a^2 \sin^{-1}(ax) \log \left(1 - e^{2i\sin^{-1}(ax)} \right) - (3) \\ &= -\frac{3}{2}ia^2 \sin^{-1}(ax)^2 - \frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{2x^2} + 3a^2 \sin^{-1}(ax) \log \left(1 - e^{2i\sin^{-1}(ax)} \right) + \frac{1}{2} \\ &= -\frac{3}{2}ia^2 \sin^{-1}(ax)^2 - \frac{3a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{2x^2} + 3a^2 \sin^{-1}(ax) \log \left(1 - e^{2i\sin^{-1}(ax)} \right) - \frac{3}{2} \end{aligned}$$

Mathematica [A] time = 0.252512, size = 92, normalized size = 0.9

$$-\frac{3}{2}ia^2 \text{PolyLog} \left(2, e^{2i\sin^{-1}(ax)} \right) - \frac{\sin^{-1}(ax) \left(3ax \left(\sqrt{1-a^2x^2} + iax \right) \sin^{-1}(ax) - 6a^2x^2 \log \left(1 - e^{2i\sin^{-1}(ax)} \right) + \sin^{-1}(ax)^2 \right)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[ArcSin[a*x]^3/x^3,x]
```

```
[Out] -(ArcSin[a*x]*(3*a*x*(I*a*x + Sqrt[1 - a^2*x^2])*ArcSin[a*x] + ArcSin[a*x]^
2 - 6*a^2*x^2*Log[1 - E^((2*I)*ArcSin[a*x])]))/(2*x^2) - ((3*I)/2)*a^2*Poly
Log[2, E^((2*I)*ArcSin[a*x])]
```

Maple [A] time = 0.098, size = 163, normalized size = 1.6

$$-\frac{3i}{2}a^2 (\arcsin(ax))^2 - \frac{3a (\arcsin(ax))^2 \sqrt{-a^2x^2 + 1}}{2x} - \frac{(\arcsin(ax))^3}{2x^2} + 3a^2 \arcsin(ax) \ln \left(1 + iax + \sqrt{-a^2x^2 + 1} \right) +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^3/x^3,x)

[Out]
$$-3/2*I*a^2*\arcsin(a*x)^2-3/2*a*\arcsin(a*x)^2*(-a^2*x^2+1)^{(1/2)}/x-1/2*\arcsin(a*x)^3/x^2+3*a^2*\arcsin(a*x)*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)})+3*a^2*\arcsin(a*x)*\ln(1-I*a*x-(-a^2*x^2+1)^{(1/2)})-3*I*a^2*\operatorname{polylog}(2,-I*a*x-(-a^2*x^2+1)^{(1/2)})-3*I*a^2*\operatorname{polylog}(2,I*a*x+(-a^2*x^2+1)^{(1/2)})$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{\frac{3}{4} \left(\sqrt{ax+1} \sqrt{-ax+1} \arctan(ax, \sqrt{ax+1} \sqrt{-ax+1})^2 + 4x \int \frac{\sqrt{ax+1} \sqrt{-ax+1} \arctan(ax, \sqrt{ax+1} \sqrt{-ax+1})^2 - 2(a^3x^3 - ax) \arctan(ax, \sqrt{ax+1} \sqrt{-ax+1})}{4(a^2x^4 - x^2)} dx \right)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x^3,x, algorithm="maxima")

[Out]
$$-1/2*(6*a*x^2*\integrate(1/2*\sqrt{a*x+1}*\sqrt{-a*x+1}*\arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1})^2/(a^2*x^4-x^2), x) + \arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1})^3)/x^2$$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\arcsin(ax)^3}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x^3,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^3/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{asin}^3(ax)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**3/x**3,x)

[Out] Integral(asin(a*x)**3/x**3, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^3}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^3/x^3,x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^3/x^3, x)
```

3.30 $\int \frac{\sin^{-1}(ax)^3}{x^4} dx$

Optimal. Leaf size=179

$$ia^3 \sin^{-1}(ax) \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - ia^3 \sin^{-1}(ax) \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - a^3 \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right) + a^3 \text{PolyLog}\left(3, e^{i \sin^{-1}(ax)}\right)$$

```
[Out] -((a^2*ArcSin[a*x])/x) - (a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(2*x^2) - ArcSin[a*x]^3/(3*x^3) - a^3*ArcSin[a*x]^2*ArcTanh[E^(I*ArcSin[a*x])] - a^3*ArcTanh[Sqrt[1 - a^2*x^2]] + I*a^3*ArcSin[a*x]*PolyLog[2, -E^(I*ArcSin[a*x])] - I*a^3*ArcSin[a*x]*PolyLog[2, E^(I*ArcSin[a*x])] - a^3*PolyLog[3, -E^(I*ArcSin[a*x])] + a^3*PolyLog[3, E^(I*ArcSin[a*x])]
```

Rubi [A] time = 0.284581, antiderivative size = 179, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 10, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {4627, 4701, 4709, 4183, 2531, 2282, 6589, 266, 63, 208}

$$ia^3 \sin^{-1}(ax) \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - ia^3 \sin^{-1}(ax) \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - a^3 \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right) + a^3 \text{PolyLog}\left(3, e^{i \sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

```
[In] Int[ArcSin[a*x]^3/x^4, x]
```

```
[Out] -((a^2*ArcSin[a*x])/x) - (a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2)/(2*x^2) - ArcSin[a*x]^3/(3*x^3) - a^3*ArcSin[a*x]^2*ArcTanh[E^(I*ArcSin[a*x])] - a^3*ArcTanh[Sqrt[1 - a^2*x^2]] + I*a^3*ArcSin[a*x]*PolyLog[2, -E^(I*ArcSin[a*x])] - I*a^3*ArcSin[a*x]*PolyLog[2, E^(I*ArcSin[a*x])] - a^3*PolyLog[3, -E^(I*ArcSin[a*x])] + a^3*PolyLog[3, E^(I*ArcSin[a*x])]
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4701

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((f_.)*(x_))^(m_.)*((d_) + (e_.)*(x_)^2)^(p_), x_Symbol]
:> Simp[((f*x)^(m + 1)*(d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(d*f*(m + 1)), x] + (Dist[(c^2*(m + 2*p + 3))/(f^2*(m + 1)), Int[(f*x)^(m + 2)*(d + e*x^2)^p*(a + b*ArcSin[c*x])^n, x], x] - Dist[(b*c*n*d*IntPart[p]*(d + e*x^2)^FracPart[p])/(f*(m + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(f*x)^(m + 1)*(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && LtQ[m, -1] && IntegerQ[m]
```

Rule 4709

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol]
:> Dist[1/(c^(m + 1)*Sqrt[d]), Subst[Int[(a + b*x)^n*Sin[x]^m, x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && IGtQ[n, 0] && IntegerQ[m]
```

Rule 4183


```
Int[csc[(e_.) + (f_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] := Simp[(-2*(c + d*x)^m*ArcTanh[E^(I*(e + f*x))])/f, x] + (-Dist[(d*m)/f, Int[(c + d*x)^m - 1]*Log[1 - E^(I*(e + f*x))], x], x] + Dist[(d*m)/f, Int[(c + d*x)^m - 1]*Log[1 + E^(I*(e + f*x))], x], x] /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^(n_.)]*((f_.) + (g_.)*(x_))^(m_.), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^m - 1]*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]
```

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 266

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_))^(n_)]^(p_), x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sin^{-1}(ax)^3}{x^4} dx &= -\frac{\sin^{-1}(ax)^3}{3x^3} + a \int \frac{\sin^{-1}(ax)^2}{x^3 \sqrt{1-a^2x^2}} dx \\
&= -\frac{a\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{2x^2} - \frac{\sin^{-1}(ax)^3}{3x^3} + a^2 \int \frac{\sin^{-1}(ax)}{x^2} dx + \frac{1}{2}a^3 \int \frac{\sin^{-1}(ax)^2}{x\sqrt{1-a^2x^2}} dx \\
&= -\frac{a^2 \sin^{-1}(ax)}{x} - \frac{a\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{2x^2} - \frac{\sin^{-1}(ax)^3}{3x^3} + \frac{1}{2}a^3 \operatorname{Subst}\left(\int x^2 \csc(x) dx, x, \sin^{-1}(ax)\right) + a^3 \operatorname{Subst}\left(\int \frac{\sin^{-1}(ax)}{x} dx, x, \sin^{-1}(ax)\right) \\
&= -\frac{a^2 \sin^{-1}(ax)}{x} - \frac{a\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{2x^2} - \frac{\sin^{-1}(ax)^3}{3x^3} - a^3 \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) + \frac{1}{2}a^3 \operatorname{Subst}\left(\int \frac{\sin^{-1}(ax)}{x} dx, x, \sin^{-1}(ax)\right) \\
&= -\frac{a^2 \sin^{-1}(ax)}{x} - \frac{a\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{2x^2} - \frac{\sin^{-1}(ax)^3}{3x^3} - a^3 \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) + ia^3 \sin^{-1}(ax) \operatorname{Li}_2\left(-e^{i \sin^{-1}(ax)}\right) \\
&= -\frac{a^2 \sin^{-1}(ax)}{x} - \frac{a\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{2x^2} - \frac{\sin^{-1}(ax)^3}{3x^3} - a^3 \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) - a^3 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) \\
&= -\frac{a^2 \sin^{-1}(ax)}{x} - \frac{a\sqrt{1-a^2x^2} \sin^{-1}(ax)^2}{2x^2} - \frac{\sin^{-1}(ax)^3}{3x^3} - a^3 \sin^{-1}(ax)^2 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right) - a^3 \tanh^{-1}\left(e^{i \sin^{-1}(ax)}\right)
\end{aligned}$$

Mathematica [A] time = 2.79478, size = 284, normalized size = 1.59

$$\frac{1}{48}a^3 \left(48i \sin^{-1}(ax) \operatorname{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 48i \sin^{-1}(ax) \operatorname{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 48 \operatorname{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right) + 48 \operatorname{PolyLog}\left(3, e^{i \sin^{-1}(ax)}\right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^3/x^4, x]

[Out] $(a^3(-24 \operatorname{ArcSin}[a*x] \operatorname{Cot}[\operatorname{ArcSin}[a*x]/2] - 4 \operatorname{ArcSin}[a*x]^3 \operatorname{Cot}[\operatorname{ArcSin}[a*x]/2] - 6 \operatorname{ArcSin}[a*x]^2 \operatorname{Csc}[\operatorname{ArcSin}[a*x]/2]^2 - a*x \operatorname{ArcSin}[a*x]^3 \operatorname{Csc}[\operatorname{ArcSin}[a*x]/2]^4 + 24 \operatorname{ArcSin}[a*x]^2 \operatorname{Log}[1 - E^{(I \operatorname{ArcSin}[a*x])}] - 24 \operatorname{ArcSin}[a*x]^2 \operatorname{Log}[1 + E^{(I \operatorname{ArcSin}[a*x])}] + 48 \operatorname{Log}[\operatorname{Tan}[\operatorname{ArcSin}[a*x]/2]] + (48I) \operatorname{ArcSin}[a*x] \operatorname{PolyLog}[2, -E^{(I \operatorname{ArcSin}[a*x])}] - (48I) \operatorname{ArcSin}[a*x] \operatorname{PolyLog}[2, E^{(I \operatorname{ArcSin}[a*x])}] - 48 \operatorname{PolyLog}[3, -E^{(I \operatorname{ArcSin}[a*x])}] + 48 \operatorname{PolyLog}[3, E^{(I \operatorname{ArcSin}[a*x])}] + 6 \operatorname{ArcSin}[a*x]^2 \operatorname{Sec}[\operatorname{ArcSin}[a*x]/2]^2 - (16 \operatorname{ArcSin}[a*x]^3 \operatorname{Sin}[\operatorname{ArcSin}[a*x]/2]^4) / (a^3 x^3) - 24 \operatorname{ArcSin}[a*x] \operatorname{Tan}[\operatorname{ArcSin}[a*x]/2] - 4 \operatorname{ArcSin}[a*x]^3 \operatorname{Tan}[\operatorname{ArcSin}[a*x]/2])) / 48$

Maple [A] time = 0.148, size = 250, normalized size = 1.4

$$-\frac{a(\arcsin(ax))^2 \sqrt{-a^2x^2+1}}{2x^2} - \frac{a^2 \arcsin(ax)}{x} - \frac{(\arcsin(ax))^3}{3x^3} - \frac{a^3(\arcsin(ax))^2}{2} \ln\left(1+iax+\sqrt{-a^2x^2+1}\right) + ia^3 \arcsin(ax)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^3/x^4, x)

[Out] $-1/2*a*\arcsin(a*x)^2*(-a^2*x^2+1)^{(1/2)}/x^2 - a^2*\arcsin(a*x)/x - 1/3*\arcsin(a*x)^3/x^3 - 1/2*a^3*\arcsin(a*x)^2*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)}) + I*a^3*\arcsin(a*x)*\operatorname{polylog}(2, -I*a*x - (-a^2*x^2+1)^{(1/2)}) - a^3*\operatorname{polylog}(3, -I*a*x - (-a^2*x^2+1)^{(1/2)}) + 1/2*a^3*\arcsin(a*x)^2*\ln(1-I*a*x - (-a^2*x^2+1)^{(1/2)}) - I*a^3*\arcsin(a*x)*\operatorname{polylog}(2, I*a*x + (-a^2*x^2+1)^{(1/2)}) + a^3*\operatorname{polylog}(3, I*a*x + (-a^2*x^2+1)^{(1/2)})$

/2))-2*a^3*arctanh(I*a*x+(-a^2*x^2+1)^(1/2))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$-\frac{3ax^3 \int \frac{\sqrt{-ax+1} \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}{\sqrt{ax+1}(ax-1)x^3} dx + \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x^4,x, algorithm="maxima")

[Out] -1/3*(3*a*x^3*integrate(sqrt(a*x + 1)*sqrt(-a*x + 1)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2/(a^2*x^5 - x^3), x) + arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3)/x^3

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^3}{x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x^4,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^3/x^4, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{asin}^3(ax)}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**3/x**4,x)

[Out] Integral(asin(a*x)**3/x**4, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^3}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x^4,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^3/x^4, x)

3.31 $\int \frac{\sin^{-1}(ax)^3}{x^5} dx$

Optimal. Leaf size=169

$$-\frac{1}{2}ia^4\text{PolyLog}\left(2, e^{2i\sin^{-1}(ax)}\right) - \frac{a^3\sqrt{1-a^2x^2}}{4x} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{1}{2}ia^4\text{PolyLog}\left(2, e^{-2i\sin^{-1}(ax)}\right)$$

[Out] $-(a^3\sqrt{1-a^2x^2})/(4x) - (a^2\text{ArcSin}[a*x])/(4x^2) - (I/2)*a^4*\text{ArcSin}[a*x]^2 - (a*\sqrt{1-a^2x^2}*\text{ArcSin}[a*x]^2)/(4x^3) - (a^3*\sqrt{1-a^2x^2}*\text{ArcSin}[a*x]^2)/(2*x) - \text{ArcSin}[a*x]^3/(4*x^4) + a^4*\text{ArcSin}[a*x]*\text{Log}[1 - E^((2*I)*\text{ArcSin}[a*x])] - (I/2)*a^4*\text{PolyLog}[2, E^((2*I)*\text{ArcSin}[a*x])]$

Rubi [A] time = 0.291772, antiderivative size = 169, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 9, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.9$, Rules used = {4627, 4701, 4681, 4625, 3717, 2190, 2279, 2391, 264}

$$-\frac{1}{2}ia^4\text{PolyLog}\left(2, e^{2i\sin^{-1}(ax)}\right) - \frac{a^3\sqrt{1-a^2x^2}}{4x} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{1}{2}ia^4\text{PolyLog}\left(2, e^{-2i\sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^3/x^5,x]

[Out] $-(a^3\sqrt{1-a^2x^2})/(4x) - (a^2\text{ArcSin}[a*x])/(4x^2) - (I/2)*a^4*\text{ArcSin}[a*x]^2 - (a*\sqrt{1-a^2x^2}*\text{ArcSin}[a*x]^2)/(4x^3) - (a^3*\sqrt{1-a^2x^2}*\text{ArcSin}[a*x]^2)/(2*x) - \text{ArcSin}[a*x]^3/(4*x^4) + a^4*\text{ArcSin}[a*x]*\text{Log}[1 - E^((2*I)*\text{ArcSin}[a*x])] - (I/2)*a^4*\text{PolyLog}[2, E^((2*I)*\text{ArcSin}[a*x])]$

Rule 4627

Int[((a_.) + ArcSin[(c_.)(x_.)]*(b_.))^ (n_.)*((d_.)(x_.))^ (m_.), x_Symbol] :> Simp[((d*x)^(m+1)*(a + b*ArcSin[c*x])^n)/(d*(m+1)), x] - Dist[(b*c*n)/(d*(m+1)), Int[((d*x)^(m+1)*(a + b*ArcSin[c*x])^(n-1))/Sqrt[1-c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4701

Int[((a_.) + ArcSin[(c_.)(x_.)]*(b_.))^ (n_.)*((f_.)(x_.))^ (m_.)*((d_.) + (e_.)(x_)^2)^ (p_.), x_Symbol] :> Simp[((f*x)^(m+1)*(d + e*x^2)^(p+1)*(a + b*ArcSin[c*x])^n)/(d*f*(m+1)), x] + (Dist[(c^2*(m+2*p+3))/(f^2*(m+1)), Int[(f*x)^(m+2)*(d + e*x^2)^p*(a + b*ArcSin[c*x])^n, x], x] - Dist[(b*c*n*d*IntPart[p]*(d + e*x^2)^FracPart[p])/(f*(m+1)*(1-c^2*x^2)^FracPart[p]), Int[(f*x)^(m+1)*(1-c^2*x^2)^(p+1/2)*(a + b*ArcSin[c*x])^(n-1), x], x]) /; FreeQ[{a, b, c, d, e, f, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && LtQ[m, -1] && IntegerQ[m]

Rule 4681

Int[((a_.) + ArcSin[(c_.)(x_.)]*(b_.))^ (n_.)*((f_.)(x_.))^ (m_.)*((d_.) + (e_.)(x_)^2)^ (p_.), x_Symbol] :> Simp[((f*x)^(m+1)*(d + e*x^2)^(p+1)*(a + b*ArcSin[c*x])^n)/(d*f*(m+1)), x] - Dist[(b*c*n*d*IntPart[p]*(d + e*x^2)^FracPart[p])/(f*(m+1)*(1-c^2*x^2)^FracPart[p]), Int[(f*x)^(m+1)*(1-c^2*x^2)^(p+1/2)*(a + b*ArcSin[c*x])^(n-1), x], x] /; FreeQ[{a, b, c, d, e, f, m, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && EqQ[m + 2*p + 3, 0] && NeQ[m, -1]

Rule 4625

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_/(x_), x_Symbol] := Subst[Int[(a + b*x)^n/Tan[x], x], x, ArcSin[c*x]] /; FreeQ[{a, b, c}, x] && IGtQ[n, 0]

Rule 3717

Int[((c_.) + (d_.)*(x_))^(m_.)*tan[(e_.) + Pi*(k_.) + (f_.)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m * E^(2*I*k*Pi) * E^(2*I*(e + f*x)))/(1 + E^(2*I*k*Pi) * E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IntegerQ[4*k] && IGtQ[m, 0]

Rule 2190

Int[(((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)*((c_.) + (d_.)*(x_))^(m_.))/((a_.) + (b_.)*((F_)^((g_.)*((e_.) + (f_.)*(x_))))^(n_.)), x_Symbol] := Simp[((c + d*x)^m * Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1) * Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_.)*((F_)^((e_.)*((c_.) + (d_.)*(x_))))^(n_.)], x_Symbol] := Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

Int[Log[(c_.)*((d_) + (e_.)*(x_)^(n_.))]/(x_), x_Symbol] := -Simp[PolyLog[2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rule 264

Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[((c*x)^(m + 1)*(a + b*x^n)^(p + 1))/(a*c*(m + 1)), x] /; FreeQ[{a, b, c, m, n, p}, x] && EqQ[(m + 1)/n + p + 1, 0] && NeQ[m, -1]

Rubi steps

$$\begin{aligned}
 \int \frac{\sin^{-1}(ax)^3}{x^5} dx &= -\frac{\sin^{-1}(ax)^3}{4x^4} + \frac{1}{4}(3a) \int \frac{\sin^{-1}(ax)^2}{x^4\sqrt{1-a^2x^2}} dx \\
 &= -\frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{\sin^{-1}(ax)^3}{4x^4} + \frac{1}{2}a^2 \int \frac{\sin^{-1}(ax)}{x^3} dx + \frac{1}{2}a^3 \int \frac{\sin^{-1}(ax)^2}{x^2\sqrt{1-a^2x^2}} dx \\
 &= -\frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{4x^4} + \frac{1}{4}a^3 \int \frac{1}{x^2\sqrt{1-a^2x^2}} dx \\
 &= -\frac{a^3\sqrt{1-a^2x^2}}{4x} - \frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} - \frac{\sin^{-1}(ax)^3}{4x^4} + \frac{1}{4}a^3 \int \frac{1}{x^2\sqrt{1-a^2x^2}} dx \\
 &= -\frac{a^3\sqrt{1-a^2x^2}}{4x} - \frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{1}{2}ia^4\sin^{-1}(ax)^2 - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} \\
 &= -\frac{a^3\sqrt{1-a^2x^2}}{4x} - \frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{1}{2}ia^4\sin^{-1}(ax)^2 - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} \\
 &= -\frac{a^3\sqrt{1-a^2x^2}}{4x} - \frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{1}{2}ia^4\sin^{-1}(ax)^2 - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x} \\
 &= -\frac{a^3\sqrt{1-a^2x^2}}{4x} - \frac{a^2\sin^{-1}(ax)}{4x^2} - \frac{1}{2}ia^4\sin^{-1}(ax)^2 - \frac{a\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{4x^3} - \frac{a^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{2x}
 \end{aligned}$$

Mathematica [A] time = 0.679215, size = 116, normalized size = 0.69

$$\frac{1}{4} \left(-\frac{\sin^{-1}(ax)^3}{x^4} + a^4 \left(-2i \operatorname{PolyLog} \left(2, e^{2i \sin^{-1}(ax)} \right) - \frac{\sqrt{1-a^2x^2} \left(\left(\frac{1}{a^2x^2} + 2 \right) \sin^{-1}(ax)^2 + 1 \right)}{ax} - \sin^{-1}(ax) \left(\frac{1}{a^2x^2} + 2i \sin^{-1}(ax) \right) \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^3/x^5,x]

[Out] $(-\operatorname{ArcSin}[a*x]^3/x^4 + a^4 * (-(\operatorname{Sqrt}[1 - a^2*x^2] * (1 + (2 + 1/(a^2*x^2)) * \operatorname{ArcSin}[a*x]^2)) / (a*x)) - \operatorname{ArcSin}[a*x] * (1/(a^2*x^2) + (2*I) * \operatorname{ArcSin}[a*x] - 4 * \operatorname{Log}[1 - E^{((2*I) * \operatorname{ArcSin}[a*x])}])) - (2*I) * \operatorname{PolyLog}[2, E^{((2*I) * \operatorname{ArcSin}[a*x])}]])) / 4$

Maple [A] time = 0.156, size = 225, normalized size = 1.3

$$-\frac{i}{2} a^4 (\arcsin(ax))^2 - \frac{a^3 (\arcsin(ax))^2}{2x} \sqrt{-a^2x^2+1} + \frac{i}{4} a^4 - \frac{a^3}{4x} \sqrt{-a^2x^2+1} - \frac{a (\arcsin(ax))^2}{4x^3} \sqrt{-a^2x^2+1} - \frac{a^2 \arcsin(ax)}{4x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^3/x^5,x)

[Out] $-1/2*I*a^4*\arcsin(a*x)^2-1/2*a^3*\arcsin(a*x)^2*(-a^2*x^2+1)^{(1/2)}/x+1/4*I*a^4-1/4*a^3*(-a^2*x^2+1)^{(1/2)}/x-1/4*a*\arcsin(a*x)^2*(-a^2*x^2+1)^{(1/2)}/x^3-1/4*a^2*\arcsin(a*x)/x^2-1/4*\arcsin(a*x)^3/x^4+a^4*\arcsin(a*x)*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)})+a^4*\arcsin(a*x)*\ln(1-I*a*x-(-a^2*x^2+1)^{(1/2)})-I*a^4*\operatorname{polylog}(2,-I*a*x-(-a^2*x^2+1)^{(1/2)})-I*a^4*\operatorname{polylog}(2,I*a*x+(-a^2*x^2+1)^{(1/2)})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{4} \left((2a^2x^2+1) \sqrt{ax+1} \sqrt{-ax+1} \arctan(ax, \sqrt{ax+1} \sqrt{-ax+1})^2 + 12x^3 \int \frac{9\sqrt{ax+1} \sqrt{-ax+1} \arctan(ax, \sqrt{ax+1} \sqrt{-ax+1})^2 - 2(2a^5x^5 - 12(a^2x^6 - x^4))}{12(a^2x^6 - x^4)} dx \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x^5,x, algorithm="maxima")

[Out] $-1/4*(12*a*x^4*\operatorname{integrate}(1/4*\operatorname{sqrt}(a*x+1)*\operatorname{sqrt}(-a*x+1)*\operatorname{arctan2}(a*x, \operatorname{sqrt}(a*x+1)*\operatorname{sqrt}(-a*x+1))^2/(a^2*x^6-x^4), x) + \operatorname{arctan2}(a*x, \operatorname{sqrt}(a*x+1)*\operatorname{sqrt}(-a*x+1))^3)/x^4$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral} \left(\frac{\arcsin(ax)^3}{x^5}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^3/x^5,x, algorithm="fricas")

[Out] `integral(arcsin(a*x)^3/x^5, x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{asin}^3(ax)}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(asin(a*x)**3/x**5,x)`

[Out] `Integral(asin(a*x)**3/x**5, x)`

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{arcsin}(ax)^3}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^3/x^5,x, algorithm="giac")`

[Out] `integrate(arcsin(a*x)^3/x^5, x)`

3.32 $\int x^5 \sin^{-1}(ax)^4 dx$

Optimal. Leaf size=282

$$\frac{65x^4}{3456a^2} + \frac{245x^2}{1152a^4} + \frac{x^5\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{9a} - \frac{x^5\sqrt{1-a^2x^2}\sin^{-1}(ax)}{54a} - \frac{5x^4\sin^{-1}(ax)^2}{48a^2} + \frac{5x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{36a^3} - 65x^6/324$$

[Out] (245*x^2)/(1152*a^4) + (65*x^4)/(3456*a^2) + x^6/324 - (245*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(576*a^5) - (65*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(864*a^3) - (x^5*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(54*a) + (245*ArcSin[a*x]^2)/(1152*a^6) - (5*x^2*ArcSin[a*x]^2)/(16*a^4) - (5*x^4*ArcSin[a*x]^2)/(48*a^2) - (x^6*ArcSin[a*x]^2)/18 + (5*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(24*a^5) + (5*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(36*a^3) + (x^5*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(9*a) - (5*ArcSin[a*x]^4)/(96*a^6) + (x^6*ArcSin[a*x]^4)/6

Rubi [A] time = 0.869246, antiderivative size = 282, normalized size of antiderivative = 1., number of steps used = 23, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4627, 4707, 4641, 30}

$$\frac{65x^4}{3456a^2} + \frac{245x^2}{1152a^4} + \frac{x^5\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{9a} - \frac{x^5\sqrt{1-a^2x^2}\sin^{-1}(ax)}{54a} - \frac{5x^4\sin^{-1}(ax)^2}{48a^2} + \frac{5x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{36a^3} - 65x^6/324$$

Antiderivative was successfully verified.

[In] Int[x^5*ArcSin[a*x]^4,x]

[Out] (245*x^2)/(1152*a^4) + (65*x^4)/(3456*a^2) + x^6/324 - (245*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(576*a^5) - (65*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(864*a^3) - (x^5*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(54*a) + (245*ArcSin[a*x]^2)/(1152*a^6) - (5*x^2*ArcSin[a*x]^2)/(16*a^4) - (5*x^4*ArcSin[a*x]^2)/(48*a^2) - (x^6*ArcSin[a*x]^2)/18 + (5*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(24*a^5) + (5*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(36*a^3) + (x^5*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(9*a) - (5*ArcSin[a*x]^4)/(96*a^6) + (x^6*ArcSin[a*x]^4)/6

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 30

Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned}
 \int x^5 \sin^{-1}(ax)^4 dx &= \frac{1}{6}x^6 \sin^{-1}(ax)^4 - \frac{1}{3}(2a) \int \frac{x^6 \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx \\
 &= \frac{x^5 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a} + \frac{1}{6}x^6 \sin^{-1}(ax)^4 - \frac{1}{3} \int x^5 \sin^{-1}(ax)^2 dx - \frac{5 \int \frac{x^4 \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx}{9a} \\
 &= -\frac{1}{18}x^6 \sin^{-1}(ax)^2 + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{36a^3} + \frac{x^5 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a} + \frac{1}{6}x^6 \sin^{-1}(ax)^4 - \frac{5 \int}{9a} \\
 &= -\frac{x^5 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{54a} - \frac{5x^4 \sin^{-1}(ax)^2}{48a^2} - \frac{1}{18}x^6 \sin^{-1}(ax)^2 + \frac{5x \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{24a^5} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{24a^5} \\
 &= \frac{x^6}{324} - \frac{65x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{864a^3} - \frac{x^5 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{54a} - \frac{5x^2 \sin^{-1}(ax)^2}{16a^4} - \frac{5x^4 \sin^{-1}(ax)^2}{48a^2} - \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{54a} \\
 &= \frac{65x^4}{3456a^2} + \frac{x^6}{324} - \frac{245x \sqrt{1-a^2x^2} \sin^{-1}(ax)}{576a^5} - \frac{65x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{864a^3} - \frac{x^5 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{54a} \\
 &= \frac{245x^2}{1152a^4} + \frac{65x^4}{3456a^2} + \frac{x^6}{324} - \frac{245x \sqrt{1-a^2x^2} \sin^{-1}(ax)}{576a^5} - \frac{65x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{864a^3} - \frac{x^5 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{54a}
 \end{aligned}$$

Mathematica [A] time = 0.0977085, size = 167, normalized size = 0.59

$$\frac{a^2x^2(32a^4x^4 + 195a^2x^2 + 2205) + 108(16a^6x^6 - 5)\sin^{-1}(ax)^4 + 144ax\sqrt{1-a^2x^2}(8a^4x^4 + 10a^2x^2 + 15)\sin^{-1}(ax)^3 - 10368a^6}{10368a^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^5*ArcSin[a*x]^4,x]

[Out] (a^2*x^2*(2205 + 195*a^2*x^2 + 32*a^4*x^4) - 6*a*x*Sqrt[1 - a^2*x^2]*(735 + 130*a^2*x^2 + 32*a^4*x^4)*ArcSin[a*x] - 9*(-245 + 360*a^2*x^2 + 120*a^4*x^4 + 64*a^6*x^6)*ArcSin[a*x]^2 + 144*a*x*Sqrt[1 - a^2*x^2]*(15 + 10*a^2*x^2 + 8*a^4*x^4)*ArcSin[a*x]^3 + 108*(-5 + 16*a^6*x^6)*ArcSin[a*x]^4)/(10368*a^6)

Maple [A] time = 0.1, size = 320, normalized size = 1.1

$$\frac{1}{a^6} \left(\frac{a^6 x^6 (\arcsin(ax))^4}{6} - \frac{(\arcsin(ax))^3}{72} \left(-8 \sqrt{-a^2x^2 + 1} a^5 x^5 - 10 a^3 x^3 \sqrt{-a^2x^2 + 1} - 15 ax \sqrt{-a^2x^2 + 1} + 15 \arcsin(ax) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5*arcsin(a*x)^4,x)

[Out] 1/a^6*(1/6*a^6*x^6*arcsin(a*x)^4-1/72*arcsin(a*x)^3*(-8*(-a^2*x^2+1)^(1/2)*a^5*x^5-10*a^3*x^3*(-a^2*x^2+1)^(1/2)-15*a*x*(-a^2*x^2+1)^(1/2)+15*arcsin(a*x))-1/18*arcsin(a*x)^2*a^6*x^6+1/432*arcsin(a*x)*(-8*(-a^2*x^2+1)^(1/2)*a^5*x^5-10*a^3*x^3*(-a^2*x^2+1)^(1/2)-15*a*x*(-a^2*x^2+1)^(1/2)+15*arcsin(a*x))

$$5x^5 - 10a^3x^3(-a^2x^2+1)^{1/2} - 15ax(-a^2x^2+1)^{1/2} + 15\arcsin(ax) + 115/1152\arcsin(ax)^2 + 1/324a^6x^6 + 65/3456a^4x^4 + 245/1152a^2x^2 - 5/48a^4x^4\arcsin(ax)^2 + 5/192\arcsin(ax)(-2a^3x^3(-a^2x^2+1)^{1/2} - 3ax(-a^2x^2+1)^{1/2} + 3\arcsin(ax)) - 5/16(a^2x^2-1)\arcsin(ax)^2 - 5/16\arcsin(ax)(ax(-a^2x^2+1)^{1/2} + \arcsin(ax)) + 5/32\arcsin(ax)^4$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{6}x^6 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^4 + 2a \int \frac{\sqrt{ax+1}\sqrt{-ax+1}x^6 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3}{3(a^2x^2-1)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*arcsin(a*x)^4,x, algorithm="maxima")

[Out] 1/6*x^6*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^4 + 2*a*integrate(1/3*sqrt(a*x + 1)*sqrt(-a*x + 1)*x^6*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3/(a^2*x^2 - 1), x)

Fricas [A] time = 2.21951, size = 383, normalized size = 1.36

$$\frac{32a^6x^6 + 195a^4x^4 + 108(16a^6x^6 - 5)\arcsin(ax)^4 + 2205a^2x^2 - 9(64a^6x^6 + 120a^4x^4 + 360a^2x^2 - 245)\arcsin(ax)^2 + 6\sqrt{-a^2x^2+1}(24(8a^5x^5 + 10a^3x^3 + 15ax)\arcsin(ax)^3 - (32a^5x^5 + 130a^3x^3 + 735ax)\arcsin(ax))}{10368a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*arcsin(a*x)^4,x, algorithm="fricas")

[Out] 1/10368*(32*a^6*x^6 + 195*a^4*x^4 + 108*(16*a^6*x^6 - 5)*arcsin(a*x)^4 + 2205*a^2*x^2 - 9*(64*a^6*x^6 + 120*a^4*x^4 + 360*a^2*x^2 - 245)*arcsin(a*x)^2 + 6*sqrt(-a^2*x^2 + 1)*(24*(8*a^5*x^5 + 10*a^3*x^3 + 15*a*x)*arcsin(a*x)^3 - (32*a^5*x^5 + 130*a^3*x^3 + 735*a*x)*arcsin(a*x)))/a^6

Sympy [A] time = 33.0018, size = 269, normalized size = 0.95

$$\left\{ \begin{array}{l} \frac{x^6 \operatorname{asin}^4(ax)}{6} - \frac{x^6 \operatorname{asin}^2(ax)}{18} + \frac{x^6}{324} + \frac{x^5 \sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{9a} - \frac{x^5 \sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{54a} - \frac{5x^4 \operatorname{asin}^2(ax)}{48a^2} + \frac{65x^4}{3456a^2} + \frac{5x^3 \sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{36a^3} - \frac{65x^3 \sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{36a^3} \\ 0 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5*asin(a*x)**4,x)

[Out] Piecewise((x**6*asin(a*x)**4/6 - x**6*asin(a*x)**2/18 + x**6/324 + x**5*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(9*a) - x**5*sqrt(-a**2*x**2 + 1)*asin(a*x)/(54*a) - 5*x**4*asin(a*x)**2/(48*a**2) + 65*x**4/(3456*a**2) + 5*x**3*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(36*a**3) - 65*x**3*sqrt(-a**2*x**2 + 1)*asin(a*x)/(864*a**3) - 5*x**2*asin(a*x)**2/(16*a**4) + 245*x**2/(1152*a**4) + 5*x*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(24*a**5) - 245*x*sqrt(-a**2*x**2 + 1)*asin(a*x)/(576*a**5) - 5*asin(a*x)**4/(96*a**6) + 245*asin(a*x)**2/(1152*a**6), Ne(a, 0)), (0, True))

Giac [A] time = 1.37513, size = 489, normalized size = 1.73

$$\frac{(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1} x \arcsin(ax)^3}{9a^5} + \frac{(a^2x^2 - 1)^3 \arcsin(ax)^4}{6a^6} - \frac{13(-a^2x^2 + 1)^{\frac{3}{2}} x \arcsin(ax)^3}{36a^5} + \frac{(a^2x^2 - 1)^2 \arcsin(ax)^4}{2a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5*arcsin(a*x)^4,x, algorithm="giac")

[Out] 1/9*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)^3/a^5 + 1/6*(a^2*x^2 - 1)^3*arcsin(a*x)^4/a^6 - 13/36*(-a^2*x^2 + 1)^(3/2)*x*arcsin(a*x)^3/a^5 + 1/2*(a^2*x^2 - 1)^2*arcsin(a*x)^4/a^6 - 1/54*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)/a^5 + 11/24*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)^3/a^5 - 1/18*(a^2*x^2 - 1)^3*arcsin(a*x)^2/a^6 + 1/2*(a^2*x^2 - 1)*arcsin(a*x)^4/a^6 + 97/864*(-a^2*x^2 + 1)^(3/2)*x*arcsin(a*x)/a^5 - 13/48*(a^2*x^2 - 1)^2*arcsin(a*x)^2/a^6 + 11/96*arcsin(a*x)^4/a^6 - 299/576*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)/a^5 + 1/324*(a^2*x^2 - 1)^3/a^6 - 11/16*(a^2*x^2 - 1)*arcsin(a*x)^2/a^6 + 97/3456*(a^2*x^2 - 1)^2/a^6 - 299/1152*arcsin(a*x)^2/a^6 + 299/1152*(a^2*x^2 - 1)/a^6 + 9971/82944/a^6

3.33 $\int x^4 \sin^{-1}(ax)^4 dx$

Optimal. Leaf size=250

$$\frac{1088x^3}{16875a^2} + \frac{4x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{25a} - \frac{24x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)}{625a} - \frac{16x^3\sin^{-1}(ax)^2}{75a^2} + \frac{16x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{75a^3} - \frac{1088x}{16875a^2}$$

[Out] (16576*x)/(5625*a^4) + (1088*x^3)/(16875*a^2) + (24*x^5)/3125 - (16576*sqrt[1 - a^2*x^2]*ArcSin[a*x])/(5625*a^5) - (1088*x^2*sqrt[1 - a^2*x^2]*ArcSin[a*x])/(5625*a^3) - (24*x^4*sqrt[1 - a^2*x^2]*ArcSin[a*x])/(625*a) - (32*x*ArcSin[a*x]^2)/(25*a^4) - (16*x^3*ArcSin[a*x]^2)/(75*a^2) - (12*x^5*ArcSin[a*x]^2)/125 + (32*sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(75*a^5) + (16*x^2*sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(75*a^3) + (4*x^4*sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(25*a) + (x^5*ArcSin[a*x]^4)/5

Rubi [A] time = 0.662997, antiderivative size = 250, normalized size of antiderivative = 1., number of steps used = 19, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4627, 4707, 4677, 4619, 8, 30}

$$\frac{1088x^3}{16875a^2} + \frac{4x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{25a} - \frac{24x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)}{625a} - \frac{16x^3\sin^{-1}(ax)^2}{75a^2} + \frac{16x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{75a^3} - \frac{1088x}{16875a^2}$$

Antiderivative was successfully verified.

[In] Int[x^4*ArcSin[a*x]^4,x]

[Out] (16576*x)/(5625*a^4) + (1088*x^3)/(16875*a^2) + (24*x^5)/3125 - (16576*sqrt[1 - a^2*x^2]*ArcSin[a*x])/(5625*a^5) - (1088*x^2*sqrt[1 - a^2*x^2]*ArcSin[a*x])/(5625*a^3) - (24*x^4*sqrt[1 - a^2*x^2]*ArcSin[a*x])/(625*a) - (32*x*ArcSin[a*x]^2)/(25*a^4) - (16*x^3*ArcSin[a*x]^2)/(75*a^2) - (12*x^5*ArcSin[a*x]^2)/125 + (32*sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(75*a^5) + (16*x^2*sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(75*a^3) + (4*x^4*sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(25*a) + (x^5*ArcSin[a*x]^4)/5

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_))/sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/sqrt[d + e*x^2], x], x] + Dist[(b*f*n*sqrt[1 - c^2*x^2])/(c*m*sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^n

- 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^n, x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned}
 \int x^4 \sin^{-1}(ax)^4 dx &= \frac{1}{5}x^5 \sin^{-1}(ax)^4 - \frac{1}{5}(4a) \int \frac{x^5 \sin^{-1}(ax)^3}{\sqrt{1 - a^2x^2}} dx \\
 &= \frac{4x^4 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^3}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^4 - \frac{12}{25} \int x^4 \sin^{-1}(ax)^2 dx - \frac{16 \int \frac{x^3 \sin^{-1}(ax)^3}{\sqrt{1 - a^2x^2}} dx}{25a} \\
 &= -\frac{12}{125}x^5 \sin^{-1}(ax)^2 + \frac{16x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^3}{75a^3} + \frac{4x^4 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^3}{25a} + \frac{1}{5}x^5 \sin^{-1}(ax)^4 - \\
 &= -\frac{24x^4 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{625a} - \frac{16x^3 \sin^{-1}(ax)^2}{75a^2} - \frac{12}{125}x^5 \sin^{-1}(ax)^2 + \frac{32 \sqrt{1 - a^2x^2} \sin^{-1}(ax)^3}{75a^5} + \\
 &= \frac{24x^5}{3125} - \frac{1088x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{5625a^3} - \frac{24x^4 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{625a} - \frac{32x \sin^{-1}(ax)^2}{25a^4} - \frac{16x^3 \sin^{-1}(ax)}{75a^2} \\
 &= \frac{1088x^3}{16875a^2} + \frac{24x^5}{3125} - \frac{16576 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{5625a^5} - \frac{1088x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{5625a^3} - \frac{24x^4 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{625a} \\
 &= \frac{16576x}{5625a^4} + \frac{1088x^3}{16875a^2} + \frac{24x^5}{3125} - \frac{16576 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{5625a^5} - \frac{1088x^2 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{5625a^3} - \frac{24x^4 \sqrt{1 - a^2x^2} \sin^{-1}(ax)}{625a}
 \end{aligned}$$

Mathematica [A] time = 0.0747238, size = 150, normalized size = 0.6

$$\frac{8ax(81a^4x^4 + 680a^2x^2 + 31080) + 16875a^5x^5 \sin^{-1}(ax)^4 - 900ax(9a^4x^4 + 20a^2x^2 + 120) \sin^{-1}(ax)^2 + 4500 \sqrt{1 - a^2x^2}}{84375a^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4*ArcSin[a*x]^4,x]

[Out] (8*a*x*(31080 + 680*a^2*x^2 + 81*a^4*x^4) - 120*Sqrt[1 - a^2*x^2]*(2072 + 136*a^2*x^2 + 27*a^4*x^4)*ArcSin[a*x] - 900*a*x*(120 + 20*a^2*x^2 + 9*a^4*x^4)*ArcSin[a*x]^2 + 4500*Sqrt[1 - a^2*x^2]*(8 + 4*a^2*x^2 + 3*a^4*x^4)*ArcSin[a*x]^3 + 16875*a^5*x^5*ArcSin[a*x]^4)/(84375*a^5)

Maple [A] time = 0.059, size = 197, normalized size = 0.8

$$\frac{1}{a^5} \left(\frac{a^5 x^5 (\arcsin(ax))^4}{5} + \frac{4 (\arcsin(ax))^3 (3a^4 x^4 + 4a^2 x^2 + 8)}{75} \sqrt{-a^2 x^2 + 1} - \frac{32 ax (\arcsin(ax))^2}{25} + \frac{16576 ax}{5625} - \frac{64 \arcsin(ax)}{25} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*arcsin(a*x)^4,x)

[Out] 1/a^5*(1/5*a^5*x^5*arcsin(a*x)^4+4/75*arcsin(a*x)^3*(3*a^4*x^4+4*a^2*x^2+8)*(-a^2*x^2+1)^(1/2)-32/25*a*x*arcsin(a*x)^2+16576/5625*a*x-64/25*arcsin(a*x)*(-a^2*x^2+1)^(1/2)-12/125*a^5*x^5*arcsin(a*x)^2-8/625*arcsin(a*x)*(3*a^4*x^4+4*a^2*x^2+8)*(-a^2*x^2+1)^(1/2)+24/3125*a^5*x^5+1088/16875*a^3*x^3-16/75*a^3*x^3*arcsin(a*x)^2-32/225*arcsin(a*x)*(a^2*x^2+2)*(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.8534, size = 279, normalized size = 1.12

$$\frac{1}{5} x^5 \arcsin(ax)^4 + \frac{4}{75} \left(\frac{3 \sqrt{-a^2 x^2 + 1} x^4}{a^2} + \frac{4 \sqrt{-a^2 x^2 + 1} x^2}{a^4} + \frac{8 \sqrt{-a^2 x^2 + 1}}{a^6} \right) a \arcsin(ax)^3 - \frac{4}{84375} \left(2a \left(\frac{15 \left(27 \sqrt{-a^2 x^2 + 1} x^4 + 136 \sqrt{-a^2 x^2 + 1} x^2 + 2072 \sqrt{-a^2 x^2 + 1} \right)}{a^2} \arcsin(ax) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^4,x, algorithm="maxima")

[Out] 1/5*x^5*arcsin(a*x)^4 + 4/75*(3*sqrt(-a^2*x^2 + 1)*x^4/a^2 + 4*sqrt(-a^2*x^2 + 1)*x^2/a^4 + 8*sqrt(-a^2*x^2 + 1)/a^6)*a*arcsin(a*x)^3 - 4/84375*(2*a*(15*(27*sqrt(-a^2*x^2 + 1)*a^2*x^4 + 136*sqrt(-a^2*x^2 + 1)*x^2 + 2072*sqrt(-a^2*x^2 + 1)/a^2)*arcsin(a*x)/a^5 - (81*a^4*x^5 + 680*a^2*x^3 + 31080*x)/a^6) + 225*(9*a^4*x^5 + 20*a^2*x^3 + 120*x)*arcsin(a*x)^2/a^5)*a

Fricas [A] time = 2.14933, size = 352, normalized size = 1.41

$$\frac{16875 a^5 x^5 \arcsin(ax)^4 + 648 a^5 x^5 + 5440 a^3 x^3 - 900 (9 a^5 x^5 + 20 a^3 x^3 + 120 ax) \arcsin(ax)^2 + 248640 ax + 60 \sqrt{-a^2 x^2 + 1}}{84375 a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^4,x, algorithm="fricas")

[Out] 1/84375*(16875*a^5*x^5*arcsin(a*x)^4 + 648*a^5*x^5 + 5440*a^3*x^3 - 900*(9*a^5*x^5 + 20*a^3*x^3 + 120*a*x)*arcsin(a*x)^2 + 248640*a*x + 60*sqrt(-a^2*x^2 + 1)*(75*(3*a^4*x^4 + 4*a^2*x^2 + 8)*arcsin(a*x)^3 - 2*(27*a^4*x^4 + 136*a^2*x^2 + 2072)*arcsin(a*x)))/a^5

Sympy [A] time = 18.6481, size = 241, normalized size = 0.96

$$\begin{cases} \frac{x^5 \operatorname{asin}^4(ax)}{5} - \frac{12x^5 \operatorname{asin}^2(ax)}{125} + \frac{24x^5}{3125} + \frac{4x^4 \sqrt{-a^2 x^2 + 1} \operatorname{asin}^3(ax)}{25a} - \frac{24x^4 \sqrt{-a^2 x^2 + 1} \operatorname{asin}(ax)}{625a} - \frac{16x^3 \operatorname{asin}^2(ax)}{75a^2} + \frac{1088x^3}{16875a^2} + \frac{16x^2 \sqrt{-a^2 x^2 + 1} \operatorname{asin}^3(ax)}{75a^3} \\ 0 \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4*asin(a*x)**4,x)

[Out] Piecewise((x**5*asin(a*x)**4/5 - 12*x**5*asin(a*x)**2/125 + 24*x**5/3125 + 4*x**4*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(25*a) - 24*x**4*sqrt(-a**2*x**2 + 1)*asin(a*x)/(625*a) - 16*x**3*asin(a*x)**2/(75*a**2) + 1088*x**3/(16875*a**2) + 16*x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(75*a**3) - 1088*x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)/(5625*a**3) - 32*x*asin(a*x)**2/(25*a**4) + 16576*x/(5625*a**4) + 32*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(75*a**5) - 16576*sqrt(-a**2*x**2 + 1)*asin(a*x)/(5625*a**5), Ne(a, 0)), (0, True))

Giac [A] time = 1.29041, size = 412, normalized size = 1.65

$$\frac{(a^2x^2 - 1)^2 x \arcsin(ax)^4}{5a^4} + \frac{2(a^2x^2 - 1)x \arcsin(ax)^4}{5a^4} - \frac{12(a^2x^2 - 1)^2 x \arcsin(ax)^2}{125a^4} + \frac{x \arcsin(ax)^4}{5a^4} + \frac{4(a^2x^2 - 1)}{5a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^4,x, algorithm="giac")

[Out] 1/5*(a^2*x^2 - 1)^2*x*arcsin(a*x)^4/a^4 + 2/5*(a^2*x^2 - 1)*x*arcsin(a*x)^4/a^4 - 12/125*(a^2*x^2 - 1)^2*x*arcsin(a*x)^2/a^4 + 1/5*x*arcsin(a*x)^4/a^4 + 4/25*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^3/a^5 - 152/375*(a^2*x^2 - 1)*x*arcsin(a*x)^2/a^4 - 8/15*(-a^2*x^2 + 1)^(3/2)*arcsin(a*x)^3/a^5 + 24/3125*(a^2*x^2 - 1)^2*x/a^4 - 596/375*x*arcsin(a*x)^2/a^4 - 24/625*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)*arcsin(a*x)/a^5 + 4/5*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^3/a^5 + 6736/84375*(a^2*x^2 - 1)*x/a^4 + 304/1125*(-a^2*x^2 + 1)^(3/2)*arcsin(a*x)/a^5 + 254728/84375*x/a^4 - 1192/375*sqrt(-a^2*x^2 + 1)*arcsin(a*x)/a^5

3.34 $\int x^3 \sin^{-1}(ax)^4 dx$

Optimal. Leaf size=198

$$\frac{45x^2}{128a^2} + \frac{x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{4a} - \frac{3x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{32a} - \frac{9x^2\sin^{-1}(ax)^2}{16a^2} + \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{8a^3} - \frac{45x\sqrt{1-a^2x^2}}{64a^3}$$

```
[Out] (45*x^2)/(128*a^2) + (3*x^4)/128 - (45*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(64
*a^3) - (3*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(32*a) + (45*ArcSin[a*x]^2)/(
128*a^4) - (9*x^2*ArcSin[a*x]^2)/(16*a^2) - (3*x^4*ArcSin[a*x]^2)/16 + (3*x
*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(8*a^3) + (x^3*Sqrt[1 - a^2*x^2]*ArcSin[a
*x]^3)/(4*a) - (3*ArcSin[a*x]^4)/(32*a^4) + (x^4*ArcSin[a*x]^4)/4
```

Rubi [A] time = 0.516077, antiderivative size = 198, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4627, 4707, 4641, 30}

$$\frac{45x^2}{128a^2} + \frac{x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{4a} - \frac{3x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)}{32a} - \frac{9x^2\sin^{-1}(ax)^2}{16a^2} + \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{8a^3} - \frac{45x\sqrt{1-a^2x^2}}{64a^3}$$

Antiderivative was successfully verified.

```
[In] Int[x^3*ArcSin[a*x]^4,x]
```

```
[Out] (45*x^2)/(128*a^2) + (3*x^4)/128 - (45*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(64
*a^3) - (3*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(32*a) + (45*ArcSin[a*x]^2)/(
128*a^4) - (9*x^2*ArcSin[a*x]^2)/(16*a^2) - (3*x^4*ArcSin[a*x]^2)/16 + (3*x
*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(8*a^3) + (x^3*Sqrt[1 - a^2*x^2]*ArcSin[a
*x]^3)/(4*a) - (3*ArcSin[a*x]^4)/(32*a^4) + (x^4*ArcSin[a*x]^4)/4
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4707

```
Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_)
+ (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*
ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)
*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*
x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1),
x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0]
&& GtQ[m, 1] && IntegerQ[m]
```

Rule 4641

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_S
ymbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; Fre
eQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```


Rubi steps

$$\begin{aligned}
\int x^3 \sin^{-1}(ax)^4 dx &= \frac{1}{4}x^4 \sin^{-1}(ax)^4 - a \int \frac{x^4 \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx \\
&= \frac{x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{4a} + \frac{1}{4}x^4 \sin^{-1}(ax)^4 - \frac{3}{4} \int x^3 \sin^{-1}(ax)^2 dx - \frac{3 \int \frac{x^2 \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx}{4a} \\
&= -\frac{3}{16}x^4 \sin^{-1}(ax)^2 + \frac{3x \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{8a^3} + \frac{x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{4a} + \frac{1}{4}x^4 \sin^{-1}(ax)^4 - \frac{3 \int \frac{x^2 \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx}{4a} \\
&= -\frac{3x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} - \frac{9x^2 \sin^{-1}(ax)^2}{16a^2} - \frac{3}{16}x^4 \sin^{-1}(ax)^2 + \frac{3x \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{8a^3} + \frac{x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{4a} \\
&= \frac{3x^4}{128} - \frac{45x \sqrt{1-a^2x^2} \sin^{-1}(ax)}{64a^3} - \frac{3x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} - \frac{9x^2 \sin^{-1}(ax)^2}{16a^2} - \frac{3}{16}x^4 \sin^{-1}(ax)^2 + \frac{3x \sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{8a^3} \\
&= \frac{45x^2}{128a^2} + \frac{3x^4}{128} - \frac{45x \sqrt{1-a^2x^2} \sin^{-1}(ax)}{64a^3} - \frac{3x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} + \frac{45 \sin^{-1}(ax)^2}{128a^4} - \frac{9x^2 \sin^{-1}(ax)^2}{16a^2}
\end{aligned}$$

Mathematica [A] time = 0.0589461, size = 135, normalized size = 0.68

$$\frac{3a^2x^2(a^2x^2+15)+4(8a^4x^4-3)\sin^{-1}(ax)^4+16ax\sqrt{1-a^2x^2}(2a^2x^2+3)\sin^{-1}(ax)^3-3(8a^4x^4+24a^2x^2-15)\sin^{-1}(ax)^2}{128a^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*ArcSin[a*x]^4,x]

[Out] (3*a^2*x^2*(15 + a^2*x^2) - 6*a*x*Sqrt[1 - a^2*x^2]*(15 + 2*a^2*x^2)*ArcSin[a*x] - 3*(-15 + 24*a^2*x^2 + 8*a^4*x^4)*ArcSin[a*x]^2 + 16*a*x*Sqrt[1 - a^2*x^2]*(3 + 2*a^2*x^2)*ArcSin[a*x]^3 + 4*(-3 + 8*a^4*x^4)*ArcSin[a*x]^4)/(128*a^4)

Maple [A] time = 0.059, size = 209, normalized size = 1.1

$$\frac{1}{a^4} \left(\frac{a^4 x^4 (\arcsin(ax))^4}{4} - \frac{(\arcsin(ax))^3}{8} \left(-2a^3 x^3 \sqrt{-a^2 x^2 + 1} - 3ax \sqrt{-a^2 x^2 + 1} + 3 \arcsin(ax) \right) - \frac{3a^4 x^4 (\arcsin(ax))^2}{16} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x)^4,x)

[Out] 1/a^4*(1/4*a^4*x^4*arcsin(a*x)^4-1/8*arcsin(a*x)^3*(-2*a^3*x^3*(-a^2*x^2+1)^(1/2)-3*a*x*(-a^2*x^2+1)^(1/2)+3*arcsin(a*x))-3/16*a^4*x^4*arcsin(a*x)^2+3/64*arcsin(a*x)*(-2*a^3*x^3*(-a^2*x^2+1)^(1/2)-3*a*x*(-a^2*x^2+1)^(1/2)+3*arcsin(a*x))+27/128*arcsin(a*x)^2+3/128*a^4*x^4+45/128*a^2*x^2-9/16*(a^2*x^2-1)*arcsin(a*x)^2-9/16*arcsin(a*x)*(a*x*(-a^2*x^2+1)^(1/2)+arcsin(a*x))+9/32*arcsin(a*x)^4)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{4}x^4 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^4 + a \int \frac{\sqrt{ax+1}\sqrt{-ax+1}x^4 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3}{a^2x^2-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^4,x, algorithm="maxima")

[Out] 1/4*x^4*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^4 + a*integrate(sqrt(a*x + 1)*sqrt(-a*x + 1)*x^4*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3/(a^2*x^2 - 1), x)

Fricas [A] time = 2.2093, size = 292, normalized size = 1.47

$$\frac{3a^4x^4 + 4(8a^4x^4 - 3)\arcsin(ax)^4 + 45a^2x^2 - 3(8a^4x^4 + 24a^2x^2 - 15)\arcsin(ax)^2 + 2\sqrt{-a^2x^2 + 1}(8(2a^3x^3 + 3ax)\arcsin(ax)^3 - 3(2a^3x^3 + 15a*x)\arcsin(ax))}{128a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^4,x, algorithm="fricas")

[Out] 1/128*(3*a^4*x^4 + 4*(8*a^4*x^4 - 3)*arcsin(a*x)^4 + 45*a^2*x^2 - 3*(8*a^4*x^4 + 24*a^2*x^2 - 15)*arcsin(a*x)^2 + 2*sqrt(-a^2*x^2 + 1)*(8*(2*a^3*x^3 + 3*a*x)*arcsin(a*x)^3 - 3*(2*a^3*x^3 + 15*a*x)*arcsin(a*x)))/a^4

Sympy [A] time = 15.126, size = 190, normalized size = 0.96

$$\left\{ \begin{array}{l} \frac{x^4 \operatorname{asin}^4(ax)}{4} - \frac{3x^4 \operatorname{asin}^2(ax)}{16} + \frac{3x^4}{128} + \frac{x^3 \sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{4a} - \frac{3x^3 \sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{32a} - \frac{9x^2 \operatorname{asin}^2(ax)}{16a^2} + \frac{45x^2}{128a^2} + \frac{3x \sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{8a^3} - \frac{45x \sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{64a^3} \\ 0 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x)**4,x)

[Out] Piecewise((x**4*asin(a*x)**4/4 - 3*x**4*asin(a*x)**2/16 + 3*x**4/128 + x**3*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(4*a) - 3*x**3*sqrt(-a**2*x**2 + 1)*asin(a*x)/(32*a) - 9*x**2*asin(a*x)**2/(16*a**2) + 45*x**2/(128*a**2) + 3*x*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(8*a**3) - 45*x*sqrt(-a**2*x**2 + 1)*asin(a*x)/(64*a**3) - 3*asin(a*x)**4/(32*a**4) + 45*asin(a*x)**2/(128*a**4), Ne(a, 0)), (0, True))

Giac [A] time = 1.41395, size = 316, normalized size = 1.6

$$-\frac{(-a^2x^2 + 1)^{\frac{3}{2}}x \arcsin(ax)^3}{4a^3} + \frac{(a^2x^2 - 1)^2 \arcsin(ax)^4}{4a^4} + \frac{5\sqrt{-a^2x^2 + 1}x \arcsin(ax)^3}{8a^3} + \frac{(a^2x^2 - 1) \arcsin(ax)^4}{2a^4} + \frac{3(-a^2x^2 + 1)^{\frac{3}{2}}x \arcsin(ax)^3}{4a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^4,x, algorithm="giac")

[Out] -1/4*(-a^2*x^2 + 1)^(3/2)*x*arcsin(a*x)^3/a^3 + 1/4*(a^2*x^2 - 1)^2*arcsin(a*x)^4/a^4 + 5/8*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)^3/a^3 + 1/2*(a^2*x^2 - 1)*arcsin(a*x)^4/a^4 + 3/32*(-a^2*x^2 + 1)^(3/2)*x*arcsin(a*x)/a^3 - 3/16*(a^2*x^2 - 1)^2*arcsin(a*x)^2/a^4 + 5/32*arcsin(a*x)^4/a^4 - 51/64*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)^3/a^3

$$\begin{aligned} &^2 + 1) * x * \arcsin(ax) / a^3 - 15/16 * (a^2 * x^2 - 1) * \arcsin(ax)^2 / a^4 + 3/128 * (\\ &a^2 * x^2 - 1)^2 / a^4 - 51/128 * \arcsin(ax)^2 / a^4 + 51/128 * (a^2 * x^2 - 1) / a^4 + \\ &195/1024 / a^4 \end{aligned}$$

3.35 $\int x^2 \sin^{-1}(ax)^4 dx$

Optimal. Leaf size=166

$$\frac{4x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{9a} + \frac{8\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{9a^3} - \frac{8x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{27a} - \frac{160\sqrt{1-a^2x^2}\sin^{-1}(ax)}{27a^3} + \frac{160x}{27a^2} - \frac{8x\sin^{-1}(ax)}{27a^3}$$

[Out] (160*x)/(27*a^2) + (8*x^3)/81 - (160*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(27*a^3) - (8*x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(27*a) - (8*x*ArcSin[a*x]^2)/(3*a^2) - (4*x^3*ArcSin[a*x]^2)/9 + (8*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(9*a^3) + (4*x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(9*a) + (x^3*ArcSin[a*x]^4)/3

Rubi [A] time = 0.353041, antiderivative size = 166, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4627, 4707, 4677, 4619, 8, 30}

$$\frac{4x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{9a} + \frac{8\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{9a^3} - \frac{8x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)}{27a} - \frac{160\sqrt{1-a^2x^2}\sin^{-1}(ax)}{27a^3} + \frac{160x}{27a^2} - \frac{8x\sin^{-1}(ax)}{27a^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*ArcSin[a*x]^4,x]

[Out] (160*x)/(27*a^2) + (8*x^3)/81 - (160*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(27*a^3) - (8*x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(27*a) - (8*x*ArcSin[a*x]^2)/(3*a^2) - (4*x^3*ArcSin[a*x]^2)/9 + (8*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(9*a^3) + (4*x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(9*a) + (x^3*ArcSin[a*x]^4)/3

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4619

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]
```

Rule 8

```
Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned} \int x^2 \sin^{-1}(ax)^4 dx &= \frac{1}{3}x^3 \sin^{-1}(ax)^4 - \frac{1}{3}(4a) \int \frac{x^3 \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx \\ &= \frac{4x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a} + \frac{1}{3}x^3 \sin^{-1}(ax)^4 - \frac{4}{3} \int x^2 \sin^{-1}(ax)^2 dx - \frac{8 \int \frac{x \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx}{9a} \\ &= -\frac{4}{9}x^3 \sin^{-1}(ax)^2 + \frac{8\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a^3} + \frac{4x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a} + \frac{1}{3}x^3 \sin^{-1}(ax)^4 - \frac{8 \int \sin^{-1}(ax) dx}{9a} \\ &= -\frac{8x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)}{27a} - \frac{8x \sin^{-1}(ax)^2}{3a^2} - \frac{4}{9}x^3 \sin^{-1}(ax)^2 + \frac{8\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a^3} + \frac{4x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a} \\ &= \frac{8x^3}{81} - \frac{160\sqrt{1-a^2x^2} \sin^{-1}(ax)}{27a^3} - \frac{8x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)}{27a} - \frac{8x \sin^{-1}(ax)^2}{3a^2} - \frac{4}{9}x^3 \sin^{-1}(ax)^2 + \frac{8\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{9a^3} \\ &= \frac{160x}{27a^2} + \frac{8x^3}{81} - \frac{160\sqrt{1-a^2x^2} \sin^{-1}(ax)}{27a^3} - \frac{8x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)}{27a} - \frac{8x \sin^{-1}(ax)^2}{3a^2} - \frac{4}{9}x^3 \sin^{-1}(ax)^2 \end{aligned}$$

Mathematica [A] time = 0.0481252, size = 114, normalized size = 0.69

$$\frac{8ax(a^2x^2 + 60) + 27a^3x^3 \sin^{-1}(ax)^4 + 36\sqrt{1-a^2x^2}(a^2x^2 + 2) \sin^{-1}(ax)^3 - 36ax(a^2x^2 + 6) \sin^{-1}(ax)^2 - 24\sqrt{1-a^2x^2} \sin^{-1}(ax)}{81a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*ArcSin[a*x]^4,x]
```

```
[Out] (8*a*x*(60 + a^2*x^2) - 24*Sqrt[1 - a^2*x^2]*(20 + a^2*x^2)*ArcSin[a*x] - 36*a*x*(6 + a^2*x^2)*ArcSin[a*x]^2 + 36*Sqrt[1 - a^2*x^2]*(2 + a^2*x^2)*ArcSin[a*x]^3 + 27*a^3*x^3*ArcSin[a*x]^4)/(81*a^3)
```

Maple [A] time = 0.048, size = 130, normalized size = 0.8

$$\frac{1}{a^3} \left(\frac{a^3 x^3 (\arcsin(ax))^4}{3} + \frac{4 (\arcsin(ax))^3 (a^2 x^2 + 2)}{9} \sqrt{-a^2 x^2 + 1} - \frac{8 ax (\arcsin(ax))^2}{3} + \frac{160 ax}{27} - \frac{16 \arcsin(ax)}{3} \sqrt{-a^2 x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*arcsin(a*x)^4,x)
```

```
[Out] 1/a^3*(1/3*a^3*x^3*arcsin(a*x)^4+4/9*arcsin(a*x)^3*(a^2*x^2+2)*(-a^2*x^2+1)^(1/2)-8/3*a*x*arcsin(a*x)^2+160/27*a*x-16/3*arcsin(a*x)*(-a^2*x^2+1)^(1/2)-4/9*a^3*x^3*arcsin(a*x)^2-8/27*arcsin(a*x)*(a^2*x^2+2)*(-a^2*x^2+1)^(1/2)+8/81*a^3*x^3)
```

Maxima [A] time = 1.68667, size = 198, normalized size = 1.19

$$\frac{1}{3}x^3 \arcsin(ax)^4 + \frac{4}{9}a \left(\frac{\sqrt{-a^2x^2+1}x^2}{a^2} + \frac{2\sqrt{-a^2x^2+1}}{a^4} \right) \arcsin(ax)^3 - \frac{4}{81} \left(2a \frac{3 \left(\sqrt{-a^2x^2+1}x^2 + \frac{20\sqrt{-a^2x^2+1}}{a^2} \right) \arcsin(ax)}{a^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*arcsin(a*x)^4,x, algorithm="maxima")
```

```
[Out] 1/3*x^3*arcsin(a*x)^4 + 4/9*a*(sqrt(-a^2*x^2 + 1)*x^2/a^2 + 2*sqrt(-a^2*x^2 + 1)/a^4)*arcsin(a*x)^3 - 4/81*(2*a*(3*(sqrt(-a^2*x^2 + 1)*x^2 + 20*sqrt(-a^2*x^2 + 1)/a^2)*arcsin(a*x)/a^3 - (a^2*x^3 + 60*x)/a^4) + 9*(a^2*x^3 + 6*x)*arcsin(a*x)^2/a^3)*a
```

Fricas [A] time = 2.01002, size = 247, normalized size = 1.49

$$\frac{27a^3x^3 \arcsin(ax)^4 + 8a^3x^3 - 36(a^3x^3 + 6ax) \arcsin(ax)^2 + 480ax + 12\sqrt{-a^2x^2+1}(3(a^2x^2+2) \arcsin(ax)^3 - 2(a^2x^2+20) \arcsin(ax))}{81a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*arcsin(a*x)^4,x, algorithm="fricas")
```

```
[Out] 1/81*(27*a^3*x^3*arcsin(a*x)^4 + 8*a^3*x^3 - 36*(a^3*x^3 + 6*a*x)*arcsin(a*x)^2 + 480*a*x + 12*sqrt(-a^2*x^2 + 1)*(3*(a^2*x^2 + 2)*arcsin(a*x)^3 - 2*(a^2*x^2 + 20)*arcsin(a*x)))/a^3
```

Sympy [A] time = 5.59197, size = 158, normalized size = 0.95

$$\left\{ \begin{array}{l} \frac{x^3 \operatorname{asin}^4(ax)}{3} - \frac{4x^3 \operatorname{asin}^2(ax)}{9} + \frac{8x^3}{81} + \frac{4x^2 \sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{9a} - \frac{8x^2 \sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{27a} - \frac{8x \operatorname{asin}^2(ax)}{3a^2} + \frac{160x}{27a^2} + \frac{8\sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{9a^3} - \frac{160\sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{27a^3} \\ 0 \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*asin(a*x)**4,x)
```

```
[Out] Piecewise((x**3*asin(a*x)**4/3 - 4*x**3*asin(a*x)**2/9 + 8*x**3/81 + 4*x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(9*a) - 8*x**2*sqrt(-a**2*x**2 + 1)*asin(a*x)/(27*a) - 8*x*asin(a*x)**2/(3*a**2) + 160*x/(27*a**2) + 8*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/(9*a**3) - 160*sqrt(-a**2*x**2 + 1)*asin(a*x)/(27*a**3), Ne(a, 0)), (0, True))
```

Giac [A] time = 1.40388, size = 238, normalized size = 1.43

$$\frac{(a^2x^2 - 1)x \arcsin(ax)^4}{3a^2} + \frac{x \arcsin(ax)^4}{3a^2} - \frac{4(a^2x^2 - 1)x \arcsin(ax)^2}{9a^2} - \frac{4(-a^2x^2 + 1)^{\frac{3}{2}} \arcsin(ax)^3}{9a^3} - \frac{28x \arcsin(ax)}{9a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^4,x, algorithm="giac")

[Out] 1/3*(a^2*x^2 - 1)*x*arcsin(a*x)^4/a^2 + 1/3*x*arcsin(a*x)^4/a^2 - 4/9*(a^2*x^2 - 1)*x*arcsin(a*x)^2/a^2 - 4/9*(-a^2*x^2 + 1)^(3/2)*arcsin(a*x)^3/a^3 - 28/9*x*arcsin(a*x)^2/a^2 + 4/3*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^3/a^3 + 8/81*(a^2*x^2 - 1)*x/a^2 + 8/27*(-a^2*x^2 + 1)^(3/2)*arcsin(a*x)/a^3 + 488/81*x/a^2 - 56/9*sqrt(-a^2*x^2 + 1)*arcsin(a*x)/a^3

3.36 $\int x \sin^{-1}(ax)^4 dx$

Optimal. Leaf size=111

$$\frac{x\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} - \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)}{2a} - \frac{\sin^{-1}(ax)^4}{4a^2} + \frac{3\sin^{-1}(ax)^2}{4a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^4 - \frac{3}{2}x^2\sin^{-1}(ax)^2 + \frac{3x^2}{4}$$

[Out] (3*x^2)/4 - (3*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(2*a) + (3*ArcSin[a*x]^2)/(4*a^2) - (3*x^2*ArcSin[a*x]^2)/2 + (x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/a - ArcSin[a*x]^4/(4*a^2) + (x^2*ArcSin[a*x]^4)/2

Rubi [A] time = 0.237692, antiderivative size = 111, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4707, 4641, 30}

$$\frac{x\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} - \frac{3x\sqrt{1-a^2x^2}\sin^{-1}(ax)}{2a} - \frac{\sin^{-1}(ax)^4}{4a^2} + \frac{3\sin^{-1}(ax)^2}{4a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^4 - \frac{3}{2}x^2\sin^{-1}(ax)^2 + \frac{3x^2}{4}$$

Antiderivative was successfully verified.

[In] Int[x*ArcSin[a*x]^4,x]

[Out] (3*x^2)/4 - (3*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/(2*a) + (3*ArcSin[a*x]^2)/(4*a^2) - (3*x^2*ArcSin[a*x]^2)/2 + (x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/a - ArcSin[a*x]^4/(4*a^2) + (x^2*ArcSin[a*x]^4)/2

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol] := Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 30

Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\begin{aligned}
\int x \sin^{-1}(ax)^4 dx &= \frac{1}{2}x^2 \sin^{-1}(ax)^4 - (2a) \int \frac{x^2 \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx \\
&= \frac{x\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{a} + \frac{1}{2}x^2 \sin^{-1}(ax)^4 - 3 \int x \sin^{-1}(ax)^2 dx - \frac{\int \frac{\sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx}{a} \\
&= -\frac{3}{2}x^2 \sin^{-1}(ax)^2 + \frac{x\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{a} - \frac{\sin^{-1}(ax)^4}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^4 + (3a) \int \frac{x^2 \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{3x\sqrt{1-a^2x^2} \sin^{-1}(ax)}{2a} - \frac{3}{2}x^2 \sin^{-1}(ax)^2 + \frac{x\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{a} - \frac{\sin^{-1}(ax)^4}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^4 \\
&= \frac{3x^2}{4} - \frac{3x\sqrt{1-a^2x^2} \sin^{-1}(ax)}{2a} + \frac{3 \sin^{-1}(ax)^2}{4a^2} - \frac{3}{2}x^2 \sin^{-1}(ax)^2 + \frac{x\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{a} - \frac{\sin^{-1}(ax)^4}{4a^2}
\end{aligned}$$

Mathematica [A] time = 0.0289746, size = 96, normalized size = 0.86

$$\frac{3a^2x^2 + (2a^2x^2 - 1) \sin^{-1}(ax)^4 + 4ax\sqrt{1-a^2x^2} \sin^{-1}(ax)^3 + (3 - 6a^2x^2) \sin^{-1}(ax)^2 - 6ax\sqrt{1-a^2x^2} \sin^{-1}(ax)}{4a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*ArcSin[a*x]^4,x]

[Out] (3*a^2*x^2 - 6*a*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x] + (3 - 6*a^2*x^2)*ArcSin[a*x]^2 + 4*a*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3 + (-1 + 2*a^2*x^2)*ArcSin[a*x]^4)/(4*a^2)

Maple [A] time = 0.039, size = 117, normalized size = 1.1

$$\frac{1}{a^2} \left(\frac{(a^2x^2 - 1) (\arcsin(ax))^4}{2} + (\arcsin(ax))^3 \left(ax\sqrt{-a^2x^2 + 1} + \arcsin(ax) \right) - \frac{(3a^2x^2 - 3) (\arcsin(ax))^2}{2} - \frac{3 \arcsin(ax)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*arcsin(a*x)^4,x)

[Out] 1/a^2*(1/2*(a^2*x^2-1)*arcsin(a*x)^4+arcsin(a*x)^3*(a*x*(-a^2*x^2+1)^(1/2)+arcsin(a*x))-3/2*(a^2*x^2-1)*arcsin(a*x)^2-3/2*arcsin(a*x)*(a*x*(-a^2*x^2+1)^(1/2)+arcsin(a*x))+3/4*arcsin(a*x)^2+3/4*a^2*x^2-3/4*arcsin(a*x)^4)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{2}x^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^4 + 2a \int \frac{\sqrt{ax+1}\sqrt{-ax+1}x^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3}{a^2x^2-1} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^4,x, algorithm="maxima")

[Out] 1/2*x^2*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^4 + 2*a*integrate(sqrt(a*x + 1)*sqrt(-a*x + 1)*x^2*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3/(a^2

$2x^2 - 1), x)$

Fricas [A] time = 2.21133, size = 205, normalized size = 1.85

$$\frac{(2a^2x^2 - 1)\arcsin(ax)^4 + 3a^2x^2 - 3(2a^2x^2 - 1)\arcsin(ax)^2 + 2(2ax\arcsin(ax)^3 - 3ax\arcsin(ax))\sqrt{-a^2x^2 + 1}}{4a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^4,x, algorithm="fricas")

[Out] 1/4*((2*a^2*x^2 - 1)*arcsin(a*x)^4 + 3*a^2*x^2 - 3*(2*a^2*x^2 - 1)*arcsin(a*x)^2 + 2*(2*a*x*arcsin(a*x)^3 - 3*a*x*arcsin(a*x))*sqrt(-a^2*x^2 + 1))/a^2

Sympy [A] time = 3.34311, size = 104, normalized size = 0.94

$$\begin{cases} \frac{x^2 \operatorname{asin}^4(ax)}{2} - \frac{3x^2 \operatorname{asin}^2(ax)}{2} + \frac{3x^2}{4} + \frac{x\sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{a} - \frac{3x\sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{2a} - \frac{\operatorname{asin}^4(ax)}{4a^2} + \frac{3 \operatorname{asin}^2(ax)}{4a^2} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*asin(a*x)**4,x)

[Out] Piecewise((x**2*asin(a*x)**4/2 - 3*x**2*asin(a*x)**2/2 + 3*x**2/4 + x*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/a - 3*x*sqrt(-a**2*x**2 + 1)*asin(a*x)/(2*a) - asin(a*x)**4/(4*a**2) + 3*asin(a*x)**2/(4*a**2), Ne(a, 0)), (0, True))

Giac [A] time = 1.40401, size = 171, normalized size = 1.54

$$\frac{\sqrt{-a^2x^2 + 1}x\arcsin(ax)^3}{a} + \frac{(a^2x^2 - 1)\arcsin(ax)^4}{2a^2} + \frac{\arcsin(ax)^4}{4a^2} - \frac{3\sqrt{-a^2x^2 + 1}x\arcsin(ax)}{2a} - \frac{3(a^2x^2 - 1)\arcsin(ax)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^4,x, algorithm="giac")

[Out] sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)^3/a + 1/2*(a^2*x^2 - 1)*arcsin(a*x)^4/a^2 + 1/4*arcsin(a*x)^4/a^2 - 3/2*sqrt(-a^2*x^2 + 1)*x*arcsin(a*x)/a - 3/2*(a^2*x^2 - 1)*arcsin(a*x)^2/a^2 - 3/4*arcsin(a*x)^2/a^2 + 3/4*(a^2*x^2 - 1)/a^2 + 3/8/a^2

3.37 $\int \sin^{-1}(ax)^4 dx$

Optimal. Leaf size=69

$$\frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} - \frac{24\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^4 - 12x\sin^{-1}(ax)^2 + 24x$$

[Out] $24*x - (24*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/a - 12*x*\text{ArcSin}[a*x]^2 + (4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^3)/a + x*\text{ArcSin}[a*x]^4$

Rubi [A] time = 0.117854, antiderivative size = 69, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4619, 4677, 8}

$$\frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} - \frac{24\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^4 - 12x\sin^{-1}(ax)^2 + 24x$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^4, x]$

[Out] $24*x - (24*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x])/a - 12*x*\text{ArcSin}[a*x]^2 + (4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^3)/a + x*\text{ArcSin}[a*x]^4$

Rule 4619

$\text{Int}[(a + \text{ArcSin}(c*x))^n, x] - \text{Dist}[b*c*n, \text{Int}[(x*(a + b*\text{ArcSin}(c*x)))^{n-1}], x] / \text{Sqrt}[1 - c^2*x^2], x] /;$ FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4677

$\text{Int}[(a + \text{ArcSin}(c*x))^n * (d + e*x^2)^p, x] := \text{Simp}[(d + e*x^2)^{p+1} * (a + b*\text{ArcSin}(c*x))^n / (2*e*(p+1)), x] + \text{Dist}[(b*n*d*\text{IntPart}[p] * (d + e*x^2)^{\text{FracPart}[p]}] / (2*c*(p+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(1 - c^2*x^2)^{p+1/2} * (a + b*\text{ArcSin}(c*x))^{n-1}], x] /;$ FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 8

$\text{Int}[a, x] := \text{Simp}[a*x, x] /;$ FreeQ[a, x]

Rubi steps

$$\begin{aligned} \int \sin^{-1}(ax)^4 dx &= x\sin^{-1}(ax)^4 - (4a) \int \frac{x\sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx \\ &= \frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} + x\sin^{-1}(ax)^4 - 12 \int \sin^{-1}(ax)^2 dx \\ &= -12x\sin^{-1}(ax)^2 + \frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} + x\sin^{-1}(ax)^4 + (24a) \int \frac{x\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\ &= -\frac{24\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} - 12x\sin^{-1}(ax)^2 + \frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} + x\sin^{-1}(ax)^4 + 24 \int 1 dx \\ &= 24x - \frac{24\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} - 12x\sin^{-1}(ax)^2 + \frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} + x\sin^{-1}(ax)^4 \end{aligned}$$

Mathematica [A] time = 0.0155383, size = 69, normalized size = 1.

$$\frac{4\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{a} - \frac{24\sqrt{1-a^2x^2}\sin^{-1}(ax)}{a} + x\sin^{-1}(ax)^4 - 12x\sin^{-1}(ax)^2 + 24x$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^4,x]

[Out] 24*x - (24*Sqrt[1 - a^2*x^2]*ArcSin[a*x])/a - 12*x*ArcSin[a*x]^2 + (4*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/a + x*ArcSin[a*x]^4

Maple [A] time = 0.026, size = 67, normalized size = 1.

$$\frac{1}{a} \left(ax (\arcsin(ax))^4 + 4 (\arcsin(ax))^3 \sqrt{-a^2x^2 + 1} - 12 ax (\arcsin(ax))^2 + 24 ax - 24 \arcsin(ax) \sqrt{-a^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^4,x)

[Out] 1/a*(a*x*arcsin(a*x)^4+4*arcsin(a*x)^3*(-a^2*x^2+1)^(1/2)-12*a*x*arcsin(a*x)^2+24*a*x-24*arcsin(a*x)*(-a^2*x^2+1)^(1/2))

Maxima [A] time = 1.76751, size = 101, normalized size = 1.46

$$x \arcsin(ax)^4 + \frac{4\sqrt{-a^2x^2+1}\arcsin(ax)^3}{a} - 12 \left(\frac{x \arcsin(ax)^2}{a} - \frac{2 \left(x - \frac{\sqrt{-a^2x^2+1}\arcsin(ax)}{a} \right)}{a} \right) a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4,x, algorithm="maxima")

[Out] x*arcsin(a*x)^4 + 4*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^3/a - 12*(x*arcsin(a*x)^2/a - 2*(x - sqrt(-a^2*x^2 + 1)*arcsin(a*x)/a)/a)*a

Fricas [A] time = 1.92647, size = 149, normalized size = 2.16

$$\frac{ax \arcsin(ax)^4 - 12ax \arcsin(ax)^2 + 24ax + 4\sqrt{-a^2x^2+1}(\arcsin(ax)^3 - 6 \arcsin(ax))}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4,x, algorithm="fricas")

[Out] (a*x*arcsin(a*x)^4 - 12*a*x*arcsin(a*x)^2 + 24*a*x + 4*sqrt(-a^2*x^2 + 1)*(arcsin(a*x)^3 - 6*arcsin(a*x)))/a

Sympy [A] time = 1.98801, size = 65, normalized size = 0.94

$$\begin{cases} x \operatorname{asin}^4(ax) - 12x \operatorname{asin}^2(ax) + 24x + \frac{4\sqrt{-a^2x^2+1} \operatorname{asin}^3(ax)}{a} - \frac{24\sqrt{-a^2x^2+1} \operatorname{asin}(ax)}{a} & \text{for } a \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**4,x)

[Out] Piecewise((x*asin(a*x)**4 - 12*x*asin(a*x)**2 + 24*x + 4*sqrt(-a**2*x**2 + 1)*asin(a*x)**3/a - 24*sqrt(-a**2*x**2 + 1)*asin(a*x)/a, Ne(a, 0)), (0, True))

Giac [A] time = 1.38978, size = 88, normalized size = 1.28

$$x \arcsin(ax)^4 - 12x \arcsin(ax)^2 + \frac{4\sqrt{-a^2x^2+1} \arcsin(ax)^3}{a} + 24x - \frac{24\sqrt{-a^2x^2+1} \arcsin(ax)}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4,x, algorithm="giac")

[Out] x*arcsin(a*x)^4 - 12*x*arcsin(a*x)^2 + 4*sqrt(-a^2*x^2 + 1)*arcsin(a*x)^3/a + 24*x - 24*sqrt(-a^2*x^2 + 1)*arcsin(a*x)/a

$$3.38 \quad \int \frac{\sin^{-1}(ax)^4}{x} dx$$

Optimal. Leaf size=113

$$-2i \sin^{-1}(ax)^3 \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + 3 \sin^{-1}(ax)^2 \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) + 3i \sin^{-1}(ax) \text{PolyLog}\left(4, e^{2i \sin^{-1}(ax)}\right) - \frac{3}{2}$$

[Out] $(-I/5)*\text{ArcSin}[a*x]^5 + \text{ArcSin}[a*x]^4*\text{Log}[1 - E^{((2*I)*\text{ArcSin}[a*x])}] - (2*I)*\text{ArcSin}[a*x]^3*\text{PolyLog}[2, E^{((2*I)*\text{ArcSin}[a*x])}] + 3*\text{ArcSin}[a*x]^2*\text{PolyLog}[3, E^{((2*I)*\text{ArcSin}[a*x])}] + (3*I)*\text{ArcSin}[a*x]*\text{PolyLog}[4, E^{((2*I)*\text{ArcSin}[a*x])}] - (3*\text{PolyLog}[5, E^{((2*I)*\text{ArcSin}[a*x])}])/2$

Rubi [A] time = 0.122287, antiderivative size = 113, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4625, 3717, 2190, 2531, 6609, 2282, 6589}

$$-2i \sin^{-1}(ax)^3 \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + 3 \sin^{-1}(ax)^2 \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) + 3i \sin^{-1}(ax) \text{PolyLog}\left(4, e^{2i \sin^{-1}(ax)}\right) - \frac{3}{2}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^4/x,x]

[Out] $(-I/5)*\text{ArcSin}[a*x]^5 + \text{ArcSin}[a*x]^4*\text{Log}[1 - E^{((2*I)*\text{ArcSin}[a*x])}] - (2*I)*\text{ArcSin}[a*x]^3*\text{PolyLog}[2, E^{((2*I)*\text{ArcSin}[a*x])}] + 3*\text{ArcSin}[a*x]^2*\text{PolyLog}[3, E^{((2*I)*\text{ArcSin}[a*x])}] + (3*I)*\text{ArcSin}[a*x]*\text{PolyLog}[4, E^{((2*I)*\text{ArcSin}[a*x])}] - (3*\text{PolyLog}[5, E^{((2*I)*\text{ArcSin}[a*x])}])/2$

Rule 4625

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)/(x_), x_Symbol] :> Subst[Int[(a + b*x)^n/Tan[x], x], x, ArcSin[c*x]] /; FreeQ[{a, b, c}, x] && IGtQ[n, 0]

Rule 3717

Int[((c_.) + (d_.)*(x_.))^(m_.)*tan[(e_.) + Pi*(k_.) + (f_.)*(x_.)], x_Symbol] :> Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m * E^(2*I*k*Pi) * E^(2*I*(e + f*x)))/(1 + E^(2*I*k*Pi) * E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IntegerQ[4*k] && IGtQ[m, 0]

Rule 2190

Int[(((F_)^(g_.)*((e_.) + (f_.)*(x_.)))^(n_.)*((c_.) + (d_.)*(x_.))^(m_.))/((a_.) + (b_.)*((F_)^(g_.)*((e_.) + (f_.)*(x_.)))^(n_.), x_Symbol] :> Simp[((c + d*x)^m * Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1) * Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2531

Int[Log[1 + (e_.)*((F_)^(c_.)*((a_.) + (b_.)*(x_.)))^(n_.)]*((f_.) + (g_.)*(x_.))^(m_.), x_Symbol] :> -Simp[((f + g*x)^m * PolyLog[2, -(e*(F^(c*(a + b*x)))^n)])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1) * PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 6609

```
Int[((e_.) + (f_.)*(x_.))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_.)))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p])/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^
(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_)^v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_.))^(p_.)]/((d_.) + (e_.)*(x_.)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int \frac{\sin^{-1}(ax)^4}{x} dx &= \text{Subst} \left(\int x^4 \cot(x) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{5}i \sin^{-1}(ax)^5 - 2i \text{Subst} \left(\int \frac{e^{2ix} x^4}{1 - e^{2ix}} dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{5}i \sin^{-1}(ax)^5 + \sin^{-1}(ax)^4 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 4 \text{Subst} \left(\int x^3 \log \left(1 - e^{2ix} \right) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{5}i \sin^{-1}(ax)^5 + \sin^{-1}(ax)^4 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 2i \sin^{-1}(ax)^3 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + 6i \text{Subst} \left(\int x^2 \log \left(1 - e^{2ix} \right) dx, x, \sin^{-1}(ax) \right) \\ &= -\frac{1}{5}i \sin^{-1}(ax)^5 + \sin^{-1}(ax)^4 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 2i \sin^{-1}(ax)^3 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + 3 \sin^{-1}(ax)^2 \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \\ &= -\frac{1}{5}i \sin^{-1}(ax)^5 + \sin^{-1}(ax)^4 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 2i \sin^{-1}(ax)^3 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + 3 \sin^{-1}(ax)^2 \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \\ &= -\frac{1}{5}i \sin^{-1}(ax)^5 + \sin^{-1}(ax)^4 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 2i \sin^{-1}(ax)^3 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + 3 \sin^{-1}(ax)^2 \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \\ &= -\frac{1}{5}i \sin^{-1}(ax)^5 + \sin^{-1}(ax)^4 \log \left(1 - e^{2i \sin^{-1}(ax)} \right) - 2i \sin^{-1}(ax)^3 \text{Li}_2 \left(e^{2i \sin^{-1}(ax)} \right) + 3 \sin^{-1}(ax)^2 \text{Li}_3 \left(e^{2i \sin^{-1}(ax)} \right) \end{aligned}$$

Mathematica [A] time = 0.0442051, size = 113, normalized size = 1.

$$2i \sin^{-1}(ax)^3 \text{PolyLog} \left(2, e^{-2i \sin^{-1}(ax)} \right) + 3 \sin^{-1}(ax)^2 \text{PolyLog} \left(3, e^{-2i \sin^{-1}(ax)} \right) - 3i \sin^{-1}(ax) \text{PolyLog} \left(4, e^{-2i \sin^{-1}(ax)} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^4/x, x]

[Out] (I/5)*ArcSin[a*x]^5 + ArcSin[a*x]^4*Log[1 - E^((-2*I)*ArcSin[a*x])] + (2*I)*ArcSin[a*x]^3*PolyLog[2, E^((-2*I)*ArcSin[a*x])] + 3*ArcSin[a*x]^2*PolyLog[3, E^((-2*I)*ArcSin[a*x])] - (3*I)*ArcSin[a*x]*PolyLog[4, E^((-2*I)*ArcSin[a*x])] - (3*PolyLog[5, E^((-2*I)*ArcSin[a*x])])/2

Maple [A] time = 0.046, size = 287, normalized size = 2.5

$$-\frac{i}{5} (\arcsin(ax))^5 + (\arcsin(ax))^4 \ln\left(1 + iax + \sqrt{-a^2x^2 + 1}\right) - 4i (\arcsin(ax))^3 \operatorname{polylog}\left(2, -iax - \sqrt{-a^2x^2 + 1}\right) + 12 (a$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^4/x,x)

[Out] $-1/5*I*\arcsin(a*x)^5 + \arcsin(a*x)^4*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)}) - 4*I*\arcsin(a*x)^3*\operatorname{polylog}(2, -I*a*x - (-a^2*x^2+1)^{(1/2)}) + 12*\arcsin(a*x)^2*\operatorname{polylog}(3, -I*a*x - (-a^2*x^2+1)^{(1/2)}) + 24*I*\arcsin(a*x)*\operatorname{polylog}(4, -I*a*x - (-a^2*x^2+1)^{(1/2)}) - 24*\operatorname{polylog}(5, -I*a*x - (-a^2*x^2+1)^{(1/2)}) + \arcsin(a*x)^4*\ln(1-I*a*x - (-a^2*x^2+1)^{(1/2)}) - 4*I*\arcsin(a*x)^3*\operatorname{polylog}(2, I*a*x + (-a^2*x^2+1)^{(1/2)}) + 12*\arcsin(a*x)^2*\operatorname{polylog}(3, I*a*x + (-a^2*x^2+1)^{(1/2)}) + 24*I*\arcsin(a*x)*\operatorname{polylog}(4, I*a*x + (-a^2*x^2+1)^{(1/2)}) - 24*\operatorname{polylog}(5, I*a*x + (-a^2*x^2+1)^{(1/2)})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^4}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4/x,x, algorithm="maxima")

[Out] integrate(arcsin(a*x)^4/x, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\arcsin(ax)^4}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4/x,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^4/x, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{asin}^4(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**4/x,x)

[Out] Integral(asin(a*x)**4/x, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^4}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^4/x,x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^4/x, x)
```

3.39 $\int \frac{\sin^{-1}(ax)^4}{x^2} dx$

Optimal. Leaf size=156

$$12ia \sin^{-1}(ax)^2 \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 12ia \sin^{-1}(ax)^2 \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 24a \sin^{-1}(ax) \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right)$$

```
[Out] -(ArcSin[a*x]^4/x) - 8*a*ArcSin[a*x]^3*ArcTanh[E^(I*ArcSin[a*x])] + (12*I)*
a*ArcSin[a*x]^2*PolyLog[2, -E^(I*ArcSin[a*x])] - (12*I)*a*ArcSin[a*x]^2*Pol
yLog[2, E^(I*ArcSin[a*x])] - 24*a*ArcSin[a*x]*PolyLog[3, -E^(I*ArcSin[a*x])
] + 24*a*ArcSin[a*x]*PolyLog[3, E^(I*ArcSin[a*x])] - (24*I)*a*PolyLog[4, -E
^(I*ArcSin[a*x])] + (24*I)*a*PolyLog[4, E^(I*ArcSin[a*x])]
```

Rubi [A] time = 0.193764, antiderivative size = 156, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4627, 4709, 4183, 2531, 6609, 2282, 6589}

$$12ia \sin^{-1}(ax)^2 \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 12ia \sin^{-1}(ax)^2 \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 24a \sin^{-1}(ax) \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

```
[In] Int[ArcSin[a*x]^4/x^2,x]
```

```
[Out] -(ArcSin[a*x]^4/x) - 8*a*ArcSin[a*x]^3*ArcTanh[E^(I*ArcSin[a*x])] + (12*I)*
a*ArcSin[a*x]^2*PolyLog[2, -E^(I*ArcSin[a*x])] - (12*I)*a*ArcSin[a*x]^2*Pol
yLog[2, E^(I*ArcSin[a*x])] - 24*a*ArcSin[a*x]*PolyLog[3, -E^(I*ArcSin[a*x])
] + 24*a*ArcSin[a*x]*PolyLog[3, E^(I*ArcSin[a*x])] - (24*I)*a*PolyLog[4, -E
^(I*ArcSin[a*x])] + (24*I)*a*PolyLog[4, E^(I*ArcSin[a*x])]
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((d_.)*(x_.))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4709

```
Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_))/Sqrt[(d_) + (e_.)*
(x_)^2], x_Symbol] :> Dist[1/(c^(m + 1)*Sqrt[d]), Subst[Int[(a + b*x)^n*Sin
[x]^m, x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d +
e, 0] && GtQ[d, 0] && IGtQ[n, 0] && IntegerQ[m]
```

Rule 4183

```
Int[csc[(e_.) + (f_.)*(x_.)]*((c_.) + (d_.)*(x_.))^(m_.), x_Symbol] :> Simp[(
-2*(c + d*x)^m*ArcTanh[E^(I*(e + f*x))])/f, x] + (-Dist[(d*m)/f, Int[(c + d
*x)^(m - 1)*Log[1 - E^(I*(e + f*x))], x], x] + Dist[(d*m)/f, Int[(c + d*x)^(
m - 1)*Log[1 + E^(I*(e + f*x))], x], x]) /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^(c_.)*((a_.) + (b_.)*(x_)))]^(n_.)*((f_.) + (g_.)
*(x_)^(m_.), x_Symbol] :> -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x
```

)))^n]]/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 6609

Int[((e_.) + (f_.)*(x_.))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_.)))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p]/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c, d, e, f, n, p}, x] && GtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))* (F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 6589

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_.))^(p_.)]/((d_.) + (e_.)*(x_.)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned}
 \int \frac{\sin^{-1}(ax)^4}{x^2} dx &= -\frac{\sin^{-1}(ax)^4}{x} + (4a) \int \frac{\sin^{-1}(ax)^3}{x\sqrt{1-a^2x^2}} dx \\
 &= -\frac{\sin^{-1}(ax)^4}{x} + (4a) \text{Subst} \left(\int x^3 \csc(x) dx, x, \sin^{-1}(ax) \right) \\
 &= -\frac{\sin^{-1}(ax)^4}{x} - 8a \sin^{-1}(ax)^3 \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) - (12a) \text{Subst} \left(\int x^2 \log(1 - e^{ix}) dx, x, \sin^{-1}(ax) \right) \\
 &= -\frac{\sin^{-1}(ax)^4}{x} - 8a \sin^{-1}(ax)^3 \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) + 12ia \sin^{-1}(ax)^2 \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) - 12ia \sin^{-1}(ax) \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) \\
 &= -\frac{\sin^{-1}(ax)^4}{x} - 8a \sin^{-1}(ax)^3 \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) + 12ia \sin^{-1}(ax)^2 \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) - 12ia \sin^{-1}(ax) \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) \\
 &= -\frac{\sin^{-1}(ax)^4}{x} - 8a \sin^{-1}(ax)^3 \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) + 12ia \sin^{-1}(ax)^2 \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) - 12ia \sin^{-1}(ax) \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) \\
 &= -\frac{\sin^{-1}(ax)^4}{x} - 8a \sin^{-1}(ax)^3 \tanh^{-1} \left(e^{i \sin^{-1}(ax)} \right) + 12ia \sin^{-1}(ax)^2 \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right) - 12ia \sin^{-1}(ax) \text{Li}_2 \left(-e^{i \sin^{-1}(ax)} \right)
 \end{aligned}$$

Mathematica [A] time = 0.266898, size = 198, normalized size = 1.27

$$a \left(12i \sin^{-1}(ax)^2 \text{PolyLog} \left(2, e^{-i \sin^{-1}(ax)} \right) + 12i \sin^{-1}(ax)^2 \text{PolyLog} \left(2, -e^{i \sin^{-1}(ax)} \right) + 24 \sin^{-1}(ax) \text{PolyLog} \left(3, e^{-i \sin^{-1}(ax)} \right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^4/x^2, x]

[Out] a*((-I/2)*Pi^4 + I*ArcSin[a*x]^4 - ArcSin[a*x]^4/(a*x) + 4*ArcSin[a*x]^3*Log[1 - E^((-I)*ArcSin[a*x])] - 4*ArcSin[a*x]^3*Log[1 + E^(I*ArcSin[a*x])] + (12*I)*ArcSin[a*x]^2*PolyLog[2, E^((-I)*ArcSin[a*x])] + (12*I)*ArcSin[a*x]^2*PolyLog[2, E^(I*ArcSin[a*x])] - 24*ArcSin[a*x]*PolyLog[3, E^((-I)*ArcSin[a*x])] - 24*ArcSin[a*x]*PolyLog[3, E^(I*ArcSin[a*x])])

$2*\text{PolyLog}[2, -E^{(I*\text{ArcSin}[a*x])}] + 24*\text{ArcSin}[a*x]*\text{PolyLog}[3, E^{((-I)*\text{ArcSin}[a*x])}] - 24*\text{ArcSin}[a*x]*\text{PolyLog}[3, -E^{(I*\text{ArcSin}[a*x])}] - (24*I)*\text{PolyLog}[4, E^{((-I)*\text{ArcSin}[a*x])}] - (24*I)*\text{PolyLog}[4, -E^{(I*\text{ArcSin}[a*x])}]$

Maple [A] time = 0.077, size = 241, normalized size = 1.5

$$-\frac{(\arcsin(ax))^4}{x} + 4a(\arcsin(ax))^3 \ln\left(1 - iax - \sqrt{-a^2x^2 + 1}\right) - 4a(\arcsin(ax))^3 \ln\left(1 + iax + \sqrt{-a^2x^2 + 1}\right) - 24a \arcsin(ax)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^4/x^2,x)

[Out] $-\arcsin(a*x)^4/x + 4*a*\arcsin(a*x)^3*\ln(1-I*a*x-(-a^2*x^2+1)^{(1/2)}) - 4*a*\arcsin(a*x)^3*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)}) - 24*a*\arcsin(a*x)*\text{polylog}(3, -I*a*x-(-a^2*x^2+1)^{(1/2)}) + 24*a*\arcsin(a*x)*\text{polylog}(3, I*a*x+(-a^2*x^2+1)^{(1/2)}) + 12*I*a*\arcsin(a*x)^2*\text{polylog}(2, -I*a*x-(-a^2*x^2+1)^{(1/2)}) - 12*I*a*\arcsin(a*x)^2*\text{polylog}(2, I*a*x+(-a^2*x^2+1)^{(1/2)}) + 24*I*a*\text{polylog}(4, I*a*x+(-a^2*x^2+1)^{(1/2)}) - 24*I*a*\text{polylog}(4, -I*a*x-(-a^2*x^2+1)^{(1/2)})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$-\frac{\arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^4 + 4ax \int \frac{\sqrt{-ax+1} \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3}{\sqrt{ax+1}(ax-1)x} dx}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4/x^2,x, algorithm="maxima")

[Out] $-(\arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1}))^4 + 4*a*x*\text{integrate}(\sqrt{a*x+1}*\sqrt{-a*x+1}*\arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1})^3/(a^2*x^3 - x), x)/x$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^4}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4/x^2,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^4/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{asin}^4(ax)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(asin(a*x)**4/x**2,x)
```

```
[Out] Integral(asin(a*x)**4/x**2, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^4}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^4/x^2,x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^4/x^2, x)
```

3.40 $\int \frac{\sin^{-1}(ax)^4}{x^3} dx$

Optimal. Leaf size=119

$$-6ia^2 \sin^{-1}(ax) \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + 3a^2 \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) - \frac{2a\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{x} - 2ia^2 \sin^{-1}(ax)^3 + 6a^2$$

[Out] $(-2*I)*a^2*ArcSin[a*x]^3 - (2*a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/x - ArcSin[a*x]^4/(2*x^2) + 6*a^2*ArcSin[a*x]^2*Log[1 - E^((2*I)*ArcSin[a*x])] - (6*I)*a^2*ArcSin[a*x]*PolyLog[2, E^((2*I)*ArcSin[a*x])] + 3*a^2*PolyLog[3, E^((2*I)*ArcSin[a*x])]$

Rubi [A] time = 0.216142, antiderivative size = 119, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 8, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.8$, Rules used = {4627, 4681, 4625, 3717, 2190, 2531, 2282, 6589}

$$-6ia^2 \sin^{-1}(ax) \text{PolyLog}\left(2, e^{2i \sin^{-1}(ax)}\right) + 3a^2 \text{PolyLog}\left(3, e^{2i \sin^{-1}(ax)}\right) - \frac{2a\sqrt{1-a^2x^2} \sin^{-1}(ax)^3}{x} - 2ia^2 \sin^{-1}(ax)^3 + 6a^2$$

Antiderivative was successfully verified.

[In] $\text{Int}[ArcSin[a*x]^4/x^3, x]$

[Out] $(-2*I)*a^2*ArcSin[a*x]^3 - (2*a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/x - ArcSin[a*x]^4/(2*x^2) + 6*a^2*ArcSin[a*x]^2*Log[1 - E^((2*I)*ArcSin[a*x])] - (6*I)*a^2*ArcSin[a*x]*PolyLog[2, E^((2*I)*ArcSin[a*x])] + 3*a^2*PolyLog[3, E^((2*I)*ArcSin[a*x])]$

Rule 4627

$\text{Int}[(a + ArcSin[(c \cdot x)](b \cdot x))^n \cdot ((d \cdot x))^m, x_Symbol] \rightarrow \text{Simp}[(d \cdot x)^{m+1} \cdot (a + b \cdot ArcSin[c \cdot x])^n / (d \cdot (m+1)), x] - \text{Dist}[(b \cdot c \cdot n) / (d \cdot (m+1)), \text{Int}[(d \cdot x)^{m+1} \cdot (a + b \cdot ArcSin[c \cdot x])^{n-1} / \text{Sqrt}[1 - c^2 \cdot x^2], x], x] /;$ $\text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 4681

$\text{Int}[(a + ArcSin[(c \cdot x)](b \cdot x))^n \cdot ((f \cdot x))^m \cdot ((d + (e \cdot x)^2)^p), x_Symbol] \rightarrow \text{Simp}[(f \cdot x)^{m+1} \cdot (d + e \cdot x^2)^{p+1} \cdot (a + b \cdot ArcSin[c \cdot x])^n / (d \cdot f \cdot (m+1)), x] - \text{Dist}[(b \cdot c \cdot n \cdot d^{\text{IntPart}[p]} \cdot (d + e \cdot x^2)^{\text{FracPart}[p]}) / (f \cdot (m+1) \cdot (1 - c^2 \cdot x^2)^{\text{FracPart}[p]}), \text{Int}[(f \cdot x)^{m+1} \cdot (1 - c^2 \cdot x^2)^{p+1/2} \cdot (a + b \cdot ArcSin[c \cdot x])^{n-1}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, e, f, m, p\}, x \ \&\& \ \text{EqQ}[c^2 \cdot d + e, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{EqQ}[m + 2 \cdot p + 3, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 4625

$\text{Int}[(a + ArcSin[(c \cdot x)](b \cdot x))^n / (x), x_Symbol] \rightarrow \text{Subst}[\text{Int}[(a + b \cdot x)^n / \text{Tan}[x], x], x, ArcSin[c \cdot x]] /;$ $\text{FreeQ}\{a, b, c\}, x \ \&\& \ \text{IGtQ}[n, 0]$

Rule 3717

$\text{Int}[(c + (d \cdot x))^m \cdot \tan[(e + \text{Pi} \cdot (k \cdot x) + (f \cdot x))], x_Symbol] \rightarrow \text{Simp}[(I \cdot (c + d \cdot x)^{m+1}) / (d \cdot (m+1)), x] - \text{Dist}[2 \cdot I, \text{Int}[(c + d \cdot x)^m \cdot E^{(2 \cdot I \cdot k \cdot \text{Pi})} \cdot E^{(2 \cdot I \cdot (e + f \cdot x))}) / (1 + E^{(2 \cdot I \cdot k \cdot \text{Pi})} \cdot E^{(2 \cdot I \cdot (e + f \cdot x))}), x],$

x] /; FreeQ[{c, d, e, f}, x] && IntegerQ[4*k] && IGtQ[m, 0]

Rule 2190

Int[(((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)*((c_) + (d_)*(x_))^(m_))/((a_) + (b_)*((F_)^((g_)*((e_) + (f_)*(x_))))^(n_)), x_Symbol] := Simp[(((c + d*x)^m*Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1)*Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]

Rule 2531

Int[Log[1 + (e_)*((F_)^((c_)*((a_) + (b_)*(x_))))^(n_)]*((f_) + (g_)*(x_))^(m_), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_)*(v_)^(n_))^(m_)] /; FreeQ[{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_)*((a_) + (b_)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 6589

Int[PolyLog[n_, (c_)*((a_) + (b_)*(x_))^(p_)]/((d_) + (e_)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned}
 \int \frac{\sin^{-1}(ax)^4}{x^3} dx &= -\frac{\sin^{-1}(ax)^4}{2x^2} + (2a) \int \frac{\sin^{-1}(ax)^3}{x^2\sqrt{1-a^2x^2}} dx \\
 &= -\frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{x} - \frac{\sin^{-1}(ax)^4}{2x^2} + (6a^2) \int \frac{\sin^{-1}(ax)^2}{x} dx \\
 &= -\frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{x} - \frac{\sin^{-1}(ax)^4}{2x^2} + (6a^2) \text{Subst} \left(\int x^2 \cot(x) dx, x, \sin^{-1}(ax) \right) \\
 &= -2ia^2 \sin^{-1}(ax)^3 - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{x} - \frac{\sin^{-1}(ax)^4}{2x^2} - (12ia^2) \text{Subst} \left(\int \frac{e^{2ix}x^2}{1-e^{2ix}} dx, x, \sin^{-1}(ax) \right) \\
 &= -2ia^2 \sin^{-1}(ax)^3 - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{x} - \frac{\sin^{-1}(ax)^4}{2x^2} + 6a^2 \sin^{-1}(ax)^2 \log \left(1 - e^{2i\sin^{-1}(ax)} \right) - 6a^2 \sin^{-1}(ax) \log \left(1 - e^{2i\sin^{-1}(ax)} \right) \\
 &= -2ia^2 \sin^{-1}(ax)^3 - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{x} - \frac{\sin^{-1}(ax)^4}{2x^2} + 6a^2 \sin^{-1}(ax)^2 \log \left(1 - e^{2i\sin^{-1}(ax)} \right) - 6a^2 \sin^{-1}(ax) \log \left(1 - e^{2i\sin^{-1}(ax)} \right) \\
 &= -2ia^2 \sin^{-1}(ax)^3 - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{x} - \frac{\sin^{-1}(ax)^4}{2x^2} + 6a^2 \sin^{-1}(ax)^2 \log \left(1 - e^{2i\sin^{-1}(ax)} \right) - 6a^2 \sin^{-1}(ax) \log \left(1 - e^{2i\sin^{-1}(ax)} \right)
 \end{aligned}$$

Mathematica [A] time = 0.282873, size = 124, normalized size = 1.04

$$-\frac{\sin^{-1}(ax)^4}{2x^2} + \frac{1}{4}a^2 \left(24i \sin^{-1}(ax) \text{PolyLog} \left(2, e^{-2i\sin^{-1}(ax)} \right) + 12 \text{PolyLog} \left(3, e^{-2i\sin^{-1}(ax)} \right) - \frac{8\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{ax} + \dots \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^4/x^3,x]

[Out] $-\text{ArcSin}[a*x]^4/(2*x^2) + (a^2*((-I)*\text{Pi}^3 + (8*I)*\text{ArcSin}[a*x]^3 - (8*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^3)/(a*x) + 24*\text{ArcSin}[a*x]^2*\text{Log}[1 - E^{((-2*I)*\text{ArcSin}[a*x])}] + (24*I)*\text{ArcSin}[a*x]*\text{PolyLog}[2, E^{((-2*I)*\text{ArcSin}[a*x])}] + 12*\text{PolyLog}[3, E^{((-2*I)*\text{ArcSin}[a*x])}]))/4$

Maple [A] time = 0.091, size = 227, normalized size = 1.9

$$-2ia^2(\arcsin(ax))^3 - 2\frac{a(\arcsin(ax))^3\sqrt{-a^2x^2+1}}{x} - \frac{(\arcsin(ax))^4}{2x^2} + 6a^2(\arcsin(ax))^2\ln\left(1+iax+\sqrt{-a^2x^2+1}\right) - 1$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^4/x^3,x)

[Out] $-2*I*a^2*\arcsin(a*x)^3 - 2*a*\arcsin(a*x)^3*(-a^2*x^2+1)^{(1/2)}/x - 1/2*\arcsin(a*x)^4/x^2 + 6*a^2*\arcsin(a*x)^2*\ln(1+I*a*x+(-a^2*x^2+1)^{(1/2)}) - 12*I*a^2*\arcsin(a*x)*\text{polylog}(2, -I*a*x - (-a^2*x^2+1)^{(1/2)}) + 12*a^2*\text{polylog}(3, -I*a*x - (-a^2*x^2+1)^{(1/2)}) + 6*a^2*\arcsin(a*x)^2*\ln(1-I*a*x - (-a^2*x^2+1)^{(1/2)}) - 12*I*a^2*\arcsin(a*x)*\text{polylog}(2, I*a*x + (-a^2*x^2+1)^{(1/2)}) + 12*a^2*\text{polylog}(3, I*a*x + (-a^2*x^2+1)^{(1/2)})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^4 + \frac{1}{2}\left(\sqrt{ax+1}\sqrt{-ax+1}\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3 + 8x \int \frac{7\sqrt{ax+1}\sqrt{-ax+1}\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}{2x^2}\right)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4/x^3,x, algorithm="maxima")

[Out] $-1/2*(\arctan2(a*x, \text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1))^4 + 4*a*x^2*\text{integrate}(\text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1)*\arctan2(a*x, \text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1))^3/(a^2*x^4 - x^2), x))/x^2$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^4}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4/x^3,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^4/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{asin}^4(ax)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**4/x**3,x)

[Out] Integral(asin(a*x)**4/x**3, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^4}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^4/x^3,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^4/x^3, x)

3.41 $\int \frac{\sin^{-1}(ax)^4}{x^4} dx$

Optimal. Leaf size=276

$$2ia^3 \sin^{-1}(ax)^2 \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 2ia^3 \sin^{-1}(ax)^2 \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 4a^3 \sin^{-1}(ax) \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right)$$

```
[Out] (-2*a^2*ArcSin[a*x]^2)/x - (2*a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(3*x^2) -
ArcSin[a*x]^4/(3*x^3) - 8*a^3*ArcSin[a*x]*ArcTanh[E^(I*ArcSin[a*x])] - (4*a
^3*ArcSin[a*x]^3*ArcTanh[E^(I*ArcSin[a*x])])/3 + (4*I)*a^3*PolyLog[2, -E^(I
*ArcSin[a*x])] + (2*I)*a^3*ArcSin[a*x]^2*PolyLog[2, -E^(I*ArcSin[a*x])] - (
4*I)*a^3*PolyLog[2, E^(I*ArcSin[a*x])] - (2*I)*a^3*ArcSin[a*x]^2*PolyLog[2,
E^(I*ArcSin[a*x])] - 4*a^3*ArcSin[a*x]*PolyLog[3, -E^(I*ArcSin[a*x])] + 4*
a^3*ArcSin[a*x]*PolyLog[3, E^(I*ArcSin[a*x])] - (4*I)*a^3*PolyLog[4, -E^(I*
ArcSin[a*x])] + (4*I)*a^3*PolyLog[4, E^(I*ArcSin[a*x])]
```

Rubi [A] time = 0.410257, antiderivative size = 276, normalized size of antiderivative = 1., number of steps used = 19, number of rules used = 10, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {4627, 4701, 4709, 4183, 2531, 6609, 2282, 6589, 2279, 2391}

$$2ia^3 \sin^{-1}(ax)^2 \text{PolyLog}\left(2, -e^{i \sin^{-1}(ax)}\right) - 2ia^3 \sin^{-1}(ax)^2 \text{PolyLog}\left(2, e^{i \sin^{-1}(ax)}\right) - 4a^3 \sin^{-1}(ax) \text{PolyLog}\left(3, -e^{i \sin^{-1}(ax)}\right)$$

Antiderivative was successfully verified.

```
[In] Int[ArcSin[a*x]^4/x^4, x]
```

```
[Out] (-2*a^2*ArcSin[a*x]^2)/x - (2*a*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^3)/(3*x^2) -
ArcSin[a*x]^4/(3*x^3) - 8*a^3*ArcSin[a*x]*ArcTanh[E^(I*ArcSin[a*x])] - (4*a
^3*ArcSin[a*x]^3*ArcTanh[E^(I*ArcSin[a*x])])/3 + (4*I)*a^3*PolyLog[2, -E^(I
*ArcSin[a*x])] + (2*I)*a^3*ArcSin[a*x]^2*PolyLog[2, -E^(I*ArcSin[a*x])] - (
4*I)*a^3*PolyLog[2, E^(I*ArcSin[a*x])] - (2*I)*a^3*ArcSin[a*x]^2*PolyLog[2,
E^(I*ArcSin[a*x])] - 4*a^3*ArcSin[a*x]*PolyLog[3, -E^(I*ArcSin[a*x])] + 4*
a^3*ArcSin[a*x]*PolyLog[3, E^(I*ArcSin[a*x])] - (4*I)*a^3*PolyLog[4, -E^(I*
ArcSin[a*x])] + (4*I)*a^3*PolyLog[4, E^(I*ArcSin[a*x])]
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4701

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_.)*((f_.)*(x_))^(m_)*((d_) + (e_
)*(x_)^2)^(p_), x_Symbol] :> Simp[((f*x)^(m + 1)*(d + e*x^2)^(p + 1)*(a + b
*ArcSin[c*x])^n)/(d*f*(m + 1)), x] + (Dist[(c^2*(m + 2*p + 3))/(f^2*(m + 1)
), Int[(f*x)^(m + 2)*(d + e*x^2)^p*(a + b*ArcSin[c*x])^n, x], x] - Dist[(b*
c*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(f*(m + 1)*(1 - c^2*x^2)^FracPart
[p]), Int[(f*x)^(m + 1)*(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1)
, x], x]) /; FreeQ[{a, b, c, d, e, f, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n,
0] && LtQ[m, -1] && IntegerQ[m]
```

Rule 4709

```
Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_))/Sqrt[(d_) + (e_.)*
(x_)^2], x_Symbol] := Dist[1/(c^(m + 1)*Sqrt[d]), Subst[Int[(a + b*x)^n*Sin
[x]^m, x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d +
e, 0] && GtQ[d, 0] && IGtQ[n, 0] && IntegerQ[m]
```

Rule 4183

```
Int[csc[(e_.) + (f_.)*(x_.)]*((c_.) + (d_.)*(x_.))^(m_.), x_Symbol] := Simp[(-
2*(c + d*x)^m*ArcTanh[E^(I*(e + f*x))])/f, x] + (-Dist[(d*m)/f, Int[(c + d
*x)^(m - 1)*Log[1 - E^(I*(e + f*x))], x], x] + Dist[(d*m)/f, Int[(c + d*x)^(
m - 1)*Log[1 + E^(I*(e + f*x))], x], x]) /; FreeQ[{c, d, e, f}, x] && IGtQ
[m, 0]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_.)))^(n_.)]*((f_.) + (g_.)
*(x_.))^(m_.), x_Symbol] := -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x)
)))^n])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m -
1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f
, g, n}, x] && GtQ[m, 0]
```

Rule 6609

```
Int[((e_.) + (f_.)*(x_.))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.)
*(x_.)))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p])/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_.))^(m_) /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_.))^(p_.)]/((d_.) + (e_.)*(x_.)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rule 2279

```
Int[Log[(a_) + (b_.)*((F_)^((e_.)*((c_.) + (d_.)*(x_.)))^(n_.)], x_Symbol]
:= Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)
))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]
```

Rule 2391

```
Int[Log[(c_.)*((d_) + (e_.)*(x_)^(n_.))]/(x_), x_Symbol] := -Simp[PolyLog[2
, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\sin^{-1}(ax)^4}{x^4} dx &= -\frac{\sin^{-1}(ax)^4}{3x^3} + \frac{1}{3}(4a) \int \frac{\sin^{-1}(ax)^3}{x^3\sqrt{1-a^2x^2}} dx \\
&= -\frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{3x^2} - \frac{\sin^{-1}(ax)^4}{3x^3} + (2a^2) \int \frac{\sin^{-1}(ax)^2}{x^2} dx + \frac{1}{3}(2a^3) \int \frac{\sin^{-1}(ax)^3}{x\sqrt{1-a^2x^2}} dx \\
&= -\frac{2a^2\sin^{-1}(ax)^2}{x} - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{3x^2} - \frac{\sin^{-1}(ax)^4}{3x^3} + \frac{1}{3}(2a^3) \text{Subst} \left(\int x^3 \csc(x) dx, x, \sin^{-1}(ax) \right) \\
&= -\frac{2a^2\sin^{-1}(ax)^2}{x} - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{3x^2} - \frac{\sin^{-1}(ax)^4}{3x^3} - \frac{4}{3}a^3 \sin^{-1}(ax)^3 \tanh^{-1} \left(e^{i\sin^{-1}(ax)} \right) - (2a^3) \int \frac{\sin^{-1}(ax)^2}{x} dx \\
&= -\frac{2a^2\sin^{-1}(ax)^2}{x} - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{3x^2} - \frac{\sin^{-1}(ax)^4}{3x^3} - 8a^3 \sin^{-1}(ax) \tanh^{-1} \left(e^{i\sin^{-1}(ax)} \right) - \frac{4}{3}a^3 \sin^{-1}(ax)^2 \int \frac{1}{x} dx \\
&= -\frac{2a^2\sin^{-1}(ax)^2}{x} - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{3x^2} - \frac{\sin^{-1}(ax)^4}{3x^3} - 8a^3 \sin^{-1}(ax) \tanh^{-1} \left(e^{i\sin^{-1}(ax)} \right) - \frac{4}{3}a^3 \sin^{-1}(ax)^2 \ln|x| \\
&= -\frac{2a^2\sin^{-1}(ax)^2}{x} - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{3x^2} - \frac{\sin^{-1}(ax)^4}{3x^3} - 8a^3 \sin^{-1}(ax) \tanh^{-1} \left(e^{i\sin^{-1}(ax)} \right) - \frac{4}{3}a^3 \sin^{-1}(ax)^2 \ln|x| \\
&= -\frac{2a^2\sin^{-1}(ax)^2}{x} - \frac{2a\sqrt{1-a^2x^2}\sin^{-1}(ax)^3}{3x^2} - \frac{\sin^{-1}(ax)^4}{3x^3} - 8a^3 \sin^{-1}(ax) \tanh^{-1} \left(e^{i\sin^{-1}(ax)} \right) - \frac{4}{3}a^3 \sin^{-1}(ax)^2 \ln|x|
\end{aligned}$$

Mathematica [A] time = 4.26995, size = 399, normalized size = 1.45

$$\frac{1}{24}a^3 \left(48i \sin^{-1}(ax)^2 \text{PolyLog} \left(2, e^{-i\sin^{-1}(ax)} \right) + 96 \sin^{-1}(ax) \text{PolyLog} \left(3, e^{-i\sin^{-1}(ax)} \right) - 96 \sin^{-1}(ax) \text{PolyLog} \left(3, -e^{i\sin^{-1}(ax)} \right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^4/x^4, x]

[Out] (a^3*((-2*I)*Pi^4 + (4*I)*ArcSin[a*x]^4 - 24*ArcSin[a*x]^2*Cot[ArcSin[a*x]/2] - 2*ArcSin[a*x]^4*Cot[ArcSin[a*x]/2] - 4*ArcSin[a*x]^3*Csc[ArcSin[a*x]/2]^2 - (a*x*ArcSin[a*x]^4*Csc[ArcSin[a*x]/2]^4)/2 + 16*ArcSin[a*x]^3*Log[1 - E^((-I)*ArcSin[a*x])] + 96*ArcSin[a*x]*Log[1 - E^(I*ArcSin[a*x])] - 96*ArcSin[a*x]*Log[1 + E^(I*ArcSin[a*x])] - 16*ArcSin[a*x]^3*Log[1 + E^(I*ArcSin[a*x])] + (48*I)*ArcSin[a*x]^2*PolyLog[2, E^((-I)*ArcSin[a*x])] + (48*I)*(2 + ArcSin[a*x]^2)*PolyLog[2, -E^(I*ArcSin[a*x])] - (96*I)*PolyLog[2, E^(I*ArcSin[a*x])] + 96*ArcSin[a*x]*PolyLog[3, E^((-I)*ArcSin[a*x])] - 96*ArcSin[a*x]*PolyLog[3, -E^(I*ArcSin[a*x])] - (96*I)*PolyLog[4, E^((-I)*ArcSin[a*x])] - (96*I)*PolyLog[4, -E^(I*ArcSin[a*x])] + 4*ArcSin[a*x]^3*Sec[ArcSin[a*x]/2]^2 - (8*ArcSin[a*x]^4*Sin[ArcSin[a*x]/2]^4)/(a^3*x^3) - 24*ArcSin[a*x]^2*Tan[ArcSin[a*x]/2] - 2*ArcSin[a*x]^4*Tan[ArcSin[a*x]/2]))/24

Maple [A] time = 0.145, size = 409, normalized size = 1.5

$$-\frac{2a(\arcsin(ax))^3}{3x^2}\sqrt{-a^2x^2+1} - 2\frac{a^2(\arcsin(ax))^2}{x} - \frac{(\arcsin(ax))^4}{3x^3} - \frac{2a^3(\arcsin(ax))^3}{3}\ln\left(1+iax+\sqrt{-a^2x^2+1}\right) + 2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^4/x^4, x)

[Out] -2/3*a*arcsin(a*x)^3*(-a^2*x^2+1)^(1/2)/x^2-2*a^2*arcsin(a*x)^2/x-1/3*arcsin(a*x)^4/x^3-2/3*a^3*arcsin(a*x)^3*ln(1+I*a*x+(-a^2*x^2+1)^(1/2))+2*I*a^3*a

$\text{rcsin}(ax)^2 \text{polylog}(2, -Iax - (-a^2x^2+1)^{1/2}) - 4a^3 \text{arcsin}(ax) \text{polylog}(3, -Iax - (-a^2x^2+1)^{1/2}) - 4Ia^3 \text{polylog}(4, -Iax - (-a^2x^2+1)^{1/2}) + 2/3a^3 \text{arcsin}(ax)^3 \ln(1 - Iax - (-a^2x^2+1)^{1/2}) - 2Ia^3 \text{arcsin}(ax)^2 \text{polylog}(2, Iax + (-a^2x^2+1)^{1/2}) + 4a^3 \text{arcsin}(ax) \text{polylog}(3, Iax + (-a^2x^2+1)^{1/2}) + 4Ia^3 \text{polylog}(4, Iax + (-a^2x^2+1)^{1/2}) - 4a^3 \text{arcsin}(ax) \ln(1 + Iax + (-a^2x^2+1)^{1/2}) + 4Ia^3 \text{polylog}(2, -Iax - (-a^2x^2+1)^{1/2}) + 4a^3 \text{arcsin}(ax) \ln(1 - Iax - (-a^2x^2+1)^{1/2}) - 4Ia^3 \text{polylog}(2, Iax + (-a^2x^2+1)^{1/2})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{4ax^3 \int \frac{\sqrt{ax+1}\sqrt{-ax+1} \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3}{a^2x^5-x^3} dx + \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^4}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(ax)^4/x^4, x, algorithm="maxima")

[Out] $-1/3*(12*a*x^3*\text{integrate}(1/3*\text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1)*\text{arctan2}(a*x, \text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1))^3/(a^2*x^5 - x^3), x) + \text{arctan2}(a*x, \text{sqrt}(a*x + 1)*\text{sqrt}(-a*x + 1))^4)/x^3$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^4}{x^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(ax)^4/x^4, x, algorithm="fricas")

[Out] integral(arcsin(ax)^4/x^4, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{asin}^4(ax)}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(ax)**4/x**4, x)

[Out] Integral(asin(ax)**4/x**4, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^4}{x^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(arcsin(a*x)^4/x^4,x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^4/x^4, x)
```

$$3.42 \quad \int \frac{x^6}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=55

$$\frac{5\text{CosIntegral}(\sin^{-1}(ax))}{64a^7} - \frac{9\text{CosIntegral}(3\sin^{-1}(ax))}{64a^7} + \frac{5\text{CosIntegral}(5\sin^{-1}(ax))}{64a^7} - \frac{\text{CosIntegral}(7\sin^{-1}(ax))}{64a^7}$$

```
[Out] (5*CosIntegral[ArcSin[a*x]])/(64*a^7) - (9*CosIntegral[3*ArcSin[a*x]])/(64*
a^7) + (5*CosIntegral[5*ArcSin[a*x]])/(64*a^7) - CosIntegral[7*ArcSin[a*x]]
/(64*a^7)
```

Rubi [A] time = 0.0965148, antiderivative size = 55, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4635, 4406, 3302}

$$\frac{5\text{CosIntegral}(\sin^{-1}(ax))}{64a^7} - \frac{9\text{CosIntegral}(3\sin^{-1}(ax))}{64a^7} + \frac{5\text{CosIntegral}(5\sin^{-1}(ax))}{64a^7} - \frac{\text{CosIntegral}(7\sin^{-1}(ax))}{64a^7}$$

Antiderivative was successfully verified.

```
[In] Int[x^6/ArcSin[a*x], x]
```

```
[Out] (5*CosIntegral[ArcSin[a*x]])/(64*a^7) - (9*CosIntegral[3*ArcSin[a*x]])/(64*
a^7) + (5*CosIntegral[5*ArcSin[a*x]])/(64*a^7) - CosIntegral[7*ArcSin[a*x]]
/(64*a^7)
```

Rule 4635

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Dist[1
/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x]
/; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]
]^n*Cos[a + b*x]^p, x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^6}{\sin^{-1}(ax)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^6(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^7} \\
&= \frac{\text{Subst}\left(\int \left(\frac{5\cos(x)}{64x} - \frac{9\cos(3x)}{64x} + \frac{5\cos(5x)}{64x} - \frac{\cos(7x)}{64x}\right) dx, x, \sin^{-1}(ax)\right)}{a^7} \\
&= -\frac{\text{Subst}\left(\int \frac{\cos(7x)}{x} dx, x, \sin^{-1}(ax)\right)}{64a^7} + \frac{5\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{64a^7} + \frac{5\text{Subst}\left(\int \frac{\cos(5x)}{x} dx, x, \sin^{-1}(ax)\right)}{64a^7} \\
&= \frac{5\text{Ci}\left(\sin^{-1}(ax)\right)}{64a^7} - \frac{9\text{Ci}\left(3\sin^{-1}(ax)\right)}{64a^7} + \frac{5\text{Ci}\left(5\sin^{-1}(ax)\right)}{64a^7} - \frac{\text{Ci}\left(7\sin^{-1}(ax)\right)}{64a^7}
\end{aligned}$$

Mathematica [A] time = 0.0164933, size = 40, normalized size = 0.73

$$\frac{-5\text{CosIntegral}\left(\sin^{-1}(ax)\right) + 9\text{CosIntegral}\left(3\sin^{-1}(ax)\right) - 5\text{CosIntegral}\left(5\sin^{-1}(ax)\right) + \text{CosIntegral}\left(7\sin^{-1}(ax)\right)}{64a^7}$$

Antiderivative was successfully verified.

[In] Integrate[x^6/ArcSin[a*x],x]

[Out] $-(5*\text{CosIntegral}[\text{ArcSin}[a*x]] + 9*\text{CosIntegral}[3*\text{ArcSin}[a*x]] - 5*\text{CosIntegral}[5*\text{ArcSin}[a*x]] + \text{CosIntegral}[7*\text{ArcSin}[a*x]])/(64*a^7)$

Maple [A] time = 0.039, size = 40, normalized size = 0.7

$$\frac{1}{a^7} \left(\frac{5\text{Ci}(\arcsin(ax))}{64} - \frac{9\text{Ci}(3\arcsin(ax))}{64} + \frac{5\text{Ci}(5\arcsin(ax))}{64} - \frac{\text{Ci}(7\arcsin(ax))}{64} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/arcsin(a*x),x)

[Out] $1/a^7*(5/64*Ci(arcsin(a*x))-9/64*Ci(3*arcsin(a*x))+5/64*Ci(5*arcsin(a*x))-1/64*Ci(7*arcsin(a*x)))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^6}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(x^6/arcsin(a*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^6}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x),x, algorithm="fricas")

[Out] integral(x^6/arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^6}{\operatorname{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6/asin(a*x),x)

[Out] Integral(x**6/asin(a*x), x)

Giac [A] time = 1.31765, size = 63, normalized size = 1.15

$$-\frac{\operatorname{Ci}(7 \operatorname{arcsin}(ax))}{64 a^7} + \frac{5 \operatorname{Ci}(5 \operatorname{arcsin}(ax))}{64 a^7} - \frac{9 \operatorname{Ci}(3 \operatorname{arcsin}(ax))}{64 a^7} + \frac{5 \operatorname{Ci}(\operatorname{arcsin}(ax))}{64 a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x),x, algorithm="giac")

[Out] -1/64*cos_integral(7*arcsin(a*x))/a^7 + 5/64*cos_integral(5*arcsin(a*x))/a^7 - 9/64*cos_integral(3*arcsin(a*x))/a^7 + 5/64*cos_integral(arcsin(a*x))/a^7

$$3.43 \quad \int \frac{x^5}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=43

$$\frac{5\text{Si}(2\sin^{-1}(ax))}{32a^6} - \frac{\text{Si}(4\sin^{-1}(ax))}{8a^6} + \frac{\text{Si}(6\sin^{-1}(ax))}{32a^6}$$

[Out] (5*SinIntegral[2*ArcSin[a*x]])/(32*a^6) - SinIntegral[4*ArcSin[a*x]]/(8*a^6) + SinIntegral[6*ArcSin[a*x]]/(32*a^6)

Rubi [A] time = 0.0803015, antiderivative size = 43, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4635, 4406, 3299}

$$\frac{5\text{Si}(2\sin^{-1}(ax))}{32a^6} - \frac{\text{Si}(4\sin^{-1}(ax))}{8a^6} + \frac{\text{Si}(6\sin^{-1}(ax))}{32a^6}$$

Antiderivative was successfully verified.

[In] Int[x^5/ArcSin[a*x], x]

[Out] (5*SinIntegral[2*ArcSin[a*x]])/(32*a^6) - SinIntegral[4*ArcSin[a*x]]/(8*a^6) + SinIntegral[6*ArcSin[a*x]]/(32*a^6)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]]^n*Cos[a + b*x]^p, x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^5}{\sin^{-1}(ax)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^5(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^6} \\ &= \frac{\text{Subst}\left(\int \left(\frac{5\sin(2x)}{32x} - \frac{\sin(4x)}{8x} + \frac{\sin(6x)}{32x}\right) dx, x, \sin^{-1}(ax)\right)}{a^6} \\ &= \frac{\text{Subst}\left(\int \frac{\sin(6x)}{x} dx, x, \sin^{-1}(ax)\right)}{32a^6} - \frac{\text{Subst}\left(\int \frac{\sin(4x)}{x} dx, x, \sin^{-1}(ax)\right)}{8a^6} + \frac{5\text{Subst}\left(\int \frac{\sin(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{32a^6} \\ &= \frac{5\text{Si}(2\sin^{-1}(ax))}{32a^6} - \frac{\text{Si}(4\sin^{-1}(ax))}{8a^6} + \frac{\text{Si}(6\sin^{-1}(ax))}{32a^6} \end{aligned}$$

Mathematica [A] time = 0.115433, size = 33, normalized size = 0.77

$$\frac{5\text{Si}\left(2\sin^{-1}(ax)\right) - 4\text{Si}\left(4\sin^{-1}(ax)\right) + \text{Si}\left(6\sin^{-1}(ax)\right)}{32a^6}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/ArcSin[a*x], x]

[Out] (5*SinIntegral[2*ArcSin[a*x]] - 4*SinIntegral[4*ArcSin[a*x]] + SinIntegral[6*ArcSin[a*x]])/(32*a^6)

Maple [A] time = 0.031, size = 33, normalized size = 0.8

$$\frac{1}{a^6} \left(\frac{5 \text{Si}(2 \arcsin(ax))}{32} - \frac{\text{Si}(4 \arcsin(ax))}{8} + \frac{\text{Si}(6 \arcsin(ax))}{32} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/arcsin(a*x), x)

[Out] 1/a^6*(5/32*Si(2*arcsin(a*x))-1/8*Si(4*arcsin(a*x))+1/32*Si(6*arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^5}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x), x, algorithm="maxima")

[Out] integrate(x^5/arcsin(a*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^5}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x), x, algorithm="fricas")

[Out] integral(x^5/arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^5}{\text{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/asin(a*x),x)

[Out] Integral(x**5/asin(a*x), x)

Giac [A] time = 1.27541, size = 50, normalized size = 1.16

$$\frac{\text{Si}(6 \arcsin(ax))}{32 a^6} - \frac{\text{Si}(4 \arcsin(ax))}{8 a^6} + \frac{5 \text{Si}(2 \arcsin(ax))}{32 a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x),x, algorithm="giac")

[Out] 1/32*sin_integral(6*arcsin(a*x))/a^6 - 1/8*sin_integral(4*arcsin(a*x))/a^6 + 5/32*sin_integral(2*arcsin(a*x))/a^6

$$3.44 \quad \int \frac{x^4}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=41

$$\frac{\text{CosIntegral}(\sin^{-1}(ax))}{8a^5} - \frac{3\text{CosIntegral}(3\sin^{-1}(ax))}{16a^5} + \frac{\text{CosIntegral}(5\sin^{-1}(ax))}{16a^5}$$

[Out] CosIntegral[ArcSin[a*x]]/(8*a^5) - (3*CosIntegral[3*ArcSin[a*x]])/(16*a^5)
+ CosIntegral[5*ArcSin[a*x]]/(16*a^5)

Rubi [A] time = 0.080892, antiderivative size = 41, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4635, 4406, 3302}

$$\frac{\text{CosIntegral}(\sin^{-1}(ax))}{8a^5} - \frac{3\text{CosIntegral}(3\sin^{-1}(ax))}{16a^5} + \frac{\text{CosIntegral}(5\sin^{-1}(ax))}{16a^5}$$

Antiderivative was successfully verified.

[In] Int[x^4/ArcSin[a*x],x]

[Out] CosIntegral[ArcSin[a*x]]/(8*a^5) - (3*CosIntegral[3*ArcSin[a*x]])/(16*a^5)
+ CosIntegral[5*ArcSin[a*x]]/(16*a^5)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)^m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \frac{x^4}{\sin^{-1}(ax)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^4(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^5} \\
&= \frac{\text{Subst}\left(\int \left(\frac{\cos(x)}{8x} - \frac{3\cos(3x)}{16x} + \frac{\cos(5x)}{16x}\right) dx, x, \sin^{-1}(ax)\right)}{a^5} \\
&= \frac{\text{Subst}\left(\int \frac{\cos(5x)}{x} dx, x, \sin^{-1}(ax)\right)}{16a^5} + \frac{\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{8a^5} - \frac{3\text{Subst}\left(\int \frac{\cos(3x)}{x} dx, x, \sin^{-1}(ax)\right)}{16a^5} \\
&= \frac{\text{Ci}\left(\sin^{-1}(ax)\right)}{8a^5} - \frac{3\text{Ci}\left(3\sin^{-1}(ax)\right)}{16a^5} + \frac{\text{Ci}\left(5\sin^{-1}(ax)\right)}{16a^5}
\end{aligned}$$

Mathematica [A] time = 0.0092898, size = 31, normalized size = 0.76

$$\frac{2\text{CosIntegral}\left(\sin^{-1}(ax)\right) - 3\text{CosIntegral}\left(3\sin^{-1}(ax)\right) + \text{CosIntegral}\left(5\sin^{-1}(ax)\right)}{16a^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/ArcSin[a*x],x]

[Out] (2*CosIntegral[ArcSin[a*x]] - 3*CosIntegral[3*ArcSin[a*x]] + CosIntegral[5*ArcSin[a*x]])/(16*a^5)

Maple [A] time = 0.023, size = 31, normalized size = 0.8

$$\frac{1}{a^5} \left(\frac{\text{Ci}(\arcsin(ax))}{8} - \frac{3\text{Ci}(3\arcsin(ax))}{16} + \frac{\text{Ci}(5\arcsin(ax))}{16} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x),x)

[Out] 1/a^5*(1/8*Ci(arcsin(a*x))-3/16*Ci(3*arcsin(a*x))+1/16*Ci(5*arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(x^4/arcsin(a*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^4}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x),x, algorithm="fricas")

[Out] integral(x^4/arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\operatorname{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/asin(a*x),x)

[Out] Integral(x**4/asin(a*x), x)

Giac [A] time = 1.3525, size = 47, normalized size = 1.15

$$\frac{\operatorname{Ci}(5 \operatorname{arcsin}(ax))}{16 a^5} - \frac{3 \operatorname{Ci}(3 \operatorname{arcsin}(ax))}{16 a^5} + \frac{\operatorname{Ci}(\operatorname{arcsin}(ax))}{8 a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x),x, algorithm="giac")

[Out] 1/16*cos_integral(5*arcsin(a*x))/a^5 - 3/16*cos_integral(3*arcsin(a*x))/a^5 + 1/8*cos_integral(arcsin(a*x))/a^5

$$3.45 \quad \int \frac{x^3}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=29

$$\frac{\text{Si}\left(2 \sin^{-1}(ax)\right)}{4a^4} - \frac{\text{Si}\left(4 \sin^{-1}(ax)\right)}{8a^4}$$

[Out] SinIntegral[2*ArcSin[a*x]]/(4*a^4) - SinIntegral[4*ArcSin[a*x]]/(8*a^4)

Rubi [A] time = 0.0623942, antiderivative size = 29, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4635, 4406, 3299}

$$\frac{\text{Si}\left(2 \sin^{-1}(ax)\right)}{4a^4} - \frac{\text{Si}\left(4 \sin^{-1}(ax)\right)}{8a^4}$$

Antiderivative was successfully verified.

[In] Int[x^3/ArcSin[a*x], x]

[Out] SinIntegral[2*ArcSin[a*x]]/(4*a^4) - SinIntegral[4*ArcSin[a*x]]/(8*a^4)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_.)]^(p_.)*((c_.) + (d_.)*(x_.))^(m_.)*Sin[(a_.) + (b_.)*(x_.)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sin^{-1}(ax)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^3(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^4} \\ &= \frac{\text{Subst}\left(\int \left(\frac{\sin(2x)}{4x} - \frac{\sin(4x)}{8x}\right) dx, x, \sin^{-1}(ax)\right)}{a^4} \\ &= -\frac{\text{Subst}\left(\int \frac{\sin(4x)}{x} dx, x, \sin^{-1}(ax)\right)}{8a^4} + \frac{\text{Subst}\left(\int \frac{\sin(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{4a^4} \\ &= \frac{\text{Si}\left(2 \sin^{-1}(ax)\right)}{4a^4} - \frac{\text{Si}\left(4 \sin^{-1}(ax)\right)}{8a^4} \end{aligned}$$

Mathematica [A] time = 0.0786934, size = 24, normalized size = 0.83

$$\frac{\text{Si}\left(4 \sin^{-1}(ax)\right) - 2\text{Si}\left(2 \sin^{-1}(ax)\right)}{8a^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/ArcSin[a*x],x]

[Out] -(-2*SinIntegral[2*ArcSin[a*x]] + SinIntegral[4*ArcSin[a*x]])/(8*a^4)

Maple [A] time = 0.022, size = 24, normalized size = 0.8

$$\frac{1}{a^4} \left(\frac{\text{Si}(2 \arcsin(ax))}{4} - \frac{\text{Si}(4 \arcsin(ax))}{8} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/arcsin(a*x),x)

[Out] 1/a^4*(1/4*Si(2*arcsin(a*x))-1/8*Si(4*arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(x^3/arcsin(a*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^3}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x),x, algorithm="fricas")

[Out] integral(x^3/arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\text{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3/asin(a*x),x)
```

```
[Out] Integral(x**3/asin(a*x), x)
```

Giac [A] time = 1.33883, size = 34, normalized size = 1.17

$$-\frac{\text{Si}(4 \arcsin(ax))}{8a^4} + \frac{\text{Si}(2 \arcsin(ax))}{4a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3/arcsin(a*x),x, algorithm="giac")
```

```
[Out] -1/8*sin_integral(4*arcsin(a*x))/a^4 + 1/4*sin_integral(2*arcsin(a*x))/a^4
```

$$3.46 \quad \int \frac{x^2}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=27

$$\frac{\text{CosIntegral}(\sin^{-1}(ax))}{4a^3} - \frac{\text{CosIntegral}(3\sin^{-1}(ax))}{4a^3}$$

[Out] CosIntegral[ArcSin[a*x]]/(4*a^3) - CosIntegral[3*ArcSin[a*x]]/(4*a^3)

Rubi [A] time = 0.0631485, antiderivative size = 27, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4635, 4406, 3302}

$$\frac{\text{CosIntegral}(\sin^{-1}(ax))}{4a^3} - \frac{\text{CosIntegral}(3\sin^{-1}(ax))}{4a^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/ArcSin[a*x],x]

[Out] CosIntegral[ArcSin[a*x]]/(4*a^3) - CosIntegral[3*ArcSin[a*x]]/(4*a^3)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sin^{-1}(ax)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^2(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^3} \\ &= \frac{\text{Subst}\left(\int \left(\frac{\cos(x)}{4x} - \frac{\cos(3x)}{4x}\right) dx, x, \sin^{-1}(ax)\right)}{a^3} \\ &= \frac{\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{4a^3} - \frac{\text{Subst}\left(\int \frac{\cos(3x)}{x} dx, x, \sin^{-1}(ax)\right)}{4a^3} \\ &= \frac{\text{Ci}(\sin^{-1}(ax))}{4a^3} - \frac{\text{Ci}(3\sin^{-1}(ax))}{4a^3} \end{aligned}$$

Mathematica [A] time = 0.0060524, size = 22, normalized size = 0.81

$$\frac{\text{CosIntegral}(\sin^{-1}(ax)) - \text{CosIntegral}(3 \sin^{-1}(ax))}{4a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/ArcSin[a*x],x]

[Out] (CosIntegral[ArcSin[a*x]] - CosIntegral[3*ArcSin[a*x]])/(4*a^3)

Maple [A] time = 0.021, size = 22, normalized size = 0.8

$$\frac{1}{a^3} \left(\frac{\text{Ci}(\arcsin(ax))}{4} - \frac{\text{Ci}(3 \arcsin(ax))}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/arcsin(a*x),x)

[Out] 1/a^3*(1/4*Ci(arcsin(a*x))-1/4*Ci(3*arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(x^2/arcsin(a*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^2}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x),x, algorithm="fricas")

[Out] integral(x^2/arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\text{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2/asin(a*x),x)
```

```
[Out] Integral(x**2/asin(a*x), x)
```

Giac [A] time = 1.37149, size = 31, normalized size = 1.15

$$-\frac{\text{Ci}(3 \arcsin(ax))}{4a^3} + \frac{\text{Ci}(\arcsin(ax))}{4a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2/arcsin(a*x),x, algorithm="giac")
```

```
[Out] -1/4*cos_integral(3*arcsin(a*x))/a^3 + 1/4*cos_integral(arcsin(a*x))/a^3
```

$$3.47 \quad \int \frac{x}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=14

$$\frac{\text{Si}(2 \sin^{-1}(ax))}{2a^2}$$

[Out] SinIntegral[2*ArcSin[a*x]]/(2*a^2)

Rubi [A] time = 0.0349063, antiderivative size = 14, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4635, 4406, 12, 3299}

$$\frac{\text{Si}(2 \sin^{-1}(ax))}{2a^2}$$

Antiderivative was successfully verified.

[In] Int[x/ArcSin[a*x],x]

[Out] SinIntegral[2*ArcSin[a*x]]/(2*a^2)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_)*(x_)^(m_.), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \frac{x}{\sin^{-1}(ax)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^2} \\
&= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{2x} dx, x, \sin^{-1}(ax)\right)}{a^2} \\
&= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{2a^2} \\
&= \frac{\text{Si}\left(2 \sin^{-1}(ax)\right)}{2a^2}
\end{aligned}$$

Mathematica [A] time = 0.0226045, size = 14, normalized size = 1.

$$\frac{\text{Si}\left(2 \sin^{-1}(ax)\right)}{2a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/ArcSin[a*x],x]

[Out] SinIntegral[2*ArcSin[a*x]]/(2*a^2)

Maple [A] time = 0.025, size = 13, normalized size = 0.9

$$\frac{\text{Si}\left(2 \arcsin(ax)\right)}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/arcsin(a*x),x)

[Out] 1/2*Si(2*arcsin(a*x))/a^2

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(x/arcsin(a*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x),x, algorithm="fricas")

[Out] integral(x/arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\operatorname{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/asin(a*x),x)

[Out] Integral(x/asin(a*x), x)

Giac [A] time = 1.34604, size = 16, normalized size = 1.14

$$\frac{\operatorname{Si}(2 \operatorname{arcsin}(ax))}{2a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x),x, algorithm="giac")

[Out] 1/2*sin_integral(2*arcsin(a*x))/a^2

$$3.48 \quad \int \frac{1}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=9

$$\frac{\text{CosIntegral}(\sin^{-1}(ax))}{a}$$

[Out] CosIntegral[ArcSin[a*x]]/a

Rubi [A] time = 0.0168823, antiderivative size = 9, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4623, 3302}

$$\frac{\text{CosIntegral}(\sin^{-1}(ax))}{a}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^(-1),x]

[Out] CosIntegral[ArcSin[a*x]]/a

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_, x_Symbol] :> Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sin^{-1}(ax)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a} \\ &= \frac{\text{Ci}(\sin^{-1}(ax))}{a} \end{aligned}$$

Mathematica [A] time = 0.0094762, size = 9, normalized size = 1.

$$\frac{\text{CosIntegral}(\sin^{-1}(ax))}{a}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^(-1),x]

[Out] CosIntegral[ArcSin[a*x]]/a

Maple [A] time = 0.017, size = 10, normalized size = 1.1

$$\frac{\text{Ci}(\arcsin(ax))}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x),x)

[Out] Ci(arcsin(a*x))/a

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(1/arcsin(a*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x),x, algorithm="fricas")

[Out] integral(1/arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\text{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/asin(a*x),x)

[Out] Integral(1/asin(a*x), x)

Giac [A] time = 1.35593, size = 12, normalized size = 1.33

$$\frac{\text{Ci}(\arcsin(ax))}{a}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/arcsin(a*x),x, algorithm="giac")
```

```
[Out] cos_integral(arcsin(a*x))/a
```

$$3.49 \quad \int \frac{1}{x \sin^{-1}(ax)} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x \sin^{-1}(ax)}, x\right)$$

[Out] Unintegrable[1/(x*ArcSin[a*x]), x]

Rubi [A] time = 0.0131449, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x \sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*ArcSin[a*x]),x]

[Out] Defer[Int][1/(x*ArcSin[a*x]), x]

Rubi steps

$$\int \frac{1}{x \sin^{-1}(ax)} dx = \int \frac{1}{x \sin^{-1}(ax)} dx$$

Mathematica [A] time = 0.19103, size = 0, normalized size = 0.

$$\int \frac{1}{x \sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*ArcSin[a*x]),x]

[Out] Integrate[1/(x*ArcSin[a*x]), x]

Maple [A] time = 0.09, size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x),x)

[Out] int(1/x/arcsin(a*x),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(1/(x*arcsin(a*x)), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x \arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x),x, algorithm="fricas")

[Out] integral(1/(x*arcsin(a*x)), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/asin(a*x),x)

[Out] Integral(1/(x*asin(a*x)), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x),x, algorithm="giac")

[Out] integrate(1/(x*arcsin(a*x)), x)

$$3.50 \quad \int \frac{1}{x^2 \sin^{-1}(ax)} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x^2 \sin^{-1}(ax)}, x\right)$$

[Out] Unintegrable[1/(x^2*ArcSin[a*x]), x]

Rubi [A] time = 0.0141847, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2 \sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*ArcSin[a*x]),x]

[Out] Defer[Int][1/(x^2*ArcSin[a*x]), x]

Rubi steps

$$\int \frac{1}{x^2 \sin^{-1}(ax)} dx = \int \frac{1}{x^2 \sin^{-1}(ax)} dx$$

Mathematica [A] time = 1.0984, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*ArcSin[a*x]),x]

[Out] Integrate[1/(x^2*ArcSin[a*x]), x]

Maple [A] time = 0.123, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/arcsin(a*x),x)

[Out] int(1/x^2/arcsin(a*x),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x),x, algorithm="maxima")

[Out] integrate(1/(x^2*arcsin(a*x)), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x^2 \arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x),x, algorithm="fricas")

[Out] integral(1/(x^2*arcsin(a*x)), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/asin(a*x),x)

[Out] Integral(1/(x**2*asin(a*x)), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x),x, algorithm="giac")

[Out] integrate(1/(x^2*arcsin(a*x)), x)

$$3.51 \quad \int \frac{x^6}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=83

$$-\frac{5\text{Si}(\sin^{-1}(ax))}{64a^7} + \frac{27\text{Si}(3\sin^{-1}(ax))}{64a^7} - \frac{25\text{Si}(5\sin^{-1}(ax))}{64a^7} + \frac{7\text{Si}(7\sin^{-1}(ax))}{64a^7} - \frac{x^6\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

[Out] $-\left(\frac{x^6\sqrt{1-a^2x^2}}{a\text{ArcSin}[ax]}\right) - \left(\frac{5\text{SinIntegral}[\text{ArcSin}[ax]]}{64a^7} + \frac{27\text{SinIntegral}[3\text{ArcSin}[ax]]}{64a^7} - \frac{25\text{SinIntegral}[5\text{ArcSin}[ax]]}{64a^7} + \frac{7\text{SinIntegral}[7\text{ArcSin}[ax]]}{64a^7}\right) - \frac{x^6\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$

Rubi [A] time = 0.0744056, antiderivative size = 83, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 2, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.2$, Rules used = {4631, 3299}

$$-\frac{5\text{Si}(\sin^{-1}(ax))}{64a^7} + \frac{27\text{Si}(3\sin^{-1}(ax))}{64a^7} - \frac{25\text{Si}(5\sin^{-1}(ax))}{64a^7} + \frac{7\text{Si}(7\sin^{-1}(ax))}{64a^7} - \frac{x^6\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^6/ArcSin[a*x]^2,x]

[Out] $-\left(\frac{x^6\sqrt{1-a^2x^2}}{a\text{ArcSin}[ax]}\right) - \left(\frac{5\text{SinIntegral}[\text{ArcSin}[ax]]}{64a^7} + \frac{27\text{SinIntegral}[3\text{ArcSin}[ax]]}{64a^7} - \frac{25\text{SinIntegral}[5\text{ArcSin}[ax]]}{64a^7} + \frac{7\text{SinIntegral}[7\text{ArcSin}[ax]]}{64a^7}\right) - \frac{x^6\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^(n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^6}{\sin^{-1}(ax)^2} dx &= -\frac{x^6\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int\left(-\frac{5\sin(x)}{64x} + \frac{27\sin(3x)}{64x} - \frac{25\sin(5x)}{64x} + \frac{7\sin(7x)}{64x}\right) dx, x, \sin^{-1}(ax)\right)}{a^7} \\ &= -\frac{x^6\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} - \frac{5\text{Subst}\left(\int\frac{\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{64a^7} + \frac{7\text{Subst}\left(\int\frac{\sin(7x)}{x} dx, x, \sin^{-1}(ax)\right)}{64a^7} - \frac{25\text{Subst}\left(\int\frac{\sin(5x)}{x} dx, x, \sin^{-1}(ax)\right)}{64a^7} \\ &= -\frac{x^6\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} - \frac{5\text{Si}(\sin^{-1}(ax))}{64a^7} + \frac{27\text{Si}(3\sin^{-1}(ax))}{64a^7} - \frac{25\text{Si}(5\sin^{-1}(ax))}{64a^7} + \frac{7\text{Si}(7\sin^{-1}(ax))}{64a^7} \end{aligned}$$

Mathematica [A] time = 0.244355, size = 86, normalized size = 1.04

$$-\frac{64a^6x^6\sqrt{1-a^2x^2} + 5\sin^{-1}(ax)\text{Si}(\sin^{-1}(ax)) - 27\sin^{-1}(ax)\text{Si}(3\sin^{-1}(ax)) + 25\sin^{-1}(ax)\text{Si}(5\sin^{-1}(ax)) - 7\sin^{-1}(ax)\text{Si}(7\sin^{-1}(ax))}{64a^7\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Integrate[x^6/ArcSin[a*x]^2,x]

[Out] $-(64a^6x^6\sqrt{1-a^2x^2} + 5\text{ArcSin}[a*x]*\text{SinIntegral}[\text{ArcSin}[a*x]] - 27\text{ArcSin}[a*x]*\text{SinIntegral}[3\text{ArcSin}[a*x]] + 25\text{ArcSin}[a*x]*\text{SinIntegral}[5\text{ArcSin}[a*x]] - 7\text{ArcSin}[a*x]*\text{SinIntegral}[7\text{ArcSin}[a*x]])/(64a^7\text{ArcSin}[a*x])$

Maple [A] time = 0.042, size = 105, normalized size = 1.3

$\frac{1}{a^7} \left(-\frac{5}{64 \arcsin(ax)} \sqrt{-a^2x^2 + 1} - \frac{5 \text{Si}(\arcsin(ax))}{64} + \frac{9 \cos(3 \arcsin(ax))}{64 \arcsin(ax)} + \frac{27 \text{Si}(3 \arcsin(ax))}{64} - \frac{5 \cos(5 \arcsin(ax))}{64 \arcsin(ax)} - \frac{25 \text{Si}(5 \arcsin(ax))}{64} + \frac{7 \cos(7 \arcsin(ax))}{64 \arcsin(ax)} + \frac{7 \text{Si}(7 \arcsin(ax))}{64} \right)$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/arcsin(a*x)^2,x)

[Out] $1/a^7*(-5/64/\arcsin(a*x)*(-a^2*x^2+1)^{(1/2)}-5/64*\text{Si}(\arcsin(a*x))+9/64/\arcsin(a*x)*\cos(3*\arcsin(a*x))+27/64*\text{Si}(3*\arcsin(a*x))-5/64/\arcsin(a*x)*\cos(5*\arcsin(a*x))-25/64*\text{Si}(5*\arcsin(a*x))+1/64/\arcsin(a*x)*\cos(7*\arcsin(a*x))+7/64*\text{Si}(7*\arcsin(a*x)))$

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$\text{integral}\left(\frac{x^6}{\arcsin(ax)^2}, x\right)$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral(x^6/arcsin(a*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$\int \frac{x^6}{\arcsin^2(ax)} dx$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6/asin(a*x)**2,x)

[Out] Integral(x**6/asin(a*x)**2, x)

Giac [B] time = 1.28651, size = 217, normalized size = 2.61

$$-\frac{(a^2x^2 - 1)^3 \sqrt{-a^2x^2 + 1}}{a^7 \arcsin(ax)} - \frac{3(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1}}{a^7 \arcsin(ax)} + \frac{7 \operatorname{Si}(7 \arcsin(ax))}{64 a^7} - \frac{25 \operatorname{Si}(5 \arcsin(ax))}{64 a^7} + \frac{27 \operatorname{Si}(3 \arcsin(ax))}{64 a^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x)^2,x, algorithm="giac")

[Out] $-(a^2x^2 - 1)^3 \sqrt{-a^2x^2 + 1} / (a^7 \arcsin(a*x)) - 3(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1} / (a^7 \arcsin(a*x)) + 7/64 \operatorname{sin_integral}(7 \arcsin(a*x)) / a^7 - 25/64 \operatorname{sin_integral}(5 \arcsin(a*x)) / a^7 + 27/64 \operatorname{sin_integral}(3 \arcsin(a*x)) / a^7 - 5/64 \operatorname{sin_integral}(\arcsin(a*x)) / a^7 + 3(-a^2x^2 + 1)^{3/2} / (a^7 \arcsin(a*x)) - \sqrt{-a^2x^2 + 1} / (a^7 \arcsin(a*x))$

$$3.52 \quad \int \frac{x^5}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=71

$$\frac{5\text{CosIntegral}(2\sin^{-1}(ax))}{16a^6} - \frac{\text{CosIntegral}(4\sin^{-1}(ax))}{2a^6} + \frac{3\text{CosIntegral}(6\sin^{-1}(ax))}{16a^6} - \frac{x^5\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

[Out] -((x^5*sqrt[1 - a^2*x^2])/(a*ArcSin[a*x])) + (5*CosIntegral[2*ArcSin[a*x]])/(16*a^6) - CosIntegral[4*ArcSin[a*x]]/(2*a^6) + (3*CosIntegral[6*ArcSin[a*x]])/(16*a^6)

Rubi [A] time = 0.0634923, antiderivative size = 71, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 2, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.2$, Rules used = {4631, 3302}

$$\frac{5\text{CosIntegral}(2\sin^{-1}(ax))}{16a^6} - \frac{\text{CosIntegral}(4\sin^{-1}(ax))}{2a^6} + \frac{3\text{CosIntegral}(6\sin^{-1}(ax))}{16a^6} - \frac{x^5\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^5/ArcSin[a*x]^2,x]

[Out] -((x^5*sqrt[1 - a^2*x^2])/(a*ArcSin[a*x])) + (5*CosIntegral[2*ArcSin[a*x]])/(16*a^6) - CosIntegral[4*ArcSin[a*x]]/(2*a^6) + (3*CosIntegral[6*ArcSin[a*x]])/(16*a^6)

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^5}{\sin^{-1}(ax)^2} dx &= -\frac{x^5\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int\left(\frac{5\cos(2x)}{16x} - \frac{\cos(4x)}{2x} + \frac{3\cos(6x)}{16x}\right) dx, x, \sin^{-1}(ax)\right)}{a^6} \\ &= -\frac{x^5\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} + \frac{3\text{Subst}\left(\int\frac{\cos(6x)}{x} dx, x, \sin^{-1}(ax)\right)}{16a^6} + \frac{5\text{Subst}\left(\int\frac{\cos(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{16a^6} - \frac{\text{Subst}\left(\int\frac{\cos(4x)}{x} dx, x, \sin^{-1}(ax)\right)}{2a^6} \\ &= -\frac{x^5\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} + \frac{5\text{Ci}(2\sin^{-1}(ax))}{16a^6} - \frac{\text{Ci}(4\sin^{-1}(ax))}{2a^6} + \frac{3\text{Ci}(6\sin^{-1}(ax))}{16a^6} \end{aligned}$$

Mathematica [A] time = 0.0445183, size = 78, normalized size = 1.1

$$\frac{-10 \sin^{-1}(ax) \operatorname{CosIntegral}\left(2 \sin^{-1}(ax)\right) + 16 \sin^{-1}(ax) \operatorname{CosIntegral}\left(4 \sin^{-1}(ax)\right) - 6 \sin^{-1}(ax) \operatorname{CosIntegral}\left(6 \sin^{-1}(ax)\right)}{32a^6 \sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Integrate[x^5/ArcSin[a*x]^2,x]

[Out] $-(10 \operatorname{ArcSin}[a*x] \operatorname{CosIntegral}[2 \operatorname{ArcSin}[a*x]] + 16 \operatorname{ArcSin}[a*x] \operatorname{CosIntegral}[4 \operatorname{ArcSin}[a*x]] - 6 \operatorname{ArcSin}[a*x] \operatorname{CosIntegral}[6 \operatorname{ArcSin}[a*x]] + 5 \operatorname{Sin}[2 \operatorname{ArcSin}[a*x]] - 4 \operatorname{Sin}[4 \operatorname{ArcSin}[a*x]] + \operatorname{Sin}[6 \operatorname{ArcSin}[a*x]]) / (32 a^6 \operatorname{ArcSin}[a*x])$

Maple [A] time = 0.033, size = 78, normalized size = 1.1

$$\frac{1}{a^6} \left(-\frac{5 \sin(2 \arcsin(ax))}{32 \arcsin(ax)} + \frac{5 \operatorname{Ci}(2 \arcsin(ax))}{16} + \frac{\sin(4 \arcsin(ax))}{8 \arcsin(ax)} - \frac{\operatorname{Ci}(4 \arcsin(ax))}{2} - \frac{\sin(6 \arcsin(ax))}{32 \arcsin(ax)} + \frac{3 \operatorname{Ci}(6 \arcsin(ax))}{16} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/arcsin(a*x)^2,x)

[Out] $1/a^6 * (-5/32/\arcsin(a*x) * \sin(2*\arcsin(a*x)) + 5/16*\operatorname{Ci}(2*\arcsin(a*x)) + 1/8/\arcsin(a*x) * \sin(4*\arcsin(a*x)) - 1/2*\operatorname{Ci}(4*\arcsin(a*x)) - 1/32/\arcsin(a*x) * \sin(6*\arcsin(a*x)) + 3/16*\operatorname{Ci}(6*\arcsin(a*x)))$

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{x^5}{\arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral(x^5/arcsin(a*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^5}{\operatorname{asin}^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/asin(a*x)**2,x)

[Out] Integral(x**5/asin(a*x)**2, x)

Giac [A] time = 1.31122, size = 162, normalized size = 2.28

$$\frac{(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1}x}{a^5 \arcsin(ax)} + \frac{2(-a^2x^2 + 1)^{\frac{3}{2}}x}{a^5 \arcsin(ax)} - \frac{\sqrt{-a^2x^2 + 1}x}{a^5 \arcsin(ax)} + \frac{3 \operatorname{Ci}(6 \arcsin(ax))}{16a^6} - \frac{\operatorname{Ci}(4 \arcsin(ax))}{2a^6} + \frac{5 \operatorname{Ci}(2 \arcsin(ax))}{a^6}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x)^2,x, algorithm="giac")

[Out] $-(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1}x / (a^5 \arcsin(a*x)) + 2(-a^2x^2 + 1)^{3/2}x / (a^5 \arcsin(a*x)) - \sqrt{-a^2x^2 + 1}x / (a^5 \arcsin(a*x)) + 3/16 * \operatorname{cos_integral}(6 * \arcsin(a*x)) / a^6 - 1/2 * \operatorname{cos_integral}(4 * \arcsin(a*x)) / a^6 + 5/16 * \operatorname{cos_integral}(2 * \arcsin(a*x)) / a^6$

$$3.53 \quad \int \frac{x^4}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=69

$$-\frac{\text{Si}(\sin^{-1}(ax))}{8a^5} + \frac{9\text{Si}(3\sin^{-1}(ax))}{16a^5} - \frac{5\text{Si}(5\sin^{-1}(ax))}{16a^5} - \frac{x^4\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

[Out] $-\left(\frac{x^4\sqrt{1-a^2x^2}}{a\text{ArcSin}[ax]}\right) - \frac{\text{SinIntegral}[\text{ArcSin}[ax]]}{(8a^5)} + \frac{(9\text{SinIntegral}[3\text{ArcSin}[ax]])}{(16a^5)} - \frac{(5\text{SinIntegral}[5\text{ArcSin}[ax]])}{(16a^5)}$

Rubi [A] time = 0.0576204, antiderivative size = 69, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 2, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.2$, Rules used = {4631, 3299}

$$-\frac{\text{Si}(\sin^{-1}(ax))}{8a^5} + \frac{9\text{Si}(3\sin^{-1}(ax))}{16a^5} - \frac{5\text{Si}(5\sin^{-1}(ax))}{16a^5} - \frac{x^4\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^4/ArcSin[a*x]^2,x]

[Out] $-\left(\frac{x^4\sqrt{1-a^2x^2}}{a\text{ArcSin}[ax]}\right) - \frac{\text{SinIntegral}[\text{ArcSin}[ax]]}{(8a^5)} + \frac{(9\text{SinIntegral}[3\text{ArcSin}[ax]])}{(16a^5)} - \frac{(5\text{SinIntegral}[5\text{ArcSin}[ax]])}{(16a^5)}$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] :> Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^4}{\sin^{-1}(ax)^2} dx &= -\frac{x^4\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int\left(-\frac{\sin(x)}{8x} + \frac{9\sin(3x)}{16x} - \frac{5\sin(5x)}{16x}\right) dx, x, \sin^{-1}(ax)\right)}{a^5} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int\frac{\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{8a^5} - \frac{5\text{Subst}\left(\int\frac{\sin(5x)}{x} dx, x, \sin^{-1}(ax)\right)}{16a^5} + \frac{9\text{Subst}\left(\int\frac{\sin(3x)}{x} dx, x, \sin^{-1}(ax)\right)}{16a^5} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} - \frac{\text{Si}(\sin^{-1}(ax))}{8a^5} + \frac{9\text{Si}(3\sin^{-1}(ax))}{16a^5} - \frac{5\text{Si}(5\sin^{-1}(ax))}{16a^5} \end{aligned}$$

Mathematica [A] time = 0.208683, size = 61, normalized size = 0.88

$$-\frac{16a^4x^4\sqrt{1-a^2x^2}}{\sin^{-1}(ax)} + \frac{2\text{Si}(\sin^{-1}(ax)) - 9\text{Si}(3\sin^{-1}(ax)) + 5\text{Si}(5\sin^{-1}(ax))}{16a^5}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/ArcSin[a*x]^2,x]

[Out] $-\left(\frac{16a^4x^4\sqrt{1-a^2x^2}}{\text{ArcSin}[a*x]} + 2\text{SinIntegral}[\text{ArcSin}[a*x]] - 9\text{SinIntegral}[3\text{ArcSin}[a*x]] + 5\text{SinIntegral}[5\text{ArcSin}[a*x]]\right)/(16a^5)$

Maple [A] time = 0.026, size = 81, normalized size = 1.2

$$\frac{1}{a^5} \left(-\frac{1}{8 \arcsin(ax)} \sqrt{-a^2x^2 + 1} - \frac{\text{Si}(\arcsin(ax))}{8} + \frac{3 \cos(3 \arcsin(ax))}{16 \arcsin(ax)} + \frac{9 \text{Si}(3 \arcsin(ax))}{16} - \frac{\cos(5 \arcsin(ax))}{16 \arcsin(ax)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x)^2,x)

[Out] $1/a^5*(-1/8/\arcsin(a*x)*(-a^2*x^2+1)^{(1/2)}-1/8*\text{Si}(\arcsin(a*x))+3/16/\arcsin(a*x)*\cos(3*\arcsin(a*x))+9/16*\text{Si}(3*\arcsin(a*x))-1/16/\arcsin(a*x)*\cos(5*\arcsin(a*x))-5/16*\text{Si}(5*\arcsin(a*x)))$

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^4}{\arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral(x^4/arcsin(a*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\text{asin}^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/asin(a*x)**2,x)

[Out] Integral(x**4/asin(a*x)**2, x)

Giac [A] time = 1.30518, size = 155, normalized size = 2.25

$$-\frac{(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1}}{a^5 \arcsin(ax)} - \frac{5 \operatorname{Si}(5 \arcsin(ax))}{16 a^5} + \frac{9 \operatorname{Si}(3 \arcsin(ax))}{16 a^5} - \frac{\operatorname{Si}(\arcsin(ax))}{8 a^5} + \frac{2(-a^2x^2 + 1)^{\frac{3}{2}}}{a^5 \arcsin(ax)} - \frac{\sqrt{-a^2x^2 + 1}}{a^5 \arcsin(ax)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^2,x, algorithm="giac")

[Out] $-(a^2x^2 - 1)^2 \sqrt{-a^2x^2 + 1} / (a^5 \arcsin(a*x)) - 5/16 \sin_integral(5 \arcsin(a*x)) / a^5 + 9/16 \sin_integral(3 \arcsin(a*x)) / a^5 - 1/8 \sin_integral(\arcsin(a*x)) / a^5 + 2(-a^2x^2 + 1)^{3/2} / (a^5 \arcsin(a*x)) - \sqrt{-a^2x^2 + 1} / (a^5 \arcsin(a*x))$

$$3.54 \quad \int \frac{x^3}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=57

$$\frac{\text{CosIntegral}(2 \sin^{-1}(ax))}{2a^4} - \frac{\text{CosIntegral}(4 \sin^{-1}(ax))}{2a^4} - \frac{x^3 \sqrt{1-a^2x^2}}{a \sin^{-1}(ax)}$$

[Out] $-\left(\frac{x^3 \sqrt{1-a^2x^2}}{a \text{ArcSin}[ax]}\right) + \frac{\text{CosIntegral}[2 \text{ArcSin}[ax]]}{2a^4} - \frac{\text{CosIntegral}[4 \text{ArcSin}[ax]]}{2a^4}$

Rubi [A] time = 0.0486051, antiderivative size = 57, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 2, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.2$, Rules used = {4631, 3302}

$$\frac{\text{CosIntegral}(2 \sin^{-1}(ax))}{2a^4} - \frac{\text{CosIntegral}(4 \sin^{-1}(ax))}{2a^4} - \frac{x^3 \sqrt{1-a^2x^2}}{a \sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^3/ArcSin[a*x]^2,x]

[Out] $-\left(\frac{x^3 \sqrt{1-a^2x^2}}{a \text{ArcSin}[ax]}\right) + \frac{\text{CosIntegral}[2 \text{ArcSin}[ax]]}{2a^4} - \frac{\text{CosIntegral}[4 \text{ArcSin}[ax]]}{2a^4}$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sin^{-1}(ax)^2} dx &= -\frac{x^3 \sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \left(\frac{\cos(2x)}{2x} - \frac{\cos(4x)}{2x}\right) dx, x, \sin^{-1}(ax)\right)}{a^4} \\ &= -\frac{x^3 \sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\cos(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{2a^4} - \frac{\text{Subst}\left(\int \frac{\cos(4x)}{x} dx, x, \sin^{-1}(ax)\right)}{2a^4} \\ &= -\frac{x^3 \sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} + \frac{\text{Ci}(2 \sin^{-1}(ax))}{2a^4} - \frac{\text{Ci}(4 \sin^{-1}(ax))}{2a^4} \end{aligned}$$

Mathematica [A] time = 0.0168856, size = 56, normalized size = 0.98

$$\frac{4 \sin^{-1}(ax) \text{CosIntegral}(2 \sin^{-1}(ax)) - 4 \sin^{-1}(ax) \text{CosIntegral}(4 \sin^{-1}(ax)) - 2 \sin(2 \sin^{-1}(ax)) + \sin(4 \sin^{-1}(ax))}{8a^4 \sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/ArcSin[a*x]^2,x]

[Out] (4*ArcSin[a*x]*CosIntegral[2*ArcSin[a*x]] - 4*ArcSin[a*x]*CosIntegral[4*ArcSin[a*x]] - 2*Sin[2*ArcSin[a*x]] + Sin[4*ArcSin[a*x]])/(8*a^4*ArcSin[a*x])

Maple [A] time = 0.021, size = 54, normalized size = 1.

$$\frac{1}{a^4} \left(-\frac{\sin(2 \arcsin(ax))}{4 \arcsin(ax)} + \frac{\text{Ci}(2 \arcsin(ax))}{2} + \frac{\sin(4 \arcsin(ax))}{8 \arcsin(ax)} - \frac{\text{Ci}(4 \arcsin(ax))}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/arcsin(a*x)^2,x)

[Out] 1/a^4*(-1/4/arcsin(a*x)*sin(2*arcsin(a*x))+1/2*Ci(2*arcsin(a*x))+1/8/arcsin(a*x)*sin(4*arcsin(a*x))-1/2*Ci(4*arcsin(a*x)))

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^3}{\arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral(x^3/arcsin(a*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\text{asin}^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/asin(a*x)**2,x)

[Out] Integral(x**3/asin(a*x)**2, x)

Giac [A] time = 1.38474, size = 97, normalized size = 1.7

$$\frac{(-a^2x^2 + 1)^{\frac{3}{2}}x}{a^3 \arcsin(ax)} - \frac{\sqrt{-a^2x^2 + 1}x}{a^3 \arcsin(ax)} - \frac{\text{Ci}(4 \arcsin(ax))}{2a^4} + \frac{\text{Ci}(2 \arcsin(ax))}{2a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^2,x, algorithm="giac")

[Out] $(-a^2x^2 + 1)^{(3/2)}x/(a^3\arcsin(a*x)) - \text{sqrt}(-a^2x^2 + 1)x/(a^3\arcsin(a*x)) - 1/2*\text{cos_integral}(4*\arcsin(a*x))/a^4 + 1/2*\text{cos_integral}(2*\arcsin(a*x))/a^4$

$$3.55 \quad \int \frac{x^2}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=55

$$-\frac{\text{Si}(\sin^{-1}(ax))}{4a^3} + \frac{3\text{Si}(3\sin^{-1}(ax))}{4a^3} - \frac{x^2\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

[Out] $-\left(\frac{x^2\sqrt{1-a^2x^2}}{a\text{ArcSin}[ax]}\right) - \frac{\text{SinIntegral}[\text{ArcSin}[ax]]}{4a^3} + \frac{3\text{SinIntegral}[3\text{ArcSin}[ax]]}{4a^3}$

Rubi [A] time = 0.0439644, antiderivative size = 55, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 2, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.2$, Rules used = {4631, 3299}

$$-\frac{\text{Si}(\sin^{-1}(ax))}{4a^3} + \frac{3\text{Si}(3\sin^{-1}(ax))}{4a^3} - \frac{x^2\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^2/ArcSin[a*x]^2,x]

[Out] $-\left(\frac{x^2\sqrt{1-a^2x^2}}{a\text{ArcSin}[ax]}\right) - \frac{\text{SinIntegral}[\text{ArcSin}[ax]]}{4a^3} + \frac{3\text{SinIntegral}[3\text{ArcSin}[ax]]}{4a^3}$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sin^{-1}(ax)^2} dx &= -\frac{x^2\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int\left(-\frac{\sin(x)}{4x} + \frac{3\sin(3x)}{4x}\right) dx, x, \sin^{-1}(ax)\right)}{a^3} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int\frac{\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{4a^3} + \frac{3\text{Subst}\left(\int\frac{\sin(3x)}{x} dx, x, \sin^{-1}(ax)\right)}{4a^3} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{a\sin^{-1}(ax)} - \frac{\text{Si}(\sin^{-1}(ax))}{4a^3} + \frac{3\text{Si}(3\sin^{-1}(ax))}{4a^3} \end{aligned}$$

Mathematica [A] time = 0.164837, size = 50, normalized size = 0.91

$$-\frac{\frac{4a^2x^2\sqrt{1-a^2x^2}}{\sin^{-1}(ax)} + \text{Si}(\sin^{-1}(ax)) - 3\text{Si}(3\sin^{-1}(ax))}{4a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/ArcSin[a*x]^2,x]

[Out] $-\frac{(4a^2x^2\sqrt{1-a^2x^2})/\text{ArcSin}[a*x] + \text{SinIntegral}[\text{ArcSin}[a*x]] - 3*\text{SinIntegral}[3*\text{ArcSin}[a*x]]}{4a^3}$

Maple [A] time = 0.023, size = 57, normalized size = 1.

$$\frac{1}{a^3} \left(-\frac{1}{4 \arcsin(ax)} \sqrt{-a^2x^2 + 1} - \frac{\text{Si}(\arcsin(ax))}{4} + \frac{\cos(3 \arcsin(ax))}{4 \arcsin(ax)} + \frac{3 \text{Si}(3 \arcsin(ax))}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/arcsin(a*x)^2,x)

[Out] $1/a^3*(-1/4/\arcsin(a*x)*(-a^2*x^2+1)^{(1/2)}-1/4*\text{Si}(\arcsin(a*x))+1/4/\arcsin(a*x)*\cos(3*\arcsin(a*x))+3/4*\text{Si}(3*\arcsin(a*x)))$

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^2}{\arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral(x^2/arcsin(a*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\text{asin}^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/asin(a*x)**2,x)

[Out] Integral(x**2/asin(a*x)**2, x)

Giac [A] time = 1.35974, size = 92, normalized size = 1.67

$$\frac{3 \operatorname{Si}(3 \arcsin(ax))}{4a^3} - \frac{\operatorname{Si}(\arcsin(ax))}{4a^3} + \frac{(-a^2x^2 + 1)^{\frac{3}{2}}}{a^3 \arcsin(ax)} - \frac{\sqrt{-a^2x^2 + 1}}{a^3 \arcsin(ax)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^2,x, algorithm="giac")

[Out] 3/4*sin_integral(3*arcsin(a*x))/a^3 - 1/4*sin_integral(arcsin(a*x))/a^3 + (-a^2*x^2 + 1)^(3/2)/(a^3*arcsin(a*x)) - sqrt(-a^2*x^2 + 1)/(a^3*arcsin(a*x))

$$3.56 \quad \int \frac{x}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=38

$$\frac{\text{CosIntegral}(2 \sin^{-1}(ax))}{a^2} - \frac{x\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)}$$

[Out] $-\left(\frac{x\sqrt{1-a^2x^2}}{a \text{ArcSin}[a*x]}\right) + \text{CosIntegral}[2*\text{ArcSin}[a*x]]/a^2$

Rubi [A] time = 0.0247518, antiderivative size = 38, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4631, 3302}

$$\frac{\text{CosIntegral}(2 \sin^{-1}(ax))}{a^2} - \frac{x\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x/ArcSin[a*x]^2,x]

[Out] $-\left(\frac{x\sqrt{1-a^2x^2}}{a \text{ArcSin}[a*x]}\right) + \text{CosIntegral}[2*\text{ArcSin}[a*x]]/a^2$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_)*(x_)^(m_.), x_Symbol] :> Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x}{\sin^{-1}(ax)^2} dx &= -\frac{x\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\cos(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^2} \\ &= -\frac{x\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} + \frac{\text{Ci}(2 \sin^{-1}(ax))}{a^2} \end{aligned}$$

Mathematica [A] time = 0.0032364, size = 32, normalized size = 0.84

$$\frac{\text{CosIntegral}(2 \sin^{-1}(ax))}{a^2} - \frac{\sin(2 \sin^{-1}(ax))}{2a^2 \sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Integrate[x/ArcSin[a*x]^2,x]

[Out] $\text{CosIntegral}[2*\text{ArcSin}[a*x]]/a^2 - \text{Sin}[2*\text{ArcSin}[a*x]]/(2*a^2*\text{ArcSin}[a*x])$

Maple [A] time = 0.024, size = 28, normalized size = 0.7

$$\frac{1}{a^2} \left(-\frac{\sin(2 \arcsin(ax))}{2 \arcsin(ax)} + \text{Ci}(2 \arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}(x/\arcsin(a*x)^2, x)$

[Out] $1/a^2*(-1/2/\arcsin(a*x)*\sin(2*\arcsin(a*x))+\text{Ci}(2*\arcsin(a*x)))$

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x/\arcsin(a*x)^2, x, \text{algorithm}="maxima")$

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x}{\arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x/\arcsin(a*x)^2, x, \text{algorithm}="fricas")$

[Out] $\text{integral}(x/\arcsin(a*x)^2, x)$

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\text{asin}^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(x/\text{asin}(a*x)**2, x)$

[Out] $\text{Integral}(x/\text{asin}(a*x)**2, x)$

Giac [A] time = 1.37361, size = 49, normalized size = 1.29

$$-\frac{\sqrt{-a^2x^2 + 1}x}{a \arcsin(ax)} + \frac{\text{Ci}(2 \arcsin(ax))}{a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x/arcsin(a*x)^2,x, algorithm="giac")
```

```
[Out] -sqrt(-a^2*x^2 + 1)*x/(a*arcsin(a*x)) + cos_integral(2*arcsin(a*x))/a^2
```

$$3.57 \quad \int \frac{1}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=36

$$-\frac{\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} - \frac{\text{Si}(\sin^{-1}(ax))}{a}$$

[Out] -(Sqrt[1 - a^2*x^2]/(a*ArcSin[a*x])) - SinIntegral[ArcSin[a*x]]/a

Rubi [A] time = 0.0779915, antiderivative size = 36, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4621, 4723, 3299}

$$-\frac{\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} - \frac{\text{Si}(\sin^{-1}(ax))}{a}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^(-2),x]

[Out] -(Sqrt[1 - a^2*x^2]/(a*ArcSin[a*x])) - SinIntegral[ArcSin[a*x]]/a

Rule 4621

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.), x_Symbol] :> Simp[(Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + Dist[c/(b*(n + 1)), Int[(x*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && LtQ[n, -1]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)*(x_)^(m_.)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3299

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sin^{-1}(ax)^2} dx &= -\frac{\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} - a \int \frac{x}{\sqrt{1-a^2x^2} \sin^{-1}(ax)} dx \\ &= -\frac{\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a} \\ &= -\frac{\sqrt{1-a^2x^2}}{a \sin^{-1}(ax)} - \frac{\text{Si}(\sin^{-1}(ax))}{a} \end{aligned}$$

Mathematica [A] time = 0.0590502, size = 32, normalized size = 0.89

$$\frac{\frac{\sqrt{1-a^2x^2}}{\sin^{-1}(ax)} + \text{Si}(\sin^{-1}(ax))}{a}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^(-2), x]

[Out] -((Sqrt[1 - a^2*x^2]/ArcSin[a*x] + SinIntegral[ArcSin[a*x]])/a)

Maple [A] time = 0.019, size = 33, normalized size = 0.9

$$\frac{1}{a} \left(-\frac{1}{\arcsin(ax)} \sqrt{-a^2x^2 + 1} - \text{Si}(\arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x)^2, x)

[Out] 1/a*(-1/arcsin(a*x)*(-a^2*x^2+1)^(1/2)-Si(arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{a^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1}) \int \frac{\sqrt{-ax+1}x}{\sqrt{ax+1}(ax-1)\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - \sqrt{ax+1}\sqrt{-ax+1}}{a \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^2, x, algorithm="maxima")

[Out] (a^2*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))*integrate(sqrt(a*x + 1)*sqrt(-a*x + 1)*x/((a^2*x^2 - 1)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))), x) - sqrt(a*x + 1)*sqrt(-a*x + 1))/(a*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)))

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{\arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^2, x, algorithm="fricas")

[Out] integral(arcsin(a*x)^(-2), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\operatorname{asin}^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/asin(a*x)**2,x)

[Out] Integral(asin(a*x)**(-2), x)

Giac [A] time = 1.33019, size = 46, normalized size = 1.28

$$-\frac{\operatorname{Si}(\operatorname{arcsin}(ax))}{a} - \frac{\sqrt{-a^2x^2 + 1}}{a \operatorname{arcsin}(ax)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^2,x, algorithm="giac")

[Out] -sin_integral(arcsin(a*x))/a - sqrt(-a^2*x^2 + 1)/(a*arcsin(a*x))

$$3.58 \quad \int \frac{1}{x \sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x \sin^{-1}(ax)^2}, x\right)$$

[Out] Unintegrable[1/(x*ArcSin[a*x]^2), x]

Rubi [A] time = 0.0120926, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x \sin^{-1}(ax)^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*ArcSin[a*x]^2),x]

[Out] Defer[Int][1/(x*ArcSin[a*x]^2), x]

Rubi steps

$$\int \frac{1}{x \sin^{-1}(ax)^2} dx = \int \frac{1}{x \sin^{-1}(ax)^2} dx$$

Mathematica [A] time = 0.903582, size = 0, normalized size = 0.

$$\int \frac{1}{x \sin^{-1}(ax)^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*ArcSin[a*x]^2),x]

[Out] Integrate[1/(x*ArcSin[a*x]^2), x]

Maple [A] time = 0.078, size = 0, normalized size = 0.

$$\int \frac{1}{x (\arcsin(ax))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x)^2,x)

[Out] int(1/x/arcsin(a*x)^2,x)

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x \arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral(1/(x*arcsin(a*x)^2), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/asin(a*x)**2,x)

[Out] Integral(1/(x*asin(a*x)**2), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^2,x, algorithm="giac")

[Out] integrate(1/(x*arcsin(a*x)^2), x)

$$3.59 \quad \int \frac{1}{x^2 \sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x^2 \sin^{-1}(ax)^2}, x\right)$$

[Out] Unintegrable[1/(x^2*ArcSin[a*x]^2), x]

Rubi [A] time = 0.0136797, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2 \sin^{-1}(ax)^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*ArcSin[a*x]^2), x]

[Out] Defer[Int][1/(x^2*ArcSin[a*x]^2), x]

Rubi steps

$$\int \frac{1}{x^2 \sin^{-1}(ax)^2} dx = \int \frac{1}{x^2 \sin^{-1}(ax)^2} dx$$

Mathematica [A] time = 9.71136, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sin^{-1}(ax)^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*ArcSin[a*x]^2), x]

[Out] Integrate[1/(x^2*ArcSin[a*x]^2), x]

Maple [A] time = 0.141, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (\arcsin(ax))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/arcsin(a*x)^2, x)

[Out] int(1/x^2/arcsin(a*x)^2, x)

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x^2 \arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral(1/(x^2*arcsin(a*x)^2), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/asin(a*x)**2,x)

[Out] Integral(1/(x**2*asin(a*x)**2), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin(ax)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^2,x, algorithm="giac")

[Out] integrate(1/(x^2*arcsin(a*x)^2), x)

$$3.60 \quad \int \frac{x^4}{\sin^{-1}(ax)^3} dx$$

Optimal. Leaf size=98

$$-\frac{\text{CosIntegral}(\sin^{-1}(ax))}{16a^5} + \frac{27\text{CosIntegral}(3\sin^{-1}(ax))}{32a^5} - \frac{25\text{CosIntegral}(5\sin^{-1}(ax))}{32a^5} - \frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{2}{a^2\sin^{-1}(ax)}$$

[Out] $-(x^4\sqrt{1-a^2x^2})/(2a\text{ArcSin}[ax]^2) - (2x^3)/(a^2\text{ArcSin}[ax]) + (5x^5)/(2\text{ArcSin}[ax]) - \text{CosIntegral}[\text{ArcSin}[ax]]/(16a^5) + (27\text{CosIntegral}[3\text{ArcSin}[ax]])/(32a^5) - (25\text{CosIntegral}[5\text{ArcSin}[ax]])/(32a^5)$

Rubi [A] time = 0.342807, antiderivative size = 98, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4633, 4719, 4635, 4406, 3302}

$$-\frac{\text{CosIntegral}(\sin^{-1}(ax))}{16a^5} + \frac{27\text{CosIntegral}(3\sin^{-1}(ax))}{32a^5} - \frac{25\text{CosIntegral}(5\sin^{-1}(ax))}{32a^5} - \frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{2}{a^2\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^4/ArcSin[a*x]^3,x]

[Out] $-(x^4\sqrt{1-a^2x^2})/(2a\text{ArcSin}[ax]^2) - (2x^3)/(a^2\text{ArcSin}[ax]) + (5x^5)/(2\text{ArcSin}[ax]) - \text{CosIntegral}[\text{ArcSin}[ax]]/(16a^5) + (27\text{CosIntegral}[3\text{ArcSin}[ax]])/(32a^5) - (25\text{CosIntegral}[5\text{ArcSin}[ax]])/(32a^5)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)(x_)]*(b_.))^ (n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1-c^2*x^2]*(a+b*ArcSin[c*x])^(n+1))/(b*c*(n+1)), x] + (Dist[(c*(m+1))/(b*(n+1)), Int[(x^(m+1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x] - Dist[m/(b*c*(n+1)), Int[(x^(m-1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int((((a_.) + ArcSin[(c_.)(x_)]*(b_.))^ (n_.)*((f_.)(x_)^(m_.))/sqrt[(d_) + (e_.)(x_)^2], x_Symbol] := Simp[((f*x)^m*(a+b*ArcSin[c*x])^(n+1))/(b*c*sqrt[d]*(n+1)), x] - Dist[(f*m)/(b*c*sqrt[d]*(n+1)), Int[(f*x)^(m-1)*(a+b*ArcSin[c*x])^(n+1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4635

Int[((a_.) + ArcSin[(c_.)(x_)]*(b_.))^ (n_.)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m+1), Subst[Int[(a+b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)(x_)]^(p_.)*((c_.) + (d_.)(x_)^(m_.))*Sin[(a_.) + (b_.)(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c+d*x)^m, Sin[a+b*x]^n*Cos[a+b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3302

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]`

Rubi steps

$$\begin{aligned} \int \frac{x^4}{\sin^{-1}(ax)^3} dx &= -\frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} + \frac{2\int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx}{a} - \frac{1}{2}(5a) \int \frac{x^5}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{2x^3}{a^2\sin^{-1}(ax)} + \frac{5x^5}{2\sin^{-1}(ax)} - \frac{25}{2} \int \frac{x^4}{\sin^{-1}(ax)} dx + \frac{6\int \frac{x^2}{\sin^{-1}(ax)} dx}{a^2} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{2x^3}{a^2\sin^{-1}(ax)} + \frac{5x^5}{2\sin^{-1}(ax)} + \frac{6\text{Subst}\left(\int \frac{\cos(x)\sin^2(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^5} - \frac{25\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^5} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{2x^3}{a^2\sin^{-1}(ax)} + \frac{5x^5}{2\sin^{-1}(ax)} + \frac{6\text{Subst}\left(\int \left(\frac{\cos(x)}{4x} - \frac{\cos(3x)}{4x}\right) dx, x, \sin^{-1}(ax)\right)}{a^5} - \frac{25\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^5} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{2x^3}{a^2\sin^{-1}(ax)} + \frac{5x^5}{2\sin^{-1}(ax)} - \frac{25\text{Subst}\left(\int \frac{\cos(5x)}{x} dx, x, \sin^{-1}(ax)\right)}{32a^5} + \frac{3\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{32a^5} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{2x^3}{a^2\sin^{-1}(ax)} + \frac{5x^5}{2\sin^{-1}(ax)} - \frac{\text{Ci}\left(\sin^{-1}(ax)\right)}{16a^5} + \frac{27\text{Ci}\left(3\sin^{-1}(ax)\right)}{32a^5} - \frac{25\text{Ci}\left(5\sin^{-1}(ax)\right)}{32a^5} \end{aligned}$$

Mathematica [A] time = 0.184825, size = 103, normalized size = 1.05

$$\frac{16a^4x^4\sqrt{1-a^2x^2} - 80a^5x^5\sin^{-1}(ax) + 64a^3x^3\sin^{-1}(ax) + 2\sin^{-1}(ax)^2\text{CosIntegral}\left(\sin^{-1}(ax)\right) - 27\sin^{-1}(ax)^2\text{CosIntegral}\left(3\sin^{-1}(ax)\right) + 25\sin^{-1}(ax)^2\text{CosIntegral}\left(5\sin^{-1}(ax)\right)}{32a^5\sin^{-1}(ax)^2}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/ArcSin[a*x]^3,x]

[Out] $-(16a^4x^4\sqrt{1-a^2x^2} + 64a^3x^3\text{ArcSin}[a*x] - 80a^5x^5\text{ArcSin}[a*x] + 2\text{ArcSin}[a*x]^2\text{CosIntegral}[\text{ArcSin}[a*x]] - 27\text{ArcSin}[a*x]^2\text{CosIntegral}[3\text{ArcSin}[a*x]] + 25\text{ArcSin}[a*x]^2\text{CosIntegral}[5\text{ArcSin}[a*x]])/(32a^5\text{ArcSin}[a*x]^2)$

Maple [A] time = 0.042, size = 121, normalized size = 1.2

$$\frac{1}{a^5} \left(-\frac{1}{16(\arcsin(ax))^2} \sqrt{-a^2x^2+1} + \frac{ax}{16\arcsin(ax)} - \frac{\text{Ci}(\arcsin(ax))}{16} + \frac{3\cos(3\arcsin(ax))}{32(\arcsin(ax))^2} - \frac{9\sin(3\arcsin(ax))}{32\arcsin(ax)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x)^3,x)

[Out] $1/a^5*(-1/16/\arcsin(a*x)^2*(-a^2*x^2+1)^(1/2)+1/16*a*x/\arcsin(a*x)-1/16*\text{Ci}(\arcsin(a*x))+3/32/\arcsin(a*x)^2*\cos(3*\arcsin(a*x))-9/32/\arcsin(a*x)*\sin(3*\arcsin(a*x))+27/32*\text{Ci}(3*\arcsin(a*x))-1/32/\arcsin(a*x)^2*\cos(5*\arcsin(a*x))+5$

$/32/\arcsin(ax)*\sin(5*\arcsin(ax))-25/32*Ci(5*\arcsin(ax))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{\sqrt{ax+1}\sqrt{-ax+1}ax^4 + \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2 \int \frac{(25a^2x^2-12)x^2}{\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - (5a^2x^5 - 4x^3) \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})}{2a^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^3,x, algorithm="maxima")

[Out] $-1/2*(\sqrt{ax+1}*\sqrt{-ax+1}*a*x^4 + \arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})^2*\int((25*a^2*x^4 - 12*x^2)/\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})*\sqrt{-ax+1}), x) - (5*a^2*x^5 - 4*x^3)*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})/(a^2*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})^2)$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^4}{\arcsin(ax)^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^3,x, algorithm="fricas")

[Out] integral(x^4/arcsin(a*x)^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\arcsin^3(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/asin(a*x)**3,x)

[Out] Integral(x**4/asin(a*x)**3, x)

Giac [A] time = 1.3283, size = 230, normalized size = 2.35

$$\frac{5(a^2x^2-1)^2x}{2a^4\arcsin(ax)} + \frac{3(a^2x^2-1)x}{a^4\arcsin(ax)} + \frac{x}{2a^4\arcsin(ax)} - \frac{25\text{Ci}(5\arcsin(ax))}{32a^5} + \frac{27\text{Ci}(3\arcsin(ax))}{32a^5} - \frac{\text{Ci}(\arcsin(ax))}{16a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^3,x, algorithm="giac")

```
[Out] 5/2*(a^2*x^2 - 1)^2*x/(a^4*arcsin(a*x)) + 3*(a^2*x^2 - 1)*x/(a^4*arcsin(a*x)) + 1/2*x/(a^4*arcsin(a*x)) - 25/32*cos_integral(5*arcsin(a*x))/a^5 + 27/32*cos_integral(3*arcsin(a*x))/a^5 - 1/16*cos_integral(arcsin(a*x))/a^5 - 1/2*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)/(a^5*arcsin(a*x)^2) + (-a^2*x^2 + 1)^(3/2)/(a^5*arcsin(a*x)^2) - 1/2*sqrt(-a^2*x^2 + 1)/(a^5*arcsin(a*x)^2)
```

$$3.61 \quad \int \frac{x^3}{\sin^{-1}(ax)^3} dx$$

Optimal. Leaf size=83

$$-\frac{\text{Si}(2\sin^{-1}(ax))}{2a^4} + \frac{\text{Si}(4\sin^{-1}(ax))}{a^4} - \frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{3x^2}{2a^2\sin^{-1}(ax)} + \frac{2x^4}{\sin^{-1}(ax)}$$

[Out] $-(x^3\sqrt{1-a^2x^2})/(2a*\text{ArcSin}[a*x]^2) - (3*x^2)/(2*a^2*\text{ArcSin}[a*x]) + (2*x^4)/\text{ArcSin}[a*x] - \text{SinIntegral}[2*\text{ArcSin}[a*x]]/(2*a^4) + \text{SinIntegral}[4*\text{ArcSin}[a*x]]/a^4$

Rubi [A] time = 0.299843, antiderivative size = 83, normalized size of antiderivative = 1., number of steps used = 12, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4633, 4719, 4635, 4406, 3299, 12}

$$-\frac{\text{Si}(2\sin^{-1}(ax))}{2a^4} + \frac{\text{Si}(4\sin^{-1}(ax))}{a^4} - \frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{3x^2}{2a^2\sin^{-1}(ax)} + \frac{2x^4}{\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^3/ArcSin[a*x]^3,x]

[Out] $-(x^3\sqrt{1-a^2x^2})/(2*a*\text{ArcSin}[a*x]^2) - (3*x^2)/(2*a^2*\text{ArcSin}[a*x]) + (2*x^4)/\text{ArcSin}[a*x] - \text{SinIntegral}[2*\text{ArcSin}[a*x]]/(2*a^4) + \text{SinIntegral}[4*\text{ArcSin}[a*x]]/a^4$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)*(x_.)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + (Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/sqrt[1 - c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)*((f_.)*(x_.))^(m_.))/sqrt[(d_.) + (e_.)*(x_.)^2], x_Symbol] := Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)*(x_.)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_.)]^(p_.)*((c_.) + (d_.)*(x_.))^(m_.)*Sin[(a_.) + (b_.)*(x_.)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sin^{-1}(ax)^3} dx &= -\frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} + \frac{3\int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx}{2a} - (2a) \int \frac{x^4}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{3x^2}{2a^2\sin^{-1}(ax)} + \frac{2x^4}{\sin^{-1}(ax)} - 8 \int \frac{x^3}{\sin^{-1}(ax)} dx + \frac{3\int \frac{x}{\sin^{-1}(ax)} dx}{a^2} \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{3x^2}{2a^2\sin^{-1}(ax)} + \frac{2x^4}{\sin^{-1}(ax)} + \frac{3\text{Subst}\left(\int \frac{\cos(x)\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^4} - \frac{8\text{Subst}\left(\int \frac{\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^4} \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{3x^2}{2a^2\sin^{-1}(ax)} + \frac{2x^4}{\sin^{-1}(ax)} + \frac{3\text{Subst}\left(\int \frac{\sin(2x)}{2x} dx, x, \sin^{-1}(ax)\right)}{a^4} - \frac{8\text{Subst}\left(\int \frac{\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^4} \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{3x^2}{2a^2\sin^{-1}(ax)} + \frac{2x^4}{\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\sin(4x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^4} + \frac{3\text{Subst}\left(\int \frac{\sin(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{2a^4} \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{3x^2}{2a^2\sin^{-1}(ax)} + \frac{2x^4}{\sin^{-1}(ax)} - \frac{\text{Si}\left(2\sin^{-1}(ax)\right)}{2a^4} + \frac{\text{Si}\left(4\sin^{-1}(ax)\right)}{a^4} \end{aligned}$$

Mathematica [A] time = 0.186956, size = 73, normalized size = 0.88

$$\frac{\frac{a^2x^2\left((4a^2x^2-3)\sin^{-1}(ax)-ax\sqrt{1-a^2x^2}\right)}{\sin^{-1}(ax)^2} - \text{Si}\left(2\sin^{-1}(ax)\right) + 2\text{Si}\left(4\sin^{-1}(ax)\right)}{2a^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3/ArcSin[a*x]^3, x]

[Out] ((a^2*x^2*(-(a*x*Sqrt[1 - a^2*x^2]) + (-3 + 4*a^2*x^2)*ArcSin[a*x]))/ArcSin[a*x]^2 - SinIntegral[2*ArcSin[a*x]] + 2*SinIntegral[4*ArcSin[a*x]])/(2*a^4)

Maple [A] time = 0.034, size = 82, normalized size = 1.

$$\frac{1}{a^4} \left(-\frac{\sin(2 \arcsin(ax))}{8 (\arcsin(ax))^2} - \frac{\cos(2 \arcsin(ax))}{4 \arcsin(ax)} - \frac{\text{Si}(2 \arcsin(ax))}{2} + \frac{\sin(4 \arcsin(ax))}{16 (\arcsin(ax))^2} + \frac{\cos(4 \arcsin(ax))}{4 \arcsin(ax)} + \text{Si}(4 \arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/arcsin(a*x)^3, x)

[Out] $1/a^4*(-1/8/\arcsin(ax)^2*\sin(2*\arcsin(ax))-1/4/\arcsin(ax)*\cos(2*\arcsin(ax))-1/2*\text{Si}(2*\arcsin(ax))+1/16/\arcsin(ax)^2*\sin(4*\arcsin(ax))+1/4/\arcsin(ax)*\cos(4*\arcsin(ax))+\text{Si}(4*\arcsin(ax))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{\sqrt{ax+1}\sqrt{-ax+1}ax^3 + 2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2 \int \frac{(8a^2x^2-3)x}{\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - (4a^2x^4 - 3x^2) \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})}{2a^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(ax)^3,x, algorithm="maxima")

[Out] $-1/2*(\sqrt{ax+1}*\sqrt{-ax+1}*ax^3 + 2*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})^2*\int \frac{(8a^2x^3 - 3x)}{\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})} dx - (4a^2x^4 - 3x^2)*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})^2)/a^2*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})^2$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^3}{\arcsin(ax)^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(ax)^3,x, algorithm="fricas")

[Out] integral(x^3/arcsin(ax)^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\text{asin}^3(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/asin(ax)**3,x)

[Out] Integral(x**3/asin(ax)**3, x)

Giac [A] time = 1.36199, size = 169, normalized size = 2.04

$$\frac{(-a^2x^2+1)^{\frac{3}{2}}x}{2a^3 \arcsin(ax)^2} + \frac{2(a^2x^2-1)^2}{a^4 \arcsin(ax)} + \frac{\text{Si}(4 \arcsin(ax))}{a^4} - \frac{\text{Si}(2 \arcsin(ax))}{2a^4} - \frac{\sqrt{-a^2x^2+1}x}{2a^3 \arcsin(ax)^2} + \frac{5(a^2x^2-1)}{2a^4 \arcsin(ax)} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3/arcsin(a*x)^3,x, algorithm="giac")
```

```
[Out] 1/2*(-a^2*x^2 + 1)^(3/2)*x/(a^3*arcsin(a*x)^2) + 2*(a^2*x^2 - 1)^2/(a^4*arcsin(a*x)) + sin_integral(4*arcsin(a*x))/a^4 - 1/2*sin_integral(2*arcsin(a*x))/a^4 - 1/2*sqrt(-a^2*x^2 + 1)*x/(a^3*arcsin(a*x)^2) + 5/2*(a^2*x^2 - 1)/(a^4*arcsin(a*x)) + 1/2/(a^4*arcsin(a*x))
```


$$3.62 \quad \int \frac{x^2}{\sin^{-1}(ax)^3} dx$$

Optimal. Leaf size=82

$$-\frac{\text{CosIntegral}(\sin^{-1}(ax))}{8a^3} + \frac{9\text{CosIntegral}(3\sin^{-1}(ax))}{8a^3} - \frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{x}{a^2\sin^{-1}(ax)} + \frac{3x^3}{2\sin^{-1}(ax)}$$

[Out] $-(x^2\sqrt{1-a^2x^2})/(2a\text{ArcSin}[ax]^2) - x/(a^2\text{ArcSin}[ax]) + (3x^3)/(2\text{ArcSin}[ax]) - \text{CosIntegral}[\text{ArcSin}[ax]]/(8a^3) + (9\text{CosIntegral}[3\text{ArcSin}[ax]])/(8a^3)$

Rubi [A] time = 0.248665, antiderivative size = 82, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4633, 4719, 4635, 4406, 3302, 4623}

$$-\frac{\text{CosIntegral}(\sin^{-1}(ax))}{8a^3} + \frac{9\text{CosIntegral}(3\sin^{-1}(ax))}{8a^3} - \frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{x}{a^2\sin^{-1}(ax)} + \frac{3x^3}{2\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^2/ArcSin[a*x]^3,x]

[Out] $-(x^2\sqrt{1-a^2x^2})/(2a\text{ArcSin}[ax]^2) - x/(a^2\text{ArcSin}[ax]) + (3x^3)/(2\text{ArcSin}[ax]) - \text{CosIntegral}[\text{ArcSin}[ax]]/(8a^3) + (9\text{CosIntegral}[3\text{ArcSin}[ax]])/(8a^3)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + (Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/sqrt[1 - c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_)*((f_.)*(x_))^(m_.))/sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 4623

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_), x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sin^{-1}(ax)^3} dx &= -\frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} + \frac{\int \frac{x}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx}{a} - \frac{1}{2}(3a) \int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{x}{a^2\sin^{-1}(ax)} + \frac{3x^3}{2\sin^{-1}(ax)} - \frac{9}{2} \int \frac{x^2}{\sin^{-1}(ax)} dx + \frac{\int \frac{1}{\sin^{-1}(ax)} dx}{a^2} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{x}{a^2\sin^{-1}(ax)} + \frac{3x^3}{2\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^3} - \frac{9 \text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{2a^3} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{x}{a^2\sin^{-1}(ax)} + \frac{3x^3}{2\sin^{-1}(ax)} + \frac{\text{Ci}\left(\sin^{-1}(ax)\right)}{a^3} - \frac{9 \text{Subst}\left(\int \left(\frac{\cos(x)}{4x} - \frac{\cos(3x)}{4x}\right) dx, x, \sin^{-1}(ax)\right)}{2a^3} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{x}{a^2\sin^{-1}(ax)} + \frac{3x^3}{2\sin^{-1}(ax)} + \frac{\text{Ci}\left(\sin^{-1}(ax)\right)}{a^3} - \frac{9 \text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{8a^3} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{x}{a^2\sin^{-1}(ax)} + \frac{3x^3}{2\sin^{-1}(ax)} - \frac{\text{Ci}\left(\sin^{-1}(ax)\right)}{8a^3} + \frac{9\text{Ci}\left(3\sin^{-1}(ax)\right)}{8a^3} \end{aligned}$$

Mathematica [A] time = 0.135634, size = 68, normalized size = 0.83

$$\frac{\frac{4ax\left((3a^2x^2-2)\sin^{-1}(ax)-ax\sqrt{1-a^2x^2}\right)}{\sin^{-1}(ax)^2} - \text{CosIntegral}\left(\sin^{-1}(ax)\right) + 9\text{CosIntegral}\left(3\sin^{-1}(ax)\right)}{8a^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2/ArcSin[a*x]^3, x]
```

```
[Out] ((4*a*x*(-(a*x*Sqrt[1 - a^2*x^2]) + (-2 + 3*a^2*x^2)*ArcSin[a*x]))/ArcSin[a*x]^2 - CosIntegral[ArcSin[a*x]] + 9*CosIntegral[3*ArcSin[a*x]])/(8*a^3)
```

Maple [A] time = 0.026, size = 82, normalized size = 1.

$$\frac{1}{a^3} \left(-\frac{1}{8(\arcsin(ax))^2} \sqrt{-a^2x^2 + 1} + \frac{ax}{8\arcsin(ax)} - \frac{\text{Ci}(\arcsin(ax))}{8} + \frac{\cos(3\arcsin(ax))}{8(\arcsin(ax))^2} - \frac{3\sin(3\arcsin(ax))}{8\arcsin(ax)} + \frac{9\text{Ci}(3\arcsin(ax))}{8} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2/arcsin(a*x)^3, x)
```

[Out] $1/a^3*(-1/8/\arcsin(ax)^2*(-a^2x^2+1)^{(1/2)}+1/8*ax/\arcsin(ax)-1/8*Ci(\arcsin(ax))+1/8/\arcsin(ax)^2*\cos(3*\arcsin(ax))-3/8/\arcsin(ax)*\sin(3*\arcsin(ax))+9/8*Ci(3*\arcsin(ax)))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{\sqrt{ax+1}\sqrt{-ax+1}ax^2 + \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2 \int \frac{9a^2x^2-2}{\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - (3a^2x^3 - 2x) \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)}{2a^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/arcsin(a*x)^3,x, algorithm="maxima")`

[Out] $-1/2*(\sqrt{ax+1}*\sqrt{-ax+1}*ax^2 + \arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1}))^2*\int((9*a^2*x^2 - 2)/\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1}), x) - (3*a^2*x^3 - 2*x)*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1}))/ (a^2*\arctan2(ax, \sqrt{ax+1}*\sqrt{-ax+1})^2)$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^2}{\arcsin(ax)^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2/arcsin(a*x)^3,x, algorithm="fricas")`

[Out] `integral(x^2/arcsin(a*x)^3, x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\arcsin^3(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2/asin(a*x)**3,x)`

[Out] `Integral(x**2/asin(a*x)**3, x)`

Giac [A] time = 1.3707, size = 138, normalized size = 1.68

$$\frac{3(a^2x^2-1)x}{2a^2\arcsin(ax)} + \frac{x}{2a^2\arcsin(ax)} + \frac{9\text{Ci}(3\arcsin(ax))}{8a^3} - \frac{\text{Ci}(\arcsin(ax))}{8a^3} + \frac{(-a^2x^2+1)^{\frac{3}{2}}}{2a^3\arcsin(ax)^2} - \frac{\sqrt{-a^2x^2+1}}{2a^3\arcsin(ax)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2/arcsin(a*x)^3,x, algorithm="giac")
```

```
[Out] 3/2*(a^2*x^2 - 1)*x/(a^2*arcsin(a*x)) + 1/2*x/(a^2*arcsin(a*x)) + 9/8*cos_i
ntegral(3*arcsin(a*x))/a^3 - 1/8*cos_integral(arcsin(a*x))/a^3 + 1/2*(-a^2*
x^2 + 1)^(3/2)/(a^3*arcsin(a*x)^2) - 1/2*sqrt(-a^2*x^2 + 1)/(a^3*arcsin(a*x
)^2)
```

3.63 $\int \frac{x}{\sin^{-1}(ax)^3} dx$

Optimal. Leaf size=64

$$-\frac{\operatorname{Si}\left(2\sin^{-1}(ax)\right)}{a^2} - \frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{1}{2a^2\sin^{-1}(ax)} + \frac{x^2}{\sin^{-1}(ax)}$$

[Out] $-(x\sqrt{1-a^2x^2})/(2a\operatorname{ArcSin}[ax]^2) - 1/(2a^2\operatorname{ArcSin}[ax]) + x^2/\operatorname{ArcSin}[ax] - \operatorname{SinIntegral}[2\operatorname{ArcSin}[ax]]/a^2$

Rubi [A] time = 0.168357, antiderivative size = 64, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.875$, Rules used = {4633, 4719, 4635, 4406, 12, 3299, 4641}

$$-\frac{\operatorname{Si}\left(2\sin^{-1}(ax)\right)}{a^2} - \frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{1}{2a^2\sin^{-1}(ax)} + \frac{x^2}{\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x/\operatorname{ArcSin}[ax]^3, x]$

[Out] $-(x\sqrt{1-a^2x^2})/(2a\operatorname{ArcSin}[ax]^2) - 1/(2a^2\operatorname{ArcSin}[ax]) + x^2/\operatorname{ArcSin}[ax] - \operatorname{SinIntegral}[2\operatorname{ArcSin}[ax]]/a^2$

Rule 4633

$\operatorname{Int}[(a + \operatorname{ArcSin}[c(x)](b))^n(x)^m, x_Symbol] := \operatorname{Simp}[(x^m\sqrt{1-c^2x^2}(a + b\operatorname{ArcSin}[cx])^{n+1})/(b^{n+1}c), x] + (\operatorname{Dist}[(c(m+1))/(b(n+1)], \operatorname{Int}[(x^{m+1}(a + b\operatorname{ArcSin}[cx])^{n+1})/\sqrt{1-c^2x^2}], x], x] - \operatorname{Dist}[m/(b^{n+1}c), \operatorname{Int}[(x^{m-1}(a + b\operatorname{ArcSin}[cx])^{n+1})/\sqrt{1-c^2x^2}], x], x]) /;$ $\operatorname{FreeQ}\{a, b, c, x\} \ \&\& \ \operatorname{IGtQ}[m, 0] \ \&\& \ \operatorname{LtQ}[n, -2]$

Rule 4719

$\operatorname{Int}[(a + \operatorname{ArcSin}[c(x)](b))^n((f(x))^m)/\sqrt{d + e(x)^2}, x_Symbol] := \operatorname{Simp}[(f(x)^m(a + b\operatorname{ArcSin}[cx])^{n+1})/(b^{n+1}c\sqrt{d}), x] - \operatorname{Dist}[(f(x)^m)/(b^{n+1}c\sqrt{d}), \operatorname{Int}[(f(x)^{m-1}(a + b\operatorname{ArcSin}[cx])^{n+1}), x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, e, f, m, x\} \ \&\& \ \operatorname{EqQ}[c^2d + e, 0] \ \&\& \ \operatorname{LtQ}[n, -1] \ \&\& \ \operatorname{GtQ}[d, 0]$

Rule 4635

$\operatorname{Int}[(a + \operatorname{ArcSin}[c(x)](b))^n(x)^m, x_Symbol] := \operatorname{Dist}[1/c^{n+1}, \operatorname{Subst}[\operatorname{Int}[(a + bx)^n\sin[x]^m\cos[x], x], x, \operatorname{ArcSin}[cx]], x] /;$ $\operatorname{FreeQ}\{a, b, c, n, x\} \ \&\& \ \operatorname{IGtQ}[m, 0]$

Rule 4406

$\operatorname{Int}[\cos[(a + b(x))^p]((c + d(x))^m)\sin[(a + b(x))^n], x_Symbol] := \operatorname{Int}[\operatorname{ExpandTrigReduce}[(c + dx)^m, \sin[a + bx]]^n\cos[a + bx]^p, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m, x\} \ \&\& \ \operatorname{IGtQ}[n, 0] \ \&\& \ \operatorname{IGtQ}[p, 0]$

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 4641

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] := Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]
```

Rubi steps

$$\begin{aligned} \int \frac{x}{\sin^{-1}(ax)^3} dx &= -\frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} + \frac{\int \frac{1}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx}{2a} - a \int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^2} dx \\ &= -\frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{1}{2a^2\sin^{-1}(ax)} + \frac{x^2}{\sin^{-1}(ax)} - 2 \int \frac{x}{\sin^{-1}(ax)} dx \\ &= -\frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{1}{2a^2\sin^{-1}(ax)} + \frac{x^2}{\sin^{-1}(ax)} - \frac{2 \operatorname{Subst}\left(\int \frac{\cos(x)\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^2} \\ &= -\frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{1}{2a^2\sin^{-1}(ax)} + \frac{x^2}{\sin^{-1}(ax)} - \frac{2 \operatorname{Subst}\left(\int \frac{\sin(2x)}{2x} dx, x, \sin^{-1}(ax)\right)}{a^2} \\ &= -\frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{1}{2a^2\sin^{-1}(ax)} + \frac{x^2}{\sin^{-1}(ax)} - \frac{\operatorname{Subst}\left(\int \frac{\sin(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{a^2} \\ &= -\frac{x\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)^2} - \frac{1}{2a^2\sin^{-1}(ax)} + \frac{x^2}{\sin^{-1}(ax)} - \frac{\operatorname{Si}\left(2\sin^{-1}(ax)\right)}{a^2} \end{aligned}$$

Mathematica [A] time = 0.0596291, size = 61, normalized size = 0.95

$$\frac{ax\sqrt{1-a^2x^2} + (1-2a^2x^2)\sin^{-1}(ax) + 2\sin^{-1}(ax)^2\operatorname{Si}\left(2\sin^{-1}(ax)\right)}{2a^2\sin^{-1}(ax)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x/ArcSin[a*x]^3, x]
```

```
[Out] -(a*x*Sqrt[1 - a^2*x^2] + (1 - 2*a^2*x^2)*ArcSin[a*x] + 2*ArcSin[a*x]^2*SinIntegral[2*ArcSin[a*x]])/(2*a^2*ArcSin[a*x]^2)
```

Maple [A] time = 0.026, size = 45, normalized size = 0.7

$$\frac{1}{a^2} \left(-\frac{\sin(2 \arcsin(ax))}{4(\arcsin(ax))^2} - \frac{\cos(2 \arcsin(ax))}{2 \arcsin(ax)} - \operatorname{Si}(2 \arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x/arcsin(a*x)^3, x)
```

[Out] $1/a^2*(-1/4/\arcsin(ax)^2*\sin(2*\arcsin(ax))-1/2/\arcsin(ax)*\cos(2*\arcsin(ax))-Si(2*\arcsin(ax))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{4a^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2 \int \frac{x}{\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx + \sqrt{ax+1}\sqrt{-ax+1}ax - (2a^2x^2 - 1) \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)}{2a^2 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^3,x, algorithm="maxima")

[Out] $-1/2*(4*a^2*\arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1})^2*\int(x/\arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1}), x) + \sqrt{a*x+1}*\sqrt{-a*x+1}*a*x - (2*a^2*x^2 - 1)*\arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1}))/a^2*\arctan2(a*x, \sqrt{a*x+1}*\sqrt{-a*x+1})^2$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\int \left(\frac{x}{\arcsin(ax)^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^3,x, algorithm="fricas")

[Out] integral(x/arcsin(a*x)^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\arcsin^3(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/asin(a*x)**3,x)

[Out] Integral(x/asin(a*x)**3, x)

Giac [A] time = 1.41823, size = 90, normalized size = 1.41

$$-\frac{\text{Si}(2 \arcsin(ax))}{a^2} - \frac{\sqrt{-a^2x^2 + 1}x}{2a \arcsin(ax)^2} + \frac{a^2x^2 - 1}{a^2 \arcsin(ax)} + \frac{1}{2a^2 \arcsin(ax)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^3,x, algorithm="giac")

[Out] $-\text{sin_integral}(2*\arcsin(a*x))/a^2 - 1/2*\sqrt{-a^2*x^2 + 1}*x/(a*\arcsin(a*x)^2) + (a^2*x^2 - 1)/(a^2*\arcsin(a*x)) + 1/2/(a^2*\arcsin(a*x))$

3.64 $\int \frac{1}{\sin^{-1}(ax)^3} dx$

Optimal. Leaf size=51

$$-\frac{\sqrt{1-a^2x^2}}{2a \sin^{-1}(ax)^2} - \frac{\text{CosIntegral}(\sin^{-1}(ax))}{2a} + \frac{x}{2 \sin^{-1}(ax)}$$

[Out] $-\text{Sqrt}[1 - a^2*x^2]/(2*a*\text{ArcSin}[a*x]^2) + x/(2*\text{ArcSin}[a*x]) - \text{CosIntegral}[\text{ArcSin}[a*x]]/(2*a)$

Rubi [A] time = 0.0845015, antiderivative size = 51, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4621, 4719, 4623, 3302}

$$-\frac{\sqrt{1-a^2x^2}}{2a \sin^{-1}(ax)^2} - \frac{\text{CosIntegral}(\sin^{-1}(ax))}{2a} + \frac{x}{2 \sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^{-3}, x]$

[Out] $-\text{Sqrt}[1 - a^2*x^2]/(2*a*\text{ArcSin}[a*x]^2) + x/(2*\text{ArcSin}[a*x]) - \text{CosIntegral}[\text{ArcSin}[a*x]]/(2*a)$

Rule 4621

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n, x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{n+1})/(b*c*(n+1)), x] + \text{Dist}[c/(b*(n+1)), \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{n+1})/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ $\text{FreeQ}\{a, b, c\}, x \ \&\& \ \text{LtQ}[n, -1]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n*(f*x)^m/\text{Sqrt}[d + (e*x)^2], x_Symbol] \rightarrow \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{n+1}/(b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{m-1}*(a + b*\text{ArcSin}[c*x])^{n+1}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, e, f, m\}, x \ \&\ \& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{LtQ}[n, -1] \ \&\& \ \text{GtQ}[d, 0]$

Rule 4623

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n, x_Symbol] \rightarrow \text{Dist}[1/(b*c), \text{Subst}[\text{Int}[x^n*\text{Cos}[a/b - x/b], x], x, a + b*\text{ArcSin}[c*x]], x] /;$ $\text{FreeQ}\{a, b, c, n\}, x$

Rule 3302

$\text{Int}[\sin[(e + f*x)/(c + d*x)], x_Symbol] \rightarrow \text{Simp}[\text{CosIntegral}[e - \text{Pi}/2 + f*x]/d, x] /;$ $\text{FreeQ}\{c, d, e, f\}, x \ \&\& \ \text{EqQ}[d*(e - \text{Pi}/2) - c*f, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sin^{-1}(ax)^3} dx &= -\frac{\sqrt{1-a^2x^2}}{2a \sin^{-1}(ax)^2} - \frac{1}{2}a \int \frac{x}{\sqrt{1-a^2x^2} \sin^{-1}(ax)^2} dx \\
&= -\frac{\sqrt{1-a^2x^2}}{2a \sin^{-1}(ax)^2} + \frac{x}{2 \sin^{-1}(ax)} - \frac{1}{2} \int \frac{1}{\sin^{-1}(ax)} dx \\
&= -\frac{\sqrt{1-a^2x^2}}{2a \sin^{-1}(ax)^2} + \frac{x}{2 \sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\cos(x)}{x} dx, x, \sin^{-1}(ax)\right)}{2a} \\
&= -\frac{\sqrt{1-a^2x^2}}{2a \sin^{-1}(ax)^2} + \frac{x}{2 \sin^{-1}(ax)} - \frac{\text{Ci}(\sin^{-1}(ax))}{2a}
\end{aligned}$$

Mathematica [A] time = 0.0224016, size = 48, normalized size = 0.94

$$-\frac{\sqrt{1-a^2x^2} + \sin^{-1}(ax)^2 \text{CosIntegral}(\sin^{-1}(ax)) - ax \sin^{-1}(ax)}{2a \sin^{-1}(ax)^2}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^(-3),x]

[Out] -(Sqrt[1 - a^2*x^2] - a*x*ArcSin[a*x] + ArcSin[a*x]^2*CosIntegral[ArcSin[a*x]])/(2*a*ArcSin[a*x]^2)

Maple [A] time = 0.021, size = 43, normalized size = 0.8

$$\frac{1}{a} \left(-\frac{1}{2 (\arcsin(ax))^2} \sqrt{-a^2x^2 + 1} + \frac{ax}{2 \arcsin(ax)} - \frac{\text{Ci}(\arcsin(ax))}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x)^3,x)

[Out] 1/a*(-1/2/arcsin(a*x)^2*(-a^2*x^2+1)^(1/2)+1/2*a*x/arcsin(a*x)-1/2*Ci(arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{a \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2 \int \frac{1}{\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - ax \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1}) + \sqrt{ax+1}\sqrt{-ax+1}}{2a \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^3,x, algorithm="maxima")

[Out] -1/2*(a*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2*integrate(1/arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)), x) - a*x*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)) + sqrt(a*x + 1)*sqrt(-a*x + 1))/(a*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{\arcsin(ax)^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^3,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^(-3), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\text{asin}^3(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/asin(a*x)**3,x)

[Out] Integral(asin(a*x)**(-3), x)

Giac [A] time = 1.33887, size = 58, normalized size = 1.14

$$\frac{x}{2 \arcsin(ax)} - \frac{\text{Ci}(\arcsin(ax))}{2a} - \frac{\sqrt{-a^2x^2 + 1}}{2a \arcsin(ax)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^3,x, algorithm="giac")

[Out] 1/2*x/arcsin(a*x) - 1/2*cos_integral(arcsin(a*x))/a - 1/2*sqrt(-a^2*x^2 + 1)/(a*arcsin(a*x)^2)

$$3.65 \quad \int \frac{1}{x \sin^{-1}(ax)^3} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x \sin^{-1}(ax)^3}, x\right)$$

[Out] Unintegrable[1/(x*ArcSin[a*x]^3), x]

Rubi [A] time = 0.0124023, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x \sin^{-1}(ax)^3} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*ArcSin[a*x]^3),x]

[Out] Defer[Int][1/(x*ArcSin[a*x]^3), x]

Rubi steps

$$\int \frac{1}{x \sin^{-1}(ax)^3} dx = \int \frac{1}{x \sin^{-1}(ax)^3} dx$$

Mathematica [A] time = 0.540825, size = 0, normalized size = 0.

$$\int \frac{1}{x \sin^{-1}(ax)^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*ArcSin[a*x]^3),x]

[Out] Integrate[1/(x*ArcSin[a*x]^3), x]

Maple [A] time = 0.078, size = 0, normalized size = 0.

$$\int \frac{1}{x (\arcsin(ax))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x)^3,x)

[Out] int(1/x/arcsin(a*x)^3,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{2x^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2 \int \frac{1}{x^3 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - \sqrt{ax+1}\sqrt{-ax+1}ax + \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})}{2a^2x^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^3,x, algorithm="maxima")

[Out] 1/2*(2*x^2*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2*integrate(1/(x^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))), x) - sqrt(a*x + 1)*sqrt(-a*x + 1)*a*x + arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)))/(a^2*x^2*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x \arcsin(ax)^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^3,x, algorithm="fricas")

[Out] integral(1/(x*arcsin(a*x)^3), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \operatorname{asin}^3(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/asin(a*x)**3,x)

[Out] Integral(1/(x*asin(a*x)**3), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^3,x, algorithm="giac")

[Out] integrate(1/(x*arcsin(a*x)^3), x)

$$3.66 \quad \int \frac{1}{x^2 \sin^{-1}(ax)^3} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x^2 \sin^{-1}(ax)^3}, x\right)$$

[Out] Unintegrable[1/(x^2*ArcSin[a*x]^3), x]

Rubi [A] time = 0.0133543, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2 \sin^{-1}(ax)^3} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*ArcSin[a*x]^3), x]

[Out] Defer[Int][1/(x^2*ArcSin[a*x]^3), x]

Rubi steps

$$\int \frac{1}{x^2 \sin^{-1}(ax)^3} dx = \int \frac{1}{x^2 \sin^{-1}(ax)^3} dx$$

Mathematica [A] time = 6.43086, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sin^{-1}(ax)^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*ArcSin[a*x]^3), x]

[Out] Integrate[1/(x^2*ArcSin[a*x]^3), x]

Maple [A] time = 0.122, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (\arcsin(ax))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/arcsin(a*x)^3, x)

[Out] int(1/x^2/arcsin(a*x)^3, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{x^3 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2 \int \frac{a^2x^2-6}{x^4 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx + \sqrt{ax+1}\sqrt{-ax+1}ax + (a^2x^2-2) \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})}{2a^2x^3 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^3,x, algorithm="maxima")

[Out] -1/2*(x^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2*integrate((a^2*x^2 - 6)/(x^4*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))), x) + sqrt(a*x + 1)*sqrt(-a*x + 1)*a*x + (a^2*x^2 - 2)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)))/(a^2*x^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x^2 \arcsin(ax)^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^3,x, algorithm="fricas")

[Out] integral(1/(x^2*arcsin(a*x)^3), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin^3(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/asin(a*x)**3,x)

[Out] Integral(1/(x**2*asin(a*x)**3), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin(ax)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^3,x, algorithm="giac")

[Out] integrate(1/(x^2*arcsin(a*x)^3), x)

$$3.67 \quad \int \frac{x^4}{\sin^{-1}(ax)^4} dx$$

Optimal. Leaf size=158

$$\frac{\text{Si}(\sin^{-1}(ax))}{48a^5} - \frac{27\text{Si}(3\sin^{-1}(ax))}{32a^5} + \frac{125\text{Si}(5\sin^{-1}(ax))}{96a^5} + \frac{25x^4\sqrt{1-a^2x^2}}{6a\sin^{-1}(ax)} - \frac{x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{2x^3}{3a^2\sin^{-1}(ax)^2} - \frac{2x^2}{a^3\sin^{-1}(ax)}$$

[Out] $-(x^4\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]^3) - (2x^3)/(3a^2\text{ArcSin}[ax]^2) + (5x^5)/(6\text{ArcSin}[ax]^2) - (2x^2\sqrt{1-a^2x^2})/(a^3\text{ArcSin}[ax]) + (25x^4\sqrt{1-a^2x^2})/(6a\text{ArcSin}[ax]) + \text{SinIntegral}[\text{ArcSin}[ax]]/(48a^5) - (27\text{SinIntegral}[3\text{ArcSin}[ax]])/(32a^5) + (125\text{SinIntegral}[5\text{ArcSin}[ax]])/(96a^5)$

Rubi [A] time = 0.314241, antiderivative size = 158, normalized size of antiderivative = 1., number of steps used = 12, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4633, 4719, 4631, 3299}

$$\frac{\text{Si}(\sin^{-1}(ax))}{48a^5} - \frac{27\text{Si}(3\sin^{-1}(ax))}{32a^5} + \frac{125\text{Si}(5\sin^{-1}(ax))}{96a^5} + \frac{25x^4\sqrt{1-a^2x^2}}{6a\sin^{-1}(ax)} - \frac{x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{2x^3}{3a^2\sin^{-1}(ax)^2} - \frac{2x^2}{a^3\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^4/ArcSin[a*x]^4, x]

[Out] $-(x^4\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]^3) - (2x^3)/(3a^2\text{ArcSin}[ax]^2) + (5x^5)/(6\text{ArcSin}[ax]^2) - (2x^2\sqrt{1-a^2x^2})/(a^3\text{ArcSin}[ax]) + (25x^4\sqrt{1-a^2x^2})/(6a\text{ArcSin}[ax]) + \text{SinIntegral}[\text{ArcSin}[ax]]/(48a^5) - (27\text{SinIntegral}[3\text{ArcSin}[ax]])/(32a^5) + (125\text{SinIntegral}[5\text{ArcSin}[ax]])/(96a^5)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1-c^2*x^2]*(a+b*ArcSin[c*x])^(n+1))/(b*c*(n+1)), x] + (Dist[(c*(m+1))/(b*(n+1)), Int[(x^(m+1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x] - Dist[m/(b*c*(n+1)), Int[(x^(m-1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*((f_.)*(x_)^(m_.))/sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[((f*x)^m*(a+b*ArcSin[c*x])^(n+1))/(b*c*sqrt[d]*(n+1)), x] - Dist[(f*m)/(b*c*sqrt[d]*(n+1)), Int[(f*x)^(m-1)*(a+b*ArcSin[c*x])^(n+1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1-c^2*x^2]*(a+b*ArcSin[c*x])^(n+1))/(b*c*(n+1)), x] - Dist[1/(b*c*(m+1)*(n+1)), Subst[Int[ExpandTrigReduce[(a+b*x)^(n+1), Sin[x]^(m-1)*(m-(m+1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :-> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^4}{\sin^{-1}(ax)^4} dx &= -\frac{x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} + \frac{4\int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx}{3a} - \frac{1}{3}(5a) \int \frac{x^5}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{2x^3}{3a^2\sin^{-1}(ax)^2} + \frac{5x^5}{6\sin^{-1}(ax)^2} - \frac{25}{6} \int \frac{x^4}{\sin^{-1}(ax)^2} dx + \frac{2\int \frac{x^2}{\sin^{-1}(ax)^2} dx}{a^2} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{2x^3}{3a^2\sin^{-1}(ax)^2} + \frac{5x^5}{6\sin^{-1}(ax)^2} - \frac{2x^2\sqrt{1-a^2x^2}}{a^3\sin^{-1}(ax)} + \frac{25x^4\sqrt{1-a^2x^2}}{6a\sin^{-1}(ax)} + \frac{2\text{Subst}\left(\int \frac{-5x}{\sin^{-1}(ax)^2} dx\right)}{a^2} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{2x^3}{3a^2\sin^{-1}(ax)^2} + \frac{5x^5}{6\sin^{-1}(ax)^2} - \frac{2x^2\sqrt{1-a^2x^2}}{a^3\sin^{-1}(ax)} + \frac{25x^4\sqrt{1-a^2x^2}}{6a\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin(x)}{x} dx\right)}{2a^2} \\ &= -\frac{x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{2x^3}{3a^2\sin^{-1}(ax)^2} + \frac{5x^5}{6\sin^{-1}(ax)^2} - \frac{2x^2\sqrt{1-a^2x^2}}{a^3\sin^{-1}(ax)} + \frac{25x^4\sqrt{1-a^2x^2}}{6a\sin^{-1}(ax)} + \frac{\text{Si}\left(\sin^{-1}(ax)\right)}{48a^5} \end{aligned}$$

Mathematica [A] time = 0.338395, size = 159, normalized size = 1.01

$$\frac{-32a^4x^4\sqrt{1-a^2x^2} + 80a^5x^5\sin^{-1}(ax) + 400a^4x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)^2 - 64a^3x^3\sin^{-1}(ax) - 192a^2x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^2}{96a^5\sin^{-1}(ax)^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^4/ArcSin[a*x]^4,x]

[Out] (-32*a^4*x^4*Sqrt[1 - a^2*x^2] - 64*a^3*x^3*ArcSin[a*x] + 80*a^5*x^5*ArcSin[a*x] - 192*a^2*x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2 + 400*a^4*x^4*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2 + 2*ArcSin[a*x]^3*SinIntegral[ArcSin[a*x]] - 81*ArcSin[a*x]^3*SinIntegral[3*ArcSin[a*x]] + 125*ArcSin[a*x]^3*SinIntegral[5*ArcSin[a*x]])/(96*a^5*ArcSin[a*x]^3)

Maple [A] time = 0.04, size = 171, normalized size = 1.1

$$\frac{1}{a^5} \left(-\frac{1}{24 (\arcsin(ax))^3} \sqrt{-a^2x^2 + 1} + \frac{ax}{48 (\arcsin(ax))^2} + \frac{1}{48 \arcsin(ax)} \sqrt{-a^2x^2 + 1} + \frac{\text{Si}(\arcsin(ax))}{48} + \frac{\cos(3 \arcsin(ax))}{16 (\arcsin(ax))^3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x)^4,x)

[Out] 1/a^5*(-1/24/arcsin(a*x)^3*(-a^2*x^2+1)^(1/2)+1/48*a*x/arcsin(a*x)^2+1/48/a*arcsin(a*x)*(-a^2*x^2+1)^(1/2)+1/48*Si(arcsin(a*x))+1/16/arcsin(a*x)^3*cos(3*arcsin(a*x))-3/32/arcsin(a*x)^2*sin(3*arcsin(a*x))-9/32/arcsin(a*x)*cos(3*arcsin(a*x))-27/32*Si(3*arcsin(a*x))-1/48/arcsin(a*x)^3*cos(5*arcsin(a*x))+5/96/arcsin(a*x)^2*sin(5*arcsin(a*x))+25/96/arcsin(a*x)*cos(5*arcsin(a*x))+125/96*Si(5*arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$a^3 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3 \int \frac{(125a^4x^5 - 136a^2x^3 + 24x)\sqrt{ax+1}\sqrt{-ax+1}}{(a^5x^2 - a^3)\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx + \left(2a^2x^4 - (25a^2x^4 - 12x^2)\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})\right)$$

$$6a^3 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^4,x, algorithm="maxima")

[Out] -1/6*(6*a^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3*integrate(1/6*(125*a^4*x^5 - 136*a^2*x^3 + 24*x)*sqrt(a*x + 1)*sqrt(-a*x + 1)/((a^5*x^2 - a^3)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))), x) + (2*a^2*x^4 - (25*a^2*x^4 - 12*x^2)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2)*sqrt(a*x + 1)*sqrt(-a*x + 1) - (5*a^3*x^5 - 4*a*x^3)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)))/(a^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^4}{\arcsin(ax)^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^4,x, algorithm="fricas")

[Out] integral(x^4/arcsin(a*x)^4, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\text{asin}^4(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/asin(a*x)**4,x)

[Out] Integral(x**4/asin(a*x)**4, x)

Giac [A] time = 1.27056, size = 338, normalized size = 2.14

$$\frac{5(a^2x^2 - 1)^2x}{6a^4 \arcsin(ax)^2} + \frac{25(a^2x^2 - 1)^2\sqrt{-a^2x^2 + 1}}{6a^5 \arcsin(ax)} + \frac{(a^2x^2 - 1)x}{a^4 \arcsin(ax)^2} + \frac{125 \text{Si}(5 \arcsin(ax))}{96a^5} - \frac{27 \text{Si}(3 \arcsin(ax))}{32a^5} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^4,x, algorithm="giac")

```
[Out] 5/6*(a^2*x^2 - 1)^2*x/(a^4*arcsin(a*x)^2) + 25/6*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)/(a^5*arcsin(a*x)) + (a^2*x^2 - 1)*x/(a^4*arcsin(a*x)^2) + 125/96*
sin_integral(5*arcsin(a*x))/a^5 - 27/32*sin_integral(3*arcsin(a*x))/a^5 + 1/
48*sin_integral(arcsin(a*x))/a^5 - 19/3*(-a^2*x^2 + 1)^(3/2)/(a^5*arcsin(a*
x)) + 1/6*x/(a^4*arcsin(a*x)^2) - 1/3*(a^2*x^2 - 1)^2*sqrt(-a^2*x^2 + 1)/(a
^5*arcsin(a*x)^3) + 13/6*sqrt(-a^2*x^2 + 1)/(a^5*arcsin(a*x)) + 2/3*(-a^2*x
^2 + 1)^(3/2)/(a^5*arcsin(a*x)^3) - 1/3*sqrt(-a^2*x^2 + 1)/(a^5*arcsin(a*x)
^3)
```

$$3.68 \quad \int \frac{x^3}{\sin^{-1}(ax)^4} dx$$

Optimal. Leaf size=144

$$-\frac{\text{CosIntegral}(2 \sin^{-1}(ax))}{3a^4} + \frac{4\text{CosIntegral}(4 \sin^{-1}(ax))}{3a^4} + \frac{8x^3\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)} - \frac{x^3\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} - \frac{x^2}{2a^2 \sin^{-1}(ax)^2} - \frac{x\sqrt{1-a^2x^2}}{a^3 \sin^{-1}(ax)}$$

[Out] $-(x^3\sqrt{1-a^2x^2})/(3*a*\text{ArcSin}[a*x]^3) - x^2/(2*a^2*\text{ArcSin}[a*x]^2) + (2*x^4)/(3*\text{ArcSin}[a*x]^2) - (x*\sqrt{1-a^2x^2})/(a^3*\text{ArcSin}[a*x]) + (8*x^3*\sqrt{1-a^2x^2})/(3*a*\text{ArcSin}[a*x]) - \text{CosIntegral}[2*\text{ArcSin}[a*x]]/(3*a^4) + (4*\text{CosIntegral}[4*\text{ArcSin}[a*x]])/(3*a^4)$

Rubi [A] time = 0.281678, antiderivative size = 144, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4633, 4719, 4631, 3302}

$$-\frac{\text{CosIntegral}(2 \sin^{-1}(ax))}{3a^4} + \frac{4\text{CosIntegral}(4 \sin^{-1}(ax))}{3a^4} + \frac{8x^3\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)} - \frac{x^3\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} - \frac{x^2}{2a^2 \sin^{-1}(ax)^2} - \frac{x\sqrt{1-a^2x^2}}{a^3 \sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^3/ArcSin[a*x]^4,x]

[Out] $-(x^3\sqrt{1-a^2x^2})/(3*a*\text{ArcSin}[a*x]^3) - x^2/(2*a^2*\text{ArcSin}[a*x]^2) + (2*x^4)/(3*\text{ArcSin}[a*x]^2) - (x*\sqrt{1-a^2x^2})/(a^3*\text{ArcSin}[a*x]) + (8*x^3*\sqrt{1-a^2x^2})/(3*a*\text{ArcSin}[a*x]) - \text{CosIntegral}[2*\text{ArcSin}[a*x]]/(3*a^4) + (4*\text{CosIntegral}[4*\text{ArcSin}[a*x]])/(3*a^4)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + (Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((f_.)*(x_.))^(m_.))/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] := Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*Sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*Sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sin^{-1}(ax)^4} dx &= -\frac{x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} + \frac{\int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx}{a} - \frac{1}{3}(4a) \int \frac{x^4}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x^2}{2a^2\sin^{-1}(ax)^2} + \frac{2x^4}{3\sin^{-1}(ax)^2} - \frac{8}{3} \int \frac{x^3}{\sin^{-1}(ax)^2} dx + \frac{\int \frac{x}{\sin^{-1}(ax)^2} dx}{a^2} \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x^2}{2a^2\sin^{-1}(ax)^2} + \frac{2x^4}{3\sin^{-1}(ax)^2} - \frac{x\sqrt{1-a^2x^2}}{a^3\sin^{-1}(ax)} + \frac{8x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\cos(2x)}{x} dx\right)}{a^4} \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x^2}{2a^2\sin^{-1}(ax)^2} + \frac{2x^4}{3\sin^{-1}(ax)^2} - \frac{x\sqrt{1-a^2x^2}}{a^3\sin^{-1}(ax)} + \frac{8x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)} + \frac{\text{Ci}(2\sin^{-1}(ax))}{a^4} \\ &= -\frac{x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x^2}{2a^2\sin^{-1}(ax)^2} + \frac{2x^4}{3\sin^{-1}(ax)^2} - \frac{x\sqrt{1-a^2x^2}}{a^3\sin^{-1}(ax)} + \frac{8x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)} - \frac{\text{Ci}(2\sin^{-1}(ax))}{3a^4} \end{aligned}$$

Mathematica [A] time = 0.359611, size = 107, normalized size = 0.74

$$\frac{ax(-2a^2x^2\sqrt{1-a^2x^2}+ax(4a^2x^2-3)\sin^{-1}(ax)+2\sqrt{1-a^2x^2}(8a^2x^2-3)\sin^{-1}(ax)^2)}{\sin^{-1}(ax)^3} - \frac{2\text{CosIntegral}(2\sin^{-1}(ax)) + 8\text{CosIntegral}(4\sin^{-1}(ax))}{6a^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3/ArcSin[a*x]^4,x]
```

```
[Out] ((a*x*(-2*a^2*x^2*Sqrt[1 - a^2*x^2] + a*x*(-3 + 4*a^2*x^2)*ArcSin[a*x] + 2*Sqrt[1 - a^2*x^2]*(-3 + 8*a^2*x^2)*ArcSin[a*x]^2))/ArcSin[a*x]^3 - 2*CosIntegral[2*ArcSin[a*x]] + 8*CosIntegral[4*ArcSin[a*x]])/(6*a^4)
```

Maple [A] time = 0.03, size = 114, normalized size = 0.8

$$\frac{1}{a^4} \left(-\frac{\sin(2 \arcsin(ax))}{12 (\arcsin(ax))^3} - \frac{\cos(2 \arcsin(ax))}{12 (\arcsin(ax))^2} + \frac{\sin(2 \arcsin(ax))}{6 \arcsin(ax)} - \frac{\text{Ci}(2 \arcsin(ax))}{3} + \frac{\sin(4 \arcsin(ax))}{24 (\arcsin(ax))^3} + \frac{\cos(4 \arcsin(ax))}{12 (\arcsin(ax))^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3/arcsin(a*x)^4,x)
```

```
[Out] 1/a^4*(-1/12/arcsin(a*x)^3*sin(2*arcsin(a*x))-1/12/arcsin(a*x)^2*cos(2*arcsin(a*x))+1/6/arcsin(a*x)*sin(2*arcsin(a*x))-1/3*Ci(2*arcsin(a*x))+1/24/arcsin(a*x)^3*sin(4*arcsin(a*x))+1/12/arcsin(a*x)^2*cos(4*arcsin(a*x))-1/3/arcsin(a*x)*sin(4*arcsin(a*x))+4/3*Ci(4*arcsin(a*x)))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$2 a^3 \arctan \left(a x, \sqrt{a x+1} \sqrt{-a x+1} \right)^3 \int \frac{(32 a^4 x^4 - 30 a^2 x^2 + 3) \sqrt{a x+1} \sqrt{-a x+1}}{(a^5 x^2 - a^3) \arctan(a x, \sqrt{a x+1} \sqrt{-a x+1})} dx + 2 \left(a^2 x^3 - (8 a^2 x^3 - 3 x) \arctan(a x, \sqrt{a x+1} \sqrt{-a x+1}) \right) / (a^5 x^2 - a^3) \arctan(a x, \sqrt{a x+1} \sqrt{-a x+1})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^4,x, algorithm="maxima")

[Out] -1/6*(6*a^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3*integrate(1/3*(32*a^4*x^4 - 30*a^2*x^2 + 3)*sqrt(a*x + 1)*sqrt(-a*x + 1)/((a^5*x^2 - a^3)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))), x) + 2*(a^2*x^3 - (8*a^2*x^3 - 3*x)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2)*sqrt(a*x + 1)*sqrt(-a*x + 1) - (4*a^3*x^4 - 3*a*x^2)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))/(a^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{x^3}{\arcsin(ax)^4}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^4,x, algorithm="fricas")

[Out] integral(x^3/arcsin(a*x)^4, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\arcsin^4(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/asin(a*x)**4,x)

[Out] Integral(x**3/asin(a*x)**4, x)

Giac [A] time = 1.37685, size = 235, normalized size = 1.63

$$-\frac{8(-a^2x^2+1)^{\frac{3}{2}}x}{3a^3\arcsin(ax)} + \frac{5\sqrt{-a^2x^2+1}x}{3a^3\arcsin(ax)} + \frac{4\text{Ci}(4\arcsin(ax))}{3a^4} - \frac{\text{Ci}(2\arcsin(ax))}{3a^4} + \frac{(-a^2x^2+1)^{\frac{3}{2}}x}{3a^3\arcsin(ax)^3} + \frac{2(a^2x^2-1)}{3a^4\arcsin(ax)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^4,x, algorithm="giac")

[Out] -8/3*(-a^2*x^2 + 1)^(3/2)*x/(a^3*arcsin(a*x)) + 5/3*sqrt(-a^2*x^2 + 1)*x/(a^3*arcsin(a*x)) + 4/3*cos_integral(4*arcsin(a*x))/a^4 - 1/3*cos_integral(2*

$$\arcsin(ax)/a^4 + 1/3*(-a^2*x^2 + 1)^{(3/2)}*x/(a^3*\arcsin(ax)^3) + 2/3*(a^2*x^2 - 1)^2/(a^4*\arcsin(ax)^2) - 1/3*\sqrt{-a^2*x^2 + 1}*x/(a^3*\arcsin(ax)^3) + 5/6*(a^2*x^2 - 1)/(a^4*\arcsin(ax)^2) + 1/6/(a^4*\arcsin(ax)^2)$$

$$3.69 \quad \int \frac{x^2}{\sin^{-1}(ax)^4} dx$$

Optimal. Leaf size=141

$$\frac{\text{Si}(\sin^{-1}(ax))}{24a^3} - \frac{9\text{Si}(3\sin^{-1}(ax))}{8a^3} + \frac{3x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)} - \frac{x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{\sqrt{1-a^2x^2}}{3a^3\sin^{-1}(ax)} - \frac{x}{3a^2\sin^{-1}(ax)^2} + \frac{x^3}{2\sin^{-1}(ax)^2}$$

[Out] $-(x^2\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]^3) - x/(3a^2\text{ArcSin}[ax]^2) + x^3/(2\text{ArcSin}[ax]^2) - \sqrt{1-a^2x^2}/(3a^3\text{ArcSin}[ax]) + (3x^2\sqrt{1-a^2x^2})/(2a\text{ArcSin}[ax]) + \text{SinIntegral}[\text{ArcSin}[ax]]/(24a^3) - (9\text{SinIntegral}[3\text{ArcSin}[ax]])/(8a^3)$

Rubi [A] time = 0.30341, antiderivative size = 141, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4633, 4719, 4631, 3299, 4621, 4723}

$$\frac{\text{Si}(\sin^{-1}(ax))}{24a^3} - \frac{9\text{Si}(3\sin^{-1}(ax))}{8a^3} + \frac{3x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)} - \frac{x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{\sqrt{1-a^2x^2}}{3a^3\sin^{-1}(ax)} - \frac{x}{3a^2\sin^{-1}(ax)^2} + \frac{x^3}{2\sin^{-1}(ax)^2}$$

Antiderivative was successfully verified.

[In] Int[x^2/ArcSin[a*x]^4,x]

[Out] $-(x^2\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]^3) - x/(3a^2\text{ArcSin}[ax]^2) + x^3/(2\text{ArcSin}[ax]^2) - \sqrt{1-a^2x^2}/(3a^3\text{ArcSin}[ax]) + (3x^2\sqrt{1-a^2x^2})/(2a\text{ArcSin}[ax]) + \text{SinIntegral}[\text{ArcSin}[ax]]/(24a^3) - (9\text{SinIntegral}[3\text{ArcSin}[ax]])/(8a^3)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)(x_)]*(b_.))^n_*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1-c^2*x^2]*(a+b*ArcSin[c*x])^(n+1))/(b*c*(n+1)), x] + (Dist[(c*(m+1))/(b*(n+1)), Int[(x^(m+1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x] - Dist[m/(b*c*(n+1)), Int[(x^(m-1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)(x_)]*(b_.))^n_)*((f_.)(x_)^(m_.))/sqrt[(d_) + (e_.)(x_)^2], x_Symbol] := Simp[((f*x)^m*(a+b*ArcSin[c*x])^(n+1))/(b*c*sqrt[d]*(n+1)), x] - Dist[(f*m)/(b*c*sqrt[d]*(n+1)), Int[(f*x)^(m-1)*(a+b*ArcSin[c*x])^(n+1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4631

Int[((a_.) + ArcSin[(c_.)(x_)]*(b_.))^n_*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1-c^2*x^2]*(a+b*ArcSin[c*x])^(n+1))/(b*c*(n+1)), x] - Dist[1/(b*c^(m+1)*(n+1)), Subst[Int[ExpandTrigReduce[(a+b*x)^(n+1), Sin[x]^(m-1)*(m-(m+1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 4621

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_), x_Symbol] := Simp[(Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + Dist[c/(b*(n + 1)), Int[(x*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && LtQ[n, -1]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*(x_)^(m_.)*((d_.) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sin^{-1}(ax)^4} dx &= -\frac{x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} + \frac{2\int \frac{x}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx}{3a} - a \int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x}{3a^2\sin^{-1}(ax)^2} + \frac{x^3}{2\sin^{-1}(ax)^2} - \frac{3}{2} \int \frac{x^2}{\sin^{-1}(ax)^2} dx + \frac{\int \frac{1}{\sin^{-1}(ax)^2} dx}{3a^2} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x}{3a^2\sin^{-1}(ax)^2} + \frac{x^3}{2\sin^{-1}(ax)^2} - \frac{\sqrt{1-a^2x^2}}{3a^3\sin^{-1}(ax)} + \frac{3x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)} - \frac{3\text{Subst}\left(\int\left(-\frac{\sin(x)}{4}\right) dx\right)}{3a} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x}{3a^2\sin^{-1}(ax)^2} + \frac{x^3}{2\sin^{-1}(ax)^2} - \frac{\sqrt{1-a^2x^2}}{3a^3\sin^{-1}(ax)} + \frac{3x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int\frac{\sin(x)}{x} dx\right)}{3a} \\ &= -\frac{x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{x}{3a^2\sin^{-1}(ax)^2} + \frac{x^3}{2\sin^{-1}(ax)^2} - \frac{\sqrt{1-a^2x^2}}{3a^3\sin^{-1}(ax)} + \frac{3x^2\sqrt{1-a^2x^2}}{2a\sin^{-1}(ax)} + \frac{\text{Si}\left(\sin^{-1}(ax)\right)}{24a^3} \end{aligned}$$

Mathematica [A] time = 0.25906, size = 102, normalized size = 0.72

$$\frac{-\frac{8a^2x^2\sqrt{1-a^2x^2}}{\sin^{-1}(ax)^3} + \frac{4ax(3a^2x^2-2)}{\sin^{-1}(ax)^2} + \frac{4\sqrt{1-a^2x^2}(9a^2x^2-2)}{\sin^{-1}(ax)} + \text{Si}\left(\sin^{-1}(ax)\right) - 27\text{Si}\left(3\sin^{-1}(ax)\right)}{24a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/ArcSin[a*x]^4, x]

[Out] ((-8*a^2*x^2*Sqrt[1 - a^2*x^2])/ArcSin[a*x]^3 + (4*a*x*(-2 + 3*a^2*x^2))/ArcSin[a*x]^2 + (4*Sqrt[1 - a^2*x^2]*(-2 + 9*a^2*x^2))/ArcSin[a*x] + SinIntegral[ArcSin[a*x]] - 27*SinIntegral[3*ArcSin[a*x]])/(24*a^3)

Maple [A] time = 0.028, size = 117, normalized size = 0.8

$$\frac{1}{a^3} \left(-\frac{1}{12 (\arcsin(ax))^3} \sqrt{-a^2x^2 + 1} + \frac{ax}{24 (\arcsin(ax))^2} + \frac{1}{24 \arcsin(ax)} \sqrt{-a^2x^2 + 1} + \frac{\text{Si}(\arcsin(ax))}{24} + \frac{\cos(3 \arcsin(ax))}{12 (\arcsin(ax))} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/arcsin(a*x)^4,x)

[Out] $\frac{1}{a^3} \left(-\frac{1}{12} \arcsin(ax)^3 (-a^2x^2+1)^{1/2} + \frac{1}{24} a^2x \arcsin(ax)^2 + \frac{1}{24} a^2 \arcsin(ax) (-a^2x^2+1)^{1/2} + \frac{1}{24} \text{Si}(\arcsin(ax)) + \frac{1}{12} \arcsin(ax)^3 \cos(3 \arcsin(ax)) - \frac{1}{8} \arcsin(ax)^2 \sin(3 \arcsin(ax)) - \frac{3}{8} \arcsin(ax) \cos(3 \arcsin(ax)) - \frac{9}{8} \text{Si}(3 \arcsin(ax)) \right)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{a^3 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3 \int \frac{(27a^2x^3-20x)\sqrt{ax+1}\sqrt{-ax+1}}{(a^3x^2-a)\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx + \left(2a^2x^2 - (9a^2x^2 - 2)\arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)\right)^3}{6a^3 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^4,x, algorithm="maxima")

[Out] $-\frac{1}{6} \left(6a^3 \arctan^2(ax, \sqrt{ax+1}\sqrt{-ax+1})^3 \int \frac{1}{6} (27a^2x^3 - 20x) \sqrt{ax+1} \sqrt{-ax+1} / ((a^3x^2 - a) \arctan^2(ax, \sqrt{ax+1}\sqrt{-ax+1})) dx + (2a^2x^2 - (9a^2x^2 - 2) \arctan^2(ax, \sqrt{ax+1}\sqrt{-ax+1}))^2 \sqrt{ax+1} \sqrt{-ax+1} - (3a^3x^3 - 2a^2x) \arctan^2(ax, \sqrt{ax+1}\sqrt{-ax+1}) / (a^3 \arctan^2(ax, \sqrt{ax+1}\sqrt{-ax+1}))^3 \right)$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^2}{\arcsin(ax)^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^4,x, algorithm="fricas")

[Out] integral(x^2/arcsin(a*x)^4, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\arcsin^4(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/asin(a*x)**4,x)

[Out] Integral(x**2/asin(a*x)**4, x)

Giac [A] time = 1.32898, size = 200, normalized size = 1.42

$$\frac{(a^2x^2 - 1)x}{2a^2 \arcsin(ax)^2} - \frac{9 \text{Si}(3 \arcsin(ax))}{8a^3} + \frac{\text{Si}(\arcsin(ax))}{24a^3} - \frac{3(-a^2x^2 + 1)^{\frac{3}{2}}}{2a^3 \arcsin(ax)} + \frac{x}{6a^2 \arcsin(ax)^2} + \frac{7\sqrt{-a^2x^2 + 1}}{6a^3 \arcsin(ax)} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2/arcsin(a*x)^4,x, algorithm="giac")
```

```
[Out] 1/2*(a^2*x^2 - 1)*x/(a^2*arcsin(a*x)^2) - 9/8*sin_integral(3*arcsin(a*x))/a^3 + 1/24*sin_integral(arcsin(a*x))/a^3 - 3/2*(-a^2*x^2 + 1)^(3/2)/(a^3*arcsin(a*x)) + 1/6*x/(a^2*arcsin(a*x)^2) + 7/6*sqrt(-a^2*x^2 + 1)/(a^3*arcsin(a*x)) + 1/3*(-a^2*x^2 + 1)^(3/2)/(a^3*arcsin(a*x)^3) - 1/3*sqrt(-a^2*x^2 + 1)/(a^3*arcsin(a*x)^3)
```

3.70 $\int \frac{x}{\sin^{-1}(ax)^4} dx$

Optimal. Leaf size=97

$$-\frac{2\text{CosIntegral}(2\sin^{-1}(ax))}{3a^2} + \frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)} - \frac{x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{1}{6a^2\sin^{-1}(ax)^2} + \frac{x^2}{3\sin^{-1}(ax)^2}$$

[Out] $-(x\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]^3) - 1/(6a^2\text{ArcSin}[ax]^2) + x^2/(3\text{ArcSin}[ax]^2) + (2x\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]) - (2\text{CosIntegral}[2\text{ArcSin}[ax]])/(3a^2)$

Rubi [A] time = 0.163607, antiderivative size = 97, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4633, 4719, 4631, 3302, 4641}

$$-\frac{2\text{CosIntegral}(2\sin^{-1}(ax))}{3a^2} + \frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)} - \frac{x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{1}{6a^2\sin^{-1}(ax)^2} + \frac{x^2}{3\sin^{-1}(ax)^2}$$

Antiderivative was successfully verified.

[In] Int[x/ArcSin[a*x]^4,x]

[Out] $-(x\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]^3) - 1/(6a^2\text{ArcSin}[ax]^2) + x^2/(3\text{ArcSin}[ax]^2) + (2x\sqrt{1-a^2x^2})/(3a\text{ArcSin}[ax]) - (2\text{CosIntegral}[2\text{ArcSin}[ax]])/(3a^2)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + (Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int((((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_)*((f_.)*(x_)^(m_.))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*Sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*Sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -

c*f, 0]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)/Sqrt[(d_.) + (e_.)*(x_.)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rubi steps

$$\begin{aligned} \int \frac{x}{\sin^{-1}(ax)^4} dx &= -\frac{x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} + \frac{\int \frac{1}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx}{3a} - \frac{1}{3}(2a) \int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^3} dx \\ &= -\frac{x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{1}{6a^2\sin^{-1}(ax)^2} + \frac{x^2}{3\sin^{-1}(ax)^2} - \frac{2}{3} \int \frac{x}{\sin^{-1}(ax)^2} dx \\ &= -\frac{x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{1}{6a^2\sin^{-1}(ax)^2} + \frac{x^2}{3\sin^{-1}(ax)^2} + \frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)} - \frac{2 \operatorname{Subst}\left(\int \frac{\cos(2x)}{x} dx, x, \sin^{-1}(ax)\right)}{3a^2} \\ &= -\frac{x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^3} - \frac{1}{6a^2\sin^{-1}(ax)^2} + \frac{x^2}{3\sin^{-1}(ax)^2} + \frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)} - \frac{2\operatorname{Ci}\left(2\sin^{-1}(ax)\right)}{3a^2} \end{aligned}$$

Mathematica [A] time = 0.137627, size = 86, normalized size = 0.89

$$\frac{-2ax\sqrt{1-a^2x^2} + 4ax\sqrt{1-a^2x^2}\sin^{-1}(ax)^2 + (2a^2x^2 - 1)\sin^{-1}(ax) - 4\sin^{-1}(ax)^3\operatorname{CosIntegral}\left(2\sin^{-1}(ax)\right)}{6a^2\sin^{-1}(ax)^3}$$

Antiderivative was successfully verified.

[In] Integrate[x/ArcSin[a*x]^4,x]

[Out] (-2*a*x*Sqrt[1 - a^2*x^2] + (-1 + 2*a^2*x^2)*ArcSin[a*x] + 4*a*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2 - 4*ArcSin[a*x]^3*CosIntegral[2*ArcSin[a*x]])/(6*a^2*ArcSin[a*x]^3)

Maple [A] time = 0.027, size = 60, normalized size = 0.6

$$\frac{1}{a^2} \left(-\frac{\sin(2 \arcsin(ax))}{6 (\arcsin(ax))^3} - \frac{\cos(2 \arcsin(ax))}{6 (\arcsin(ax))^2} + \frac{\sin(2 \arcsin(ax))}{3 \arcsin(ax)} - \frac{2 \operatorname{Ci}(2 \arcsin(ax))}{3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/arcsin(a*x)^4,x)

[Out] 1/a^2*(-1/6/arcsin(a*x)^3*sin(2*arcsin(a*x))-1/6/arcsin(a*x)^2*cos(2*arcsin(a*x))+1/3/arcsin(a*x)*sin(2*arcsin(a*x))-2/3*Ci(2*arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{4a^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3 \int \frac{(2a^2x^2-1)\sqrt{ax+1}\sqrt{-ax+1}}{(a^3x^2-a)\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - 2 \left(2ax \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^2 - ax \right)}{6a^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^4,x, algorithm="maxima")

[Out] $-1/6*(6*a^2*\arctan2(a*x, \sqrt{a*x + 1}*\sqrt{-a*x + 1})^3*\int (2/3*(2*a^2*x^2 - 1)*\sqrt{a*x + 1}*\sqrt{-a*x + 1}/((a^3*x^2 - a)*\arctan2(a*x, \sqrt{a*x + 1}*\sqrt{-a*x + 1})), x) - 2*(2*a*x*\arctan2(a*x, \sqrt{a*x + 1}*\sqrt{-a*x + 1})^2 - a*x)*\sqrt{a*x + 1}*\sqrt{-a*x + 1} - (2*a^2*x^2 - 1)*\arctan2(a*x, \sqrt{a*x + 1}*\sqrt{-a*x + 1})/(a^2*\arctan2(a*x, \sqrt{a*x + 1}*\sqrt{-a*x + 1})^3)$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\arcsin(ax)^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^4,x, algorithm="fricas")

[Out] integral(x/arcsin(a*x)^4, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\arcsin^4(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/asin(a*x)**4,x)

[Out] Integral(x/asin(a*x)**4, x)

Giac [A] time = 1.2573, size = 124, normalized size = 1.28

$$\frac{2\sqrt{-a^2x^2+1}x}{3a\arcsin(ax)} - \frac{2\operatorname{Ci}(2\arcsin(ax))}{3a^2} - \frac{\sqrt{-a^2x^2+1}x}{3a\arcsin(ax)^3} + \frac{a^2x^2-1}{3a^2\arcsin(ax)^2} + \frac{1}{6a^2\arcsin(ax)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^4,x, algorithm="giac")

[Out] $2/3*\sqrt{-a^2*x^2 + 1}*x/(a*\arcsin(a*x)) - 2/3*\operatorname{cos_integral}(2*\arcsin(a*x))/a^2 - 1/3*\sqrt{-a^2*x^2 + 1}*x/(a*\arcsin(a*x)^3) + 1/3*(a^2*x^2 - 1)/(a^2*\arcsin(a*x)^2) + 1/6/(a^2*\arcsin(a*x)^2)$

$$3.71 \quad \int \frac{1}{\sin^{-1}(ax)^4} dx$$

Optimal. Leaf size=78

$$\frac{\sqrt{1-a^2x^2}}{6a \sin^{-1}(ax)} - \frac{\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} + \frac{\text{Si}(\sin^{-1}(ax))}{6a} + \frac{x}{6 \sin^{-1}(ax)^2}$$

[Out] $-\text{Sqrt}[1 - a^2*x^2]/(3*a*\text{ArcSin}[a*x]^3) + x/(6*\text{ArcSin}[a*x]^2) + \text{Sqrt}[1 - a^2*x^2]/(6*a*\text{ArcSin}[a*x]) + \text{SinIntegral}[\text{ArcSin}[a*x]]/(6*a)$

Rubi [A] time = 0.152712, antiderivative size = 78, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4621, 4719, 4723, 3299}

$$\frac{\sqrt{1-a^2x^2}}{6a \sin^{-1}(ax)} - \frac{\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} + \frac{\text{Si}(\sin^{-1}(ax))}{6a} + \frac{x}{6 \sin^{-1}(ax)^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^{-4}, x]$

[Out] $-\text{Sqrt}[1 - a^2*x^2]/(3*a*\text{ArcSin}[a*x]^3) + x/(6*\text{ArcSin}[a*x]^2) + \text{Sqrt}[1 - a^2*x^2]/(6*a*\text{ArcSin}[a*x]) + \text{SinIntegral}[\text{ArcSin}[a*x]]/(6*a)$

Rule 4621

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n, x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{n+1})/(b*c*(n+1)), x] + \text{Dist}[c/(b*(n+1)), \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{n+1})/\text{Sqrt}[1 - c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c\}, x \ \&\& \text{LtQ}[n, -1]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n*(f*x)^m/\text{Sqrt}[d + e*x^2], x_Symbol] \rightarrow \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{n+1}/(b*c*\text{Sqrt}[d + e*x^2]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d + e*x^2]*(n+1)), \text{Int}[(f*x)^{m-1}*(a + b*\text{ArcSin}[c*x])^{n+1}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x \ \&\& \text{EqQ}[c^2*d + e, 0] \ \&\& \text{LtQ}[n, -1] \ \&\& \text{GtQ}[d, 0]$

Rule 4723

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n*(d + e*x^2)^p, x_Symbol] \rightarrow \text{Dist}[d^p/c^{m+1}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x]^{2*p+1}, x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c, d, e, n\}, x \ \&\& \text{EqQ}[c^2*d + e, 0] \ \&\& \text{IntegerQ}[2*p] \ \&\& \text{GtQ}[p, -1] \ \&\& \text{IGtQ}[m, 0] \ \&\& (\text{IntegerQ}[p] \ || \ \text{GtQ}[d, 0])$

Rule 3299

$\text{Int}[\text{Sin}[(e + f*x)/(c + d*x)], x_Symbol] \rightarrow \text{Simp}[\text{SinIntegral}[e + f*x]/d, x] /; \text{FreeQ}\{c, d, e, f\}, x \ \&\& \text{EqQ}[d*e - c*f, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sin^{-1}(ax)^4} dx &= -\frac{\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} - \frac{1}{3}a \int \frac{x}{\sqrt{1-a^2x^2} \sin^{-1}(ax)^3} dx \\
&= -\frac{\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} + \frac{x}{6 \sin^{-1}(ax)^2} - \frac{1}{6} \int \frac{1}{\sin^{-1}(ax)^2} dx \\
&= -\frac{\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} + \frac{x}{6 \sin^{-1}(ax)^2} + \frac{\sqrt{1-a^2x^2}}{6a \sin^{-1}(ax)} + \frac{1}{6}a \int \frac{x}{\sqrt{1-a^2x^2} \sin^{-1}(ax)} dx \\
&= -\frac{\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} + \frac{x}{6 \sin^{-1}(ax)^2} + \frac{\sqrt{1-a^2x^2}}{6a \sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\sin(x)}{x} dx, x, \sin^{-1}(ax)\right)}{6a} \\
&= -\frac{\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^3} + \frac{x}{6 \sin^{-1}(ax)^2} + \frac{\sqrt{1-a^2x^2}}{6a \sin^{-1}(ax)} + \frac{\text{Si}(\sin^{-1}(ax))}{6a}
\end{aligned}$$

Mathematica [A] time = 0.0621412, size = 70, normalized size = 0.9

$$\frac{-2\sqrt{1-a^2x^2} + \sqrt{1-a^2x^2} \sin^{-1}(ax)^2 + \sin^{-1}(ax)^3 \text{Si}(\sin^{-1}(ax)) + ax \sin^{-1}(ax)}{6a \sin^{-1}(ax)^3}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^(-4),x]

[Out] (-2*Sqrt[1 - a^2*x^2] + a*x*ArcSin[a*x] + Sqrt[1 - a^2*x^2]*ArcSin[a*x]^2 + ArcSin[a*x]^3*SinIntegral[ArcSin[a*x]])/(6*a*ArcSin[a*x]^3)

Maple [A] time = 0.023, size = 63, normalized size = 0.8

$$\frac{1}{a} \left(-\frac{1}{3 (\arcsin(ax))^3} \sqrt{-a^2x^2 + 1} + \frac{ax}{6 (\arcsin(ax))^2} + \frac{1}{6 \arcsin(ax)} \sqrt{-a^2x^2 + 1} + \frac{\text{Si}(\arcsin(ax))}{6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x)^4,x)

[Out] 1/a*(-1/3/arcsin(a*x)^3*(-a^2*x^2+1)^(1/2)+1/6*a*x/arcsin(a*x)^2+1/6/arcsin(a*x)*(-a^2*x^2+1)^(1/2)+1/6*Si(arcsin(a*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{a^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3 \int \frac{\sqrt{ax+1}\sqrt{-ax+1}x}{(a^2x^2-1)\arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - ax \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1}) - \sqrt{ax+1}}{6a \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^4,x, algorithm="maxima")

[Out] -1/6*(6*a^2*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3*integrate(1/6*sqrt(a*x + 1)*sqrt(-a*x + 1)*x/((a^2*x^2 - 1)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-

```
a*x + 1))), x) - a*x*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)) - sqrt(a*x
+ 1)*sqrt(-a*x + 1)*(arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2 - 2))/(a*
arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3)
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{\arcsin(ax)^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/arcsin(a*x)^4,x, algorithm="fricas")
```

```
[Out] integral(arcsin(a*x)^(-4), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\text{asin}^4(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/asin(a*x)**4,x)
```

```
[Out] Integral(asin(a*x)**(-4), x)
```

Giac [A] time = 1.2452, size = 89, normalized size = 1.14

$$\frac{\text{Si}(\arcsin(ax))}{6a} + \frac{x}{6\arcsin(ax)^2} + \frac{\sqrt{-a^2x^2+1}}{6a\arcsin(ax)} - \frac{\sqrt{-a^2x^2+1}}{3a\arcsin(ax)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/arcsin(a*x)^4,x, algorithm="giac")
```

```
[Out] 1/6*sin_integral(arcsin(a*x))/a + 1/6*x/arcsin(a*x)^2 + 1/6*sqrt(-a^2*x^2 +
1)/(a*arcsin(a*x)) - 1/3*sqrt(-a^2*x^2 + 1)/(a*arcsin(a*x)^3)
```


$$3.72 \quad \int \frac{1}{x \sin^{-1}(ax)^4} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x \sin^{-1}(ax)^4}, x\right)$$

[Out] Unintegrable[1/(x*ArcSin[a*x]^4), x]

Rubi [A] time = 0.0124201, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x \sin^{-1}(ax)^4} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*ArcSin[a*x]^4), x]

[Out] Defer[Int][1/(x*ArcSin[a*x]^4), x]

Rubi steps

$$\int \frac{1}{x \sin^{-1}(ax)^4} dx = \int \frac{1}{x \sin^{-1}(ax)^4} dx$$

Mathematica [A] time = 2.33967, size = 0, normalized size = 0.

$$\int \frac{1}{x \sin^{-1}(ax)^4} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*ArcSin[a*x]^4), x]

[Out] Integrate[1/(x*ArcSin[a*x]^4), x]

Maple [A] time = 0.075, size = 0, normalized size = 0.

$$\int \frac{1}{x (\arcsin(ax))^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x)^4, x)

[Out] int(1/x/arcsin(a*x)^4, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{2 a^3 x^3 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3 \int \frac{(2 a^2 x^2 - 3)\sqrt{ax+1}\sqrt{-ax+1}}{(a^5 x^6 - a^3 x^4) \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - ax \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right) + 2 \left(a^2 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})\right)^2}{6 a^3 x^3 \arctan\left(ax, \sqrt{ax+1}\sqrt{-ax+1}\right)^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^4,x, algorithm="maxima")

[Out] -1/6*(6*a^3*x^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3*integrate(1/3*(2*a^2*x^2 - 3)*sqrt(a*x + 1)*sqrt(-a*x + 1)/((a^5*x^6 - a^3*x^4)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))), x) - a*x*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1)) + 2*(a^2*x^2 + arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2)*sqrt(a*x + 1)*sqrt(-a*x + 1)/(a^3*x^3*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x \arcsin(ax)^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^4,x, algorithm="fricas")

[Out] integral(1/(x*arcsin(a*x)^4), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \operatorname{asin}^4(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/asin(a*x)**4,x)

[Out] Integral(1/(x*asin(a*x)**4), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^4,x, algorithm="giac")

[Out] integrate(1/(x*arcsin(a*x)^4), x)

$$3.73 \quad \int \frac{1}{x^2 \sin^{-1}(ax)^4} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{1}{x^2 \sin^{-1}(ax)^4}, x\right)$$

[Out] Unintegrable[1/(x^2*ArcSin[a*x]^4), x]

Rubi [A] time = 0.0140271, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2 \sin^{-1}(ax)^4} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*ArcSin[a*x]^4), x]

[Out] Defer[Int][1/(x^2*ArcSin[a*x]^4), x]

Rubi steps

$$\int \frac{1}{x^2 \sin^{-1}(ax)^4} dx = \int \frac{1}{x^2 \sin^{-1}(ax)^4} dx$$

Mathematica [A] time = 17.8693, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sin^{-1}(ax)^4} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*ArcSin[a*x]^4), x]

[Out] Integrate[1/(x^2*ArcSin[a*x]^4), x]

Maple [A] time = 0.118, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (\arcsin(ax))^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/arcsin(a*x)^4, x)

[Out] int(1/x^2/arcsin(a*x)^4, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$a^3 x^4 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3 \int \frac{(a^4 x^4 - 20 a^2 x^2 + 24) \sqrt{ax+1} \sqrt{-ax+1}}{(a^5 x^7 - a^3 x^5) \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})} dx - \left(2 a^2 x^2 - (a^2 x^2 - 6) \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1}) \right) \frac{6 a^3 x^4 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3}{6 a^3 x^4 \arctan(ax, \sqrt{ax+1}\sqrt{-ax+1})^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^4,x, algorithm="maxima")

[Out] 1/6*(6*a^3*x^4*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3*integrate(1/6*(a^4*x^4 - 20*a^2*x^2 + 24)*sqrt(a*x + 1)*sqrt(-a*x + 1)/((a^5*x^7 - a^3*x^5)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))), x) - (2*a^2*x^2 - (a^2*x^2 - 6)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^2)*sqrt(a*x + 1)*sqrt(-a*x + 1) - (a^3*x^3 - 2*a*x)*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))/(a^3*x^4*arctan2(a*x, sqrt(a*x + 1)*sqrt(-a*x + 1))^3)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{x^2 \arcsin(ax)^4}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^4,x, algorithm="fricas")

[Out] integral(1/(x^2*arcsin(a*x)^4), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin^4(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/asin(a*x)**4,x)

[Out] Integral(1/(x**2*asin(a*x)**4), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \arcsin(ax)^4} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/arcsin(a*x)^4,x, algorithm="giac")

[Out] integrate(1/(x^2*arcsin(a*x)^4), x)

3.74 $\int x^4 \sqrt{\sin^{-1}(ax)} dx$

Optimal. Leaf size=121

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^5} + \frac{\sqrt{\frac{\pi}{6}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{16a^5} - \frac{\sqrt{\frac{\pi}{10}} S\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{80a^5} + \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)}$$

```
[Out] (x^5*Sqrt[ArcSin[a*x]])/5 - (Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^5) + (Sqrt[Pi/6]*FresnelS[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(16*a^5) - (Sqrt[Pi/10]*FresnelS[Sqrt[10/Pi]*Sqrt[ArcSin[a*x]]])/(80*a^5)
```

Rubi [A] time = 0.241509, antiderivative size = 121, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4629, 4723, 3312, 3305, 3351}

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^5} + \frac{\sqrt{\frac{\pi}{6}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{16a^5} - \frac{\sqrt{\frac{\pi}{10}} S\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{80a^5} + \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

```
[In] Int[x^4*Sqrt[ArcSin[a*x]], x]
```

```
[Out] (x^5*Sqrt[ArcSin[a*x]])/5 - (Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^5) + (Sqrt[Pi/6]*FresnelS[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(16*a^5) - (Sqrt[Pi/10]*FresnelS[Sqrt[10/Pi]*Sqrt[ArcSin[a*x]]])/(80*a^5)
```

Rule 4629

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c^n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]
```

Rule 4723

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.)*((d_.) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_)^(m_.))*sin[(e_.) + (f_.)*(x_)^(n_.)], x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))²], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int x^4 \sqrt{\sin^{-1}(ax)} dx &= \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)} - \frac{1}{10} a \int \frac{x^5}{\sqrt{1 - a^2 x^2} \sqrt{\sin^{-1}(ax)}} dx \\ &= \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin^5(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{10a^5} \\ &= \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \left(\frac{5 \sin(x)}{8\sqrt{x}} - \frac{5 \sin(3x)}{16\sqrt{x}} + \frac{\sin(5x)}{16\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{10a^5} \\ &= \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin(5x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{160a^5} + \frac{\text{Subst}\left(\int \frac{\sin(3x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{32a^5} - \frac{\text{Subst}\left(\int \frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{16a^5} \\ &= \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \sin(5x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{80a^5} + \frac{\text{Subst}\left(\int \sin(3x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{16a^5} - \frac{\text{Subst}\left(\int \sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{16a^5} \\ &= \frac{1}{5} x^5 \sqrt{\sin^{-1}(ax)} - \frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^5} + \frac{\sqrt{\frac{\pi}{6}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{16a^5} - \frac{\sqrt{\frac{\pi}{10}} S\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{80a^5} \end{aligned}$$

Mathematica [C] time = 0.0990047, size = 204, normalized size = 1.69

$$i \sqrt{\sin^{-1}(ax)} \left(-150 \sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, -i \sin^{-1}(ax)\right) + 150 \sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, i \sin^{-1}(ax)\right) + 25 \sqrt{3} \sqrt{i \sin^{-1}(ax)} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x⁴*Sqrt[ArcSin[a*x]], x]

[Out] ((I/2400)*Sqrt[ArcSin[a*x]]*(-150*Sqrt[I*ArcSin[a*x]]*Gamma[3/2, (-I)*ArcSin[a*x]] + 150*Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, I*ArcSin[a*x]] + 25*Sqrt[3]*Sqrt[I*ArcSin[a*x]]*Gamma[3/2, (-3*I)*ArcSin[a*x]] - 25*Sqrt[3]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (3*I)*ArcSin[a*x]] - 3*Sqrt[5]*Sqrt[I*ArcSin[a*x]]*Gamma[3/2, (-5*I)*ArcSin[a*x]] + 3*Sqrt[5]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (5*I)*ArcSin[a*x]]))/(a⁵*Sqrt[ArcSin[a*x]²])

Maple [A] time = 0.074, size = 143, normalized size = 1.2

$$-\frac{1}{2400 a^5} \left(3 \sqrt{5} \sqrt{2} \sqrt{\arcsin(ax)} \sqrt{\pi} \text{FresnelS}\left(\frac{\sqrt{5} \sqrt{2} \sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) - 25 \sqrt{3} \sqrt{2} \sqrt{\arcsin(ax)} \sqrt{\pi} \text{FresnelS}\left(\frac{\sqrt{3} \sqrt{2} \sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x⁴*arcsin(a*x)^(1/2), x)

[Out] -1/2400/a⁵/arcsin(a*x)^(1/2)*(3*5^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*5^(1/2)*arcsin(a*x)^(1/2))-25*3^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*3^(1/2)*arcsin(a*x)^(1/2)

))+150*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))-300*a*x*arcsin(a*x)+150*arcsin(a*x)*sin(3*arcsin(a*x))-30*arcsin(a*x)*sin(5*arcsin(a*x)))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^(1/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^4 \sqrt{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4*asin(a*x)**(1/2),x)

[Out] Integral(x**4*sqrt(asin(a*x)), x)

Giac [C] time = 1.3452, size = 333, normalized size = 2.75

$$-\frac{(i-1)\sqrt{10}\sqrt{\pi}\operatorname{erf}\left(\left(\frac{1}{2}i-\frac{1}{2}\right)\sqrt{10}\sqrt{\arcsin(ax)}\right)}{3200a^5} + \frac{(i+1)\sqrt{10}\sqrt{\pi}\operatorname{erf}\left(-\left(\frac{1}{2}i+\frac{1}{2}\right)\sqrt{10}\sqrt{\arcsin(ax)}\right)}{3200a^5} + \frac{(i-1)\sqrt{6}\sqrt{7}}{3200a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4*arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] $-(1/3200*I - 1/3200)*\sqrt{10}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{10}*\sqrt{\arcsin(a*x)})/a^5 + (1/3200*I + 1/3200)*\sqrt{10}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{10}*\sqrt{\arcsin(a*x)})/a^5 + (1/384*I - 1/384)*\sqrt{6}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{6}*\sqrt{\arcsin(a*x)})/a^5 - (1/384*I + 1/384)*\sqrt{6}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{6}*\sqrt{\arcsin(a*x)})/a^5 - (1/64*I - 1/64)*\sqrt{6}*\sqrt{7}/a^5$

$$\begin{aligned}
& (2) \sqrt{\pi} \operatorname{erf}\left(\frac{1}{2}i - \frac{1}{2}\sqrt{2}\sqrt{\arcsin(ax)}\right)/a^5 + (1/64i + 1/64)\sqrt{2}\sqrt{\pi} \operatorname{erf}\left(-\frac{1}{2}i + \frac{1}{2}\sqrt{2}\sqrt{\arcsin(ax)}\right)/a^5 - 1/160i\sqrt{\arcsin(ax)}e^{(5i\arcsin(ax))}/a^5 + 1/32i\sqrt{\arcsin(ax)}e^{(3i\arcsin(ax))}/a^5 - 1/16i\sqrt{\arcsin(ax)}e^{(i\arcsin(ax))}/a^5 + 1/16i\sqrt{\arcsin(ax)}e^{(-i\arcsin(ax))}/a^5 - 1/32i\sqrt{\arcsin(ax)}e^{(-3i\arcsin(ax))}/a^5 + 1/160i\sqrt{\arcsin(ax)}e^{(-5i\arcsin(ax))}/a^5
\end{aligned}$$

3.75 $\int x^3 \sqrt{\sin^{-1}(ax)} dx$

Optimal. Leaf size=95

$$-\frac{\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(2\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{64a^4} + \frac{\sqrt{\pi} \operatorname{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{16a^4} - \frac{3\sqrt{\sin^{-1}(ax)}}{32a^4} + \frac{1}{4}x^4 \sqrt{\sin^{-1}(ax)}$$

[Out] $(-3*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/(32*a^4) + (x^4*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/4 - (\operatorname{Sqrt}[\pi/2]*\operatorname{FresnelC}[2*\operatorname{Sqrt}[2/\pi]*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/(64*a^4) + (\operatorname{Sqrt}[\pi]*\operatorname{FresnelC}[(2*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/\operatorname{Sqrt}[\pi]])/(16*a^4)$

Rubi [A] time = 0.189416, antiderivative size = 95, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4629, 4723, 3312, 3304, 3352}

$$-\frac{\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(2\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{64a^4} + \frac{\sqrt{\pi} \operatorname{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{16a^4} - \frac{3\sqrt{\sin^{-1}(ax)}}{32a^4} + \frac{1}{4}x^4 \sqrt{\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^3*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]], x]$

[Out] $(-3*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/(32*a^4) + (x^4*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/4 - (\operatorname{Sqrt}[\pi/2]*\operatorname{FresnelC}[2*\operatorname{Sqrt}[2/\pi]*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/(64*a^4) + (\operatorname{Sqrt}[\pi]*\operatorname{FresnelC}[(2*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/\operatorname{Sqrt}[\pi]])/(16*a^4)$

Rule 4629

$\operatorname{Int}[(a + \operatorname{ArcSin}(c*x))*b]^n * x^m, x_{\text{Symbol}}] \rightarrow \operatorname{Simp}[x^{m+1}*(a + b*\operatorname{ArcSin}[c*x])^n / (m+1), x] - \operatorname{Dist}[(b*c*n)/(m+1), \operatorname{Int}[x^{m+1}*(a + b*\operatorname{ArcSin}[c*x])^{n-1}]/\operatorname{Sqrt}[1 - c^2*x^2], x], x] /;$ $\operatorname{FreeQ}\{a, b, c\}, x$ && $\operatorname{IGtQ}[m, 0]$ && $\operatorname{GtQ}[n, 0]$

Rule 4723

$\operatorname{Int}[(a + \operatorname{ArcSin}(c*x))*b]^n * x^m * (d + e*x)^2)^p, x_{\text{Symbol}}] \rightarrow \operatorname{Dist}[d^p/c^{m+1}, \operatorname{Subst}[\operatorname{Int}[(a + b*x)^n * \operatorname{Sin}[x]^m * \operatorname{Cos}[x]^{2*p+1}], x], x, \operatorname{ArcSin}[c*x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, e, n\}, x$ && $\operatorname{EqQ}[c^2*d + e, 0]$ && $\operatorname{IntegerQ}[2*p]$ && $\operatorname{GtQ}[p, -1]$ && $\operatorname{IGtQ}[m, 0]$ && $(\operatorname{IntegerQ}[p] \parallel \operatorname{GtQ}[d, 0])$

Rule 3312

$\operatorname{Int}[(c + d*x)^m * \operatorname{sin}[e + f*x]^n, x_{\text{Symbol}}] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigReduce}[(c + d*x)^m, \operatorname{Sin}[e + f*x]^n, x], x] /;$ $\operatorname{FreeQ}\{c, d, e, f, m\}, x$ && $\operatorname{IGtQ}[n, 1]$ && $(\operatorname{!RationalQ}[m] \parallel (\operatorname{GeQ}[m, -1] \&\& \operatorname{LtQ}[m, 1]))$

Rule 3304

$\operatorname{Int}[\operatorname{sin}[\pi/2 + (e + f*x)]/\operatorname{Sqrt}[c + d*x], x_{\text{Symbol}}] \rightarrow \operatorname{Dist}[2/d, \operatorname{Subst}[\operatorname{Int}[\operatorname{Cos}[(f*x^2)/d], x], x, \operatorname{Sqrt}[c + d*x], x] /;$ $\operatorname{FreeQ}\{c, d, e, f\}, x$ && $\operatorname{ComplexFreeQ}[f]$ && $\operatorname{EqQ}[d*e - c*f, 0]$

Rule 3352

Int[Cos[(d_.)*(e_.) + (f_.)*(x_)]^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
 \int x^3 \sqrt{\sin^{-1}(ax)} dx &= \frac{1}{4} x^4 \sqrt{\sin^{-1}(ax)} - \frac{1}{8} a \int \frac{x^4}{\sqrt{1 - a^2 x^2} \sqrt{\sin^{-1}(ax)}} dx \\
 &= \frac{1}{4} x^4 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin^4(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^4} \\
 &= \frac{1}{4} x^4 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \left(\frac{3}{8\sqrt{x}} - \frac{\cos(2x)}{2\sqrt{x}} + \frac{\cos(4x)}{8\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{8a^4} \\
 &= -\frac{3\sqrt{\sin^{-1}(ax)}}{32a^4} + \frac{1}{4} x^4 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\cos(4x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{64a^4} + \frac{\text{Subst}\left(\int \frac{\cos(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{16a^4} \\
 &= -\frac{3\sqrt{\sin^{-1}(ax)}}{32a^4} + \frac{1}{4} x^4 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \cos(4x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{32a^4} + \frac{\text{Subst}\left(\int \cos(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{8a^4} \\
 &= -\frac{3\sqrt{\sin^{-1}(ax)}}{32a^4} + \frac{1}{4} x^4 \sqrt{\sin^{-1}(ax)} - \frac{\sqrt{\frac{\pi}{2}} C\left(2\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{64a^4} + \frac{\sqrt{\pi} C\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{16a^4}
 \end{aligned}$$

Mathematica [C] time = 0.0610767, size = 138, normalized size = 1.45

$$\frac{\sqrt{\sin^{-1}(ax)} \left(-4\sqrt{2}\sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, -2i \sin^{-1}(ax)\right) - 4\sqrt{2}\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, 2i \sin^{-1}(ax)\right) + \sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, -2i \sin^{-1}(ax)\right) + \sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, 2i \sin^{-1}(ax)\right) \right)}{128a^4 \sqrt{\sin^{-1}(ax)}^2}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3*Sqrt[ArcSin[a*x]], x]

[Out] (Sqrt[ArcSin[a*x]]*(-4*Sqrt[2]*Sqrt[I*ArcSin[a*x]]*Gamma[3/2, (-2*I)*ArcSin[a*x]] - 4*Sqrt[2]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (2*I)*ArcSin[a*x]] + Sqrt[I*ArcSin[a*x]]*Gamma[3/2, (-4*I)*ArcSin[a*x]] + Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (4*I)*ArcSin[a*x]]))/(128*a^4*Sqrt[ArcSin[a*x]^2])

Maple [A] time = 0.049, size = 91, normalized size = 1.

$$\frac{1}{128a^4} \left(-\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\text{FresnelC}\left(2\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + 4\arcsin(ax)\cos(4\arcsin(ax)) - 16\arcsin(ax)\cos(2\arcsin(ax)) + 8\arcsin(ax)\cos(2\arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x)^(1/2), x)

[Out] 1/128/a^4/arcsin(a*x)^(1/2)*(-2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2*2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))+4*arcsin(a*x)*cos(4*arcsin(a*x))-16*arcsin(a*x)*cos(2*arcsin(a*x))+8*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2*arcsin

$(a*x)^{(1/2)}/\text{Pi}^{(1/2)})$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(1/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \sqrt{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x)**(1/2),x)

[Out] Integral(x**3*sqrt(asin(a*x)), x)

Giac [C] time = 1.43165, size = 207, normalized size = 2.18

$$\frac{(i+1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left((i-1)\sqrt{2}\sqrt{\arcsin(ax)}\right)}{512a^4} - \frac{(i-1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-(i+1)\sqrt{2}\sqrt{\arcsin(ax)}\right)}{512a^4} - \frac{(i+1)\sqrt{\pi}\operatorname{erf}\left((i-1)\sqrt{\arcsin(ax)}\right)}{64a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] $(1/512*I + 1/512)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}((I - 1)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a^4 - (1/512*I - 1/512)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-(I + 1)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a^4 - (1/64*I + 1/64)*\sqrt{\pi}*\operatorname{erf}((I - 1)*\sqrt{\arcsin(a*x)})/a^4 + (1/64*I - 1/64)*\sqrt{\pi}*\operatorname{erf}(-(I + 1)*\sqrt{\arcsin(a*x)})/a^4 + 1/64*\sqrt{\arcsin(a*x)}*e^{(4*I*\arcsin(a*x))}/a^4 - 1/16*\sqrt{\arcsin(a*x)}*e^{(2*I*\arcsin(a*x))}/a^4 - 1/16*\sqrt{\arcsin(a*x)}*e^{(-2*I*\arcsin(a*x))}/a^4 + 1/64*\sqrt{\arcsin(a*x)}*e^{(-4*I*\arcsin(a*x))}/a^4$

3.76 $\int x^2 \sqrt{\sin^{-1}(ax)} dx$

Optimal. Leaf size=86

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^3} + \frac{\sqrt{\frac{\pi}{6}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{12a^3} + \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)}$$

[Out] (x^3*Sqrt[ArcSin[a*x]])/3 - (Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4*a^3) + (Sqrt[Pi/6]*FresnelS[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(12*a^3)

Rubi [A] time = 0.180875, antiderivative size = 86, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4629, 4723, 3312, 3305, 3351}

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^3} + \frac{\sqrt{\frac{\pi}{6}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{12a^3} + \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[x^2*Sqrt[ArcSin[a*x]],x]

[Out] (x^3*Sqrt[ArcSin[a*x]])/3 - (Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4*a^3) + (Sqrt[Pi/6]*FresnelS[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(12*a^3)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*(x_)^(m_.)*((d_.) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*(e_.) + (f_.)*(x_)^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int x^2 \sqrt{\sin^{-1}(ax)} dx &= \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)} - \frac{1}{6} a \int \frac{x^3}{\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}} dx \\ &= \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin^3(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{6a^3} \\ &= \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \left(\frac{3\sin(x)}{4\sqrt{x}} - \frac{\sin(3x)}{4\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{6a^3} \\ &= \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\sin(3x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{24a^3} - \frac{\text{Subst}\left(\int \frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^3} \\ &= \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \sin(3x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{12a^3} - \frac{\text{Subst}\left(\int \sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^3} \\ &= \frac{1}{3} x^3 \sqrt{\sin^{-1}(ax)} - \frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^3} + \frac{\sqrt{\frac{\pi}{6}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{12a^3} \end{aligned}$$

Mathematica [C] time = 0.0495305, size = 126, normalized size = 1.47

$$\frac{9\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, -i \sin^{-1}(ax)\right) + 9\sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, i \sin^{-1}(ax)\right) - \sqrt{3} \left(\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, -i \sin^{-1}(ax)\right) + \sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, i \sin^{-1}(ax)\right)\right)}{72a^3 \sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2*Sqrt[ArcSin[a*x]], x]

[Out] (9*Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (-I)*ArcSin[a*x]] + 9*Sqrt[I*ArcSin[a*x]]*Gamma[3/2, I*ArcSin[a*x]] - Sqrt[3]*(Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (-3*I)*ArcSin[a*x]] + Sqrt[I*ArcSin[a*x]]*Gamma[3/2, (3*I)*ArcSin[a*x]]))/ (72*a^3*Sqrt[ArcSin[a*x]])

Maple [A] time = 0.044, size = 96, normalized size = 1.1

$$-\frac{1}{72a^3} \left(-\sqrt{3}\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\text{FresnelS}\left(\frac{\sqrt{3}\sqrt{2}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right) + 9\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\text{FresnelS}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*arcsin(a*x)^(1/2), x)

[Out] -1/72/a^3/arcsin(a*x)^(1/2)*(-3^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*3^(1/2)*arcsin(a*x)^(1/2))+9*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))-18*a*x*arcsin(a*x)+6*arcsin(a*x)*sin(3*arcsin(a*x))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^(1/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \sqrt{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*asin(a*x)**(1/2),x)

[Out] Integral(x**2*sqrt(asin(a*x)), x)

Giac [C] time = 1.48785, size = 223, normalized size = 2.59

$$\frac{(i-1) \sqrt{6} \sqrt{\pi} \operatorname{erf}\left(\left(\frac{1}{2}i - \frac{1}{2}\right) \sqrt{6} \sqrt{\arcsin(ax)}\right)}{288 a^3} - \frac{(i+1) \sqrt{6} \sqrt{\pi} \operatorname{erf}\left(-\left(\frac{1}{2}i + \frac{1}{2}\right) \sqrt{6} \sqrt{\arcsin(ax)}\right)}{288 a^3} - \frac{(i-1) \sqrt{2} \sqrt{\pi} \operatorname{erf}\left(\left(\frac{1}{2}i\right) \sqrt{2} \sqrt{\arcsin(ax)}\right)}{32 a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] (1/288*I - 1/288)*sqrt(6)*sqrt(pi)*erf((1/2*I - 1/2)*sqrt(6)*sqrt(arcsin(a*x)))/a^3 - (1/288*I + 1/288)*sqrt(6)*sqrt(pi)*erf(-(1/2*I + 1/2)*sqrt(6)*sqrt(arcsin(a*x)))/a^3 - (1/32*I - 1/32)*sqrt(2)*sqrt(pi)*erf((1/2*I - 1/2)*sqrt(2)*sqrt(arcsin(a*x)))/a^3 + (1/32*I + 1/32)*sqrt(2)*sqrt(pi)*erf(-(1/2*I + 1/2)*sqrt(2)*sqrt(arcsin(a*x)))/a^3 + 1/24*I*sqrt(arcsin(a*x))*e^(3*I*arcsin(a*x))/a^3 - 1/8*I*sqrt(arcsin(a*x))*e^(I*arcsin(a*x))/a^3 + 1/8*I*sqrt(arcsin(a*x))*e^(-I*arcsin(a*x))/a^3 - 1/24*I*sqrt(arcsin(a*x))*e^(-3*I*arcsin(a*x))/a^3

3.77 $\int x\sqrt{\sin^{-1}(ax)} dx$

Optimal. Leaf size=59

$$\frac{\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{8a^2} - \frac{\sqrt{\sin^{-1}(ax)}}{4a^2} + \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)}$$

[Out] $-\text{Sqrt}[\text{ArcSin}[a*x]]/(4*a^2) + (x^2*\text{Sqrt}[\text{ArcSin}[a*x]])/2 + (\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(8*a^2)$

Rubi [A] time = 0.150785, antiderivative size = 59, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4629, 4723, 3312, 3304, 3352}

$$\frac{\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{8a^2} - \frac{\sqrt{\sin^{-1}(ax)}}{4a^2} + \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{Sqrt}[\text{ArcSin}[a*x]], x]$

[Out] $-\text{Sqrt}[\text{ArcSin}[a*x]]/(4*a^2) + (x^2*\text{Sqrt}[\text{ArcSin}[a*x]])/2 + (\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(8*a^2)$

Rule 4629

$\text{Int}[(c + \text{ArcSin}[c*x])^n * x^m, x] \rightarrow \text{Simp}[(x^{m+1} * (a + b * \text{ArcSin}[c*x])^n) / (m+1), x] - \text{Dist}[(b*c*n) / (m+1), \text{Int}[(x^{m+1} * (a + b * \text{ArcSin}[c*x])^{n-1}) / \text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4723

$\text{Int}[(c + \text{ArcSin}[c*x])^n * x^m * (d + e*x)^p, x] \rightarrow \text{Dist}[d^p / c^{m+1}, \text{Subst}[\text{Int}[(a + b*x)^n * \text{Sin}[x]^m * \text{Cos}[x]^{2*p+1}, x], x, \text{ArcSin}[c*x]], x] /;$ FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3312

$\text{Int}[(c + d*x)^m * \text{Sin}[e + f*x]^n, x] \rightarrow \text{Int}[\text{ExpandTrigReduce}[(c + d*x)^m, \text{Sin}[e + f*x]^n, x], x] /;$ FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3304

$\text{Int}[\text{Sin}[\text{Pi}/2 + e + f*x] / \text{Sqrt}[c + d*x], x] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Cos}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /;$ FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
 \int x\sqrt{\sin^{-1}(ax)} dx &= \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)} - \frac{1}{4}a \int \frac{x^2}{\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}} dx \\
 &= \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin^2(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{4a^2} \\
 &= \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \left(\frac{1}{2\sqrt{x}} - \frac{\cos(2x)}{2\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{4a^2} \\
 &= -\frac{\sqrt{\sin^{-1}(ax)}}{4a^2} + \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \frac{\cos(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^2} \\
 &= -\frac{\sqrt{\sin^{-1}(ax)}}{4a^2} + \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)} + \frac{\text{Subst}\left(\int \cos(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^2} \\
 &= -\frac{\sqrt{\sin^{-1}(ax)}}{4a^2} + \frac{1}{2}x^2\sqrt{\sin^{-1}(ax)} + \frac{\sqrt{\pi}C\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{8a^2}
 \end{aligned}$$

Mathematica [C] time = 0.021174, size = 81, normalized size = 1.37

$$\frac{\sqrt{\sin^{-1}(ax)}\left(\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{3}{2}, -2i\sin^{-1}(ax)\right) + \sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{3}{2}, 2i\sin^{-1}(ax)\right)\right)}{8\sqrt{2}a^2\sqrt{\sin^{-1}(ax)^2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*Sqrt[ArcSin[a*x]], x]

[Out] -(Sqrt[ArcSin[a*x]]*(Sqrt[I*ArcSin[a*x]]*Gamma[3/2, (-2*I)*ArcSin[a*x]] + Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (2*I)*ArcSin[a*x]]))/(8*Sqrt[2]*a^2*Sqrt[ArcSin[a*x]^2])

Maple [A] time = 0.033, size = 42, normalized size = 0.7

$$\frac{1}{8a^2\sqrt{\pi}}\left(-2\sqrt{\arcsin(ax)}\sqrt{\pi}\cos(2\arcsin(ax)) + \pi\text{FresnelC}\left(2\frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*arcsin(a*x)^(1/2), x)

[Out] 1/8/a^2/Pi^(1/2)*(-2*arcsin(a*x)^(1/2)*Pi^(1/2)*cos(2*arcsin(a*x))+Pi*FresnelC(2*arcsin(a*x)^(1/2)/Pi^(1/2)))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^(1/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x\sqrt{\operatorname{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*asin(a*x)**(1/2),x)

[Out] Integral(x*sqrt(asin(a*x)), x)

Giac [C] time = 1.37763, size = 96, normalized size = 1.63

$$-\frac{(i+1)\sqrt{\pi}\operatorname{erf}\left((i-1)\sqrt{\operatorname{arcsin}(ax)}\right)}{32a^2} + \frac{(i-1)\sqrt{\pi}\operatorname{erf}\left(-(i+1)\sqrt{\operatorname{arcsin}(ax)}\right)}{32a^2} - \frac{\sqrt{\operatorname{arcsin}(ax)}e^{2i\operatorname{arcsin}(ax)}}{8a^2} - \frac{\sqrt{\operatorname{arcsin}(ax)}}{8a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] $-(1/32*I + 1/32)*\sqrt{\pi}*\operatorname{erf}((I - 1)*\sqrt{\operatorname{arcsin}(a*x)})/a^2 + (1/32*I - 1/32)*\sqrt{\pi}*\operatorname{erf}(-(I + 1)*\sqrt{\operatorname{arcsin}(a*x)})/a^2 - 1/8*\sqrt{\operatorname{arcsin}(a*x)}*e^{(2*I*\operatorname{arcsin}(a*x))/a^2} - 1/8*\sqrt{\operatorname{arcsin}(a*x)}*e^{(-2*I*\operatorname{arcsin}(a*x))/a^2}$

3.78 $\int \sqrt{\sin^{-1}(ax)} dx$

Optimal. Leaf size=44

$$x\sqrt{\sin^{-1}(ax)} - \frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a}$$

[Out] x*Sqrt[ArcSin[a*x]] - (Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/a

Rubi [A] time = 0.0896557, antiderivative size = 44, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4619, 4723, 3305, 3351}

$$x\sqrt{\sin^{-1}(ax)} - \frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[ArcSin[a*x]], x]

[Out] x*Sqrt[ArcSin[a*x]] - (Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/a

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*(x_)^(m_.)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
\int \sqrt{\sin^{-1}(ax)} dx &= x\sqrt{\sin^{-1}(ax)} - \frac{1}{2}a \int \frac{x}{\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}} dx \\
&= x\sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{2a} \\
&= x\sqrt{\sin^{-1}(ax)} - \frac{\text{Subst}\left(\int \sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a} \\
&= x\sqrt{\sin^{-1}(ax)} - \frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a}
\end{aligned}$$

Mathematica [C] time = 0.0308365, size = 66, normalized size = 1.5

$$\frac{\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, -i \sin^{-1}(ax)\right) + \sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{3}{2}, i \sin^{-1}(ax)\right)}{2a \sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[Sqrt[ArcSin[a*x]], x]

[Out] (Sqrt[(-I)*ArcSin[a*x]]*Gamma[3/2, (-I)*ArcSin[a*x]] + Sqrt[I*ArcSin[a*x]]*Gamma[3/2, I*ArcSin[a*x]])/(2*a*Sqrt[ArcSin[a*x]])

Maple [A] time = 0.032, size = 49, normalized size = 1.1

$$\frac{1}{2a} \left(-\sqrt{2} \sqrt{\arcsin(ax)} \sqrt{\pi} \text{FresnelS}\left(\frac{\sqrt{2}}{\sqrt{\pi}} \sqrt{\arcsin(ax)}\right) + 2ax \arcsin(ax) \right) \frac{1}{\sqrt{\arcsin(ax)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^(1/2), x)

[Out] 1/2/a/arcsin(a*x)^(1/2)*(-2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))+2*a*x*arcsin(a*x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(1/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{\operatorname{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**(1/2),x)

[Out] Integral(sqrt(asin(a*x)), x)

Giac [C] time = 1.3613, size = 112, normalized size = 2.55

$$-\frac{(i-1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(\left(\frac{1}{2}i-\frac{1}{2}\right)\sqrt{2}\sqrt{\operatorname{asin}(ax)}\right)}{8a} + \frac{(i+1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-\left(\frac{1}{2}i+\frac{1}{2}\right)\sqrt{2}\sqrt{\operatorname{asin}(ax)}\right)}{8a} - \frac{i\sqrt{\operatorname{asin}(ax)}e^{(i\operatorname{asin}(ax))}}{2a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] $-(1/8*I - 1/8)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{2}*\sqrt{\operatorname{asin}(a*x)})/a + (1/8*I + 1/8)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{2}*\sqrt{\operatorname{asin}(a*x)})/a - 1/2*I*\sqrt{\operatorname{asin}(a*x)}*e^{(I*\operatorname{asin}(a*x))}/a + 1/2*I*\sqrt{\operatorname{asin}(a*x)}*e^{(-I*\operatorname{asin}(a*x))}/a$

$$3.79 \quad \int \frac{\sqrt{\sin^{-1}(ax)}}{x} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable} \left(\frac{\sqrt{\sin^{-1}(ax)}}{x}, x \right)$$

[Out] Unintegrable[Sqrt[ArcSin[a*x]]/x, x]

Rubi [A] time = 0.0127665, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sqrt{\sin^{-1}(ax)}}{x} dx$$

Verification is Not applicable to the result.

[In] Int[Sqrt[ArcSin[a*x]]/x,x]

[Out] Defer[Int][Sqrt[ArcSin[a*x]]/x, x]

Rubi steps

$$\int \frac{\sqrt{\sin^{-1}(ax)}}{x} dx = \int \frac{\sqrt{\sin^{-1}(ax)}}{x} dx$$

Mathematica [A] time = 0.398712, size = 0, normalized size = 0.

$$\int \frac{\sqrt{\sin^{-1}(ax)}}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[Sqrt[ArcSin[a*x]]/x,x]

[Out] Integrate[Sqrt[ArcSin[a*x]]/x, x]

Maple [A] time = 0.078, size = 0, normalized size = 0.

$$\int \frac{1}{x} \sqrt{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^(1/2)/x,x)

[Out] `int(arcsin(a*x)^(1/2)/x,x)`

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^(1/2)/x,x, algorithm="maxima")`

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^(1/2)/x,x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{\operatorname{asin}(ax)}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(asin(a*x)**(1/2)/x,x)`

[Out] `Integral(sqrt(asin(a*x))/x, x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{\operatorname{arcsin}(ax)}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(arcsin(a*x)^(1/2)/x,x, algorithm="giac")`

[Out] `integrate(sqrt(arcsin(a*x))/x, x)`

3.80 $\int x^4 \sin^{-1}(ax)^{3/2} dx$

Optimal. Leaf size=214

$$-\frac{3\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^5} + \frac{\sqrt{\frac{\pi}{6}}\text{FresnelC}\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{32a^5} - \frac{3\sqrt{\frac{\pi}{10}}\text{FresnelC}\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{800a^5} + \frac{3x^4\sqrt{1-a^2x^2}\text{ArcSin}[ax]}{50a}$$

```
[Out] (4*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(25*a^5) + (2*x^2*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(25*a^3) + (3*x^4*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(50*a) + (x^5*ArcSin[a*x]^(3/2))/5 - (3*Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(16*a^5) + (Sqrt[Pi/6]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(32*a^5) - (3*Sqrt[Pi/10]*FresnelC[Sqrt[10/Pi]*Sqrt[ArcSin[a*x]]])/(800*a^5)
```

Rubi [A] time = 0.532559, antiderivative size = 282, normalized size of antiderivative = 1.32, number of steps used = 23, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4629, 4707, 4677, 4623, 3304, 3352, 4635, 4406}

$$-\frac{2\sqrt{2\pi}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{25a^5} - \frac{11\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{400a^5} + \frac{3\sqrt{\frac{3\pi}{2}}\text{FresnelC}\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{800a^5} + \frac{\sqrt{\frac{\pi}{6}}\text{FresnelC}\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{800a^5} + \frac{3x^4\sqrt{1-a^2x^2}\text{ArcSin}[ax]}{50a}$$

Antiderivative was successfully verified.

```
[In] Int[x^4*ArcSin[a*x]^(3/2), x]
```

```
[Out] (4*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(25*a^5) + (2*x^2*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(25*a^3) + (3*x^4*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(50*a) + (x^5*ArcSin[a*x]^(3/2))/5 - (11*Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(400*a^5) - (2*Sqrt[2*Pi]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(25*a^5) + (Sqrt[Pi/6]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(50*a^5) + (3*Sqrt[(3*Pi)/2]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(800*a^5) - (3*Sqrt[Pi/10]*FresnelC[Sqrt[10/Pi]*Sqrt[ArcSin[a*x]]])/(800*a^5)
```

Rule 4629

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]
```

Rule 4707

```
Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((f_.)*(x_)^(m_.))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]
```

Rule 4677

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1
```

$-c^2x^2)^{\text{FracPart}[p]}$, $\text{Int}[(1 - c^2x^2)^{p + 1/2}(a + b\text{ArcSin}[cx])^{n-1}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, e, p\}, x] \ \&\& \ \text{EqQ}[c^2d + e, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{NeQ}[p, -1]$

Rule 4623

$\text{Int}[(a + \text{ArcSin}[c(x)](b))^n, x_{\text{Symbol}}] \text{:>} \text{Dist}[1/(bc), \text{Subst}[\text{Int}[x^n \text{Cos}[a/b - x/b], x], x, a + b\text{ArcSin}[cx]], x] /;$ $\text{FreeQ}\{a, b, c, n\}, x]$

Rule 3304

$\text{Int}[\sin[\text{Pi}/2 + (e) + (f)(x)]/\text{Sqrt}[(c) + (d)(x)], x_{\text{Symbol}}] \text{:>} \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Cos}[(fx^2)/d], x], x, \text{Sqrt}[c + dx]], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x] \ \&\& \ \text{ComplexFreeQ}[f] \ \&\& \ \text{EqQ}[d*e - c*f, 0]$

Rule 3352

$\text{Int}[\text{Cos}[(d)((e) + (f)(x))^2], x_{\text{Symbol}}] \text{:>} \text{Simp}[(\text{Sqrt}[\text{Pi}/2] * \text{FresnelC}[\text{Sqrt}[2/\text{Pi}] * \text{Rt}[d, 2] * (e + fx)]) / (f * \text{Rt}[d, 2]), x] /;$ $\text{FreeQ}\{d, e, f\}, x]$

Rule 4635

$\text{Int}[(a + \text{ArcSin}[c(x)](b))^n(x)^m, x_{\text{Symbol}}] \text{:>} \text{Dist}[1/c^{m+1}, \text{Subst}[\text{Int}[(a + bx)^n \text{Sin}[x]^m \text{Cos}[x], x], x, \text{ArcSin}[cx]], x] /;$ $\text{FreeQ}\{a, b, c, n\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 4406

$\text{Int}[\text{Cos}[(a) + (b)(x)]^{p((c) + (d)(x))^m \text{Sin}[(a) + (b)(x)]^n}, x_{\text{Symbol}}] \text{:>} \text{Int}[\text{ExpandTrigReduce}[(c + dx)^m, \text{Sin}[a + bx]^n \text{Cos}[a + bx]^p, x], x] /;$ $\text{FreeQ}\{a, b, c, d, m\}, x] \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{IGtQ}[p, 0]$

Rubi steps

$$\begin{aligned}
\int x^4 \sin^{-1}(ax)^{3/2} dx &= \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2} - \frac{1}{10} (3a) \int \frac{x^5 \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{3x^4 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{50a} + \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2} - \frac{3}{100} \int \frac{x^4}{\sqrt{\sin^{-1}(ax)}} dx - \frac{6}{25a} \int \frac{x^3 \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{2x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^3} + \frac{3x^4 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{50a} + \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst} \left(\int \frac{\cos(x) s}{\sqrt{s}} dx \right)}{1} \\
&= \frac{4\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^3} + \frac{3x^4 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{50a} + \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2} \\
&= \frac{4\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^3} + \frac{3x^4 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{50a} + \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2} \\
&= \frac{4\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^3} + \frac{3x^4 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{50a} + \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2} \\
&= \frac{4\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^3} + \frac{3x^4 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{50a} + \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2} \\
&= \frac{4\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{25a^3} + \frac{3x^4 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{50a} + \frac{1}{5} x^5 \sin^{-1}(ax)^{3/2}
\end{aligned}$$

Mathematica [C] time = 0.0647914, size = 202, normalized size = 0.94

$$\sqrt{\sin^{-1}(ax)} \left(2250 \sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{5}{2}, -i \sin^{-1}(ax)\right) + 2250 \sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{5}{2}, i \sin^{-1}(ax)\right) - 125 \sqrt{3} \sqrt{i \sin^{-1}(ax)} \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^4*ArcSin[a*x]^(3/2), x]

[Out] (Sqrt[ArcSin[a*x]]*(2250*Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (-I)*ArcSin[a*x]] + 2250*Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, I*ArcSin[a*x]] - 125*Sqrt[3]*Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (-3*I)*ArcSin[a*x]] - 125*Sqrt[3]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, (3*I)*ArcSin[a*x]] + 9*Sqrt[5]*Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (-5*I)*ArcSin[a*x]] + 9*Sqrt[5]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, (5*I)*ArcSin[a*x]]))/(36000*a^5*Sqrt[ArcSin[a*x]^2])

Maple [A] time = 0.079, size = 193, normalized size = 0.9

$$-\frac{1}{24000 a^5} \left(-3000 a x (\arcsin(ax))^2 + 9 \sqrt{5} \sqrt{2} \sqrt{\arcsin(ax)} \sqrt{\pi} \operatorname{FresnelC} \left(\frac{\sqrt{5} \sqrt{2} \sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) - 125 \sqrt{3} \sqrt{2} \sqrt{\arcsin(ax)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*arcsin(a*x)^(3/2), x)

```
[Out] -1/24000/a^5/arcsin(a*x)^(1/2)*(-3000*a*x*arcsin(a*x)^2+9*5^(1/2)*2^(1/2)*a
rcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2^(1/2)/Pi^(1/2)*5^(1/2)*arcsin(a*x)^(1/
2))-125*3^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2^(1/2)/Pi^(1/2
))*3^(1/2)*arcsin(a*x)^(1/2))+1500*arcsin(a*x)^2*sin(3*arcsin(a*x))-300*arcs
in(a*x)^2*sin(5*arcsin(a*x))+2250*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*Fresne
lC(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))-4500*arcsin(a*x)*(-a^2*x^2+1)^(1/2)+
750*arcsin(a*x)*cos(3*arcsin(a*x))-90*arcsin(a*x)*cos(5*arcsin(a*x)))
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*arcsin(a*x)^(3/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*arcsin(a*x)^(3/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*asin(a*x)**(3/2),x)
```

```
[Out] Timed out
```

Giac [C] time = 1.40054, size = 479, normalized size = 2.24

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*arcsin(a*x)^(3/2),x, algorithm="giac")
```

```
[Out] -1/160*I*arcsin(a*x)^(3/2)*e^(5*I*arcsin(a*x))/a^5 + 1/32*I*arcsin(a*x)^(3/
2)*e^(3*I*arcsin(a*x))/a^5 - 1/16*I*arcsin(a*x)^(3/2)*e^(I*arcsin(a*x))/a^5
+ 1/16*I*arcsin(a*x)^(3/2)*e^(-I*arcsin(a*x))/a^5 - 1/32*I*arcsin(a*x)^(3/
```

$$\begin{aligned}
& 2) * e^{(-3*I*\arcsin(a*x))/a^5} + 1/160 * I * \arcsin(a*x)^{(3/2)} * e^{(-5*I*\arcsin(a*x))/a^5} \\
& + (3/32000 * I + 3/32000) * \sqrt{10} * \sqrt{\pi} * \operatorname{erf}((1/2 * I - 1/2) * \sqrt{10} * \sqrt{\arcsin(a*x)}) / a^5 \\
& - (3/32000 * I - 3/32000) * \sqrt{10} * \sqrt{\pi} * \operatorname{erf}(-(1/2 * I + 1/2) * \sqrt{10} * \sqrt{\arcsin(a*x)}) / a^5 \\
& - (1/768 * I + 1/768) * \sqrt{6} * \sqrt{\pi} * \operatorname{erf}((1/2 * I - 1/2) * \sqrt{6} * \sqrt{\arcsin(a*x)}) / a^5 \\
& + (1/768 * I - 1/768) * \sqrt{6} * \sqrt{\pi} * \operatorname{erf}(-(1/2 * I + 1/2) * \sqrt{6} * \sqrt{\arcsin(a*x)}) / a^5 \\
& + (3/128 * I + 3/128) * \sqrt{2} * \sqrt{\pi} * \operatorname{erf}((1/2 * I - 1/2) * \sqrt{2} * \sqrt{\arcsin(a*x)}) / a^5 \\
& - (3/128 * I - 3/128) * \sqrt{2} * \sqrt{\pi} * \operatorname{erf}(-(1/2 * I + 1/2) * \sqrt{2} * \sqrt{\arcsin(a*x)}) / a^5 \\
& + 3/1600 * \sqrt{\arcsin(a*x)} * e^{(5*I*\arcsin(a*x))/a^5} - 1/64 * \sqrt{\arcsin(a*x)} * e^{(3*I*\arcsin(a*x))/a^5} \\
& + 3/32 * \sqrt{\arcsin(a*x)} * e^{(I*\arcsin(a*x))/a^5} + 3/32 * \sqrt{\arcsin(a*x)} * e^{(-I*\arcsin(a*x))/a^5} \\
& - 1/64 * \sqrt{\arcsin(a*x)} * e^{(-3*I*\arcsin(a*x))/a^5} + 3/1600 * \sqrt{\arcsin(a*x)} * e^{(-5*I*\arcsin(a*x))/a^5}
\end{aligned}$$

3.81 $\int x^3 \sin^{-1}(ax)^{3/2} dx$

Optimal. Leaf size=157

$$\frac{3\sqrt{\frac{\pi}{2}}S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{512a^4} - \frac{3\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{64a^4} + \frac{3x^3\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{32a} + \frac{9x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{64a^3} - \frac{3\sin^{-1}(ax)^{3/2}}{32a^4}$$

[Out] (9*x*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(64*a^3) + (3*x^3*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(32*a) - (3*ArcSin[a*x]^(3/2))/(32*a^4) + (x^4*ArcSin[a*x]^(3/2))/4 + (3*Sqrt[Pi/2]*FresnelS[2*Sqrt[2/Pi]*Sqrt[ArcSin[a*x]])]/(512*a^4) - (3*Sqrt[Pi]*FresnelS[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(64*a^4)

Rubi [A] time = 0.378891, antiderivative size = 157, normalized size of antiderivative = 1., number of steps used = 16, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4629, 4707, 4641, 4635, 4406, 12, 3305, 3351}

$$\frac{3\sqrt{\frac{\pi}{2}}S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{512a^4} - \frac{3\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{64a^4} + \frac{3x^3\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{32a} + \frac{9x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{64a^3} - \frac{3\sin^{-1}(ax)^{3/2}}{32a^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*ArcSin[a*x]^(3/2), x]

[Out] (9*x*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(64*a^3) + (3*x^3*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(32*a) - (3*ArcSin[a*x]^(3/2))/(32*a^4) + (x^4*ArcSin[a*x]^(3/2))/4 + (3*Sqrt[Pi/2]*FresnelS[2*Sqrt[2/Pi]*Sqrt[ArcSin[a*x]])]/(512*a^4) - (3*Sqrt[Pi]*FresnelS[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(64*a^4)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)*((f_.)*(x_)^(m_.))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_.)*(x_)^(m_.), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x]

;/; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
 \int x^3 \sin^{-1}(ax)^{3/2} dx &= \frac{1}{4}x^4 \sin^{-1}(ax)^{3/2} - \frac{1}{8}(3a) \int \frac{x^4 \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx \\
 &= \frac{3x^3 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{32a} + \frac{1}{4}x^4 \sin^{-1}(ax)^{3/2} - \frac{3}{64} \int \frac{x^3}{\sqrt{\sin^{-1}(ax)}} dx - \frac{9}{32a} \int \frac{x^2 \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx \\
 &= \frac{9x \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{64a^3} + \frac{3x^3 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{32a} + \frac{1}{4}x^4 \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst}\left(\int \frac{\cos(x) \sin^{-1}(ax)}{\sqrt{x}} dx\right)}{64a^3} \\
 &= \frac{9x \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{64a^3} + \frac{3x^3 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{32a} - \frac{3 \sin^{-1}(ax)^{3/2}}{32a^4} + \frac{1}{4}x^4 \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst}\left(\int \frac{\cos(x) \sin^{-1}(ax)}{\sqrt{x}} dx\right)}{64a^3} \\
 &= \frac{9x \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{64a^3} + \frac{3x^3 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{32a} - \frac{3 \sin^{-1}(ax)^{3/2}}{32a^4} + \frac{1}{4}x^4 \sin^{-1}(ax)^{3/2} + \frac{3 \operatorname{Subst}\left(\int \frac{\cos(x) \sin^{-1}(ax)}{\sqrt{x}} dx\right)}{64a^3} \\
 &= \frac{9x \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{64a^3} + \frac{3x^3 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{32a} - \frac{3 \sin^{-1}(ax)^{3/2}}{32a^4} + \frac{1}{4}x^4 \sin^{-1}(ax)^{3/2} + \frac{3 \operatorname{Subst}\left(\int \frac{\cos(x) \sin^{-1}(ax)}{\sqrt{x}} dx\right)}{64a^3} \\
 &= \frac{9x \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{64a^3} + \frac{3x^3 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{32a} - \frac{3 \sin^{-1}(ax)^{3/2}}{32a^4} + \frac{1}{4}x^4 \sin^{-1}(ax)^{3/2} + \frac{3 \operatorname{Subst}\left(\int \frac{\cos(x) \sin^{-1}(ax)}{\sqrt{x}} dx\right)}{64a^3}
 \end{aligned}$$

Mathematica [C] time = 0.0327046, size = 130, normalized size = 0.83

$$\frac{8\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{5}{2}, -2i\sin^{-1}(ax)\right) + 8\sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{5}{2}, 2i\sin^{-1}(ax)\right) - \sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{5}{2}\right) - \sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{5}{2}\right)}{512a^4\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3*ArcSin[a*x]^(3/2), x]

[Out] (8*Sqrt[2]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, (-2*I)*ArcSin[a*x]] + 8*Sqrt[2]*Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (2*I)*ArcSin[a*x]] - Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, (-4*I)*ArcSin[a*x]] - Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (4*I)*ArcSin[a*x]])/(512*a^4*Sqrt[ArcSin[a*x]])

Maple [A] time = 0.053, size = 121, normalized size = 0.8

$$-\frac{1}{1024a^4} \left(-3\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\text{FresnelS}\left(2\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + 128(\arcsin(ax))^2\cos(2\arcsin(ax)) - 32(\arcsin(ax))\cos(4\arcsin(ax)) + 48\arcsin(ax)\sqrt{\pi}\text{FresnelS}(2\arcsin(ax))\sqrt{\pi} - 96\arcsin(ax)\sin(2\arcsin(ax)) + 12\arcsin(ax)\sin(4\arcsin(ax)) \right) / \arcsin(ax)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x)^(3/2), x)

[Out] -1/1024/a^4*(-3*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2*2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))+128*arcsin(a*x)^2*cos(2*arcsin(a*x))-32*arcsin(a*x)^2*cos(4*arcsin(a*x))+48*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2*arcsin(a*x)^(1/2)/Pi^(1/2))-96*arcsin(a*x)*sin(2*arcsin(a*x))+12*arcsin(a*x)*sin(4*arcsin(a*x)))/arcsin(a*x)^(1/2)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(3/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(3/2), x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \operatorname{asin}^{\frac{3}{2}}(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x)**(3/2), x)

[Out] Integral(x**3*asin(a*x)**(3/2), x)

Giac [C] time = 1.39818, size = 304, normalized size = 1.94

$$\frac{\operatorname{arcsin}(ax)^{\frac{3}{2}} e^{4i \operatorname{arcsin}(ax)}}{64 a^4} - \frac{\operatorname{arcsin}(ax)^{\frac{3}{2}} e^{2i \operatorname{arcsin}(ax)}}{16 a^4} - \frac{\operatorname{arcsin}(ax)^{\frac{3}{2}} e^{-2i \operatorname{arcsin}(ax)}}{16 a^4} + \frac{\operatorname{arcsin}(ax)^{\frac{3}{2}} e^{-4i \operatorname{arcsin}(ax)}}{64 a^4} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(3/2), x, algorithm="giac")

[Out] $\frac{1}{64} \operatorname{arcsin}(a*x)^{\frac{3}{2}} e^{4i \operatorname{arcsin}(a*x)} / a^4 - \frac{1}{16} \operatorname{arcsin}(a*x)^{\frac{3}{2}} e^{-2i \operatorname{arcsin}(a*x)} / a^4 + \frac{1}{64} \operatorname{arcsin}(a*x)^{\frac{3}{2}} e^{-4i \operatorname{arcsin}(a*x)} / a^4 + \frac{(3/4096*i - 3/4096) \sqrt{2} \sqrt{\pi} \operatorname{erf}((i - 1) \sqrt{2} \sqrt{\operatorname{arcsin}(a*x)})}{a^4} - \frac{(3/4096*i + 3/4096) \sqrt{2} \sqrt{\pi} \operatorname{erf}(-(i + 1) \sqrt{2} \sqrt{\operatorname{arcsin}(a*x)})}{a^4} - \frac{(3/256*i - 3/256) \sqrt{\pi} \operatorname{erf}((i - 1) \sqrt{\operatorname{arcsin}(a*x)})}{a^4} + \frac{(3/256*i + 3/256) \sqrt{\pi} \operatorname{erf}(-(i + 1) \sqrt{\operatorname{arcsin}(a*x)})}{a^4} + \frac{3/512*i \sqrt{\operatorname{arcsin}(a*x)} e^{4i \operatorname{arcsin}(a*x)}}{a^4} - \frac{3/64*i \sqrt{\operatorname{arcsin}(a*x)} e^{2i \operatorname{arcsin}(a*x)}}{a^4} + \frac{3/64*i \sqrt{\operatorname{arcsin}(a*x)} e^{-2i \operatorname{arcsin}(a*x)}}{a^4} - \frac{3/512*i \sqrt{\operatorname{arcsin}(a*x)} e^{-4i \operatorname{arcsin}(a*x)}}{a^4}$

3.82 $\int x^2 \sin^{-1}(ax)^{3/2} dx$

Optimal. Leaf size=147

$$-\frac{3\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^3} + \frac{\sqrt{\frac{\pi}{6}}\text{FresnelC}\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{24a^3} + \frac{x^2\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{6a} + \frac{\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{3a^3}$$

[Out] (Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(3*a^3) + (x^2*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(6*a) + (x^3*ArcSin[a*x]^(3/2))/3 - (3*Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^3) + (Sqrt[Pi/6]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(24*a^3)

Rubi [A] time = 0.302717, antiderivative size = 147, normalized size of antiderivative = 1., number of steps used = 13, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4629, 4707, 4677, 4623, 3304, 3352, 4635, 4406}

$$-\frac{3\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^3} + \frac{\sqrt{\frac{\pi}{6}}\text{FresnelC}\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{24a^3} + \frac{x^2\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{6a} + \frac{\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{3a^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*ArcSin[a*x]^(3/2), x]

[Out] (Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(3*a^3) + (x^2*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(6*a) + (x^3*ArcSin[a*x]^(3/2))/3 - (3*Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^3) + (Sqrt[Pi/6]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(24*a^3)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_)*((f_.)*(x_)^(m_))/Sqrt[(d_ + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)*((d_ + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d*IntPart[p]*(d + e*x^2)^FracPart[p]]/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_], x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)^m_], x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^m_*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rubi steps

$$\begin{aligned}
 \int x^2 \sin^{-1}(ax)^{3/2} dx &= \frac{1}{3}x^3 \sin^{-1}(ax)^{3/2} - \frac{1}{2}a \int \frac{x^3 \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx \\
 &= \frac{x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{6a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{3/2} - \frac{1}{12} \int \frac{x^2}{\sqrt{\sin^{-1}(ax)}} dx - \frac{\int \frac{x \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx}{3a} \\
 &= \frac{\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{3a^3} + \frac{x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{6a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{3/2} - \frac{\text{Subst}\left(\int \frac{\cos(x) \sin^2(x)}{\sqrt{x}} dx\right)}{12a^3} \\
 &= \frac{\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{3a^3} + \frac{x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{6a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{3/2} - \frac{\text{Subst}\left(\int \left(\frac{\cos(x)}{4\sqrt{x}} - \frac{\cos(x)}{4\sqrt{x}}\right) dx\right)}{12a^3} \\
 &= \frac{\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{3a^3} + \frac{x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{6a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{3/2} - \frac{\text{Subst}\left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, s\right)}{48a^3} \\
 &= \frac{\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{3a^3} + \frac{x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{6a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{3/2} - \frac{\sqrt{\frac{\pi}{2}} C\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{3a^3} \\
 &= \frac{\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{3a^3} + \frac{x^2 \sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{6a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{3/2} - \frac{3\sqrt{\frac{\pi}{2}} C\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^3}
 \end{aligned}$$

Mathematica [C] time = 0.0591148, size = 136, normalized size = 0.93

$$\frac{\sqrt{\sin^{-1}(ax)} \left(27\sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{5}{2}, -i \sin^{-1}(ax)\right) + 27\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{5}{2}, i \sin^{-1}(ax)\right) - \sqrt{3} \left(\sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{5}{2}, -i \sin^{-1}(ax)\right) + \sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{5}{2}, i \sin^{-1}(ax)\right) \right) \right)}{216a^3 \sqrt{\sin^{-1}(ax)^2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2*ArcSin[a*x]^(3/2),x]

[Out] (Sqrt[ArcSin[a*x]]*(27*Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (-I)*ArcSin[a*x]] + 27*Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, I*ArcSin[a*x]] - Sqrt[3]*(Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (-3*I)*ArcSin[a*x]] + Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, (3*I)*ArcSin[a*x]])))/(216*a^3*Sqrt[ArcSin[a*x]^2])

Maple [A] time = 0.05, size = 131, normalized size = 0.9

$$-\frac{1}{144a^3} \left(-36ax (\arcsin(ax))^2 - \sqrt{3}\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\text{FresnelC}\left(\frac{\sqrt{3}\sqrt{2}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right) + 12 (\arcsin(ax))^2 \sin(3 \arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*arcsin(a*x)^(3/2),x)

[Out] -1/144/a^3/arcsin(a*x)^(1/2)*(-36*a*x*arcsin(a*x)^2-3^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2^(1/2)/Pi^(1/2)*3^(1/2)*arcsin(a*x)^(1/2))+12*arcsin(a*x)^2*sin(3*arcsin(a*x))+27*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))-54*arcsin(a*x)*(-a^2*x^2+1)^(1/2)+6*arcsin(a*x)*cos(3*arcsin(a*x))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^(3/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \operatorname{asin}^{\frac{3}{2}}(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*asin(a*x)**(3/2), x)

[Out] Integral(x**2*asin(a*x)**(3/2), x)

Giac [C] time = 1.39175, size = 320, normalized size = 2.18

$$\frac{i \operatorname{asin}(ax)^{\frac{3}{2}} e^{3i \operatorname{asin}(ax)}}{24 a^3} - \frac{i \operatorname{asin}(ax)^{\frac{3}{2}} e^{i \operatorname{asin}(ax)}}{8 a^3} + \frac{i \operatorname{asin}(ax)^{\frac{3}{2}} e^{-i \operatorname{asin}(ax)}}{8 a^3} - \frac{i \operatorname{asin}(ax)^{\frac{3}{2}} e^{-3i \operatorname{asin}(ax)}}{24 a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^(3/2), x, algorithm="giac")

[Out] $\frac{1}{24} I \operatorname{arcsin}(a x)^{\frac{3}{2}} e^{3 I \operatorname{arcsin}(a x)} / a^3 - \frac{1}{8} I \operatorname{arcsin}(a x)^{\frac{3}{2}} e^{I \operatorname{arcsin}(a x)} / a^3 + \frac{1}{8} I \operatorname{arcsin}(a x)^{\frac{3}{2}} e^{-I \operatorname{arcsin}(a x)} / a^3 - \frac{1}{24} I \operatorname{arcsin}(a x)^{\frac{3}{2}} e^{-3 I \operatorname{arcsin}(a x)} / a^3 - \frac{(1/576 I + 1/576) \sqrt{6} \sqrt{\pi} \operatorname{erf}((1/2 I - 1/2) \sqrt{6} \sqrt{\operatorname{arcsin}(a x)})}{a^3} + \frac{(1/576 I - 1/576) \sqrt{6} \sqrt{\pi} \operatorname{erf}(-(1/2 I + 1/2) \sqrt{6} \sqrt{\operatorname{arcsin}(a x)})}{a^3} + \frac{(3/64 I + 3/64) \sqrt{2} \sqrt{\pi} \operatorname{erf}((1/2 I - 1/2) \sqrt{2} \sqrt{\operatorname{arcsin}(a x)})}{a^3} - \frac{(3/64 I - 3/64) \sqrt{2} \sqrt{\pi} \operatorname{erf}(-(1/2 I + 1/2) \sqrt{2} \sqrt{\operatorname{arcsin}(a x)})}{a^3} - \frac{1}{48} \sqrt{\operatorname{arcsin}(a x)} e^{3 I \operatorname{arcsin}(a x)} / a^3 + \frac{3}{16} \sqrt{\operatorname{arcsin}(a x)} e^{I \operatorname{arcsin}(a x)} / a^3 + \frac{3}{16} \sqrt{\operatorname{arcsin}(a x)} e^{-I \operatorname{arcsin}(a x)} / a^3 - \frac{1}{48} \sqrt{\operatorname{arcsin}(a x)} e^{-3 I \operatorname{arcsin}(a x)} / a^3$

3.83 $\int x \sin^{-1}(ax)^{3/2} dx$

Optimal. Leaf size=89

$$-\frac{3\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{32a^2} + \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} - \frac{\sin^{-1}(ax)^{3/2}}{4a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^{3/2}$$

[Out] (3*x*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(8*a) - ArcSin[a*x]^(3/2)/(4*a^2) + (x^2*ArcSin[a*x]^(3/2))/2 - (3*Sqrt[Pi]*FresnelS[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(32*a^2)

Rubi [A] time = 0.182785, antiderivative size = 89, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 8, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.8$, Rules used = {4629, 4707, 4641, 4635, 4406, 12, 3305, 3351}

$$-\frac{3\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{32a^2} + \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} - \frac{\sin^{-1}(ax)^{3/2}}{4a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[x*ArcSin[a*x]^(3/2),x]

[Out] (3*x*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(8*a) - ArcSin[a*x]^(3/2)/(4*a^2) + (x^2*ArcSin[a*x]^(3/2))/2 - (3*Sqrt[Pi]*FresnelS[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(32*a^2)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned}
\int x \sin^{-1}(ax)^{3/2} dx &= \frac{1}{2}x^2 \sin^{-1}(ax)^{3/2} - \frac{1}{4}(3a) \int \frac{x^2 \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} + \frac{1}{2}x^2 \sin^{-1}(ax)^{3/2} - \frac{3}{16} \int \frac{x}{\sqrt{\sin^{-1}(ax)}} dx - \frac{3 \int \frac{\sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx}{8a} \\
&= \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} - \frac{\sin^{-1}(ax)^{3/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst}\left(\int \frac{\cos(x)\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{16a^2} \\
&= \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} - \frac{\sin^{-1}(ax)^{3/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst}\left(\int \frac{\sin(2x)}{2\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{16a^2} \\
&= \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} - \frac{\sin^{-1}(ax)^{3/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst}\left(\int \frac{\sin(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{32a^2} \\
&= \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} - \frac{\sin^{-1}(ax)^{3/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst}\left(\int \sin(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{16a^2} \\
&= \frac{3x\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{8a} - \frac{\sin^{-1}(ax)^{3/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{3/2} - \frac{3\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{32a^2}
\end{aligned}$$

Mathematica [C] time = 0.0151286, size = 71, normalized size = 0.8

$$\frac{\sqrt{-i \sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{5}{2}, -2i \sin^{-1}(ax)\right) + \sqrt{i \sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{5}{2}, 2i \sin^{-1}(ax)\right)}{16\sqrt{2}a^2\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*ArcSin[a*x]^(3/2), x]

[Out] $(\text{Sqrt}[(-1)*\text{ArcSin}[a*x]]*\text{Gamma}[5/2, (-2*I)*\text{ArcSin}[a*x]] + \text{Sqrt}[I*\text{ArcSin}[a*x]]*\text{Gamma}[5/2, (2*I)*\text{ArcSin}[a*x]])/(16*\text{Sqrt}[2]*a^2*\text{Sqrt}[\text{ArcSin}[a*x]])$

Maple [A] time = 0.036, size = 64, normalized size = 0.7

$$-\frac{1}{32a^2} \left(8 (\arcsin(ax))^2 \cos(2 \arcsin(ax)) + 3 \sqrt{\arcsin(ax)} \sqrt{\pi} \text{FresnelS} \left(2 \frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) - 6 \arcsin(ax) \sin(2 \arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*arcsin(a*x)^(3/2),x)`

[Out] $-1/32/a^2*(8*\arcsin(a*x)^2*\cos(2*\arcsin(a*x))+3*\arcsin(a*x)^{(1/2)}*\text{Pi}^{(1/2)}*\text{FresnelS}(2*\arcsin(a*x)^{(1/2)}/\text{Pi}^{(1/2)})-6*\arcsin(a*x)*\sin(2*\arcsin(a*x)))/\arcsin(a*x)^{(1/2)}$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*arcsin(a*x)^(3/2),x, algorithm="maxima")`

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*arcsin(a*x)^(3/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \arcsin^{\frac{3}{2}}(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*asin(a*x)**(3/2),x)`

[Out] `Integral(x*asin(a*x)**(3/2), x)`

Giac [C] time = 1.34236, size = 144, normalized size = 1.62

$$-\frac{\arcsin(ax)^{\frac{3}{2}} e^{2i \arcsin(ax)}}{8a^2} - \frac{\arcsin(ax)^{\frac{3}{2}} e^{-2i \arcsin(ax)}}{8a^2} - \frac{(3i-3)\sqrt{\pi} \operatorname{erf}\left((i-1)\sqrt{\arcsin(ax)}\right)}{128a^2} + \frac{(3i+3)\sqrt{\pi} \operatorname{erf}\left((i+1)\sqrt{\arcsin(ax)}\right)}{128a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] -1/8*arcsin(a*x)^(3/2)*e^(2*I*arcsin(a*x))/a^2 - 1/8*arcsin(a*x)^(3/2)*e^(-2*I*arcsin(a*x))/a^2 - (3/128*I - 3/128)*sqrt(pi)*erf((I - 1)*sqrt(arcsin(a*x)))/a^2 + (3/128*I + 3/128)*sqrt(pi)*erf(-(I + 1)*sqrt(arcsin(a*x)))/a^2 - 3/32*I*sqrt(arcsin(a*x))*e^(2*I*arcsin(a*x))/a^2 + 3/32*I*sqrt(arcsin(a*x))*e^(-2*I*arcsin(a*x))/a^2

3.84 $\int \sin^{-1}(ax)^{3/2} dx$

Optimal. Leaf size=75

$$\frac{3\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{2a} - \frac{3\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{2a} + x\sin^{-1}(ax)^{3/2}$$

[Out] (3*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(2*a) + x*ArcSin[a*x]^(3/2) - (3*Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(2*a)

Rubi [A] time = 0.0991487, antiderivative size = 75, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4619, 4677, 4623, 3304, 3352}

$$\frac{3\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}}{2a} - \frac{3\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{2a} + x\sin^{-1}(ax)^{3/2}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^(3/2), x]

[Out] (3*Sqrt[1 - a^2*x^2]*Sqrt[ArcSin[a*x]])/(2*a) + x*ArcSin[a*x]^(3/2) - (3*Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(2*a)

Rule 4619

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.), x_Symbol] :> Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]
```

Rule 4677

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*(x_)*((d_.) + (e_.)*(x_)^2)^ (p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]
```

Rule 4623

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.), x_Symbol] :> Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_)^2)], x_Symbol] :> Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/ (f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```


Rubi steps

$$\begin{aligned}
\int \sin^{-1}(ax)^{3/2} dx &= x \sin^{-1}(ax)^{3/2} - \frac{1}{2}(3a) \int \frac{x \sqrt{\sin^{-1}(ax)}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{3\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{2a} + x \sin^{-1}(ax)^{3/2} - \frac{3}{4} \int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx \\
&= \frac{3\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{2a} + x \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst} \left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax) \right)}{4a} \\
&= \frac{3\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{2a} + x \sin^{-1}(ax)^{3/2} - \frac{3 \operatorname{Subst} \left(\int \cos(x^2) dx, x, \sqrt{\sin^{-1}(ax)} \right)}{2a} \\
&= \frac{3\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}}{2a} + x \sin^{-1}(ax)^{3/2} - \frac{3\sqrt{\frac{\pi}{2}} C \left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)} \right)}{2a}
\end{aligned}$$

Mathematica [C] time = 0.0433252, size = 76, normalized size = 1.01

$$\frac{\sqrt{\sin^{-1}(ax)} \left(\sqrt{i \sin^{-1}(ax)} \operatorname{Gamma} \left(\frac{5}{2}, -i \sin^{-1}(ax) \right) + \sqrt{-i \sin^{-1}(ax)} \operatorname{Gamma} \left(\frac{5}{2}, i \sin^{-1}(ax) \right) \right)}{2a \sqrt{\sin^{-1}(ax)^2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^(3/2), x]

[Out] (Sqrt[ArcSin[a*x]]*(Sqrt[I*ArcSin[a*x]]*Gamma[5/2, (-I)*ArcSin[a*x]] + Sqrt[(-I)*ArcSin[a*x]]*Gamma[5/2, I*ArcSin[a*x]]))/(2*a*Sqrt[ArcSin[a*x]^2])

Maple [A] time = 0.036, size = 72, normalized size = 1.

$$\frac{\sqrt{2}}{4a\sqrt{\pi}} \left(2 (\arcsin(ax))^{3/2} \sqrt{2}\sqrt{\pi}xa + 3 \sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\sqrt{-a^2x^2+1} - 3\pi \operatorname{FresnelC} \left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^(3/2), x)

[Out] 1/4/a*2^(1/2)*(2*arcsin(a*x)^(3/2)*2^(1/2)*Pi^(1/2)*x*a+3*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*(-a^2*x^2+1)^(1/2)-3*Pi*FresnelC(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))/Pi^(1/2)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(3/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{asin}^{\frac{3}{2}}(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**(3/2),x)

[Out] Integral(asin(a*x)**(3/2), x)

Giac [C] time = 1.46949, size = 161, normalized size = 2.15

$$-\frac{i \operatorname{arcsin}(ax)^{\frac{3}{2}} e^{i \operatorname{arcsin}(ax)}}{2a} + \frac{i \operatorname{arcsin}(ax)^{\frac{3}{2}} e^{-i \operatorname{arcsin}(ax)}}{2a} + \frac{(3i+3) \sqrt{2} \sqrt{\pi} \operatorname{erf}\left(\left(\frac{1}{2}i - \frac{1}{2}\right) \sqrt{2} \sqrt{\operatorname{arcsin}(ax)}\right)}{16a} - \frac{(3i-3) \sqrt{2} \sqrt{\pi} \operatorname{erf}\left(\left(\frac{1}{2}i + \frac{1}{2}\right) \sqrt{2} \sqrt{\operatorname{arcsin}(ax)}\right)}{16a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] $-1/2*I*\operatorname{arcsin}(a*x)^{(3/2)}*e^{(I*\operatorname{arcsin}(a*x))}/a + 1/2*I*\operatorname{arcsin}(a*x)^{(3/2)}*e^{(-I*\operatorname{arcsin}(a*x))}/a + (3/16*I + 3/16)*\operatorname{sqrt}(2)*\operatorname{sqrt}(\pi)*\operatorname{erf}((1/2*I - 1/2)*\operatorname{sqrt}(2)*\operatorname{sqrt}(\operatorname{arcsin}(a*x)))/a - (3/16*I - 3/16)*\operatorname{sqrt}(2)*\operatorname{sqrt}(\pi)*\operatorname{erf}(-(1/2*I + 1/2)*\operatorname{sqrt}(2)*\operatorname{sqrt}(\operatorname{arcsin}(a*x)))/a + 3/4*\operatorname{sqrt}(\operatorname{arcsin}(a*x))*e^{(I*\operatorname{arcsin}(a*x))}/a + 3/4*\operatorname{sqrt}(\operatorname{arcsin}(a*x))*e^{(-I*\operatorname{arcsin}(a*x))}/a$

$$3.85 \quad \int \frac{\sin^{-1}(ax)^{3/2}}{x} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{\sin^{-1}(ax)^{3/2}}{x}, x\right)$$

[Out] Unintegrable[ArcSin[a*x]^(3/2)/x, x]

Rubi [A] time = 0.0131838, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin^{-1}(ax)^{3/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Int[ArcSin[a*x]^(3/2)/x, x]

[Out] Defer[Int][ArcSin[a*x]^(3/2)/x, x]

Rubi steps

$$\int \frac{\sin^{-1}(ax)^{3/2}}{x} dx = \int \frac{\sin^{-1}(ax)^{3/2}}{x} dx$$

Mathematica [A] time = 0.371563, size = 0, normalized size = 0.

$$\int \frac{\sin^{-1}(ax)^{3/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[ArcSin[a*x]^(3/2)/x, x]

[Out] Integrate[ArcSin[a*x]^(3/2)/x, x]

Maple [A] time = 0.063, size = 0, normalized size = 0.

$$\int \frac{1}{x} (\arcsin(ax))^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^(3/2)/x, x)

[Out] int(arcsin(a*x)^(3/2)/x, x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(3/2)/x,x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(3/2)/x,x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{asin}^2(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**(3/2)/x,x)

[Out] Integral(asin(a*x)**(3/2)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{arcsin}(ax)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(3/2)/x,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^(3/2)/x, x)

3.86 $\int x^4 \sin^{-1}(ax)^{5/2} dx$

Optimal. Leaf size=263

$$\frac{15\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{32a^5} - \frac{5\sqrt{\frac{\pi}{6}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{192a^5} + \frac{3\sqrt{\frac{\pi}{10}}S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{1600a^5} + \frac{x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{10a} - \frac{x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^{1/2}}{15a^2}$$

[Out] $(-2*x*\text{Sqrt}[\text{ArcSin}[a*x]])/(5*a^4) - (x^3*\text{Sqrt}[\text{ArcSin}[a*x]])/(15*a^2) - (3*x^5*\text{Sqrt}[\text{ArcSin}[a*x]])/100 + (4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^{(3/2)})/(15*a^5) + (2*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^{(3/2)})/(15*a^3) + (x^4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^{(3/2)})/(10*a) + (x^5*\text{ArcSin}[a*x]^{(5/2)})/5 + (15*\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(32*a^5) - (5*\text{Sqrt}[\text{Pi}/6]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(192*a^5) + (3*\text{Sqrt}[\text{Pi}/10]*\text{FresnelS}[\text{Sqrt}[10/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(1600*a^5)$

Rubi [A] time = 0.803417, antiderivative size = 298, normalized size of antiderivative = 1.13, number of steps used = 26, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4629, 4707, 4677, 4619, 4723, 3305, 3351, 3312}

$$\frac{15\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{32a^5} - \frac{\sqrt{\frac{3\pi}{2}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{320a^5} - \frac{\sqrt{\frac{\pi}{6}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{60a^5} + \frac{3\sqrt{\frac{\pi}{10}}S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{1600a^5} + \frac{x^4\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{10a} - \frac{x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^{1/2}}{15a^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^4*\text{ArcSin}[a*x]^{(5/2)}, x]$

[Out] $(-2*x*\text{Sqrt}[\text{ArcSin}[a*x]])/(5*a^4) - (x^3*\text{Sqrt}[\text{ArcSin}[a*x]])/(15*a^2) - (3*x^5*\text{Sqrt}[\text{ArcSin}[a*x]])/100 + (4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^{(3/2)})/(15*a^5) + (2*x^2*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^{(3/2)})/(15*a^3) + (x^4*\text{Sqrt}[1 - a^2*x^2]*\text{ArcSin}[a*x]^{(3/2)})/(10*a) + (x^5*\text{ArcSin}[a*x]^{(5/2)})/5 + (15*\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(32*a^5) - (\text{Sqrt}[\text{Pi}/6]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(60*a^5) - (\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(320*a^5) + (3*\text{Sqrt}[\text{Pi}/10]*\text{FresnelS}[\text{Sqrt}[10/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(1600*a^5)$

Rule 4629

$\text{Int}[(a + \text{ArcSin}[c*x])^n * (b + x)^m, x] := \text{Simp}[(x^{m+1} * (a + b*\text{ArcSin}[c*x])^n) / (m+1), x] - \text{Dist}[(b*c^n) / (m+1), \text{Int}[(x^{m+1} * (a + b*\text{ArcSin}[c*x])^{n-1}) / \text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

$\text{Int}[(a + \text{ArcSin}[c*x])^n * (d + e*x^2)^m, x] := \text{Simp}[(f*(f*x)^{m-1} * \text{Sqrt}[d + e*x^2] * (a + b*\text{ArcSin}[c*x])^n) / (e*m), x] + (\text{Dist}[(f^2*(m-1)) / (c^2*m), \text{Int}[(f*x)^{m-2} * (a + b*\text{ArcSin}[c*x])^n] / \text{Sqrt}[d + e*x^2], x], x] + \text{Dist}[(b*f*n*\text{Sqrt}[1 - c^2*x^2]) / (c*m*\text{Sqrt}[d + e*x^2]), \text{Int}[(f*x)^{m-1} * (a + b*\text{ArcSin}[c*x])^{n-1}], x] /;$ FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

$\text{Int}[(a + \text{ArcSin}[c*x])^n * (d + e*x^2)^p, x] := \text{Simp}[(d + e*x^2)^{p+1} * (a + b*\text{ArcSin}[c*x])^n] / (2*e*(p + 1)) + \text{Dist}[(b*c^n) / (2*e*(p + 1)), \text{Int}[(d + e*x^2)^p * (a + b*\text{ArcSin}[c*x])^n], x] /;$ FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d + e, 0] && GtQ[p, 0] && IntegerQ[p]

```
1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]
```

Rule 4619

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]
```

Rule 4723

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rubi steps

$$\begin{aligned}
\int x^4 \sin^{-1}(ax)^{5/2} dx &= \frac{1}{5}x^5 \sin^{-1}(ax)^{5/2} - \frac{1}{2}a \int \frac{x^5 \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{x^4 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{10a} + \frac{1}{5}x^5 \sin^{-1}(ax)^{5/2} - \frac{3}{20} \int x^4 \sqrt{\sin^{-1}(ax)} dx - \frac{2}{5a} \int \frac{x^3 \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{3}{100}x^5 \sqrt{\sin^{-1}(ax)} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^3} + \frac{x^4 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{10a} + \frac{1}{5}x^5 \sin^{-1}(ax)^{5/2} \\
&= -\frac{x^3 \sqrt{\sin^{-1}(ax)}}{15a^2} - \frac{3}{100}x^5 \sqrt{\sin^{-1}(ax)} + \frac{4\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^3} + \dots \\
&= -\frac{2x \sqrt{\sin^{-1}(ax)}}{5a^4} - \frac{x^3 \sqrt{\sin^{-1}(ax)}}{15a^2} - \frac{3}{100}x^5 \sqrt{\sin^{-1}(ax)} + \frac{4\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^3} + \dots \\
&= -\frac{2x \sqrt{\sin^{-1}(ax)}}{5a^4} - \frac{x^3 \sqrt{\sin^{-1}(ax)}}{15a^2} - \frac{3}{100}x^5 \sqrt{\sin^{-1}(ax)} + \frac{4\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^3} + \dots \\
&= -\frac{2x \sqrt{\sin^{-1}(ax)}}{5a^4} - \frac{x^3 \sqrt{\sin^{-1}(ax)}}{15a^2} - \frac{3}{100}x^5 \sqrt{\sin^{-1}(ax)} + \frac{4\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^3} + \dots \\
&= -\frac{2x \sqrt{\sin^{-1}(ax)}}{5a^4} - \frac{x^3 \sqrt{\sin^{-1}(ax)}}{15a^2} - \frac{3}{100}x^5 \sqrt{\sin^{-1}(ax)} + \frac{4\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^5} + \frac{2x^2 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{15a^3} + \dots
\end{aligned}$$

Mathematica [C] time = 0.0706802, size = 204, normalized size = 0.78

$$\frac{i\sqrt{\sin^{-1}(ax)} \left(33750\sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, -i \sin^{-1}(ax)\right) - 33750\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, i \sin^{-1}(ax)\right) - 625\sqrt{3}\sqrt{\sin^{-1}(ax)} \right)}{a^5}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^4*ArcSin[a*x]^(5/2),x]

[Out] ((I/540000)*Sqrt[ArcSin[a*x]]*(33750*Sqrt[I*ArcSin[a*x]]*Gamma[7/2, (-I)*ArcSin[a*x]] - 33750*Sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, I*ArcSin[a*x]] - 625*Sqrt[3]*Sqrt[I*ArcSin[a*x]]*Gamma[7/2, (-3*I)*ArcSin[a*x]] + 625*Sqrt[3]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (3*I)*ArcSin[a*x]] + 27*Sqrt[5]*Sqrt[I*ArcSin[a*x]]*Gamma[7/2, (-5*I)*ArcSin[a*x]] - 27*Sqrt[5]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (5*I)*ArcSin[a*x]]))/(a^5*Sqrt[ArcSin[a*x]^2])

Maple [A] time = 0.077, size = 233, normalized size = 0.9

$$-\frac{1}{144000a^5} \left(-18000ax(\arcsin(ax))^3 + 9000(\arcsin(ax))^3 \sin(3\arcsin(ax)) - 1800(\arcsin(ax))^3 \sin(5\arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4*arcsin(a*x)^(5/2),x)

```
[Out] -1/144000/a^5/arcsin(a*x)^(1/2)*(-18000*a*x*arcsin(a*x)^3+9000*arcsin(a*x)^3*
sin(3*arcsin(a*x))-1800*arcsin(a*x)^3*sin(5*arcsin(a*x))-27*5^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*
Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*5^(1/2)*arcsin(a*x)^(1/2))+625*3^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*
Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*3^(1/2)*arcsin(a*x)^(1/2))-45000*arcsin(a*x)^2*(-a^2*x^2+1)^(1/2)+7500*
arcsin(a*x)^2*cos(3*arcsin(a*x))-900*arcsin(a*x)^2*cos(5*arcsin(a*x))-33750*2^(1/2)*arcsin(a*x)^(1/2)*
Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))+67500*a*x*arcsin(a*x)-3750*arcsin(a*x)*sin(3*arcsin(a*x))+270*arcsi
n(a*x)*sin(5*arcsin(a*x)))
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*arcsin(a*x)^(5/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*arcsin(a*x)^(5/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*asin(a*x)**(5/2),x)
```

```
[Out] Timed out
```

Giac [C] time = 1.47479, size = 625, normalized size = 2.38

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*arcsin(a*x)^(5/2),x, algorithm="giac")
```

```
[Out] -1/160*I*arcsin(a*x)^(5/2)*e^(5*I*arcsin(a*x))/a^5 + 1/32*I*arcsin(a*x)^(5/2)*e^(3*I*arcsin(a*x))/a^5 - 1/16*I*arcsin(a*x)^(5/2)*e^(I*arcsin(a*x))/a^5
```


$$\begin{aligned}
& + 1/16*I*\arcsin(ax)^{(5/2)}*e^{(-I*\arcsin(ax))}/a^5 - 1/32*I*\arcsin(ax)^{(5/2)}*e^{(-3*I*\arcsin(ax))}/a^5 + 1/160*I*\arcsin(ax)^{(5/2)}*e^{(-5*I*\arcsin(ax))}/a^5 + 1/320*\arcsin(ax)^{(3/2)}*e^{(5*I*\arcsin(ax))}/a^5 - 5/192*\arcsin(ax)^{(3/2)}*e^{(3*I*\arcsin(ax))}/a^5 + 5/32*\arcsin(ax)^{(3/2)}*e^{(I*\arcsin(ax))}/a^5 + 5/32*\arcsin(ax)^{(3/2)}*e^{(-I*\arcsin(ax))}/a^5 - 5/192*\arcsin(ax)^{(3/2)}*e^{(-3*I*\arcsin(ax))}/a^5 + 1/320*\arcsin(ax)^{(3/2)}*e^{(-5*I*\arcsin(ax))}/a^5 + (3/64000*I - 3/64000)*\sqrt{10}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{10}*\sqrt{\arcsin(ax)})/a^5 - (3/64000*I + 3/64000)*\sqrt{10}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{10}*\sqrt{\arcsin(ax)})/a^5 - (5/4608*I - 5/4608)*\sqrt{6}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{6}*\sqrt{\arcsin(ax)})/a^5 + (5/4608*I + 5/4608)*\sqrt{6}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{6}*\sqrt{\arcsin(ax)})/a^5 + (15/256*I - 15/256)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{2}*\sqrt{\arcsin(ax)})/a^5 - (15/256*I + 15/256)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{2}*\sqrt{\arcsin(ax)})/a^5 + 3/3200*I*\sqrt{\arcsin(ax)}*e^{(5*I*\arcsin(ax))}/a^5 - 5/384*I*\sqrt{\arcsin(ax)}*e^{(3*I*\arcsin(ax))}/a^5 + 15/64*I*\sqrt{\arcsin(ax)}*e^{(I*\arcsin(ax))}/a^5 - 15/64*I*\sqrt{\arcsin(ax)}*e^{(-I*\arcsin(ax))}/a^5 + 5/384*I*\sqrt{\arcsin(ax)}*e^{(-3*I*\arcsin(ax))}/a^5 - 3/3200*I*\sqrt{\arcsin(ax)}*e^{(-5*I*\arcsin(ax))}/a^5
\end{aligned}$$

3.87 $\int x^3 \sin^{-1}(ax)^{5/2} dx$

Optimal. Leaf size=205

$$\frac{15\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{4096a^4} - \frac{15\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{256a^4} + \frac{5x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{32a} - \frac{45x^2\sqrt{\sin^{-1}(ax)}}{256a^2} + 1$$

[Out] (225*Sqrt[ArcSin[a*x]])/(2048*a^4) - (45*x^2*Sqrt[ArcSin[a*x]])/(256*a^2) - (15*x^4*Sqrt[ArcSin[a*x]])/256 + (15*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(64*a^3) + (5*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(32*a) - (3*ArcSin[a*x]^(5/2))/(32*a^4) + (x^4*ArcSin[a*x]^(5/2))/4 + (15*Sqrt[Pi/2]*FresnelC[2*Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4096*a^4) - (15*Sqrt[Pi]*FresnelC[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(256*a^4)

Rubi [A] time = 0.600391, antiderivative size = 205, normalized size of antiderivative = 1., number of steps used = 18, number of rules used = 7, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.583$, Rules used = {4629, 4707, 4641, 4723, 3312, 3304, 3352}

$$\frac{15\sqrt{\frac{\pi}{2}}\text{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{4096a^4} - \frac{15\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{256a^4} + \frac{5x^3\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{32a} - \frac{45x^2\sqrt{\sin^{-1}(ax)}}{256a^2} + 1$$

Antiderivative was successfully verified.

[In] Int[x^3*ArcSin[a*x]^(5/2), x]

[Out] (225*Sqrt[ArcSin[a*x]])/(2048*a^4) - (45*x^2*Sqrt[ArcSin[a*x]])/(256*a^2) - (15*x^4*Sqrt[ArcSin[a*x]])/256 + (15*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(64*a^3) + (5*x^3*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(32*a) - (3*ArcSin[a*x]^(5/2))/(32*a^4) + (x^4*ArcSin[a*x]^(5/2))/4 + (15*Sqrt[Pi/2]*FresnelC[2*Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4096*a^4) - (15*Sqrt[Pi]*FresnelC[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(256*a^4)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_ + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_.)^(m_.)*((d_.) + (e_.)*(x_.)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3312

Int[((c_.) + (d_.)*(x_.))^(m_.)*sin[(e_.) + (f_.)*(x_.)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_.)]/Sqrt[(c_.) + (d_.)*(x_.)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
 \int x^3 \sin^{-1}(ax)^{5/2} dx &= \frac{1}{4}x^4 \sin^{-1}(ax)^{5/2} - \frac{1}{8}(5a) \int \frac{x^4 \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
 &= \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{32a} + \frac{1}{4}x^4 \sin^{-1}(ax)^{5/2} - \frac{15}{64} \int x^3 \sqrt{\sin^{-1}(ax)} dx - \frac{15 \int \frac{x^2 \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx}{32a} \\
 &= -\frac{15}{256}x^4 \sqrt{\sin^{-1}(ax)} + \frac{15x \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{64a^3} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{32a} + \frac{1}{4}x^4 \sin^{-1}(ax) \\
 &= -\frac{45x^2 \sqrt{\sin^{-1}(ax)}}{256a^2} - \frac{15}{256}x^4 \sqrt{\sin^{-1}(ax)} + \frac{15x \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{64a^3} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} \\
 &= -\frac{45x^2 \sqrt{\sin^{-1}(ax)}}{256a^2} - \frac{15}{256}x^4 \sqrt{\sin^{-1}(ax)} + \frac{15x \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{64a^3} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} \\
 &= \frac{45 \sqrt{\sin^{-1}(ax)}}{2048a^4} - \frac{45x^2 \sqrt{\sin^{-1}(ax)}}{256a^2} - \frac{15}{256}x^4 \sqrt{\sin^{-1}(ax)} + \frac{15x \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{64a^3} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} \\
 &= \frac{225 \sqrt{\sin^{-1}(ax)}}{2048a^4} - \frac{45x^2 \sqrt{\sin^{-1}(ax)}}{256a^2} - \frac{15}{256}x^4 \sqrt{\sin^{-1}(ax)} + \frac{15x \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{64a^3} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} \\
 &= \frac{225 \sqrt{\sin^{-1}(ax)}}{2048a^4} - \frac{45x^2 \sqrt{\sin^{-1}(ax)}}{256a^2} - \frac{15}{256}x^4 \sqrt{\sin^{-1}(ax)} + \frac{15x \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{64a^3} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a} \\
 &= \frac{225 \sqrt{\sin^{-1}(ax)}}{2048a^4} - \frac{45x^2 \sqrt{\sin^{-1}(ax)}}{256a^2} - \frac{15}{256}x^4 \sqrt{\sin^{-1}(ax)} + \frac{15x \sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{64a^3} + \frac{5x^3 \sqrt{1-a^2x^2} \sin^{-1}(ax)}{32a}
 \end{aligned}$$

Mathematica [C] time = 0.0413394, size = 140, normalized size = 0.68

$$\frac{\sqrt{\sin^{-1}(ax)} \left(16\sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{7}{2}, -2i\sin^{-1}(ax)\right) + 16\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{7}{2}, 2i\sin^{-1}(ax)\right) - \sqrt{i\sin^{-1}(ax)} \right)}{2048a^4\sqrt{\sin^{-1}(ax)^2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3*ArcSin[a*x]^(5/2),x]

[Out] (Sqrt[ArcSin[a*x]]*(16*Sqrt[2]*Sqrt[I*ArcSin[a*x]]*Gamma[7/2, (-2*I)*ArcSin[a*x]] + 16*Sqrt[2]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (2*I)*ArcSin[a*x]] - Sqrt[I*ArcSin[a*x]]*Gamma[7/2, (-4*I)*ArcSin[a*x]] - Sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (4*I)*ArcSin[a*x]]))/(2048*a^4*Sqrt[ArcSin[a*x]^2])

Maple [A] time = 0.056, size = 154, normalized size = 0.8

$$-\frac{1}{8192a^4\sqrt{\pi}} \left(1024 (\arcsin(ax))^{5/2} \sqrt{\pi} \cos(2 \arcsin(ax)) - 256 (\arcsin(ax))^{5/2} \sqrt{\pi} \cos(4 \arcsin(ax)) - 1280 (\arcsin(ax))^{3/2} \sqrt{\pi} \cos(2 \arcsin(ax)) + 160 (\arcsin(ax))^{3/2} \sqrt{\pi} \cos(4 \arcsin(ax)) - 15\pi^{3/2} \operatorname{FresnelC}\left(\frac{2\sqrt{2}\arcsin(ax)}{\sqrt{\pi}}\right) - 960 (\arcsin(ax))^{1/2} \sqrt{\pi} \cos(2 \arcsin(ax)) + 60 (\arcsin(ax))^{1/2} \sqrt{\pi} \cos(4 \arcsin(ax)) + 480\pi \operatorname{FresnelC}\left(\frac{2\sqrt{2}\arcsin(ax)}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x)^(5/2),x)

[Out] -1/8192/a^4/Pi^(1/2)*(1024*arcsin(a*x)^(5/2)*Pi^(1/2)*cos(2*arcsin(a*x))-256*arcsin(a*x)^(5/2)*Pi^(1/2)*cos(4*arcsin(a*x))-1280*arcsin(a*x)^(3/2)*Pi^(1/2)*sin(2*arcsin(a*x))+160*arcsin(a*x)^(3/2)*Pi^(1/2)*sin(4*arcsin(a*x))-15*Pi*2^(1/2)*FresnelC(2*2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))-960*arcsin(a*x)^(1/2)*Pi^(1/2)*cos(2*arcsin(a*x))+60*arcsin(a*x)^(1/2)*Pi^(1/2)*cos(4*arcsin(a*x))+480*Pi*FresnelC(2*arcsin(a*x)^(1/2)/Pi^(1/2)))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x)**(5/2),x)

[Out] Timed out

Giac [C] time = 1.49425, size = 401, normalized size = 1.96

$$\frac{\arcsin(ax)^{\frac{5}{2}} e^{4i \arcsin(ax)}}{64 a^4} - \frac{\arcsin(ax)^{\frac{5}{2}} e^{2i \arcsin(ax)}}{16 a^4} - \frac{\arcsin(ax)^{\frac{5}{2}} e^{-2i \arcsin(ax)}}{16 a^4} + \frac{\arcsin(ax)^{\frac{5}{2}} e^{-4i \arcsin(ax)}}{64 a^4} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^(5/2),x, algorithm="giac")

[Out] $\frac{1}{64} \arcsin(ax)^{5/2} e^{4i \arcsin(ax)} / a^4 - \frac{1}{16} \arcsin(ax)^{5/2} e^{2i \arcsin(ax)} / a^4 + \frac{1}{16} \arcsin(ax)^{5/2} e^{-2i \arcsin(ax)} / a^4 - \frac{1}{64} \arcsin(ax)^{5/2} e^{-4i \arcsin(ax)} / a^4 + \frac{5}{512} i \arcsin(ax)^{3/2} e^{4i \arcsin(ax)} / a^4 - \frac{5}{64} i \arcsin(ax)^{3/2} e^{2i \arcsin(ax)} / a^4 + \frac{5}{64} i \arcsin(ax)^{3/2} e^{-2i \arcsin(ax)} / a^4 - \frac{5}{512} i \arcsin(ax)^{3/2} e^{-4i \arcsin(ax)} / a^4 - \frac{(15/32768 i + 15/32768) \sqrt{2} \sqrt{\pi} \operatorname{erf}((i-1)\sqrt{2}\sqrt{\arcsin(ax)})}{a^4} + \frac{(15/32768 i - 15/32768) \sqrt{2} \sqrt{\pi} \operatorname{erf}(-(i+1)\sqrt{2}\sqrt{\arcsin(ax)})}{a^4} + \frac{(15/1024 i + 15/1024) \sqrt{\pi} \operatorname{erf}((i-1)\sqrt{\arcsin(ax)})}{a^4} - \frac{(15/1024 i - 15/1024) \sqrt{\pi} \operatorname{erf}(-(i+1)\sqrt{\arcsin(ax)})}{a^4} - \frac{15}{4096} \sqrt{\arcsin(ax)} e^{4i \arcsin(ax)} / a^4 + \frac{15}{256} \sqrt{\arcsin(ax)} e^{2i \arcsin(ax)} / a^4 + \frac{15}{256} \sqrt{\arcsin(ax)} e^{-2i \arcsin(ax)} / a^4 - \frac{15}{4096} \sqrt{\arcsin(ax)} e^{-4i \arcsin(ax)} / a^4$

3.88 $\int x^2 \sin^{-1}(ax)^{5/2} dx$

Optimal. Leaf size=178

$$\frac{15\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^3} - \frac{5\sqrt{\frac{\pi}{6}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{144a^3} + \frac{5x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{18a} + \frac{5\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{9a^3} - \frac{5x\sqrt{\sin^{-1}(ax)}}{6a}$$

[Out] (-5*x*Sqrt[ArcSin[a*x]])/(6*a^2) - (5*x^3*Sqrt[ArcSin[a*x]])/36 + (5*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(9*a^3) + (5*x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(18*a) + (x^3*ArcSin[a*x]^(5/2))/3 + (15*Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(16*a^3) - (5*Sqrt[Pi/6]*FresnelS[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(144*a^3)

Rubi [A] time = 0.4692, antiderivative size = 178, normalized size of antiderivative = 1., number of steps used = 15, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4629, 4707, 4677, 4619, 4723, 3305, 3351, 3312}

$$\frac{15\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^3} - \frac{5\sqrt{\frac{\pi}{6}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{144a^3} + \frac{5x^2\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{18a} + \frac{5\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{9a^3} - \frac{5x\sqrt{\sin^{-1}(ax)}}{6a}$$

Antiderivative was successfully verified.

[In] Int[x^2*ArcSin[a*x]^(5/2),x]

[Out] (-5*x*Sqrt[ArcSin[a*x]])/(6*a^2) - (5*x^3*Sqrt[ArcSin[a*x]])/36 + (5*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(9*a^3) + (5*x^2*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(18*a) + (x^3*ArcSin[a*x]^(5/2))/3 + (15*Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(16*a^3) - (5*Sqrt[Pi/6]*FresnelS[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(144*a^3)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((f_.)*(x_.))^(m_.))/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_.)*((d_.) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d*IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n

, 0] && NeQ[p, -1]

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rubi steps

$$\begin{aligned}
\int x^2 \sin^{-1}(ax)^{5/2} dx &= \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{1}{6}(5a) \int \frac{x^3 \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{5x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{18a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{5}{12} \int x^2 \sqrt{\sin^{-1}(ax)} dx - \frac{5 \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx}{9a} \\
&= -\frac{5}{36}x^3 \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{9a^3} + \frac{5x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{18a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{5}{3} \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{5x\sqrt{\sin^{-1}(ax)}}{6a^2} - \frac{5}{36}x^3 \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{9a^3} + \frac{5x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{18a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{5}{3} \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{5x\sqrt{\sin^{-1}(ax)}}{6a^2} - \frac{5}{36}x^3 \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{9a^3} + \frac{5x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{18a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{5}{3} \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{5x\sqrt{\sin^{-1}(ax)}}{6a^2} - \frac{5}{36}x^3 \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{9a^3} + \frac{5x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{18a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{5}{3} \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{5x\sqrt{\sin^{-1}(ax)}}{6a^2} - \frac{5}{36}x^3 \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{9a^3} + \frac{5x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{18a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{5}{3} \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{5x\sqrt{\sin^{-1}(ax)}}{6a^2} - \frac{5}{36}x^3 \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{9a^3} + \frac{5x^2\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{18a} + \frac{1}{3}x^3 \sin^{-1}(ax)^{5/2} - \frac{5}{3} \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx
\end{aligned}$$

Mathematica [C] time = 0.0465538, size = 125, normalized size = 0.7

$$\frac{-81\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, -i \sin^{-1}(ax)\right) - 81\sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, i \sin^{-1}(ax)\right) + \sqrt{3} \left(\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, -i \sin^{-1}(ax)\right) + \sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, i \sin^{-1}(ax)\right) \right)}{648a^3 \sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2*ArcSin[a*x]^(5/2),x]

[Out] (-81*sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (-I)*ArcSin[a*x]] - 81*sqrt[I*ArcSin[a*x]]*Gamma[7/2, I*ArcSin[a*x]] + sqrt[3]*(sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (-3*I)*ArcSin[a*x]] + sqrt[I*ArcSin[a*x]]*Gamma[7/2, (3*I)*ArcSin[a*x]]))/(648*a^3*sqrt[ArcSin[a*x]])

Maple [A] time = 0.055, size = 156, normalized size = 0.9

$$-\frac{1}{864a^3} \left(-216ax (\arcsin(ax))^3 + 72 (\arcsin(ax))^3 \sin(3 \arcsin(ax)) + 5\sqrt{3}\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi} \operatorname{FresnelS}\left(\frac{\sqrt{3}\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*arcsin(a*x)^(5/2),x)

[Out] -1/864/a^3/arcsin(a*x)^(1/2)*(-216*a*x*arcsin(a*x)^3+72*arcsin(a*x)^3*sin(3*arcsin(a*x))+5*3^(1/2)*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*3^(1/2)*arcsin(a*x)^(1/2))-540*arcsin(a*x)^2*(-a^2*x^2+1)^(1/2)+60*arcsin(a*x)^2*cos(3*arcsin(a*x))-405*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*F


```
resnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))+810*a*x*arcsin(a*x)-30*arcsin(a*x)*sin(3*arcsin(a*x))
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*arcsin(a*x)^(5/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*arcsin(a*x)^(5/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*asin(a*x)**(5/2),x)
```

```
[Out] Timed out
```

Giac [C] time = 1.43601, size = 417, normalized size = 2.34

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*arcsin(a*x)^(5/2),x, algorithm="giac")
```

```
[Out] 1/24*I*arcsin(a*x)^(5/2)*e^(3*I*arcsin(a*x))/a^3 - 1/8*I*arcsin(a*x)^(5/2)*
e^(I*arcsin(a*x))/a^3 + 1/8*I*arcsin(a*x)^(5/2)*e^(-I*arcsin(a*x))/a^3 - 1/
24*I*arcsin(a*x)^(5/2)*e^(-3*I*arcsin(a*x))/a^3 - 5/144*arcsin(a*x)^(3/2)*e
^(3*I*arcsin(a*x))/a^3 + 5/16*arcsin(a*x)^(3/2)*e^(I*arcsin(a*x))/a^3 + 5/1
6*arcsin(a*x)^(3/2)*e^(-I*arcsin(a*x))/a^3 - 5/144*arcsin(a*x)^(3/2)*e^(-3*
I*arcsin(a*x))/a^3 - (5/3456*I - 5/3456)*sqrt(6)*sqrt(pi)*erf((1/2*I - 1/2)
*sqrt(6)*sqrt(arcsin(a*x)))/a^3 + (5/3456*I + 5/3456)*sqrt(6)*sqrt(pi)*erf(
-(1/2*I + 1/2)*sqrt(6)*sqrt(arcsin(a*x)))/a^3 + (15/128*I - 15/128)*sqrt(2)
```

$$\begin{aligned}
& * \sqrt{\pi} \operatorname{erf}\left(\frac{1}{2}I - \frac{1}{2}\right) \sqrt{2} \sqrt{\arcsin(ax)} / a^3 - \left(\frac{15}{128}I + \frac{15}{128}\right) \sqrt{2} \sqrt{\pi} \operatorname{erf}\left(-\frac{1}{2}I + \frac{1}{2}\right) \sqrt{2} \sqrt{\arcsin(ax)} / a^3 - \\
& \frac{5}{288}I \sqrt{\arcsin(ax)} e^{3I \arcsin(ax)} / a^3 + \frac{15}{32}I \sqrt{\arcsin(ax)} e^{I \arcsin(ax)} / a^3 - \frac{15}{32}I \sqrt{\arcsin(ax)} e^{-I \arcsin(ax)} / a^3 \\
& + \frac{5}{288}I \sqrt{\arcsin(ax)} e^{-3I \arcsin(ax)} / a^3
\end{aligned}$$

3.89 $\int x \sin^{-1}(ax)^{5/2} dx$

Optimal. Leaf size=119

$$\frac{15\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{128a^2} + \frac{5x\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{15\sqrt{\sin^{-1}(ax)}}{64a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^{5/2} - \frac{15}{32}x^2$$

[Out] (15*Sqrt[ArcSin[a*x]])/(64*a^2) - (15*x^2*Sqrt[ArcSin[a*x]])/32 + (5*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(8*a) - ArcSin[a*x]^(5/2)/(4*a^2) + (x^2*ArcSin[a*x]^(5/2))/2 - (15*Sqrt[Pi]*FresnelC[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(128*a^2)

Rubi [A] time = 0.312713, antiderivative size = 119, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {4629, 4707, 4641, 4723, 3312, 3304, 3352}

$$\frac{15\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{128a^2} + \frac{5x\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{15\sqrt{\sin^{-1}(ax)}}{64a^2} + \frac{1}{2}x^2\sin^{-1}(ax)^{5/2} - \frac{15}{32}x^2$$

Antiderivative was successfully verified.

[In] Int[x*ArcSin[a*x]^(5/2),x]

[Out] (15*Sqrt[ArcSin[a*x]])/(64*a^2) - (15*x^2*Sqrt[ArcSin[a*x]])/32 + (5*x*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(8*a) - ArcSin[a*x]^(5/2)/(4*a^2) + (x^2*ArcSin[a*x]^(5/2))/2 - (15*Sqrt[Pi]*FresnelC[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(128*a^2)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((f_.)*(x_)^(m_.))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sqrt[x]^m*C

```
os[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] &&
EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (Integer
Q[p] || GtQ[d, 0])
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] :> In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> D
ist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d
, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] :> Simp[(Sqrt[Pi/2]*Fresne
lC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned}
\int x \sin^{-1}(ax)^{5/2} dx &= \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} - \frac{1}{4}(5a) \int \frac{x^2 \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{5x\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{8a} + \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} - \frac{15}{16} \int x \sqrt{\sin^{-1}(ax)} dx - \frac{5 \int \frac{\sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx}{8a} \\
&= -\frac{15}{32}x^2 \sqrt{\sin^{-1}(ax)} + \frac{5x\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} + \frac{1}{64}(15a) \int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx \\
&= -\frac{15}{32}x^2 \sqrt{\sin^{-1}(ax)} + \frac{5x\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} + \frac{15 \text{Subst}\left(\int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx\right)}{64} \\
&= -\frac{15}{32}x^2 \sqrt{\sin^{-1}(ax)} + \frac{5x\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} + \frac{15 \text{Subst}\left(\int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx\right)}{64} \\
&= \frac{15\sqrt{\sin^{-1}(ax)}}{64a^2} - \frac{15}{32}x^2 \sqrt{\sin^{-1}(ax)} + \frac{5x\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} - \frac{15 \text{Subst}\left(\int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx\right)}{64} \\
&= \frac{15\sqrt{\sin^{-1}(ax)}}{64a^2} - \frac{15}{32}x^2 \sqrt{\sin^{-1}(ax)} + \frac{5x\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} - \frac{15 \text{Subst}\left(\int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx\right)}{64} \\
&= \frac{15\sqrt{\sin^{-1}(ax)}}{64a^2} - \frac{15}{32}x^2 \sqrt{\sin^{-1}(ax)} + \frac{5x\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{8a} - \frac{\sin^{-1}(ax)^{5/2}}{4a^2} + \frac{1}{2}x^2 \sin^{-1}(ax)^{5/2} - \frac{15 \text{Subst}\left(\int \frac{\sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx\right)}{64}
\end{aligned}$$

Mathematica [C] time = 0.0195838, size = 81, normalized size = 0.68

$$\frac{\sqrt{\sin^{-1}(ax)} \left(\sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, -2i \sin^{-1}(ax)\right) + \sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{7}{2}, 2i \sin^{-1}(ax)\right) \right)}{32\sqrt{2}a^2\sqrt{\sin^{-1}(ax)^2}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[x*ArcSin[a*x]^(5/2), x]
```

```
[Out] (Sqrt[ArcSin[a*x]]*(Sqrt[I*ArcSin[a*x]]*Gamma[7/2, (-2*I)*ArcSin[a*x]] + Sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (2*I)*ArcSin[a*x]]))/(32*Sqrt[2]*a^2*Sqrt[ArcSin[a*x]^2])
```

Maple [A] time = 0.036, size = 79, normalized size = 0.7

$$-\frac{1}{128 a^2 \sqrt{\pi}} \left(32 (\arcsin(ax))^{5/2} \sqrt{\pi} \cos(2 \arcsin(ax)) - 40 (\arcsin(ax))^{3/2} \sqrt{\pi} \sin(2 \arcsin(ax)) - 30 \sqrt{\arcsin(ax)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*arcsin(a*x)^(5/2),x)
```

```
[Out] -1/128/a^2/Pi^(1/2)*(32*arcsin(a*x)^(5/2)*Pi^(1/2)*cos(2*arcsin(a*x))-40*arcsin(a*x)^(3/2)*Pi^(1/2)*sin(2*arcsin(a*x))-30*arcsin(a*x)^(1/2)*Pi^(1/2)*cos(2*arcsin(a*x))+15*Pi*FresnelC(2*arcsin(a*x)^(1/2)/Pi^(1/2)))
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*arcsin(a*x)^(5/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*arcsin(a*x)^(5/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*asin(a*x)**(5/2),x)
```

```
[Out] Timed out
```

Giac [C] time = 1.46285, size = 193, normalized size = 1.62

$$-\frac{\arcsin(ax)^{\frac{5}{2}} e^{2i \arcsin(ax)}}{8 a^2} - \frac{\arcsin(ax)^{\frac{5}{2}} e^{-2i \arcsin(ax)}}{8 a^2} - \frac{5i \arcsin(ax)^{\frac{3}{2}} e^{2i \arcsin(ax)}}{32 a^2} + \frac{5i \arcsin(ax)^{\frac{3}{2}} e^{-2i \arcsin(ax)}}{32 a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*arcsin(a*x)^(5/2),x, algorithm="giac")

[Out] $-1/8*\arcsin(a*x)^{(5/2)}*e^{(2*I*\arcsin(a*x))}/a^2 - 1/8*\arcsin(a*x)^{(5/2)}*e^{(-2*I*\arcsin(a*x))}/a^2 - 5/32*I*\arcsin(a*x)^{(3/2)}*e^{(2*I*\arcsin(a*x))}/a^2 + 5/32*I*\arcsin(a*x)^{(3/2)}*e^{(-2*I*\arcsin(a*x))}/a^2 + (15/512*I + 15/512)*\sqrt{\pi}*\operatorname{erf}((I - 1)*\sqrt{\arcsin(a*x)})/a^2 - (15/512*I - 15/512)*\sqrt{\pi}*\operatorname{erf}(-(I + 1)*\sqrt{\arcsin(a*x)})/a^2 + 15/128*\sqrt{\arcsin(a*x)}*e^{(2*I*\arcsin(a*x))}/a^2 + 15/128*\sqrt{\arcsin(a*x)}*e^{(-2*I*\arcsin(a*x))}/a^2$

3.90 $\int \sin^{-1}(ax)^{5/2} dx$

Optimal. Leaf size=88

$$\frac{5\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{2a} + \frac{15\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{4a} + x\sin^{-1}(ax)^{5/2} - \frac{15}{4}x\sqrt{\sin^{-1}(ax)}$$

[Out] (-15*x*Sqrt[ArcSin[a*x]])/4 + (5*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(2*a) + x*ArcSin[a*x]^(5/2) + (15*Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4*a)

Rubi [A] time = 0.164965, antiderivative size = 88, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4619, 4677, 4723, 3305, 3351}

$$\frac{5\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}}{2a} + \frac{15\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{4a} + x\sin^{-1}(ax)^{5/2} - \frac{15}{4}x\sqrt{\sin^{-1}(ax)}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^(5/2), x]

[Out] (-15*x*Sqrt[ArcSin[a*x]])/4 + (5*Sqrt[1 - a^2*x^2]*ArcSin[a*x]^(3/2))/(2*a) + x*ArcSin[a*x]^(5/2) + (15*Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4*a)

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^(2)], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned}
\int \sin^{-1}(ax)^{5/2} dx &= x \sin^{-1}(ax)^{5/2} - \frac{1}{2}(5a) \int \frac{x \sin^{-1}(ax)^{3/2}}{\sqrt{1-a^2x^2}} dx \\
&= \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{2a} + x \sin^{-1}(ax)^{5/2} - \frac{15}{4} \int \sqrt{\sin^{-1}(ax)} dx \\
&= -\frac{15}{4} x \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{2a} + x \sin^{-1}(ax)^{5/2} + \frac{1}{8}(15a) \int \frac{x}{\sqrt{1-a^2x^2} \sqrt{\sin^{-1}(ax)}} dx \\
&= -\frac{15}{4} x \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{2a} + x \sin^{-1}(ax)^{5/2} + \frac{15 \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a} \\
&= -\frac{15}{4} x \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{2a} + x \sin^{-1}(ax)^{5/2} + \frac{15 \operatorname{Subst}\left(\int \sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a} \\
&= -\frac{15}{4} x \sqrt{\sin^{-1}(ax)} + \frac{5\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}}{2a} + x \sin^{-1}(ax)^{5/2} + \frac{15\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a}
\end{aligned}$$

Mathematica [C] time = 0.0354744, size = 68, normalized size = 0.77

$$\frac{-\sqrt{-i \sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{7}{2}, -i \sin^{-1}(ax)\right) - \sqrt{i \sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{7}{2}, i \sin^{-1}(ax)\right)}{2a \sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[ArcSin[a*x]^(5/2), x]
```

```
[Out] (-(Sqrt[(-I)*ArcSin[a*x]]*Gamma[7/2, (-I)*ArcSin[a*x]]) - Sqrt[I*ArcSin[a*x]]*Gamma[7/2, I*ArcSin[a*x]])/(2*a*Sqrt[ArcSin[a*x]])
```

Maple [A] time = 0.037, size = 88, normalized size = 1.

$$\frac{\sqrt{2}}{8a\sqrt{\pi}} \left(4 (\arcsin(ax))^{5/2} \sqrt{2}\sqrt{\pi}xa + 10 (\arcsin(ax))^{3/2} \sqrt{2}\sqrt{\pi}\sqrt{-a^2x^2+1} - 15 \sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}xa + 15 \pi \operatorname{FresnelS} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(arcsin(a*x)^(5/2), x)
```

```
[Out] 1/8/a*2^(1/2)/Pi^(1/2)*(4*arcsin(a*x)^(5/2)*2^(1/2)*Pi^(1/2)*x*a+10*arcsin(a*x)^(3/2)*2^(1/2)*Pi^(1/2)*(-a^2*x^2+1)^(1/2)-15*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*x*a+15*Pi*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))
```


Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**(5/2),x)

[Out] Timed out

Giac [C] time = 1.51359, size = 209, normalized size = 2.38

$$\frac{i \arcsin(ax)^{\frac{5}{2}} e^{i \arcsin(ax)}}{2a} + \frac{i \arcsin(ax)^{\frac{5}{2}} e^{-i \arcsin(ax)}}{2a} + \frac{5 \arcsin(ax)^{\frac{3}{2}} e^{i \arcsin(ax)}}{4a} + \frac{5 \arcsin(ax)^{\frac{3}{2}} e^{-i \arcsin(ax)}}{4a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(5/2),x, algorithm="giac")

[Out] $-1/2*I*\arcsin(a*x)^{(5/2)}*e^{(I*\arcsin(a*x))/a} + 1/2*I*\arcsin(a*x)^{(5/2)}*e^{(-I*\arcsin(a*x))/a} + 5/4*\arcsin(a*x)^{(3/2)}*e^{(I*\arcsin(a*x))/a} + 5/4*\arcsin(a*x)^{(3/2)}*e^{(-I*\arcsin(a*x))/a} + (15/32*I - 15/32)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a - (15/32*I + 15/32)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a + 15/8*I*\sqrt{\arcsin(a*x)}*e^{(I*\arcsin(a*x))/a} - 15/8*I*\sqrt{\arcsin(a*x)}*e^{(-I*\arcsin(a*x))/a}$

$$3.91 \quad \int \frac{\sin^{-1}(ax)^{5/2}}{x} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{\sin^{-1}(ax)^{5/2}}{x}, x\right)$$

[Out] Unintegrable[ArcSin[a*x]^(5/2)/x, x]

Rubi [A] time = 0.0125499, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin^{-1}(ax)^{5/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Int[ArcSin[a*x]^(5/2)/x,x]

[Out] Defer[Int][ArcSin[a*x]^(5/2)/x, x]

Rubi steps

$$\int \frac{\sin^{-1}(ax)^{5/2}}{x} dx = \int \frac{\sin^{-1}(ax)^{5/2}}{x} dx$$

Mathematica [A] time = 0.373316, size = 0, normalized size = 0.

$$\int \frac{\sin^{-1}(ax)^{5/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[ArcSin[a*x]^(5/2)/x,x]

[Out] Integrate[ArcSin[a*x]^(5/2)/x, x]

Maple [A] time = 0.063, size = 0, normalized size = 0.

$$\int \frac{1}{x} (\arcsin(ax))^{\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^(5/2)/x,x)

[Out] int(arcsin(a*x)^(5/2)/x,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(5/2)/x,x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(5/2)/x,x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**(5/2)/x,x)

[Out] Timed out

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^{\frac{5}{2}}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^(5/2)/x,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^(5/2)/x, x)

$$3.92 \quad \int \frac{x^4}{\sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=106

$$\frac{\sqrt{\frac{\pi}{2}} \text{FresnelC}\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{\sqrt{\frac{3\pi}{2}} \text{FresnelC}\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^5} + \frac{\sqrt{\frac{\pi}{10}} \text{FresnelC}\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^5}$$

[Out] (Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4*a^5) - (Sqrt[(3*Pi)/2]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^5) + (Sqrt[Pi/10]*FresnelC[Sqrt[10/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^5)

Rubi [A] time = 0.111608, antiderivative size = 106, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4635, 4406, 3304, 3352}

$$\frac{\sqrt{\frac{\pi}{2}} \text{FresnelC}\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{\sqrt{\frac{3\pi}{2}} \text{FresnelC}\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^5} + \frac{\sqrt{\frac{\pi}{10}} \text{FresnelC}\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{8a^5}$$

Antiderivative was successfully verified.

[In] Int[x^4/Sqrt[ArcSin[a*x]],x]

[Out] (Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(4*a^5) - (Sqrt[(3*Pi)/2]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^5) + (Sqrt[Pi/10]*FresnelC[Sqrt[10/Pi]*Sqrt[ArcSin[a*x]]])/(8*a^5)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_)*(x_)^(m_), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] :> Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
\int \frac{x^4}{\sqrt{\sin^{-1}(ax)}} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^4(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^5} \\
&= \frac{\text{Subst}\left(\int \left(\frac{\cos(x)}{8\sqrt{x}} - \frac{3\cos(3x)}{16\sqrt{x}} + \frac{\cos(5x)}{16\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^5} \\
&= \frac{\text{Subst}\left(\int \frac{\cos(5x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{16a^5} + \frac{\text{Subst}\left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^5} - \frac{3\text{Subst}\left(\int \frac{\cos(3x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{16a^5} \\
&= \frac{\text{Subst}\left(\int \cos(5x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{8a^5} + \frac{\text{Subst}\left(\int \cos(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{3\text{Subst}\left(\int \cos(3x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{16a^5} \\
&= \frac{\sqrt{\frac{\pi}{2}}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{\sqrt{\frac{3\pi}{2}}C\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^5} + \frac{\sqrt{\frac{\pi}{10}}C\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^5}
\end{aligned}$$

Mathematica [C] time = 0.0565194, size = 193, normalized size = 1.82

$$i\left(10\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right) - 10\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, i\sin^{-1}(ax)\right) - 5\sqrt{3}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right) + 5\sqrt{3}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, i\sin^{-1}(ax)\right)\right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^4/Sqrt[ArcSin[a*x]], x]

[Out] $((-I/160)*(10*\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\Gamma[1/2, (-I)*\text{ArcSin}[a*x]] - 10*\text{Sqrt}[I*\text{ArcSin}[a*x]]*\Gamma[1/2, I*\text{ArcSin}[a*x]] - 5*\text{Sqrt}[3]*\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\Gamma[1/2, (-3*I)*\text{ArcSin}[a*x]] + 5*\text{Sqrt}[3]*\text{Sqrt}[I*\text{ArcSin}[a*x]]*\Gamma[1/2, (3*I)*\text{ArcSin}[a*x]] + \text{Sqrt}[5]*\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\Gamma[1/2, (-5*I)*\text{ArcSin}[a*x]] - \text{Sqrt}[5]*\text{Sqrt}[I*\text{ArcSin}[a*x]]*\Gamma[1/2, (5*I)*\text{ArcSin}[a*x]]))/(a^5*\text{Sqrt}[\text{ArcSin}[a*x]])$

Maple [A] time = 0.055, size = 72, normalized size = 0.7

$$\frac{\sqrt{2}\sqrt{\pi}}{80a^5}\left(\sqrt{5}\text{FresnelC}\left(\frac{\sqrt{2}\sqrt{5}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right) - 5\sqrt{3}\text{FresnelC}\left(\frac{\sqrt{2}\sqrt{3}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + 10\text{FresnelC}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x)^(1/2), x)

[Out] $1/80/a^5*2^{(1/2)}*\text{Pi}^{(1/2)}*(5^{(1/2)}*\text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)}*5^{(1/2)}*\arcsin(a*x)^{(1/2)}) - 5*3^{(1/2)}*\text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)}*3^{(1/2)}*\arcsin(a*x)^{(1/2)}) + 10*\text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)}*\arcsin(a*x)^{(1/2)})$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(1/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/asin(a*x)**(1/2),x)

[Out] Integral(x**4/sqrt(asin(a*x)), x)

Giac [C] time = 1.45233, size = 188, normalized size = 1.77

$$\frac{(i+1)\sqrt{10}\sqrt{\pi}\operatorname{erf}\left(\left(\frac{1}{2}i-\frac{1}{2}\right)\sqrt{10}\sqrt{\arcsin(ax)}\right)}{320a^5} + \frac{(i-1)\sqrt{10}\sqrt{\pi}\operatorname{erf}\left(-\left(\frac{1}{2}i+\frac{1}{2}\right)\sqrt{10}\sqrt{\arcsin(ax)}\right)}{320a^5} + \frac{(i+1)\sqrt{6}\sqrt{\pi}\operatorname{erf}\left(\left(\frac{1}{2}i-\frac{1}{2}\right)\sqrt{6}\sqrt{\arcsin(ax)}\right)}{320a^5} + \frac{(i-1)\sqrt{6}\sqrt{\pi}\operatorname{erf}\left(-\left(\frac{1}{2}i+\frac{1}{2}\right)\sqrt{6}\sqrt{\arcsin(ax)}\right)}{320a^5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] $-(1/320*I + 1/320)*\sqrt{10}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{10}*\sqrt{\arcsin(a*x)})/a^5 + (1/320*I - 1/320)*\sqrt{10}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{10}*\sqrt{\arcsin(a*x)})/a^5 + (1/64*I + 1/64)*\sqrt{6}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{6}*\sqrt{\arcsin(a*x)})/a^5 - (1/64*I - 1/64)*\sqrt{6}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{6}*\sqrt{\arcsin(a*x)})/a^5 - (1/32*I + 1/32)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a^5 + (1/32*I - 1/32)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a^5$

$$3.93 \quad \int \frac{x^3}{\sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=65

$$\frac{\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{4a^4} - \frac{\sqrt{\frac{\pi}{2}} S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^4}$$

[Out] -(Sqrt [Pi/2]*FresnelS [2*Sqrt [2/Pi]*Sqrt [ArcSin [a*x]]])/(8*a^4) + (Sqrt [Pi]*FresnelS [(2*Sqrt [ArcSin [a*x]])/Sqrt [Pi]])/(4*a^4)

Rubi [A] time = 0.0826256, antiderivative size = 65, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4635, 4406, 3305, 3351}

$$\frac{\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{4a^4} - \frac{\sqrt{\frac{\pi}{2}} S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^4}$$

Antiderivative was successfully verified.

[In] Int [x^3/Sqrt [ArcSin [a*x]], x]

[Out] -(Sqrt [Pi/2]*FresnelS [2*Sqrt [2/Pi]*Sqrt [ArcSin [a*x]]])/(8*a^4) + (Sqrt [Pi]*FresnelS [(2*Sqrt [ArcSin [a*x]])/Sqrt [Pi]])/(4*a^4)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_.)*(x_)^ (m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^ (p_.)*((c_.) + (d_.)*(x_)) ^ (m_.)*Sin[(a_.) + (b_.)*(x_)]^ (n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt [Pi/2]*FresnelS [Sqrt [2/Pi]*Rt [d, 2]*(e + f*x)])/(f*Rt [d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
\int \frac{x^3}{\sqrt{\sin^{-1}(ax)}} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^3(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^4} \\
&= \frac{\text{Subst}\left(\int \left(\frac{\sin(2x)}{4\sqrt{x}} - \frac{\sin(4x)}{8\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^4} \\
&= -\frac{\text{Subst}\left(\int \frac{\sin(4x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^4} + \frac{\text{Subst}\left(\int \frac{\sin(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{4a^4} \\
&= -\frac{\text{Subst}\left(\int \sin(4x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^4} + \frac{\text{Subst}\left(\int \sin(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{2a^4} \\
&= -\frac{\sqrt{\frac{\pi}{2}} S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^4} + \frac{\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{4a^4}
\end{aligned}$$

Mathematica [C] time = 0.0323625, size = 128, normalized size = 1.97

$$\frac{-2\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) - 2\sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right) + \sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right) + \sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, i\sin^{-1}(ax)\right)}{32a^4\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3/Sqrt[ArcSin[a*x]], x]

[Out] $(-2*\text{Sqrt}[2]*\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\Gamma[1/2, (-2*I)*\text{ArcSin}[a*x]] - 2*\text{Sqrt}[2]*\text{Sqrt}[I*\text{ArcSin}[a*x]]*\Gamma[1/2, (2*I)*\text{ArcSin}[a*x]] + \text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\Gamma[1/2, (-4*I)*\text{ArcSin}[a*x]] + \text{Sqrt}[I*\text{ArcSin}[a*x]]*\Gamma[1/2, (4*I)*\text{ArcSin}[a*x]])/(32*a^4*\text{Sqrt}[\text{ArcSin}[a*x]])$

Maple [A] time = 0.039, size = 44, normalized size = 0.7

$$\frac{\sqrt{\pi}}{16a^4} \left(-\sqrt{2}\text{FresnelS}\left(2\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + 4\text{FresnelS}\left(2\frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/arcsin(a*x)^(1/2), x)

[Out] $1/16/a^4*\text{Pi}^{(1/2)}*(-2^{(1/2)}*\text{FresnelS}(2*2^{(1/2)}/\text{Pi}^{(1/2)}*\arcsin(a*x)^{(1/2)})+4*\text{FresnelS}(2*\arcsin(a*x)^{(1/2)}/\text{Pi}^{(1/2)}))$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^(1/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x³/arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/asin(a*x)**(1/2),x)

[Out] Integral(x**3/sqrt(asin(a*x)), x)

Giac [C] time = 1.47587, size = 109, normalized size = 1.68

$$-\frac{(i-1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left((i-1)\sqrt{2}\sqrt{\arcsin(ax)}\right)}{64a^4} + \frac{(i+1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-(i+1)\sqrt{2}\sqrt{\arcsin(ax)}\right)}{64a^4} + \frac{(i-1)\sqrt{\pi}\operatorname{erf}\left((i-1)\sqrt{\arcsin(ax)}\right)}{16a^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x³/arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] $-(1/64*I - 1/64)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}((I - 1)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a^4 + (1/64*I + 1/64)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-(I + 1)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a^4 + (1/16*I - 1/16)*\sqrt{\pi}*\operatorname{erf}((I - 1)*\sqrt{\arcsin(a*x)})/a^4 - (1/16*I + 1/16)*\sqrt{\pi}*\operatorname{erf}(-(I + 1)*\sqrt{\arcsin(a*x)})/a^4$

$$3.94 \quad \int \frac{x^2}{\sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=71

$$\frac{\sqrt{\frac{\pi}{2}} \text{FresnelC}\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^3} - \frac{\sqrt{\frac{\pi}{6}} \text{FresnelC}\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^3}$$

[Out] (Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(2*a^3) - (Sqrt[Pi/6]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(2*a^3)

Rubi [A] time = 0.0892158, antiderivative size = 71, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4635, 4406, 3304, 3352}

$$\frac{\sqrt{\frac{\pi}{2}} \text{FresnelC}\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^3} - \frac{\sqrt{\frac{\pi}{6}} \text{FresnelC}\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/Sqrt[ArcSin[a*x]], x]

[Out] (Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(2*a^3) - (Sqrt[Pi/6]*FresnelC[Sqrt[6/Pi]*Sqrt[ArcSin[a*x]]])/(2*a^3)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_)*(x_)^(m_), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] :> Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/ (f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
\int \frac{x^2}{\sqrt{\sin^{-1}(ax)}} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin^2(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^3} \\
&= \frac{\text{Subst}\left(\int \left(\frac{\cos(x)}{4\sqrt{x}} - \frac{\cos(3x)}{4\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^3} \\
&= \frac{\text{Subst}\left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{4a^3} - \frac{\text{Subst}\left(\int \frac{\cos(3x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{4a^3} \\
&= \frac{\text{Subst}\left(\int \cos(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{2a^3} - \frac{\text{Subst}\left(\int \cos(3x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{2a^3} \\
&= \frac{\sqrt{\frac{\pi}{2}} C\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^3} - \frac{\sqrt{\frac{\pi}{6}} C\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^3}
\end{aligned}$$

Mathematica [C] time = 0.0508396, size = 128, normalized size = 1.8

$$\frac{i\left(3\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right) - 3\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, i\sin^{-1}(ax)\right) + \sqrt{3}\left(\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, \sqrt{3}i\sin^{-1}(ax)\right) - \sqrt{3}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -\sqrt{3}i\sin^{-1}(ax)\right)\right)\right)}{24a^3\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2/Sqrt[ArcSin[a*x]], x]

[Out] ((-I/24)*(3*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-I)*ArcSin[a*x]] - 3*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, I*ArcSin[a*x]] + Sqrt[3]*(-(Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-3*I)*ArcSin[a*x]]) + Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (3*I)*ArcSin[a*x]])))/(a^3*Sqrt[ArcSin[a*x]])

Maple [A] time = 0.039, size = 51, normalized size = 0.7

$$\frac{\sqrt{2}\sqrt{\pi}}{12a^3} \left(-\sqrt{3}\text{FresnelC}\left(\frac{\sqrt{2}\sqrt{3}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right) + 3\text{FresnelC}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/arcsin(a*x)^(1/2), x)

[Out] 1/12/a^3*2^(1/2)*Pi^(1/2)*(-3^(1/2)*FresnelC(2^(1/2)/Pi^(1/2)*3^(1/2)*arcsin(a*x)^(1/2))+3*FresnelC(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(1/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/asin(a*x)**(1/2),x)

[Out] Integral(x**2/sqrt(asin(a*x)), x)

Giac [C] time = 1.4345, size = 126, normalized size = 1.77

$$\frac{(i+1)\sqrt{6}\sqrt{\pi}\operatorname{erf}\left(\left(\frac{1}{2}i-\frac{1}{2}\right)\sqrt{6}\sqrt{\arcsin(ax)}\right)}{48a^3} - \frac{(i-1)\sqrt{6}\sqrt{\pi}\operatorname{erf}\left(-\left(\frac{1}{2}i+\frac{1}{2}\right)\sqrt{6}\sqrt{\arcsin(ax)}\right)}{48a^3} - \frac{(i+1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(\left(\frac{1}{2}i\right)\sqrt{2}\sqrt{\arcsin(ax)}\right)}{16a^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] (1/48*I + 1/48)*sqrt(6)*sqrt(pi)*erf((1/2*I - 1/2)*sqrt(6)*sqrt(arcsin(a*x)))/a^3 - (1/48*I - 1/48)*sqrt(6)*sqrt(pi)*erf(-(1/2*I + 1/2)*sqrt(6)*sqrt(arcsin(a*x)))/a^3 - (1/16*I + 1/16)*sqrt(2)*sqrt(pi)*erf((1/2*I - 1/2)*sqrt(2)*sqrt(arcsin(a*x)))/a^3 + (1/16*I - 1/16)*sqrt(2)*sqrt(pi)*erf(-(1/2*I + 1/2)*sqrt(2)*sqrt(arcsin(a*x)))/a^3

$$3.95 \quad \int \frac{x}{\sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=28

$$\frac{\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{2a^2}$$

[Out] (Sqrt[Pi]*FresnelS[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(2*a^2)

Rubi [A] time = 0.0447623, antiderivative size = 28, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4635, 4406, 12, 3305, 3351}

$$\frac{\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{2a^2}$$

Antiderivative was successfully verified.

[In] Int[x/Sqrt[ArcSin[a*x]],x]

[Out] (Sqrt[Pi]*FresnelS[(2*Sqrt[ArcSin[a*x]])/Sqrt[Pi]])/(2*a^2)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
\int \frac{x}{\sqrt{\sin^{-1}(ax)}} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^2} \\
&= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{2\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^2} \\
&= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{2a^2} \\
&= \frac{\text{Subst}\left(\int \sin(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a^2} \\
&= \frac{\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{2a^2}
\end{aligned}$$

Mathematica [C] time = 0.0173538, size = 71, normalized size = 2.54

$$\frac{\sqrt{-i \sin^{-1}(ax)} \Gamma\left(\frac{1}{2}, -2i \sin^{-1}(ax)\right) + \sqrt{i \sin^{-1}(ax)} \Gamma\left(\frac{1}{2}, 2i \sin^{-1}(ax)\right)}{4\sqrt{2}a^2\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x/Sqrt[ArcSin[a*x]], x]

[Out] -(Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-2*I)*ArcSin[a*x]] + Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (2*I)*ArcSin[a*x]])/(4*Sqrt[2]*a^2*Sqrt[ArcSin[a*x]])

Maple [A] time = 0.029, size = 21, normalized size = 0.8

$$\frac{\sqrt{\pi}}{2a^2} \text{FresnelS}\left(2 \frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/arcsin(a*x)^(1/2), x)

[Out] 1/2*FresnelS(2*arcsin(a*x)^(1/2)/Pi^(1/2))*Pi^(1/2)/a^2

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(1/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\sqrt{\operatorname{asin}(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/asin(a*x)**(1/2),x)

[Out] Integral(x/sqrt(asin(a*x)), x)

Giac [C] time = 1.47883, size = 47, normalized size = 1.68

$$\frac{(i-1)\sqrt{\pi}\operatorname{erf}\left((i-1)\sqrt{\operatorname{arcsin}(ax)}\right)}{8a^2} - \frac{(i+1)\sqrt{\pi}\operatorname{erf}\left(-(i+1)\sqrt{\operatorname{arcsin}(ax)}\right)}{8a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] (1/8*I - 1/8)*sqrt(pi)*erf((I - 1)*sqrt(arcsin(a*x)))/a^2 - (1/8*I + 1/8)*sqrt(pi)*erf(-(I + 1)*sqrt(arcsin(a*x)))/a^2

$$3.96 \quad \int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=30

$$\frac{\sqrt{2\pi}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a}$$

[Out] (Sqrt[2*Pi]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/a

Rubi [A] time = 0.0244487, antiderivative size = 30, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {4623, 3304, 3352}

$$\frac{\sqrt{2\pi}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a}$$

Antiderivative was successfully verified.

[In] Int[1/Sqrt[ArcSin[a*x]],x]

[Out] (Sqrt[2*Pi]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/a

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_], x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a} \\ &= \frac{2 \text{Subst}\left(\int \cos(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a} \\ &= \frac{\sqrt{2\pi}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a} \end{aligned}$$

Mathematica [C] time = 0.0256741, size = 69, normalized size = 2.3

$$\frac{i\left(\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right) - \sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, i\sin^{-1}(ax)\right)\right)}{2a\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[1/Sqrt[ArcSin[a*x]], x]

[Out] $((-I/2)*(\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\Gamma[1/2, (-I)*\text{ArcSin}[a*x]] - \text{Sqrt}[I*\text{ArcSin}[a*x]]*\Gamma[1/2, I*\text{ArcSin}[a*x]]))/(a*\text{Sqrt}[\text{ArcSin}[a*x]])$

Maple [A] time = 0.028, size = 25, normalized size = 0.8

$$\frac{\sqrt{2}\sqrt{\pi}}{a}\text{FresnelC}\left(\frac{\sqrt{2}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x)^(1/2), x)

[Out] $\text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)}*\arcsin(a*x)^{(1/2)})*2^{(1/2)}*\text{Pi}^{(1/2)}/a$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(1/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(1/2), x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/asin(a*x)**(1/2),x)

[Out] Integral(1/sqrt(asin(a*x)), x)

Giac [C] time = 1.36933, size = 63, normalized size = 2.1

$$-\frac{(i+1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(\left(\frac{1}{2}i-\frac{1}{2}\right)\sqrt{2}\sqrt{\arcsin(ax)}\right)}{4a} + \frac{(i-1)\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-\left(\frac{1}{2}i+\frac{1}{2}\right)\sqrt{2}\sqrt{\arcsin(ax)}\right)}{4a}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] $-(1/4*I + 1/4)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}((1/2*I - 1/2)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a + (1/4*I - 1/4)*\sqrt{2}*\sqrt{\pi}*\operatorname{erf}(-(1/2*I + 1/2)*\sqrt{2}*\sqrt{\arcsin(a*x)})/a$

$$3.97 \quad \int \frac{1}{x\sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{1}{x\sqrt{\sin^{-1}(ax)}}, x\right)$$

[Out] Unintegrable[1/(x*Sqrt[ArcSin[a*x]]), x]

Rubi [A] time = 0.0141105, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x\sqrt{\sin^{-1}(ax)}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*Sqrt[ArcSin[a*x]]), x]

[Out] Defer[Int][1/(x*Sqrt[ArcSin[a*x]]), x]

Rubi steps

$$\int \frac{1}{x\sqrt{\sin^{-1}(ax)}} dx = \int \frac{1}{x\sqrt{\sin^{-1}(ax)}} dx$$

Mathematica [A] time = 0.356249, size = 0, normalized size = 0.

$$\int \frac{1}{x\sqrt{\sin^{-1}(ax)}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*Sqrt[ArcSin[a*x]]), x]

[Out] Integrate[1/(x*Sqrt[ArcSin[a*x]]), x]

Maple [A] time = 0.069, size = 0, normalized size = 0.

$$\int \frac{1}{x\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x)^(1/2), x)

[Out] `int(1/x/arcsin(a*x)^(1/2),x)`

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/arcsin(a*x)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/arcsin(a*x)^(1/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/asin(a*x)**(1/2),x)`

[Out] `Integral(1/(x*sqrt(asin(a*x))), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/arcsin(a*x)^(1/2),x, algorithm="giac")`

[Out] `integrate(1/(x*sqrt(arcsin(a*x))), x)`

$$3.98 \quad \int \frac{1}{x^2 \sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable} \left(\frac{1}{x^2 \sqrt{\sin^{-1}(ax)}}, x \right)$$

[Out] Unintegrable[1/(x^2*Sqrt[ArcSin[a*x]]), x]

Rubi [A] time = 0.0131443, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2 \sqrt{\sin^{-1}(ax)}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*Sqrt[ArcSin[a*x]]), x]

[Out] Defer[Int][1/(x^2*Sqrt[ArcSin[a*x]]), x]

Rubi steps

$$\int \frac{1}{x^2 \sqrt{\sin^{-1}(ax)}} dx = \int \frac{1}{x^2 \sqrt{\sin^{-1}(ax)}} dx$$

Mathematica [A] time = 2.99319, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sqrt{\sin^{-1}(ax)}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*Sqrt[ArcSin[a*x]]), x]

[Out] Integrate[1/(x^2*Sqrt[ArcSin[a*x]]), x]

Maple [A] time = 0.122, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/arcsin(a*x)^(1/2), x)

[Out] `int(1/x^2/arcsin(a*x)^(1/2),x)`

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/arcsin(a*x)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/arcsin(a*x)^(1/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/asin(a*x)**(1/2),x)`

[Out] `Integral(1/(x**2*sqrt(asin(a*x))), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/arcsin(a*x)^(1/2),x, algorithm="giac")`

[Out] `integrate(1/(x^2*sqrt(arcsin(a*x))), x)`

$$3.99 \quad \int \frac{x^6}{\sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=171

$$\frac{5\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} + \frac{9\sqrt{\frac{3\pi}{2}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} - \frac{5\sqrt{\frac{5\pi}{2}}S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} + \frac{\sqrt{\frac{7\pi}{2}}S\left(\sqrt{\frac{14}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} - \frac{2}{a}$$

[Out] $(-2*x^6*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (5*\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7) + (9*\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7) - (5*\text{Sqrt}[(5*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[10/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7) + (\text{Sqrt}[(7*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[14/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7)$

Rubi [A] time = 0.14418, antiderivative size = 171, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4631, 3305, 3351}

$$\frac{5\sqrt{\frac{\pi}{2}}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} + \frac{9\sqrt{\frac{3\pi}{2}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} - \frac{5\sqrt{\frac{5\pi}{2}}S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} + \frac{\sqrt{\frac{7\pi}{2}}S\left(\sqrt{\frac{14}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} - \frac{2}{a}$$

Antiderivative was successfully verified.

[In] Int[x^6/ArcSin[a*x]^(3/2), x]

[Out] $(-2*x^6*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (5*\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7) + (9*\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7) - (5*\text{Sqrt}[(5*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[10/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7) + (\text{Sqrt}[(7*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[14/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(16*a^7)$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
\int \frac{x^6}{\sin^{-1}(ax)^{3/2}} dx &= -\frac{2x^6\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2 \operatorname{Subst}\left(\int \left(-\frac{5\sin(x)}{64\sqrt{x}} + \frac{27\sin(3x)}{64\sqrt{x}} - \frac{25\sin(5x)}{64\sqrt{x}} + \frac{7\sin(7x)}{64\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^7} \\
&= -\frac{2x^6\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{5 \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{32a^7} + \frac{7 \operatorname{Subst}\left(\int \frac{\sin(7x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{32a^7} - \frac{25 \operatorname{Subst}\left(\int \frac{\sin(5x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{32a^7} \\
&= -\frac{2x^6\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{5 \operatorname{Subst}\left(\int \sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{16a^7} + \frac{7 \operatorname{Subst}\left(\int \sin(7x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{16a^7} \\
&= -\frac{2x^6\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{5\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} + \frac{9\sqrt{\frac{3\pi}{2}} S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7} - \frac{5\sqrt{\frac{5\pi}{2}} S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{16a^7}
\end{aligned}$$

Mathematica [C] time = 0.233579, size = 427, normalized size = 2.5

$$\frac{5\left(e^{i\sin^{-1}(ax)} - \sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right)\right)}{64\sqrt{\sin^{-1}(ax)}} - \frac{5\left(e^{-i\sin^{-1}(ax)} - \sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, i\sin^{-1}(ax)\right)\right)}{64\sqrt{\sin^{-1}(ax)}} + \frac{9\left(e^{3i\sin^{-1}(ax)} - \sqrt{3}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -3i\sin^{-1}(ax)\right)\right)}{64\sqrt{\sin^{-1}(ax)}} - \frac{9\left(e^{-3i\sin^{-1}(ax)} - \sqrt{3}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 3i\sin^{-1}(ax)\right)\right)}{64\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^6/ArcSin[a*x]^(3/2), x]

[Out] $\left(\frac{(-5*(E^{(I*ArcSin[a*x])} - Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-I)*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]]) - (5*(E^{((-I)*ArcSin[a*x])} - Sqrt[I*ArcSin[a*x]]*Gamma[1/2, I*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]]) + (9*(E^{((3*I)*ArcSin[a*x])} - Sqrt[3]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-3*I)*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]]) + (9*(E^{((-3*I)*ArcSin[a*x])} - Sqrt[3]*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (3*I)*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]]) - (5*(E^{((5*I)*ArcSin[a*x])} - Sqrt[5]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-5*I)*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]]) - (5*(E^{((-5*I)*ArcSin[a*x])} - Sqrt[5]*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (5*I)*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]]) + (E^{((7*I)*ArcSin[a*x])} - Sqrt[7]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-7*I)*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]]) + (E^{((-7*I)*ArcSin[a*x])} - Sqrt[7]*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (7*I)*ArcSin[a*x]])/(64*Sqrt[ArcSin[a*x]])\right)}/a^7$

Maple [A] time = 0.077, size = 184, normalized size = 1.1

$$-\frac{1}{32a^7} \left(-\sqrt{2}\sqrt{\pi}\sqrt{7}\operatorname{FresnelS}\left(\frac{\sqrt{2}\sqrt{7}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right)\sqrt{\arcsin(ax)} + 5\sqrt{5}\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\operatorname{FresnelS}\left(\frac{\sqrt{5}\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^6/arcsin(a*x)^(3/2), x)

[Out] $-1/32/a^7*(-2^{(1/2)}*Pi^{(1/2)}*7^{(1/2)}*\operatorname{FresnelS}(2^{(1/2)}/Pi^{(1/2)}*7^{(1/2)}*\arcsin(a*x)^{(1/2)})*\arcsin(a*x)^{(1/2)}+5*5^{(1/2)}*2^{(1/2)}*\arcsin(a*x)^{(1/2)}*Pi^{(1/2)}*\operatorname{FresnelS}(2^{(1/2)}/Pi^{(1/2)}*5^{(1/2)}*\arcsin(a*x)^{(1/2)})-9*3^{(1/2)}*2^{(1/2)}*\arcsin(a*x)^{(1/2)}*Pi^{(1/2)}*\operatorname{FresnelS}(2^{(1/2)}/Pi^{(1/2)}*3^{(1/2)}*\arcsin(a*x)^{(1/2)})$

2)) + 5*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2)) + 5*(-a^2*x^2+1)^(1/2) - 9*cos(3*arcsin(a*x)) + 5*cos(5*arcsin(a*x)) - cos(7*arcsin(a*x))/arcsin(a*x)^(1/2)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x)^(3/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x)^(3/2), x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^6}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6/asin(a*x)**(3/2), x)

[Out] Integral(x**6/asin(a*x)**(3/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^6}{\operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6/arcsin(a*x)^(3/2), x, algorithm="giac")

[Out] integrate(x^6/arcsin(a*x)^(3/2), x)

$$3.100 \quad \int \frac{x^5}{\sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=127

$$-\frac{\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^6} + \frac{\sqrt{3\pi} \operatorname{FresnelC}\left(2\sqrt{\frac{3}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^6} + \frac{5\sqrt{\pi} \operatorname{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{8a^6} - \frac{2x^5\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x^5*\sqrt{1 - a^2*x^2})/(a*\sqrt{\operatorname{ArcSin}[a*x]}) - (\sqrt{\pi/2}*\operatorname{FresnelC}[2*\operatorname{Sqrt}[2/\pi]*\sqrt{\operatorname{ArcSin}[a*x]}])/a^6 + (\sqrt{3*\pi}*\operatorname{FresnelC}[2*\operatorname{Sqrt}[3/\pi]*\sqrt{\operatorname{ArcSin}[a*x]}])/(8*a^6) + (5*\sqrt{\pi}*\operatorname{FresnelC}[(2*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/ \operatorname{Sqrt}[\pi]])/(8*a^6)$

Rubi [A] time = 0.106607, antiderivative size = 127, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4631, 3304, 3352}

$$-\frac{\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^6} + \frac{\sqrt{3\pi} \operatorname{FresnelC}\left(2\sqrt{\frac{3}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^6} + \frac{5\sqrt{\pi} \operatorname{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{8a^6} - \frac{2x^5\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^5/\operatorname{ArcSin}[a*x]^{(3/2)}, x]$

[Out] $(-2*x^5*\sqrt{1 - a^2*x^2})/(a*\sqrt{\operatorname{ArcSin}[a*x]}) - (\sqrt{\pi/2}*\operatorname{FresnelC}[2*\operatorname{Sqrt}[2/\pi]*\sqrt{\operatorname{ArcSin}[a*x]}])/a^6 + (\sqrt{3*\pi}*\operatorname{FresnelC}[2*\operatorname{Sqrt}[3/\pi]*\sqrt{\operatorname{ArcSin}[a*x]}])/(8*a^6) + (5*\sqrt{\pi}*\operatorname{FresnelC}[(2*\operatorname{Sqrt}[\operatorname{ArcSin}[a*x]])/ \operatorname{Sqrt}[\pi]])/(8*a^6)$

Rule 4631

$\operatorname{Int}[(a_. + \operatorname{ArcSin}(c_.)*(x_.))*(b_.)^{(n_.)}*(x_.)^{(m_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(x^m*\sqrt{1 - c^2*x^2}*(a + b*\operatorname{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] - \operatorname{Dist}[1/(b*c^{(m+1)}*(n+1)), \operatorname{Subst}[\operatorname{Int}[\operatorname{ExpandTrigReduce}[(a + b*x)^{(n+1)}, \operatorname{Sin}[x]^{(m-1)}*(m - (m+1)*\operatorname{Sin}[x]^2)], x], x, \operatorname{ArcSin}[c*x]], x] /;$ $\operatorname{FreeQ}\{a, b, c\}, x \&\& \operatorname{IGtQ}[m, 0] \&\& \operatorname{GeQ}[n, -2] \&\& \operatorname{LtQ}[n, -1]$

Rule 3304

$\operatorname{Int}[\sin[\pi/2 + (e_.) + (f_.)*(x_.)]/\sqrt{(c_.) + (d_.)*(x_.)}, x_Symbol] \rightarrow \operatorname{Dist}[2/d, \operatorname{Subst}[\operatorname{Int}[\operatorname{Cos}[(f*x^2)/d], x], x, \sqrt{c + d*x}], x] /;$ $\operatorname{FreeQ}\{c, d, e, f\}, x \&\& \operatorname{ComplexFreeQ}[f] \&\& \operatorname{EqQ}[d*e - c*f, 0]$

Rule 3352

$\operatorname{Int}[\operatorname{Cos}[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] \rightarrow \operatorname{Simp}[(\sqrt{\pi/2}*\operatorname{FresnelC}[\operatorname{Sqrt}[2/\pi]*\operatorname{Rt}[d, 2]*(e + f*x)])/(\operatorname{Rt}[d, 2]), x] /;$ $\operatorname{FreeQ}\{d, e, f\}, x]$

Rubi steps

$$\begin{aligned}
\int \frac{x^5}{\sin^{-1}(ax)^{3/2}} dx &= -\frac{2x^5\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2 \operatorname{Subst}\left(\int\left(\frac{5\cos(2x)}{16\sqrt{x}} - \frac{\cos(4x)}{2\sqrt{x}} + \frac{3\cos(6x)}{16\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^6} \\
&= -\frac{2x^5\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{3 \operatorname{Subst}\left(\int\frac{\cos(6x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^6} + \frac{5 \operatorname{Subst}\left(\int\frac{\cos(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^6} - \frac{3 \operatorname{Subst}\left(\int\frac{\cos(4x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^6} \\
&= -\frac{2x^5\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{3 \operatorname{Subst}\left(\int\cos(6x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^6} + \frac{5 \operatorname{Subst}\left(\int\cos(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^6} - \frac{3 \operatorname{Subst}\left(\int\cos(4x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^6} \\
&= -\frac{2x^5\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\sqrt{\frac{\pi}{2}}C\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^6} + \frac{\sqrt{3\pi}C\left(2\sqrt{\frac{3}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{8a^6} + \frac{5\sqrt{\pi}C\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{8a^6}
\end{aligned}$$

Mathematica [C] time = 0.135244, size = 231, normalized size = 1.82

$$5i\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) - 5i\sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right) - 8i\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) + 8i\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^5/ArcSin[a*x]^(3/2), x]

[Out] $-\left((5I)\sqrt{2}\sqrt{(-I)\operatorname{ArcSin}[a*x]}\Gamma\left[\frac{1}{2}, (-2I)\operatorname{ArcSin}[a*x]\right] - (5I)\sqrt{2}\sqrt{I\operatorname{ArcSin}[a*x]}\Gamma\left[\frac{1}{2}, (2I)\operatorname{ArcSin}[a*x]\right] - (8I)\sqrt{(-I)\operatorname{ArcSin}[a*x]}\Gamma\left[\frac{1}{2}, (-4I)\operatorname{ArcSin}[a*x]\right] + (8I)\sqrt{I\operatorname{ArcSin}[a*x]}\Gamma\left[\frac{1}{2}, (4I)\operatorname{ArcSin}[a*x]\right] + I\sqrt{6}\sqrt{(-I)\operatorname{ArcSin}[a*x]}\Gamma\left[\frac{1}{2}, (-6I)\operatorname{ArcSin}[a*x]\right] - I\sqrt{6}\sqrt{I\operatorname{ArcSin}[a*x]}\Gamma\left[\frac{1}{2}, (6I)\operatorname{ArcSin}[a*x]\right] + 10\sin[2\operatorname{ArcSin}[a*x]] - 8\sin[4\operatorname{ArcSin}[a*x]] + 2\sin[6\operatorname{ArcSin}[a*x]]\right)/(32a^6\sqrt{\operatorname{ArcSin}[a*x]})$

Maple [A] time = 0.067, size = 121, normalized size = 1.

$$-\frac{1}{16a^6}\left(-2\sqrt{\pi}\sqrt{3}\operatorname{FresnelC}\left(\frac{\sqrt{2}\sqrt{6}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)\sqrt{\arcsin(ax)} + 8\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\operatorname{FresnelC}\left(2\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)\sqrt{\arcsin(ax)}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^5/arcsin(a*x)^(3/2), x)

[Out] $-1/16/a^6/\arcsin(a*x)^{(1/2)}*(-2*\Pi^{(1/2)}*3^{(1/2)}*\operatorname{FresnelC}(2^{(1/2)}/\Pi^{(1/2)}*6^{(1/2)}*\arcsin(a*x)^{(1/2)})*\arcsin(a*x)^{(1/2)}+8*2^{(1/2)}*\arcsin(a*x)^{(1/2)}*\Pi^{(1/2)}*\operatorname{FresnelC}(2*2^{(1/2)}/\Pi^{(1/2)}*\arcsin(a*x)^{(1/2)})-10*\arcsin(a*x)^{(1/2)}*\Pi^{(1/2)}*\operatorname{FresnelC}(2*\arcsin(a*x)^{(1/2)}/\Pi^{(1/2)})+5*\sin(2*\arcsin(a*x))-4*\sin(4*\arcsin(a*x))+\sin(6*\arcsin(a*x))$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x)^(3/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^5}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**5/asin(a*x)**(3/2),x)

[Out] Integral(x**5/asin(a*x)**(3/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^5}{\operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^5/arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] integrate(x^5/arcsin(a*x)^(3/2), x)

$$3.101 \quad \int \frac{x^4}{\sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=136

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^5} + \frac{3\sqrt{\frac{3\pi}{2}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{\sqrt{\frac{5\pi}{2}} S\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{2x^4 \sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x^4*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(2*a^5) + (3*\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(4*a^5) - (\text{Sqrt}[(5*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[10/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(4*a^5)$

Rubi [A] time = 0.098155, antiderivative size = 136, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4631, 3305, 3351}

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^5} + \frac{3\sqrt{\frac{3\pi}{2}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{\sqrt{\frac{5\pi}{2}} S\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{2x^4 \sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^4/\text{ArcSin}[a*x]^{(3/2)}, x]$

[Out] $(-2*x^4*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(2*a^5) + (3*\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(4*a^5) - (\text{Sqrt}[(5*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[10/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(4*a^5)$

Rule 4631

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(x)^m, x_Symbol] \rightarrow \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{n+1})/(b*c*(n+1)), x] - \text{Dist}[1/(b*c^{m+1}*(n+1)), \text{Subst}[\text{Int}[\text{ExpandTrigReduce}[(a + b*x)^{n+1}, \text{Sin}[x]^{m-1}*(m - (m+1)*\text{Sin}[x]^2), x], x], x, \text{ArcSin}[c*x], x] /;$ $\text{FreeQ}\{a, b, c\}, x \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ \text{GeQ}[n, -2] \ \&\& \ \text{LtQ}[n, -1]$

Rule 3305

$\text{Int}[\sin[(e + (f*x))/\text{Sqrt}[(c + (d*x))], x_Symbol] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x \ \&\& \ \text{ComplexFreeQ}[f] \ \&\& \ \text{EqQ}[d*e - c*f, 0]$

Rule 3351

$\text{Int}[\text{Sin}[(d + (e + (f*x))^2), x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Rt}[d, 2]*(e + f*x)])/(f*\text{Rt}[d, 2]), x] /;$ $\text{FreeQ}\{d, e, f\}, x]$

Rubi steps

$$\begin{aligned}
\int \frac{x^4}{\sin^{-1}(ax)^{3/2}} dx &= -\frac{2x^4\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2 \operatorname{Subst}\left(\int\left(-\frac{\sin(x)}{8\sqrt{x}} + \frac{9\sin(3x)}{16\sqrt{x}} - \frac{5\sin(5x)}{16\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^5} \\
&= -\frac{2x^4\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\operatorname{Subst}\left(\int\frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{4a^5} - \frac{5 \operatorname{Subst}\left(\int\frac{\sin(5x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{8a^5} + \frac{9 \operatorname{Subst}\left(\int\frac{\sin(9x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{16a^5} \\
&= -\frac{2x^4\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\operatorname{Subst}\left(\int\sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{2a^5} - \frac{5 \operatorname{Subst}\left(\int\sin(5x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{4a^5} \\
&= -\frac{2x^4\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{2a^5} + \frac{3\sqrt{\frac{3\pi}{2}} S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{4a^5} - \frac{\sqrt{\frac{5\pi}{2}} S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{4a^5}
\end{aligned}$$

Mathematica [C] time = 0.151671, size = 319, normalized size = 2.35

$$\frac{e^{i\sin^{-1}(ax)} - \sqrt{-i\sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{1}{2}, -i\sin^{-1}(ax)\right)}{8\sqrt{\sin^{-1}(ax)}} - \frac{e^{-i\sin^{-1}(ax)} - \sqrt{i\sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{1}{2}, i\sin^{-1}(ax)\right)}{8\sqrt{\sin^{-1}(ax)}} + \frac{3\left(e^{3i\sin^{-1}(ax)} - \sqrt{3}\sqrt{-i\sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{1}{2}, -3i\sin^{-1}(ax)\right)\right)}{16\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^4/ArcSin[a*x]^(3/2), x]

[Out] $(- (E^{(I*ArcSin[a*x])} - Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-I)*ArcSin[a*x]]) / (8*Sqrt[ArcSin[a*x]]) - (E^{((-I)*ArcSin[a*x])} - Sqrt[I*ArcSin[a*x]]*Gamma[1/2, I*ArcSin[a*x]]) / (8*Sqrt[ArcSin[a*x]]) + (3*(E^{((3*I)*ArcSin[a*x])} - Sqrt[3]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-3*I)*ArcSin[a*x]])) / (16*Sqrt[ArcSin[a*x]]) + (3*(E^{((-3*I)*ArcSin[a*x])} - Sqrt[3]*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (3*I)*ArcSin[a*x]])) / (16*Sqrt[ArcSin[a*x]]) - (E^{((5*I)*ArcSin[a*x])} - Sqrt[5]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-5*I)*ArcSin[a*x]]) / (16*Sqrt[ArcSin[a*x]]) - (E^{((-5*I)*ArcSin[a*x])} - Sqrt[5]*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (5*I)*ArcSin[a*x]]) / (16*Sqrt[ArcSin[a*x]])) / a^5$

Maple [A] time = 0.051, size = 138, normalized size = 1.

$$-\frac{1}{8a^5} \left(\sqrt{5}\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\operatorname{FresnelS}\left(\frac{\sqrt{5}\sqrt{2}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right) - 3\sqrt{3}\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\operatorname{FresnelS}\left(\frac{\sqrt{3}\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x)^(3/2), x)

[Out] $-1/8/a^5*(5^{(1/2)}*2^{(1/2)}*\arcsin(a*x)^{(1/2)}*\Pi^{(1/2)}*\operatorname{FresnelS}(2^{(1/2)}/\Pi^{(1/2)})*5^{(1/2)}*\arcsin(a*x)^{(1/2)} - 3*3^{(1/2)}*2^{(1/2)}*\arcsin(a*x)^{(1/2)}*\Pi^{(1/2)}*\operatorname{FresnelS}(2^{(1/2)}/\Pi^{(1/2)})*3^{(1/2)}*\arcsin(a*x)^{(1/2)} + 2*2^{(1/2)}*\arcsin(a*x)^{(1/2)}*\Pi^{(1/2)}*\operatorname{FresnelS}(2^{(1/2)}/\Pi^{(1/2)})*\arcsin(a*x)^{(1/2)} + 2*(-a^2*x^2+1)^{(1/2)} - 3*\cos(3*\arcsin(a*x)) + \cos(5*\arcsin(a*x))) / \arcsin(a*x)^{(1/2)}$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(3/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/asin(a*x)**(3/2),x)

[Out] Integral(x**4/asin(a*x)**(3/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] integrate(x^4/arcsin(a*x)^(3/2), x)

$$3.102 \quad \int \frac{x^3}{\sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=90

$$-\frac{\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^4} + \frac{\sqrt{\pi} \operatorname{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{a^4} - \frac{2x^3\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x^3*\sqrt{1 - a^2*x^2})/(a*\sqrt{\operatorname{ArcSin}[a*x]}) - (\sqrt{\operatorname{Pi}/2}*\operatorname{FresnelC}[2*\operatorname{Sqrt}[2/\operatorname{Pi}]*\sqrt{\operatorname{ArcSin}[a*x]}])/a^4 + (\sqrt{\operatorname{Pi}}*\operatorname{FresnelC}[(2*\sqrt{\operatorname{ArcSin}[a*x]})/\sqrt{\operatorname{Pi}}])/a^4$

Rubi [A] time = 0.0696889, antiderivative size = 90, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4631, 3304, 3352}

$$-\frac{\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^4} + \frac{\sqrt{\pi} \operatorname{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{a^4} - \frac{2x^3\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^3/\operatorname{ArcSin}[a*x]^{(3/2)}, x]$

[Out] $(-2*x^3*\sqrt{1 - a^2*x^2})/(a*\sqrt{\operatorname{ArcSin}[a*x]}) - (\sqrt{\operatorname{Pi}/2}*\operatorname{FresnelC}[2*\operatorname{Sqrt}[2/\operatorname{Pi}]*\sqrt{\operatorname{ArcSin}[a*x]}])/a^4 + (\sqrt{\operatorname{Pi}}*\operatorname{FresnelC}[(2*\sqrt{\operatorname{ArcSin}[a*x]})/\sqrt{\operatorname{Pi}}])/a^4$

Rule 4631

$\operatorname{Int}[(a_. + \operatorname{ArcSin}[(c_.)*(x_.)]*(b_.))^{(n_.)}*(x_.)^{(m_.)}, x_Symbol] \rightarrow \operatorname{Simp}[(x^m*\sqrt{1 - c^2*x^2}*(a + b*\operatorname{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] - \operatorname{Dist}[1/(b*c^{(m+1)}*(n+1)), \operatorname{Subst}[\operatorname{Int}[\operatorname{ExpandTrigReduce}[(a + b*x)^{(n+1)}, \operatorname{Sin}[x]^{(m-1)}*(m - (m+1)*\operatorname{Sin}[x]^2)], x], x], x, \operatorname{ArcSin}[c*x], x] /;$ $\operatorname{FreeQ}\{a, b, c\}, x \&\& \operatorname{IGtQ}[m, 0] \&\& \operatorname{GeQ}[n, -2] \&\& \operatorname{LtQ}[n, -1]$

Rule 3304

$\operatorname{Int}[\sin[\operatorname{Pi}/2 + (e_.) + (f_.)*(x_.)]/\sqrt{(c_.) + (d_.)*(x_.)}, x_Symbol] \rightarrow \operatorname{Dist}[2/d, \operatorname{Subst}[\operatorname{Int}[\operatorname{Cos}[(f*x^2)/d], x], x, \sqrt{c + d*x}], x] /;$ $\operatorname{FreeQ}\{c, d, e, f\}, x \&\& \operatorname{ComplexFreeQ}[f] \&\& \operatorname{EqQ}[d*e - c*f, 0]$

Rule 3352

$\operatorname{Int}[\operatorname{Cos}[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] \rightarrow \operatorname{Simp}[(\sqrt{\operatorname{Pi}/2}*\operatorname{FresnelC}[\sqrt{2/\operatorname{Pi}}*\operatorname{Rt}[d, 2]*(e + f*x)])/(f*\operatorname{Rt}[d, 2]), x] /;$ $\operatorname{FreeQ}\{d, e, f\}, x]$

Rubi steps

$$\begin{aligned}
\int \frac{x^3}{\sin^{-1}(ax)^{3/2}} dx &= -\frac{2x^3\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2 \operatorname{Subst}\left(\int \left(\frac{\cos(2x)}{2\sqrt{x}} - \frac{\cos(4x)}{2\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^4} \\
&= -\frac{2x^3\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{\operatorname{Subst}\left(\int \frac{\cos(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^4} - \frac{\operatorname{Subst}\left(\int \frac{\cos(4x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^4} \\
&= -\frac{2x^3\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2 \operatorname{Subst}\left(\int \cos(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a^4} - \frac{2 \operatorname{Subst}\left(\int \cos(4x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a^4} \\
&= -\frac{2x^3\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\sqrt{\frac{\pi}{2}} C\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^4} + \frac{\sqrt{\pi} C\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{a^4}
\end{aligned}$$

Mathematica [C] time = 0.0458816, size = 154, normalized size = 1.71

$$\frac{-i\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) + i\sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right) + i\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) + i\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right)}{4a^4\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3/ArcSin[a*x]^(3/2), x]

[Out] ((-I)*Sqrt[2]*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-2*I)*ArcSin[a*x]] + I*Sqrt[2]*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (2*I)*ArcSin[a*x]] + I*Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-4*I)*ArcSin[a*x]] - I*Sqrt[I*ArcSin[a*x]]*Gamma[1/2, (4*I)*ArcSin[a*x]] - 2*Sin[2*ArcSin[a*x]] + Sin[4*ArcSin[a*x]])/(4*a^4*Sqrt[ArcSin[a*x]])

Maple [A] time = 0.042, size = 83, normalized size = 0.9

$$-\frac{1}{4a^4} \left(2\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\operatorname{FresnelC}\left(2\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) - 4\sqrt{\arcsin(ax)}\sqrt{\pi}\operatorname{FresnelC}\left(2\frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + 2\sin(2\arcsin(ax)) - \sin(4\arcsin(ax)) \right) / \arcsin(ax)^{1/2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/arcsin(a*x)^(3/2), x)

[Out] -1/4/a^4*(2*2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2*2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))-4*arcsin(a*x)^(1/2)*Pi^(1/2)*FresnelC(2*arcsin(a*x)^(1/2)/Pi^(1/2))+2*sin(2*arcsin(a*x))-sin(4*arcsin(a*x)))/arcsin(a*x)^(1/2)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3/arcsin(a*x)^(3/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3/arcsin(a*x)^(3/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3/asin(a*x)**(3/2),x)
```

```
[Out] Integral(x**3/asin(a*x)**(3/2), x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3/arcsin(a*x)^(3/2),x, algorithm="giac")
```

```
[Out] integrate(x^3/arcsin(a*x)^(3/2), x)
```

$$3.103 \quad \int \frac{x^2}{\sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=96

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a^3} + \frac{\sqrt{\frac{3\pi}{2}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a^3} - \frac{2x^2 \sqrt{1-a^2x^2}}{a \sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x^2*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/a^3 + (\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/a^3$

Rubi [A] time = 0.0692069, antiderivative size = 96, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4631, 3305, 3351}

$$-\frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a^3} + \frac{\sqrt{\frac{3\pi}{2}} S\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a^3} - \frac{2x^2 \sqrt{1-a^2x^2}}{a \sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2/\text{ArcSin}[a*x]^{(3/2)}, x]$

[Out] $(-2*x^2*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/a^3 + (\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelS}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/a^3$

Rule 4631

$\text{Int}[(c_.) + \text{ArcSin}[(c_.)*(x_)]*(b_.)^{(n_)}*(x_)^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c^{(n+1)}), x] - \text{Dist}[1/(b*c^{(m+1)}*(n+1)), \text{Subst}[\text{Int}[\text{ExpandTrigReduce}[(a + b*x)^{(n+1)}, \text{Sin}[x]^{(m-1)}*(m - (m+1)*\text{Sin}[x]^2), x], x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{IGtQ}[m, 0] \&\& \text{GeQ}[n, -2] \&\& \text{LtQ}[n, -1]$

Rule 3305

$\text{Int}[\text{sin}[(e_.) + (f_.)*(x_)]/\text{Sqrt}[(c_.) + (d_.)*(x_)], x_Symbol] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /; \text{FreeQ}\{c, d, e, f\}, x] \&\& \text{ComplexFreeQ}[f] \&\& \text{EqQ}[d*e - c*f, 0]$

Rule 3351

$\text{Int}[\text{Sin}[(d_.)*((e_.) + (f_.)*(x_))^{(2)}], x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Rt}[d, 2]*(e + f*x)])/(f*\text{Rt}[d, 2]), x] /; \text{FreeQ}\{d, e, f\}, x]$

Rubi steps

$$\begin{aligned}
\int \frac{x^2}{\sin^{-1}(ax)^{3/2}} dx &= -\frac{2x^2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2 \operatorname{Subst}\left(\int\left(-\frac{\sin(x)}{4\sqrt{x}} + \frac{3\sin(3x)}{4\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^3} \\
&= -\frac{2x^2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\operatorname{Subst}\left(\int\frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{2a^3} + \frac{3 \operatorname{Subst}\left(\int\frac{\sin(3x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{2a^3} \\
&= -\frac{2x^2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\operatorname{Subst}\left(\int\sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a^3} + \frac{3 \operatorname{Subst}\left(\int\sin(3x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a^3} \\
&= -\frac{2x^2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{\sqrt{\frac{\pi}{2}} S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^3} + \frac{\sqrt{\frac{3\pi}{2}} S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^3}
\end{aligned}$$

Mathematica [C] time = 0.0720673, size = 211, normalized size = 2.2

$$\frac{e^{i\sin^{-1}(ax)} - \sqrt{-i\sin^{-1}(ax)} \Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right)}{4\sqrt{\sin^{-1}(ax)}} - \frac{e^{-i\sin^{-1}(ax)} - \sqrt{i\sin^{-1}(ax)} \Gamma\left(\frac{1}{2}, i\sin^{-1}(ax)\right)}{4\sqrt{\sin^{-1}(ax)}} + \frac{e^{3i\sin^{-1}(ax)} - \sqrt{3}\sqrt{-i\sin^{-1}(ax)} \Gamma\left(\frac{1}{2}, -3i\sin^{-1}(ax)\right)}{4\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2/ArcSin[a*x]^(3/2), x]

[Out] $(- (E^{(I \cdot \text{ArcSin}[a \cdot x])} - \text{Sqrt}[(-I) \cdot \text{ArcSin}[a \cdot x]] \cdot \Gamma[1/2, (-I) \cdot \text{ArcSin}[a \cdot x]]) / (4 \cdot \text{Sqrt}[\text{ArcSin}[a \cdot x]]) - (E^{((-I) \cdot \text{ArcSin}[a \cdot x])} - \text{Sqrt}[I \cdot \text{ArcSin}[a \cdot x]] \cdot \Gamma[1/2, I \cdot \text{ArcSin}[a \cdot x]]) / (4 \cdot \text{Sqrt}[\text{ArcSin}[a \cdot x]]) + (E^{((3 \cdot I) \cdot \text{ArcSin}[a \cdot x])} - \text{Sqrt}[3 \cdot \text{Sqrt}[(-I) \cdot \text{ArcSin}[a \cdot x]] \cdot \Gamma[1/2, (-3 \cdot I) \cdot \text{ArcSin}[a \cdot x]]) / (4 \cdot \text{Sqrt}[\text{ArcSin}[a \cdot x]]) + (E^{((-3 \cdot I) \cdot \text{ArcSin}[a \cdot x])} - \text{Sqrt}[3 \cdot \text{Sqrt}[I \cdot \text{ArcSin}[a \cdot x]] \cdot \Gamma[1/2, (3 \cdot I) \cdot \text{ArcSin}[a \cdot x]]) / (4 \cdot \text{Sqrt}[\text{ArcSin}[a \cdot x]])) / a^3$

Maple [A] time = 0.046, size = 95, normalized size = 1.

$$\frac{1}{2a^3} \left(\sqrt{3}\sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\text{FresnelS}\left(\frac{\sqrt{3}\sqrt{2}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right) - \sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\text{FresnelS}\left(\frac{\sqrt{2}}{\sqrt{\pi}}\sqrt{\arcsin(ax)}\right) - \sqrt{-a^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/arcsin(a*x)^(3/2), x)

[Out] $1/2/a^3*(3^{(1/2)}*2^{(1/2)}*\arcsin(a*x)^{(1/2)}*\text{Pi}^{(1/2)}*\text{FresnelS}(2^{(1/2)}/\text{Pi}^{(1/2)}*3^{(1/2)}*\arcsin(a*x)^{(1/2)}) - 2^{(1/2)}*\arcsin(a*x)^{(1/2)}*\text{Pi}^{(1/2)}*\text{FresnelS}(2^{(1/2)}/\text{Pi}^{(1/2)}*\arcsin(a*x)^{(1/2)}) - (-a^2*x^2+1)^{(1/2)}+\cos(3*\arcsin(a*x)))/a\arcsin(a*x)^{(1/2)}$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2/arcsin(a*x)^(3/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2/arcsin(a*x)^(3/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2/asin(a*x)**(3/2),x)
```

```
[Out] Integral(x**2/asin(a*x)**(3/2), x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2/arcsin(a*x)^(3/2),x, algorithm="giac")
```

```
[Out] integrate(x^2/arcsin(a*x)^(3/2), x)
```

3.104 $\int \frac{x}{\sin^{-1}(ax)^{3/2}} dx$

Optimal. Leaf size=55

$$\frac{2\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{a^2} - \frac{2x\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (2*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/a^2$

Rubi [A] time = 0.031562, antiderivative size = 55, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4631, 3304, 3352}

$$\frac{2\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{a^2} - \frac{2x\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x/\text{ArcSin}[a*x]^{(3/2)}, x]$

[Out] $(-2*x*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (2*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/a^2$

Rule 4631

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/ (f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned}
\int \frac{x}{\sin^{-1}(ax)^{3/2}} dx &= -\frac{2x\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2 \operatorname{Subst}\left(\int \frac{\cos(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^2} \\
&= -\frac{2x\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{4 \operatorname{Subst}\left(\int \cos(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a^2} \\
&= -\frac{2x\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} + \frac{2\sqrt{\pi}C\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{a^2}
\end{aligned}$$

Mathematica [C] time = 0.0326046, size = 91, normalized size = 1.65

$$\frac{i\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) - i\sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right) + 2\sin\left(2\sin^{-1}(ax)\right)}{2a^2\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x/ArcSin[a*x]^(3/2), x]

[Out] $-(I*\sqrt{2}*\sqrt{(-I)*\text{ArcSin}[a*x]})*\Gamma[1/2, (-2*I)*\text{ArcSin}[a*x]] - I*\sqrt{2}*\sqrt{I*\text{ArcSin}[a*x]})*\Gamma[1/2, (2*I)*\text{ArcSin}[a*x]] + 2*\sin[2*\text{ArcSin}[a*x]]/(2*a^2*\sqrt{\text{ArcSin}[a*x]})$

Maple [A] time = 0.031, size = 43, normalized size = 0.8

$$-\frac{1}{a^2} \left(-2\sqrt{\arcsin(ax)}\sqrt{\pi}\operatorname{FresnelC}\left(2\frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + \sin(2\arcsin(ax)) \right) \frac{1}{\sqrt{\arcsin(ax)}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/arcsin(a*x)^(3/2), x)

[Out] $-1/a^2/\arcsin(a*x)^{(1/2)}*(-2*\arcsin(a*x)^{(1/2)}*\pi^{(1/2)}*\operatorname{FresnelC}(2*\arcsin(a*x)^{(1/2)}/\pi^{(1/2)})+\sin(2*\arcsin(a*x)))$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(3/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/asin(a*x)**(3/2),x)

[Out] Integral(x/asin(a*x)**(3/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\arcsin(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] integrate(x/arcsin(a*x)^(3/2), x)

$$3.105 \quad \int \frac{1}{\sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=59

$$-\frac{2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{2\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a}$$

[Out] $(-2*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (2*\text{Sqrt}[2*Pi]*\text{FresnelS}[\text{Sqrt}[2/Pi]*\text{Sqrt}[\text{ArcSin}[a*x]]])/a$

Rubi [A] time = 0.0904898, antiderivative size = 59, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4621, 4723, 3305, 3351}

$$-\frac{2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{2\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^{(-3/2)}, x]$

[Out] $(-2*\text{Sqrt}[1 - a^2*x^2])/(a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (2*\text{Sqrt}[2*Pi]*\text{FresnelS}[\text{Sqrt}[2/Pi]*\text{Sqrt}[\text{ArcSin}[a*x]]])/a$

Rule 4621

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n, x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{n+1})/(b*c*(n+1)), x] + \text{Dist}[c/(b*(n+1)), \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{n+1})/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ $\text{FreeQ}\{a, b, c\}, x \ \&\& \ \text{LtQ}[n, -1]$

Rule 4723

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^n*(x)^m*((d + (e*x)^2)^p), x_Symbol] \rightarrow \text{Dist}[d^p/c^{m+1}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x]^{2*p+1}, x], x, \text{ArcSin}[c*x]], x] /;$ $\text{FreeQ}\{a, b, c, d, e, n\}, x \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{IntegerQ}[2*p] \ \&\& \ \text{GtQ}[p, -1] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (\text{IntegerQ}[p] \ || \ \text{GtQ}[d, 0])$

Rule 3305

$\text{Int}[\text{sin}[(e + (f*x)^2)/d]/\text{Sqrt}[(c + (d*x)^2)], x_Symbol] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x \ \&\& \ \text{ComplexFreeQ}[f] \ \&\& \ \text{EqQ}[d*e - c*f, 0]$

Rule 3351

$\text{Int}[\text{Sin}[(d + (e + (f*x)^2))]^2], x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[Pi/2]*\text{FresnelS}[\text{Sqrt}[2/Pi]*\text{Rt}[d, 2]*(e + f*x)])/(f*\text{Rt}[d, 2]), x] /;$ $\text{FreeQ}\{d, e, f\}, x$

Rubi steps

$$\begin{aligned}
\int \frac{1}{\sin^{-1}(ax)^{3/2}} dx &= -\frac{2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - (2a) \int \frac{x}{\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}} dx \\
&= -\frac{2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{2 \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a} \\
&= -\frac{2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{4 \operatorname{Subst}\left(\int \sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{a} \\
&= -\frac{2\sqrt{1-a^2x^2}}{a\sqrt{\sin^{-1}(ax)}} - \frac{2\sqrt{2\pi} S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a}
\end{aligned}$$

Mathematica [C] time = 0.0951994, size = 87, normalized size = 1.47

$$\frac{\sqrt{-i \sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{1}{2}, -i \sin^{-1}(ax)\right) + \sqrt{i \sin^{-1}(ax)} \operatorname{Gamma}\left(\frac{1}{2}, i \sin^{-1}(ax)\right) - e^{-i \sin^{-1}(ax)} (1 + e^{2i \sin^{-1}(ax)})}{a\sqrt{\sin^{-1}(ax)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^(-3/2), x]

[Out] (-((1 + E^((2*I)*ArcSin[a*x]))/E^(I*ArcSin[a*x])) + Sqrt[(-I)*ArcSin[a*x]]*Gamma[1/2, (-I)*ArcSin[a*x]] + Sqrt[I*ArcSin[a*x]]*Gamma[1/2, I*ArcSin[a*x]])/(a*Sqrt[ArcSin[a*x]])

Maple [A] time = 0.035, size = 65, normalized size = 1.1

$$-\frac{\sqrt{2}}{a\sqrt{\pi} \arcsin(ax)} \left(2 \arcsin(ax) \pi \operatorname{FresnelS}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + \sqrt{2}\sqrt{\arcsin(ax)}\sqrt{\pi}\sqrt{-a^2x^2+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x)^(3/2), x)

[Out] -1/a*2^(1/2)/Pi^(1/2)*(2*arcsin(a*x)*Pi*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))+2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*(-a^2*x^2+1)^(1/2))/arcsin(a*x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(3/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/asin(a*x)**(3/2),x)

[Out] Integral(asin(a*x)**(-3/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] integrate(arcsin(a*x)^(-3/2), x)

$$3.106 \quad \int \frac{1}{x \sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{1}{x \sin^{-1}(ax)^{3/2}}, x\right)$$

[Out] Unintegrable[1/(x*ArcSin[a*x]^(3/2)), x]

Rubi [A] time = 0.0136693, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x \sin^{-1}(ax)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*ArcSin[a*x]^(3/2)), x]

[Out] Defer[Int][1/(x*ArcSin[a*x]^(3/2)), x]

Rubi steps

$$\int \frac{1}{x \sin^{-1}(ax)^{3/2}} dx = \int \frac{1}{x \sin^{-1}(ax)^{3/2}} dx$$

Mathematica [A] time = 0.455303, size = 0, normalized size = 0.

$$\int \frac{1}{x \sin^{-1}(ax)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*ArcSin[a*x]^(3/2)), x]

[Out] Integrate[1/(x*ArcSin[a*x]^(3/2)), x]

Maple [A] time = 0.063, size = 0, normalized size = 0.

$$\int \frac{1}{x} (\arcsin(ax))^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x)^(3/2), x)

[Out] int(1/x/arcsin(a*x)^(3/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(3/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/asin(a*x)**(3/2),x)

[Out] Integral(1/(x*asin(a*x)**(3/2)), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] integrate(1/(x*arcsin(a*x)^(3/2)), x)

$$3.107 \quad \int \frac{x^4}{\sin^{-1}(ax)^{5/2}} dx$$

Optimal. Leaf size=171

$$\frac{\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{3a^5} + \frac{3\sqrt{\frac{3\pi}{2}} \operatorname{FresnelC}\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{2a^5} - \frac{5\sqrt{\frac{5\pi}{2}} \operatorname{FresnelC}\left(\sqrt{\frac{10}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{6a^5} - \frac{2x^4 \sqrt{1-x^2}}{3a \sin^{-1}(ax)}$$

[Out] $(-2*x^4*\sqrt{1 - a^2*x^2})/(3*a*\operatorname{ArcSin}[a*x]^{(3/2)}) - (16*x^3)/(3*a^2*\sqrt{\operatorname{ArcSin}[a*x]}) + (20*x^5)/(3*\sqrt{\operatorname{ArcSin}[a*x]}) - (\sqrt{\operatorname{Pi}/2}*\operatorname{FresnelC}[\sqrt{2/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/(3*a^5) + (3*\sqrt{(3*\operatorname{Pi})/2}*\operatorname{FresnelC}[\sqrt{6/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/(2*a^5) - (5*\sqrt{(5*\operatorname{Pi})/2}*\operatorname{FresnelC}[\sqrt{10/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/(6*a^5)$

Rubi [A] time = 0.434386, antiderivative size = 235, normalized size of antiderivative = 1.37, number of steps used = 19, number of rules used = 6, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4633, 4719, 4635, 4406, 3304, 3352}

$$\frac{4\sqrt{2\pi} \operatorname{FresnelC}\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a^5} - \frac{25\sqrt{\frac{\pi}{2}} \operatorname{FresnelC}\left(\sqrt{\frac{2}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{3a^5} - \frac{4\sqrt{\frac{2\pi}{3}} \operatorname{FresnelC}\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a^5} + \frac{25\sqrt{\frac{\pi}{6}} \operatorname{FresnelC}\left(\sqrt{\frac{6}{\pi}} \sqrt{\sin^{-1}(ax)}\right)}{a^5}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x^4/\operatorname{ArcSin}[a*x]^{(5/2)}, x]$

[Out] $(-2*x^4*\sqrt{1 - a^2*x^2})/(3*a*\operatorname{ArcSin}[a*x]^{(3/2)}) - (16*x^3)/(3*a^2*\sqrt{\operatorname{ArcSin}[a*x]}) + (20*x^5)/(3*\sqrt{\operatorname{ArcSin}[a*x]}) - (25*\sqrt{\operatorname{Pi}/2}*\operatorname{FresnelC}[\sqrt{2/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/(3*a^5) + (4*\sqrt{2*\operatorname{Pi}}*\operatorname{FresnelC}[\sqrt{2/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/a^5 + (25*\sqrt{\operatorname{Pi}/6}*\operatorname{FresnelC}[\sqrt{6/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/(2*a^5) - (4*\sqrt{(2*\operatorname{Pi})/3}*\operatorname{FresnelC}[\sqrt{6/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/a^5 - (5*\sqrt{(5*\operatorname{Pi})/2}*\operatorname{FresnelC}[\sqrt{10/\operatorname{Pi}}*\sqrt{\operatorname{ArcSin}[a*x]}])/(6*a^5)$

Rule 4633

$\operatorname{Int}[(a_.) + \operatorname{ArcSin}[(c_.)*(x_)]*(b_.)^{(n_)}*(x_)^{(m_)}, x_Symbol] \rightarrow \operatorname{Simp}[(x^m*\sqrt{1 - c^2*x^2}*(a + b*\operatorname{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] + (\operatorname{Dist}[(c*(m+1))/(b*(n+1)), \operatorname{Int}[(x^{(m+1)}*(a + b*\operatorname{ArcSin}[c*x])^{(n+1)})/\sqrt{1 - c^2*x^2}, x], x] - \operatorname{Dist}[m/(b*c*(n+1)), \operatorname{Int}[(x^{(m-1)}*(a + b*\operatorname{ArcSin}[c*x])^{(n+1)})/\sqrt{1 - c^2*x^2}, x], x]) /; \operatorname{FreeQ}\{a, b, c\}, x \&\& \operatorname{IGtQ}[m, 0] \&\& \operatorname{LtQ}[n, -2]$

Rule 4719

$\operatorname{Int}[((a_.) + \operatorname{ArcSin}[(c_.)*(x_)]*(b_.)^{(n_)}*((f_.)*(x_))^{(m_)}), x_Symbol] \rightarrow \operatorname{Simp}[(f*x)^m*(a + b*\operatorname{ArcSin}[c*x])^{(n+1)})/(b*c*\sqrt{d}*(n+1)), x] - \operatorname{Dist}[(f*m)/(b*c*\sqrt{d}*(n+1)), \operatorname{Int}[(f*x)^{(m-1)}*(a + b*\operatorname{ArcSin}[c*x])^{(n+1)}, x], x] /; \operatorname{FreeQ}\{a, b, c, d, e, f, m\}, x \&\& \operatorname{EqQ}[c^2*d + e, 0] \&\& \operatorname{LtQ}[n, -1] \&\& \operatorname{GtQ}[d, 0]$

Rule 4635

$\operatorname{Int}[(a_.) + \operatorname{ArcSin}[(c_.)*(x_)]*(b_.)^{(n_)}*(x_)^{(m_)}, x_Symbol] \rightarrow \operatorname{Dist}[1/c^{(m+1)}, \operatorname{Subst}[\operatorname{Int}[(a + b*x)^n*\sin[x]^m*\cos[x], x], x, \operatorname{ArcSin}[c*x]], x]$

;/; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
 \int \frac{x^4}{\sin^{-1}(ax)^{5/2}} dx &= -\frac{2x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} + \frac{8\int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx}{3a} - \frac{1}{3}(10a) \int \frac{x^5}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx \\
 &= -\frac{2x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{16x^3}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{20x^5}{3\sqrt{\sin^{-1}(ax)}} - \frac{100}{3} \int \frac{x^4}{\sqrt{\sin^{-1}(ax)}} dx + \frac{16\int \frac{x^2}{\sqrt{\sin^{-1}(ax)}} dx}{a^2} \\
 &= -\frac{2x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{16x^3}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{20x^5}{3\sqrt{\sin^{-1}(ax)}} + \frac{16\text{Subst}\left(\int \frac{\cos(x)\sin^2(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^5} \\
 &= -\frac{2x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{16x^3}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{20x^5}{3\sqrt{\sin^{-1}(ax)}} + \frac{16\text{Subst}\left(\int \left(\frac{\cos(x)}{4\sqrt{x}} - \frac{\cos(3x)}{4\sqrt{x}}\right) dx, x, \sin^{-1}(ax)\right)}{a^5} \\
 &= -\frac{2x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{16x^3}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{20x^5}{3\sqrt{\sin^{-1}(ax)}} - \frac{25\text{Subst}\left(\int \frac{\cos(5x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{12a^5} + \frac{4\text{Subst}\left(\int \frac{\cos(5x^2)}{\sqrt{x}} dx, x, \sqrt{\sin^{-1}(ax)}\right)}{6a^5} \\
 &= -\frac{2x^4\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{16x^3}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{20x^5}{3\sqrt{\sin^{-1}(ax)}} - \frac{25\sqrt{\frac{\pi}{2}}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^5} + \frac{4\sqrt{2\pi}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^5}
 \end{aligned}$$

Mathematica [C] time = 0.328869, size = 418, normalized size = 2.44

$$\frac{i e^{i \sin^{-1}(ax)} (-2 \sin^{-1}(ax) + i) - 2 (-i \sin^{-1}(ax))^{3/2} \Gamma\left(\frac{1}{2}, -i \sin^{-1}(ax)\right)}{24 \sin^{-1}(ax)^{3/2}} - \frac{e^{-i \sin^{-1}(ax)} (2 e^{i \sin^{-1}(ax)} (i \sin^{-1}(ax))^{3/2} \Gamma\left(\frac{1}{2}, i \sin^{-1}(ax)\right) - 2 i \sin^{-1}(ax) + i)}{24 \sin^{-1}(ax)^{3/2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^4/ArcSin[a*x]^(5/2),x]

[Out]
$$\frac{\left((I E^{(I \text{ArcSin}[a*x])} (I - 2 \text{ArcSin}[a*x]) - 2 ((-I) \text{ArcSin}[a*x])^{(3/2)} \Gamma[1/2, (-I) \text{ArcSin}[a*x]]) / (24 \text{ArcSin}[a*x]^{(3/2)}) - (1 - (2I) \text{ArcSin}[a*x] + 2 E^{(I \text{ArcSin}[a*x])} (I \text{ArcSin}[a*x])^{(3/2)} \Gamma[1/2, I \text{ArcSin}[a*x]]) / (24 E^{(I \text{ArcSin}[a*x])} \text{ArcSin}[a*x]^{(3/2)}) - (I E^{((3I) \text{ArcSin}[a*x])} (I - 6 \text{ArcSin}[a*x]) - 6 \sqrt{3} ((-I) \text{ArcSin}[a*x])^{(3/2)} \Gamma[1/2, (-3I) \text{ArcSin}[a*x]]) / (16 \text{ArcSin}[a*x]^{(3/2)}) + (1 - (6I) \text{ArcSin}[a*x] + 6 \sqrt{3} E^{((3I) \text{ArcSin}[a*x])} (I \text{ArcSin}[a*x])^{(3/2)} \Gamma[1/2, (3I) \text{ArcSin}[a*x]]) / (16 E^{((3I) \text{ArcSin}[a*x])} \text{ArcSin}[a*x]^{(3/2)}) + (I E^{((5I) \text{ArcSin}[a*x])} (I - 10 \text{ArcSin}[a*x]) - 10 \sqrt{5} ((-I) \text{ArcSin}[a*x])^{(3/2)} \Gamma[1/2, (-5I) \text{ArcSin}[a*x]]) / (48 \text{ArcSin}[a*x]^{(3/2)}) - (1 - (10I) \text{ArcSin}[a*x] + 10 \sqrt{5} E^{((5I) \text{ArcSin}[a*x])} (I \text{ArcSin}[a*x])^{(3/2)} \Gamma[1/2, (5I) \text{ArcSin}[a*x]]) / (48 E^{((5I) \text{ArcSin}[a*x])} \text{ArcSin}[a*x]^{(3/2)}) \right) / a^5$$

Maple [A] time = 0.07, size = 175, normalized size = 1.

$$\frac{1}{24 a^5} \left(18 \sqrt{2} \sqrt{\pi} \sqrt{3} \text{FresnelC} \left(\frac{\sqrt{2} \sqrt{3} \sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) (\arcsin(ax))^{3/2} - 10 \sqrt{2} \sqrt{\pi} \sqrt{5} \text{FresnelC} \left(\frac{\sqrt{2} \sqrt{5} \sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) (\arcsin(ax))^{3/2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x)^(5/2),x)

[Out]
$$\frac{1}{24 a^5} \left((18 \sqrt{2} \sqrt{\pi} \sqrt{3} \text{FresnelC} \left(\frac{\sqrt{2} \sqrt{3} \sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) (\arcsin(ax))^{3/2} - 10 \sqrt{2} \sqrt{\pi} \sqrt{5} \text{FresnelC} \left(\frac{\sqrt{2} \sqrt{5} \sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) (\arcsin(ax))^{3/2} - 4 \sqrt{2} \sqrt{\pi} \sqrt{5} \text{FresnelC} \left(\frac{\sqrt{2} \sqrt{5} \sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) (\arcsin(ax))^{3/2} + 4 a x \arcsin(ax) + 10 \arcsin(ax) \sin(5 \arcsin(ax)) - 18 \arcsin(ax) \sin(3 \arcsin(ax)) - 2 (-a^2 x^2 + 1)^{1/2} - \cos(5 \arcsin(ax)) + 3 \cos(3 \arcsin(ax)) \right) / \arcsin(ax)^{(3/2)}$$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\operatorname{asin}^{\frac{5}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**4/asin(a*x)**(5/2),x)

[Out] Integral(x**4/asin(a*x)**(5/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\operatorname{arcsin}(ax)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(5/2),x, algorithm="giac")

[Out] integrate(x^4/arcsin(a*x)^(5/2), x)

$$3.108 \quad \int \frac{x^3}{\sin^{-1}(ax)^{5/2}} dx$$

Optimal. Leaf size=126

$$\frac{4\sqrt{2\pi}S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^4} - \frac{4\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{3a^4} - \frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x^3*\text{Sqrt}[1 - a^2*x^2])/(3*a*\text{ArcSin}[a*x]^{(3/2)}) - (4*x^2)/(a^2*\text{Sqrt}[\text{ArcSin}[a*x]]) + (16*x^4)/(3*\text{Sqrt}[\text{ArcSin}[a*x]]) + (4*\text{Sqrt}[2*\text{Pi}]*\text{FresnelS}[2*\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(3*a^4) - (4*\text{Sqrt}[\text{Pi}]*\text{FresnelS}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(3*a^4)$

Rubi [A] time = 0.338175, antiderivative size = 126, normalized size of antiderivative = 1., number of steps used = 15, number of rules used = 7, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.583$, Rules used = {4633, 4719, 4635, 4406, 3305, 3351, 12}

$$\frac{4\sqrt{2\pi}S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^4} - \frac{4\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{3a^4} - \frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] Int[x^3/ArcSin[a*x]^(5/2), x]

[Out] $(-2*x^3*\text{Sqrt}[1 - a^2*x^2])/(3*a*\text{ArcSin}[a*x]^{(3/2)}) - (4*x^2)/(a^2*\text{Sqrt}[\text{ArcSin}[a*x]]) + (16*x^4)/(3*\text{Sqrt}[\text{ArcSin}[a*x]]) + (4*\text{Sqrt}[2*\text{Pi}]*\text{FresnelS}[2*\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(3*a^4) - (4*\text{Sqrt}[\text{Pi}]*\text{FresnelS}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(3*a^4)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_)*(x_)^(m_.), x_Symbol] :> Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + (Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_)*((f_.)*(x_)^(m_.))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*Sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*Sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_)*(x_)^(m_.), x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rubi steps

$$\begin{aligned}
 \int \frac{x^3}{\sin^{-1}(ax)^{5/2}} dx &= -\frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} + \frac{2\int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx}{a} - \frac{1}{3}(8a)\int \frac{x^4}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx \\
 &= -\frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}} - \frac{64}{3}\int \frac{x^3}{\sqrt{\sin^{-1}(ax)}} dx + \frac{8\int \frac{x}{\sqrt{\sin^{-1}(ax)}} dx}{a^2} \\
 &= -\frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}} + \frac{8\text{Subst}\left(\int \frac{\cos(x)\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^4} - \frac{64}{3}\int \frac{x^2}{\sqrt{\sin^{-1}(ax)}} dx \\
 &= -\frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}} + \frac{8\text{Subst}\left(\int \frac{\sin(2x)}{2\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^4} - \frac{64}{3}\int \frac{x}{\sqrt{\sin^{-1}(ax)}} dx \\
 &= -\frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}} + \frac{8\text{Subst}\left(\int \frac{\sin(4x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{3a^4} + \frac{4\text{Subst}\left(\int \frac{1}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^4} \\
 &= -\frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}} + \frac{16\text{Subst}\left(\int \sin(4x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{3a^4} + \frac{4\text{Subst}\left(\int \frac{1}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{a^4} \\
 &= -\frac{2x^3\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4x^2}{a^2\sqrt{\sin^{-1}(ax)}} + \frac{16x^4}{3\sqrt{\sin^{-1}(ax)}} + \frac{4\sqrt{2}\pi S\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^4} - \frac{4\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{3a^4}
 \end{aligned}$$

Mathematica [C] time = 0.393931, size = 200, normalized size = 1.59

$$-4\sin^{-1}(ax)\left(-\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) - \sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right) + e^{-2i\sin^{-1}(ax)}\right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3/ArcSin[a*x]^(5/2),x]

[Out] $(-4 \operatorname{ArcSin}[a x] (E^{(-2 I) \operatorname{ArcSin}[a x]} + E^{(2 I) \operatorname{ArcSin}[a x]}) - \sqrt{2} \operatorname{Sqrt}[(-I) \operatorname{ArcSin}[a x]] \operatorname{Gamma}[1/2, (-2 I) \operatorname{ArcSin}[a x]] - \sqrt{2} \operatorname{Sqrt}[I \operatorname{ArcSin}[a x]] \operatorname{Gamma}[1/2, (2 I) \operatorname{ArcSin}[a x]]) + 4 \operatorname{ArcSin}[a x] (E^{(-4 I) \operatorname{ArcSin}[a x]} + E^{(4 I) \operatorname{ArcSin}[a x]}) - 2 \operatorname{Sqrt}[(-I) \operatorname{ArcSin}[a x]] \operatorname{Gamma}[1/2, (-4 I) \operatorname{ArcSin}[a x]] - 2 \operatorname{Sqrt}[I \operatorname{ArcSin}[a x]] \operatorname{Gamma}[1/2, (4 I) \operatorname{ArcSin}[a x]]) - 2 \operatorname{Sin}[2 \operatorname{ArcSin}[a x]] + \operatorname{Sin}[4 \operatorname{ArcSin}[a x]]) / (12 a^4 \operatorname{ArcSin}[a x]^{(3/2)})$

Maple [A] time = 0.057, size = 109, normalized size = 0.9

$$-\frac{1}{12 a^4} \left(-16 \sqrt{2} \sqrt{\pi} \operatorname{FresnelS} \left(2 \frac{\sqrt{2} \sqrt{\operatorname{arcsin}(a x)}}{\sqrt{\pi}} \right) (\operatorname{arcsin}(a x))^{3/2} + 16 \sqrt{\pi} \operatorname{FresnelS} \left(2 \frac{\sqrt{\operatorname{arcsin}(a x)}}{\sqrt{\pi}} \right) (\operatorname{arcsin}(a x))^{3/2} + \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/arcsin(a*x)^(5/2),x)

[Out] $-1/12/a^4 * (-16*2^{(1/2)}*Pi^{(1/2)}*FresnelS(2*2^{(1/2)}/Pi^{(1/2)}*arcsin(a*x)^{(1/2)}*arcsin(a*x)^{(3/2)} + 16*Pi^{(1/2)}*FresnelS(2*arcsin(a*x)^{(1/2)}/Pi^{(1/2)})*arcsin(a*x)^{(3/2)} + 8*arcsin(a*x)*cos(2*arcsin(a*x)) - 8*arcsin(a*x)*cos(4*arcsin(a*x)) + 2*sin(2*arcsin(a*x)) - sin(4*arcsin(a*x))) / arcsin(a*x)^{(3/2)}$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\operatorname{asin}^{\frac{5}{2}}(a x)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/asin(a*x)**(5/2), x)

[Out] Integral(x**3/asin(a*x)**(5/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\arcsin(ax)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^(5/2), x, algorithm="giac")

[Out] integrate(x^3/arcsin(a*x)^(5/2), x)

$$3.109 \quad \int \frac{x^2}{\sin^{-1}(ax)^{5/2}} dx$$

Optimal. Leaf size=125

$$-\frac{\sqrt{2\pi}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^3} + \frac{\sqrt{6\pi}\text{FresnelC}\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^3} - \frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x^2*\text{Sqrt}[1 - a^2*x^2])/(3*a*\text{ArcSin}[a*x]^{(3/2)}) - (8*x)/(3*a^2*\text{Sqrt}[\text{ArcSin}[a*x]]) + (4*x^3)/\text{Sqrt}[\text{ArcSin}[a*x]] - (\text{Sqrt}[2*\text{Pi}]*\text{FresnelC}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(3*a^3) + (\text{Sqrt}[6*\text{Pi}]*\text{FresnelC}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]])/a^3$

Rubi [A] time = 0.301204, antiderivative size = 125, normalized size of antiderivative = 1., number of steps used = 13, number of rules used = 7, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.583$, Rules used = {4633, 4719, 4635, 4406, 3304, 3352, 4623}

$$-\frac{\sqrt{2\pi}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^3} + \frac{\sqrt{6\pi}\text{FresnelC}\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^3} - \frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2/\text{ArcSin}[a*x]^{(5/2)}, x]$

[Out] $(-2*x^2*\text{Sqrt}[1 - a^2*x^2])/(3*a*\text{ArcSin}[a*x]^{(3/2)}) - (8*x)/(3*a^2*\text{Sqrt}[\text{ArcSin}[a*x]]) + (4*x^3)/\text{Sqrt}[\text{ArcSin}[a*x]] - (\text{Sqrt}[2*\text{Pi}]*\text{FresnelC}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(3*a^3) + (\text{Sqrt}[6*\text{Pi}]*\text{FresnelC}[\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]])/a^3$

Rule 4633

$\text{Int}[(a_. + \text{ArcSin}[c_.*(x_.)]*(b_.))^{(n_.)}*(x_.)^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] + (\text{Dist}[(c*(m+1))/(b*(n+1)), \text{Int}[(x^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x] - \text{Dist}[m/(b*c*(n+1)), \text{Int}[(x^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x]) /; \text{FreeQ}\{a, b, c\}, x \&\& \text{IGtQ}[m, 0] \&\& \text{LtQ}[n, -2]$

Rule 4719

$\text{Int}[(((a_. + \text{ArcSin}[c_.*(x_.)]*(b_.))^{(n_.)}*((f_.)*(x_.))^{(m_.)})/\text{Sqrt}[(d_. + (e_.)*(x_.)^2], x_Symbol] \rightarrow \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{LtQ}[n, -1] \&\& \text{GtQ}[d, 0]$

Rule 4635

$\text{Int}[(a_. + \text{ArcSin}[c_.*(x_.)]*(b_.))^{(n_.)}*(x_.)^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[1/c^{(m+1)}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x], x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c, n\}, x \&\& \text{IGtQ}[m, 0]$

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 4623

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^n, x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sin^{-1}(ax)^{5/2}} dx &= -\frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} + \frac{4\int \frac{x}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx}{3a} - (2a) \int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}} - 12 \int \frac{x^2}{\sqrt{\sin^{-1}(ax)}} dx + \frac{8\int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx}{3a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}} + \frac{8\text{Subst}\left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{3a^3} - \frac{12\text{Subst}\left(\int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx, x, \sin^{-1}(ax)\right)}{3a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}} + \frac{16\text{Subst}\left(\int \cos(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{3a^3} - \frac{12\text{Subst}\left(\int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx, x, \sin^{-1}(ax)\right)}{3a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}} + \frac{8\sqrt{2\pi}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^3} - \frac{3\text{Subst}\left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{3a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}} + \frac{8\sqrt{2\pi}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^3} - \frac{6\text{Subst}\left(\int \cos(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{3a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{8x}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{4x^3}{\sqrt{\sin^{-1}(ax)}} - \frac{\sqrt{2\pi}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^3} + \frac{\sqrt{6\pi}C\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^3} \end{aligned}$$

Mathematica [C] time = 0.207792, size = 277, normalized size = 2.22

$$\frac{i e^{i \sin^{-1}(ax)} (-2 \sin^{-1}(ax) + i) - 2 (-i \sin^{-1}(ax))^{3/2} \Gamma\left(\frac{1}{2}, -i \sin^{-1}(ax)\right)}{12 \sin^{-1}(ax)^{3/2}} - \frac{e^{-i \sin^{-1}(ax)} (2 e^{i \sin^{-1}(ax)} (i \sin^{-1}(ax))^{3/2} \Gamma\left(\frac{1}{2}, i \sin^{-1}(ax)\right) - 2 i \sin^{-1}(ax) + i)}{12 \sin^{-1}(ax)^{3/2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2/ArcSin[a*x]^(5/2),x]

[Out]
$$\frac{\left((I * E^{(I * \text{ArcSin}[a * x])} * (I - 2 * \text{ArcSin}[a * x]) - 2 * ((-I) * \text{ArcSin}[a * x])^{(3/2)} * \text{Gamma}[1/2, (-I) * \text{ArcSin}[a * x]]) / (12 * \text{ArcSin}[a * x]^{(3/2)}) - (1 - (2 * I) * \text{ArcSin}[a * x] + 2 * E^{(I * \text{ArcSin}[a * x])} * (I * \text{ArcSin}[a * x])^{(3/2)} * \text{Gamma}[1/2, I * \text{ArcSin}[a * x]]) / (12 * E^{(I * \text{ArcSin}[a * x])} * \text{ArcSin}[a * x]^{(3/2)}) - (I * E^{((3 * I) * \text{ArcSin}[a * x])} * (I - 6 * \text{ArcSin}[a * x]) - 6 * \text{Sqrt}[3] * ((-I) * \text{ArcSin}[a * x])^{(3/2)} * \text{Gamma}[1/2, (-3 * I) * \text{ArcSin}[a * x]]) / (12 * \text{ArcSin}[a * x]^{(3/2)}) + (1 - (6 * I) * \text{ArcSin}[a * x] + 6 * \text{Sqrt}[3] * E^{((3 * I) * \text{ArcSin}[a * x])} * (I * \text{ArcSin}[a * x])^{(3/2)} * \text{Gamma}[1/2, (3 * I) * \text{ArcSin}[a * x]]) / (12 * E^{((3 * I) * \text{ArcSin}[a * x])} * \text{ArcSin}[a * x]^{(3/2)}) \right) / a^3$$

Maple [A] time = 0.055, size = 117, normalized size = 0.9

$$-\frac{1}{6a^3} \left(-6\sqrt{2}\sqrt{\pi}\sqrt{3}\text{FresnelC}\left(\frac{\sqrt{2}\sqrt{3}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) (\arcsin(ax))^{3/2} + 2\sqrt{2}\sqrt{\pi}\text{FresnelC}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) (\arcsin(ax))^{3/2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/arcsin(a*x)^(5/2),x)

[Out]
$$-1/6/a^3 * (-6 * 2^{(1/2)} * \text{Pi}^{(1/2)} * 3^{(1/2)} * \text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)} * 3^{(1/2)} * \arcsin(a * x)^{(1/2)}) * \arcsin(a * x)^{(3/2)} + 2 * 2^{(1/2)} * \text{Pi}^{(1/2)} * \text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)} * \arcsin(a * x)^{(1/2)}) * \arcsin(a * x)^{(3/2)} - 2 * a * x * \arcsin(a * x) + 6 * \arcsin(a * x) * \sin(3 * \arcsin(a * x)) + (-a^2 * x^2 + 1)^{(1/2)} - \cos(3 * \arcsin(a * x))) / \arcsin(a * x)^{(3/2)}$$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\operatorname{asin}^{\frac{5}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/asin(a*x)**(5/2), x)

[Out] Integral(x**2/asin(a*x)**(5/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\operatorname{arcsin}(ax)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(5/2), x, algorithm="giac")

[Out] integrate(x^2/arcsin(a*x)^(5/2), x)

$$3.110 \quad \int \frac{x}{\sin^{-1}(ax)^{5/2}} dx$$

Optimal. Leaf size=89

$$-\frac{8\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{3a^2} - \frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}}$$

[Out] $(-2*x*\text{Sqrt}[1 - a^2*x^2])/(3*a*\text{ArcSin}[a*x]^{(3/2)}) - 4/(3*a^2*\text{Sqrt}[\text{ArcSin}[a*x]]) + (8*x^2)/(3*\text{Sqrt}[\text{ArcSin}[a*x]]) - (8*\text{Sqrt}[\text{Pi}]*\text{FresnelS}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(3*a^2)$

Rubi [A] time = 0.179532, antiderivative size = 89, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 8, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.8$, Rules used = {4633, 4719, 4635, 4406, 12, 3305, 3351, 4641}

$$-\frac{8\sqrt{\pi}S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{3a^2} - \frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x/\text{ArcSin}[a*x]^{(5/2)}, x]$

[Out] $(-2*x*\text{Sqrt}[1 - a^2*x^2])/(3*a*\text{ArcSin}[a*x]^{(3/2)}) - 4/(3*a^2*\text{Sqrt}[\text{ArcSin}[a*x]]) + (8*x^2)/(3*\text{Sqrt}[\text{ArcSin}[a*x]]) - (8*\text{Sqrt}[\text{Pi}]*\text{FresnelS}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(3*a^2)$

Rule 4633

$\text{Int}[(a_. + \text{ArcSin}[(c_.)*(x_.)]*(b_.))^{(n_.)}*(x_.)^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] + (\text{Dist}[(c*(m+1))/(b*(n+1)), \text{Int}[(x^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x] - \text{Dist}[m/(b*c*(n+1)), \text{Int}[(x^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x]) /; \text{FreeQ}\{a, b, c\}, x \&\& \text{IGtQ}[m, 0] \&\& \text{LtQ}[n, -2]$

Rule 4719

$\text{Int}[(a_. + \text{ArcSin}[(c_.)*(x_.)]*(b_.))^{(n_.)}*((f_.)*(x_.))^{(m_.)}/\text{Sqrt}[(d_. + (e_.)*(x_.)^2], x_Symbol] \rightarrow \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{LtQ}[n, -1] \&\& \text{GtQ}[d, 0]$

Rule 4635

$\text{Int}[(a_. + \text{ArcSin}[(c_.)*(x_.)]*(b_.))^{(n_.)}*(x_.)^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[1/c^{(m+1)}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x], x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c, n\}, x \&\& \text{IGtQ}[m, 0]$

Rule 4406

$\text{Int}[\text{Cos}[(a_. + (b_.)*(x_.))^{(p_.)}*((c_. + (d_.)*(x_.))^{(m_.)}*\text{Sin}[(a_. + (b_.)*(x_.))^{(n_.)}], x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigReduce}[(c + d*x)^m, \text{Sin}[a + b*x$

$]^n \cos[a + b \cdot x]^p, x] /;$ FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3305

Int[sin[(e_) + (f_)*(x_)]/Sqrt[(c_) + (d_)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_)*((e_) + (f_)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 4641

Int[((a_) + ArcSin[(c_)*(x_)]*(b_))^(n_)/Sqrt[(d_) + (e_)*(x_)^2], x_Symbol] := Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rubi steps

$$\begin{aligned} \int \frac{x}{\sin^{-1}(ax)^{5/2}} dx &= -\frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} + \frac{2 \int \frac{1}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx}{3a} - \frac{1}{3}(4a) \int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{3/2}} dx \\ &= -\frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}} - \frac{16}{3} \int \frac{x}{\sqrt{\sin^{-1}(ax)}} dx \\ &= -\frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}} - \frac{16 \operatorname{Subst}\left(\int \frac{\cos(x)\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{3a^2} \\ &= -\frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}} - \frac{16 \operatorname{Subst}\left(\int \frac{\sin(2x)}{2\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{3a^2} \\ &= -\frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}} - \frac{8 \operatorname{Subst}\left(\int \frac{\sin(2x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{3a^2} \\ &= -\frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}} - \frac{16 \operatorname{Subst}\left(\int \sin(2x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{3a^2} \\ &= -\frac{2x\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4}{3a^2\sqrt{\sin^{-1}(ax)}} + \frac{8x^2}{3\sqrt{\sin^{-1}(ax)}} - \frac{8\sqrt{\pi} S\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{3a^2} \end{aligned}$$

Mathematica [C] time = 0.225307, size = 112, normalized size = 1.26

$$\frac{\sin(2\sin^{-1}(ax)) + 2\sin^{-1}(ax)\left(-\sqrt{2}\sqrt{-i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) - \sqrt{2}\sqrt{i\sin^{-1}(ax)}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right)\right)}{3a^2\sin^{-1}(ax)^{3/2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x/ArcSin[a*x]^(5/2),x]

[Out] $-(2*\text{ArcSin}[a*x]*(E^{((-2*I)*\text{ArcSin}[a*x])} + E^{((2*I)*\text{ArcSin}[a*x])}) - \text{Sqrt}[2]*\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\text{Gamma}[1/2, (-2*I)*\text{ArcSin}[a*x]] - \text{Sqrt}[2]*\text{Sqrt}[I*\text{ArcSin}[a*x]]*\text{Gamma}[1/2, (2*I)*\text{ArcSin}[a*x]]) + \text{Sin}[2*\text{ArcSin}[a*x]])/(3*a^2*\text{ArcSin}[a*x]^{(3/2)})$

Maple [A] time = 0.039, size = 56, normalized size = 0.6

$$-\frac{1}{3a^2} \left(8\sqrt{\pi} \text{FresnelS} \left(2 \frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) (\arcsin(ax))^{3/2} + 4 \arcsin(ax) \cos(2 \arcsin(ax)) + \sin(2 \arcsin(ax)) \right) (\arcsin(ax))^{3/2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/arcsin(a*x)^(5/2),x)

[Out] $-1/3/a^2*(8*\text{Pi}^{(1/2)}*\text{FresnelS}(2*\arcsin(a*x)^{(1/2)}/\text{Pi}^{(1/2)})*\arcsin(a*x)^{(3/2)}+4*\arcsin(a*x)*\cos(2*\arcsin(a*x))+\sin(2*\arcsin(a*x)))/\arcsin(a*x)^{(3/2)}$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\text{asin}^{\frac{5}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/asin(a*x)**(5/2),x)

[Out] Integral(x/asin(a*x)**(5/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\arcsin(ax)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(5/2),x, algorithm="giac")

[Out] integrate(x/arcsin(a*x)^(5/2), x)

$$3.111 \quad \int \frac{1}{\sin^{-1}(ax)^{5/2}} dx$$

Optimal. Leaf size=76

$$-\frac{2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4\sqrt{2\pi}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a} + \frac{4x}{3\sqrt{\sin^{-1}(ax)}}$$

[Out] (-2*Sqrt[1 - a^2*x^2])/(3*a*ArcSin[a*x]^(3/2)) + (4*x)/(3*Sqrt[ArcSin[a*x]]) - (4*Sqrt[2*Pi]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(3*a)

Rubi [A] time = 0.0989886, antiderivative size = 76, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4621, 4719, 4623, 3304, 3352}

$$-\frac{2\sqrt{1-a^2x^2}}{3a\sin^{-1}(ax)^{3/2}} - \frac{4\sqrt{2\pi}\text{FresnelC}\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a} + \frac{4x}{3\sqrt{\sin^{-1}(ax)}}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^(-5/2), x]

[Out] (-2*Sqrt[1 - a^2*x^2])/(3*a*ArcSin[a*x]^(3/2)) + (4*x)/(3*Sqrt[ArcSin[a*x]]) - (4*Sqrt[2*Pi]*FresnelC[Sqrt[2/Pi]*Sqrt[ArcSin[a*x]]])/(3*a)

Rule 4621

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_), x_Symbol] :> Simp[(Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + Dist[c/(b*(n + 1)), Int[(x*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && LtQ[n, -1]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_))*((f_.)*(x_.))^ (m_.)/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] :> Simp[((f*x)^(m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*Sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*Sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^ (n_), x_Symbol] :> Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_.)]/Sqrt[(c_.) + (d_.)*(x_.)], x_Symbol] :> Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*(e_.) + (f_.)*(x_.)]^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sin^{-1}(ax)^{5/2}} dx &= -\frac{2\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^{3/2}} - \frac{1}{3}(2a) \int \frac{x}{\sqrt{1-a^2x^2} \sin^{-1}(ax)^{3/2}} dx \\ &= -\frac{2\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^{3/2}} + \frac{4x}{3\sqrt{\sin^{-1}(ax)}} - \frac{4}{3} \int \frac{1}{\sqrt{\sin^{-1}(ax)}} dx \\ &= -\frac{2\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^{3/2}} + \frac{4x}{3\sqrt{\sin^{-1}(ax)}} - \frac{4 \operatorname{Subst}\left(\int \frac{\cos(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{3a} \\ &= -\frac{2\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^{3/2}} + \frac{4x}{3\sqrt{\sin^{-1}(ax)}} - \frac{8 \operatorname{Subst}\left(\int \cos(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{3a} \\ &= -\frac{2\sqrt{1-a^2x^2}}{3a \sin^{-1}(ax)^{3/2}} + \frac{4x}{3\sqrt{\sin^{-1}(ax)}} - \frac{4\sqrt{2\pi}C\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a} \end{aligned}$$

Mathematica [C] time = 0.127191, size = 138, normalized size = 1.82

$$\frac{-4(-i \sin^{-1}(ax))^{3/2} \operatorname{Gamma}\left(\frac{1}{2}, -i \sin^{-1}(ax)\right) - 2ie^{i \sin^{-1}(ax)}(2 \sin^{-1}(ax) - i)}{6a \sin^{-1}(ax)^{3/2}} + \frac{e^{-i \sin^{-1}(ax)}(-4e^{i \sin^{-1}(ax)}(i \sin^{-1}(ax))^{3/2})}{6a}$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^(-5/2), x]

[Out] ((-2*I)*E^(I*ArcSin[a*x])*(-I + 2*ArcSin[a*x]) - 4*((-I)*ArcSin[a*x])^(3/2) *Gamma[1/2, (-I)*ArcSin[a*x]])/(6*a*ArcSin[a*x]^(3/2)) + (-2 + (4*I)*ArcSin[a*x] - 4*E^(I*ArcSin[a*x])*(I*ArcSin[a*x])^(3/2)*Gamma[1/2, I*ArcSin[a*x]])/(6*a*E^(I*ArcSin[a*x])*ArcSin[a*x]^(3/2))

Maple [A] time = 0.042, size = 83, normalized size = 1.1

$$-\frac{\sqrt{2}}{3a\sqrt{\pi}(\arcsin(ax))^2} \left(4(\arcsin(ax))^2 \pi \operatorname{FresnelC}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) - 2(\arcsin(ax))^{3/2} \sqrt{2}\sqrt{\pi}xa + \sqrt{2}\sqrt{\arcsin(ax)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x)^(5/2), x)

[Out] -1/3/a*2^(1/2)/Pi^(1/2)*(4*arcsin(a*x)^2*Pi*FresnelC(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))-2*arcsin(a*x)^(3/2)*2^(1/2)*Pi^(1/2)*x*a+2^(1/2)*arcsin(a*x)^(1/2)*Pi^(1/2)*(-a^2*x^2+1)^(1/2))/arcsin(a*x)^2

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\operatorname{asin}^{\frac{5}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/asin(a*x)**(5/2),x)

[Out] Integral(asin(a*x)**(-5/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\operatorname{arcsin}(ax)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/arcsin(a*x)^(5/2),x, algorithm="giac")

[Out] integrate(arcsin(a*x)^(-5/2), x)

$$3.112 \quad \int \frac{1}{x \sin^{-1}(ax)^{5/2}} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{1}{x \sin^{-1}(ax)^{5/2}}, x\right)$$

[Out] Unintegrable[1/(x*ArcSin[a*x]^(5/2)), x]

Rubi [A] time = 0.0133551, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x \sin^{-1}(ax)^{5/2}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*ArcSin[a*x]^(5/2)), x]

[Out] Defer[Int][1/(x*ArcSin[a*x]^(5/2)), x]

Rubi steps

$$\int \frac{1}{x \sin^{-1}(ax)^{5/2}} dx = \int \frac{1}{x \sin^{-1}(ax)^{5/2}} dx$$

Mathematica [A] time = 0.462145, size = 0, normalized size = 0.

$$\int \frac{1}{x \sin^{-1}(ax)^{5/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*ArcSin[a*x]^(5/2)), x]

[Out] Integrate[1/(x*ArcSin[a*x]^(5/2)), x]

Maple [A] time = 0.069, size = 0, normalized size = 0.

$$\int \frac{1}{x} (\arcsin(ax))^{-\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x)^(5/2), x)

[Out] int(1/x/arcsin(a*x)^(5/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \operatorname{asin}^{\frac{5}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/asin(a*x)**(5/2),x)

[Out] Integral(1/(x*asin(a*x)**(5/2)), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \operatorname{arcsin}(ax)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(5/2),x, algorithm="giac")

[Out] integrate(1/(x*arcsin(a*x)^(5/2)), x)

$$3.113 \quad \int \frac{x^4}{\sin^{-1}(ax)^{7/2}} dx$$

Optimal. Leaf size=264

$$\frac{\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a^5} + \frac{8\sqrt{6\pi}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{5a^5} - \frac{5\sqrt{\frac{3\pi}{2}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^5} + \frac{5\sqrt{\frac{5\pi}{2}}S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^5} + \frac{40\sqrt{\frac{3\pi}{2}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^5}$$

[Out] $(-2x^4\sqrt{1-a^2x^2})/(5a\text{ArcSin}[ax]^{5/2}) - (16x^3)/(15a^2\text{ArcSin}[ax]^{3/2}) + (4x^5)/(3\text{ArcSin}[ax]^{3/2}) - (32x^2\sqrt{1-a^2x^2})/(5a^3\sqrt{\text{ArcSin}[ax]}) + (40x^4\sqrt{1-a^2x^2})/(3a\sqrt{\text{ArcSin}[ax]}) + (\sqrt{2\pi}\text{FresnelS}[\sqrt{2/\pi}\sqrt{\text{ArcSin}[ax]}])/(15a^5) - (5\sqrt{3\pi/2}\text{FresnelS}[\sqrt{6/\pi}\sqrt{\text{ArcSin}[ax]}])/a^5 + (8\sqrt{6\pi}\text{FresnelS}[\sqrt{6/\pi}\sqrt{\text{ArcSin}[ax]}])/(5a^5) + (5\sqrt{5\pi/2}\text{FresnelS}[\sqrt{10/\pi}\sqrt{\text{ArcSin}[ax]}])/(3a^5) + (40\sqrt{3\pi/2}\text{FresnelS}[\sqrt{6/\pi}\sqrt{\text{ArcSin}[ax]}])/(3a^5)$

Rubi [A] time = 0.39587, antiderivative size = 264, normalized size of antiderivative = 1., number of steps used = 17, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4633, 4719, 4631, 3305, 3351}

$$\frac{\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a^5} + \frac{8\sqrt{6\pi}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{5a^5} - \frac{5\sqrt{\frac{3\pi}{2}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{a^5} + \frac{5\sqrt{\frac{5\pi}{2}}S\left(\sqrt{\frac{10}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^5} + \frac{40\sqrt{\frac{3\pi}{2}}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{3a^5}$$

Antiderivative was successfully verified.

[In] Int[x^4/ArcSin[a*x]^(7/2),x]

[Out] $(-2x^4\sqrt{1-a^2x^2})/(5a\text{ArcSin}[ax]^{5/2}) - (16x^3)/(15a^2\text{ArcSin}[ax]^{3/2}) + (4x^5)/(3\text{ArcSin}[ax]^{3/2}) - (32x^2\sqrt{1-a^2x^2})/(5a^3\sqrt{\text{ArcSin}[ax]}) + (40x^4\sqrt{1-a^2x^2})/(3a\sqrt{\text{ArcSin}[ax]}) + (\sqrt{2\pi}\text{FresnelS}[\sqrt{2/\pi}\sqrt{\text{ArcSin}[ax]}])/(15a^5) - (5\sqrt{3\pi/2}\text{FresnelS}[\sqrt{6/\pi}\sqrt{\text{ArcSin}[ax]}])/a^5 + (8\sqrt{6\pi}\text{FresnelS}[\sqrt{6/\pi}\sqrt{\text{ArcSin}[ax]}])/(5a^5) + (5\sqrt{5\pi/2}\text{FresnelS}[\sqrt{10/\pi}\sqrt{\text{ArcSin}[ax]}])/(3a^5) + (40\sqrt{3\pi/2}\text{FresnelS}[\sqrt{6/\pi}\sqrt{\text{ArcSin}[ax]}])/(3a^5)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1-c^2*x^2]*(a+b*ArcSin[c*x])^(n+1))/(b*c*(n+1)), x] + (Dist[(c*(m+1))/(b*(n+1)), Int[(x^(m+1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x] - Dist[m/(b*c*(n+1)), Int[(x^(m-1)*(a+b*ArcSin[c*x])^(n+1))/sqrt[1-c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*((f_.)*(x_))^(m_.))/sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[((f*x)^m*(a+b*ArcSin[c*x])^(n+1))/(b*c*sqrt[d]*(n+1)), x] - Dist[(f*m)/(b*c*sqrt[d]*(n+1)), Int[(f*x)^(m-1)*(a+b*ArcSin[c*x])^(n+1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4631

```
Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(
x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1)/(b*c*(n + 1)), x] - Dist
[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin
[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a
, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_.)]/Sqrt[(c_.) + (d_.)*(x_.)], x_Symbol] := Dist[2/d
, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}
, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{x^4}{\sin^{-1}(ax)^{7/2}} dx &= -\frac{2x^4\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} + \frac{8\int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx}{5a} - (2a) \int \frac{x^5}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx \\ &= -\frac{2x^4\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{16x^3}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^5}{3\sin^{-1}(ax)^{3/2}} - \frac{20}{3} \int \frac{x^4}{\sin^{-1}(ax)^{3/2}} dx + \frac{16\int \frac{x^2}{\sin^{-1}(ax)^{3/2}} dx}{5a^2} \\ &= -\frac{2x^4\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{16x^3}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^5}{3\sin^{-1}(ax)^{3/2}} - \frac{32x^2\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{40x^4\sqrt{1-a^2x^2}}{3a\sqrt{\sin^{-1}(ax)}} + \frac{32\text{Subst}}{5a^2} \\ &= -\frac{2x^4\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{16x^3}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^5}{3\sin^{-1}(ax)^{3/2}} - \frac{32x^2\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{40x^4\sqrt{1-a^2x^2}}{3a\sqrt{\sin^{-1}(ax)}} - \frac{8\text{Subst}}{5a^2} \\ &= -\frac{2x^4\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{16x^3}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^5}{3\sin^{-1}(ax)^{3/2}} - \frac{32x^2\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{40x^4\sqrt{1-a^2x^2}}{3a\sqrt{\sin^{-1}(ax)}} - \frac{16\text{Subst}}{5a^2} \\ &= -\frac{2x^4\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{16x^3}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^5}{3\sin^{-1}(ax)^{3/2}} - \frac{32x^2\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{40x^4\sqrt{1-a^2x^2}}{3a\sqrt{\sin^{-1}(ax)}} + \frac{\sqrt{2\pi S}}{5a^2} \end{aligned}$$

Mathematica [C] time = 0.772494, size = 417, normalized size = 1.58

$$-8\sqrt{-i\sin^{-1}(ax)}\sin^{-1}(ax)^2\Gamma\left(\frac{1}{2}, -i\sin^{-1}(ax)\right) + 108\sqrt{3}\sqrt{-i\sin^{-1}(ax)}\sin^{-1}(ax)^2\Gamma\left(\frac{1}{2}, -3i\sin^{-1}(ax)\right) - 10$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[x^4/ArcSin[a*x]^(7/2), x]
```

```
[Out] (9*E^((3*I)*ArcSin[a*x])*(1 + (2*I)*ArcSin[a*x] - 12*ArcSin[a*x]^2) + 2*E^(
I*ArcSin[a*x])*(-3 - (2*I)*ArcSin[a*x] + 4*ArcSin[a*x]^2) + E^((5*I)*ArcSin
[a*x])*(-3 - (10*I)*ArcSin[a*x] + 100*ArcSin[a*x]^2) - 8*Sqrt[(-I)*ArcSin[a
*x]]*ArcSin[a*x]^2*Gamma[1/2, (-I)*ArcSin[a*x]] + (-6 + (4*I)*ArcSin[a*x] +
8*ArcSin[a*x]^2 + 8*E^(I*ArcSin[a*x])*(I*ArcSin[a*x])^(5/2)*Gamma[1/2, I*A
```

$$\text{rcSin}[a*x]]/E^{(I*\text{ArcSin}[a*x])} + 108*\text{Sqrt}[3]*\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\text{ArcSin}[a*x]^2*\text{Gamma}[1/2, (-3*I)*\text{ArcSin}[a*x]] - (9*(-1 + (2*I)*\text{ArcSin}[a*x] + 12*\text{ArcSin}[a*x]^2 + 12*\text{Sqrt}[3]*E^{((3*I)*\text{ArcSin}[a*x])}*(I*\text{ArcSin}[a*x])^{5/2}*\text{Gamma}[1/2, (3*I)*\text{ArcSin}[a*x]]))/E^{((3*I)*\text{ArcSin}[a*x])} - 100*\text{Sqrt}[5]*\text{Sqrt}[(-I)*\text{ArcSin}[a*x]]*\text{ArcSin}[a*x]^2*\text{Gamma}[1/2, (-5*I)*\text{ArcSin}[a*x]] + (-3 + (10*I)*\text{ArcSin}[a*x] + 100*\text{ArcSin}[a*x]^2 + 100*\text{Sqrt}[5]*E^{((5*I)*\text{ArcSin}[a*x])}*(I*\text{ArcSin}[a*x])^{5/2}*\text{Gamma}[1/2, (5*I)*\text{ArcSin}[a*x]]))/E^{((5*I)*\text{ArcSin}[a*x])})/(240*a^{5*\text{ArcSin}[a*x]^{5/2}}$$

Maple [A] time = 0.083, size = 225, normalized size = 0.9

$$-\frac{1}{120a^5} \left(-100\sqrt{2}\sqrt{\pi}\sqrt{5}\text{FresnelS}\left(\frac{\sqrt{2}\sqrt{5}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) (\arcsin(ax))^{5/2} + 108\sqrt{2}\sqrt{\pi}\sqrt{3}\text{FresnelS}\left(\frac{\sqrt{2}\sqrt{3}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) (\arcsin(ax))^{5/2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^4/arcsin(a*x)^(7/2),x)

[Out] $-1/120/a^{5*(-100*2^{(1/2)}*\text{Pi}^{(1/2)}*5^{(1/2)}*\text{FresnelS}(2^{(1/2)}/\text{Pi}^{(1/2)}*5^{(1/2)}*\arcsin(a*x)^{(1/2)})*\arcsin(a*x)^{(5/2)}+108*2^{(1/2)}*\text{Pi}^{(1/2)}*3^{(1/2)}*\text{FresnelS}(2^{(1/2)}/\text{Pi}^{(1/2)}*3^{(1/2)}*\arcsin(a*x)^{(1/2)})*\arcsin(a*x)^{(5/2)}-8*2^{(1/2)}*\text{Pi}^{(1/2)}*\text{FresnelS}(2^{(1/2)}/\text{Pi}^{(1/2)}*\arcsin(a*x)^{(1/2)})*\arcsin(a*x)^{(5/2)}+108*\arcsin(a*x)^2*\cos(3*\arcsin(a*x))-100*\arcsin(a*x)^2*\cos(5*\arcsin(a*x))-8*\arcsin(a*x)^2*(-a^2*x^2+1)^{(1/2)}-4*a*x*\arcsin(a*x)+18*\arcsin(a*x)*\sin(3*\arcsin(a*x))-10*\arcsin(a*x)*\sin(5*\arcsin(a*x))-9*\cos(3*\arcsin(a*x))+3*\cos(5*\arcsin(a*x))+6*(-a^2*x^2+1)^{(1/2)})/\arcsin(a*x)^{(5/2)}$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(7/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^4/arcsin(a*x)^(7/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4/asin(a*x)**(7/2),x)
```

```
[Out] Timed out
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^4}{\arcsin(ax)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4/arcsin(a*x)^(7/2),x, algorithm="giac")
```

```
[Out] integrate(x^4/arcsin(a*x)^(7/2), x)
```

$$3.114 \quad \int \frac{x^3}{\sin^{-1}(ax)^{7/2}} dx$$

Optimal. Leaf size=190

$$\frac{32\sqrt{2\pi}\text{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a^4} - \frac{16\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{15a^4} + \frac{128x^3\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4x^3}{5a^2\sin^{-1}(ax)^{3/2}}$$

[Out] $(-2*x^3*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) - (4*x^2)/(5*a^2*\text{ArcSin}[a*x]^{(3/2)}) + (16*x^4)/(15*\text{ArcSin}[a*x]^{(3/2)}) - (16*x*\text{Sqrt}[1 - a^2*x^2])/(5*a^3*\text{Sqrt}[\text{ArcSin}[a*x]]) + (128*x^3*\text{Sqrt}[1 - a^2*x^2])/(15*a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (32*\text{Sqrt}[2*\text{Pi}]*\text{FresnelC}[2*\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(15*a^4) - (16*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(15*a^4)$

Rubi [A] time = 0.318782, antiderivative size = 190, normalized size of antiderivative = 1., number of steps used = 12, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4633, 4719, 4631, 3304, 3352}

$$\frac{32\sqrt{2\pi}\text{FresnelC}\left(2\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a^4} - \frac{16\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{15a^4} + \frac{128x^3\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4x^3}{5a^2\sin^{-1}(ax)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[x^3/ArcSin[a*x]^(7/2), x]

[Out] $(-2*x^3*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) - (4*x^2)/(5*a^2*\text{ArcSin}[a*x]^{(3/2)}) + (16*x^4)/(15*\text{ArcSin}[a*x]^{(3/2)}) - (16*x*\text{Sqrt}[1 - a^2*x^2])/(5*a^3*\text{Sqrt}[\text{ArcSin}[a*x]]) + (128*x^3*\text{Sqrt}[1 - a^2*x^2])/(15*a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (32*\text{Sqrt}[2*\text{Pi}]*\text{FresnelC}[2*\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(15*a^4) - (16*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(15*a^4)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*((f_.)*(x_)^(m_.))/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] := Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*Sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*Sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin

$[x]^{(m-1)*(m-(m+1)*\text{Sin}[x]^2), x], x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{IGtQ}[m, 0] \&\& \text{GeQ}[n, -2] \&\& \text{LtQ}[n, -1]$

Rule 3304

$\text{Int}[\text{sin}[\text{Pi}/2 + (e_.) + (f_.)*(x_.)]/\text{Sqrt}[(c_.) + (d_.)*(x_.)], x_Symbol] \text{:> Dist}[2/d, \text{Subst}[\text{Int}[\text{Cos}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /; \text{FreeQ}\{c, d, e, f\}, x] \&\& \text{ComplexFreeQ}[f] \&\& \text{EqQ}[d*e - c*f, 0]$

Rule 3352

$\text{Int}[\text{Cos}[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] \text{:> Simp}[(\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[\text{Sqrt}[2/\text{Pi}]*\text{Rt}[d, 2]*(e + f*x)])/(f*\text{Rt}[d, 2]), x] /; \text{FreeQ}\{d, e, f\}, x]$

Rubi steps

$$\begin{aligned} \int \frac{x^3}{\sin^{-1}(ax)^{7/2}} dx &= -\frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} + \frac{6\int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx}{5a} - \frac{1}{5}(8a)\int \frac{x^4}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx \\ &= -\frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4x^2}{5a^2\sin^{-1}(ax)^{3/2}} + \frac{16x^4}{15\sin^{-1}(ax)^{3/2}} - \frac{64}{15}\int \frac{x^3}{\sin^{-1}(ax)^{3/2}} dx + \frac{8\int \frac{x}{\sin^{-1}(ax)^{3/2}} dx}{5a^2} \\ &= -\frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4x^2}{5a^2\sin^{-1}(ax)^{3/2}} + \frac{16x^4}{15\sin^{-1}(ax)^{3/2}} - \frac{16x\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{128x^3\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} + \frac{16\text{Su}}{5a^2} \\ &= -\frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4x^2}{5a^2\sin^{-1}(ax)^{3/2}} + \frac{16x^4}{15\sin^{-1}(ax)^{3/2}} - \frac{16x\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{128x^3\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{64\text{Su}}{5a^2} \\ &= -\frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4x^2}{5a^2\sin^{-1}(ax)^{3/2}} + \frac{16x^4}{15\sin^{-1}(ax)^{3/2}} - \frac{16x\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{128x^3\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} + \frac{16\sqrt{\pi}}{5a^2} \\ &= -\frac{2x^3\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4x^2}{5a^2\sin^{-1}(ax)^{3/2}} + \frac{16x^4}{15\sin^{-1}(ax)^{3/2}} - \frac{16x\sqrt{1-a^2x^2}}{5a^3\sqrt{\sin^{-1}(ax)}} + \frac{128x^3\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} + \frac{32\sqrt{2}}{5a^2} \end{aligned}$$

Mathematica [C] time = 1.18683, size = 272, normalized size = 1.43

$$4\sin^{-1}(ax)\left(-4\sqrt{2}\left(-i\sin^{-1}(ax)\right)^{3/2}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) + e^{-2i\sin^{-1}(ax)}\left(-4\sqrt{2}e^{2i\sin^{-1}(ax)}\left(i\sin^{-1}(ax)\right)^{3/2}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right) + e^{2i\sin^{-1}(ax)}\left(-4\sqrt{2}\left(-i\sin^{-1}(ax)\right)^{3/2}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) + e^{-2i\sin^{-1}(ax)}\left(-4\sqrt{2}e^{2i\sin^{-1}(ax)}\left(i\sin^{-1}(ax)\right)^{3/2}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right)\right)\right)\right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^3/ArcSin[a*x]^(7/2), x]

[Out] $(4*\text{ArcSin}[a*x]*(\text{I}*E^{((2*\text{I})*\text{ArcSin}[a*x])}*(\text{I} - 4*\text{ArcSin}[a*x]) - 4*\text{Sqrt}[2]*((- \text{I})*\text{ArcSin}[a*x])^{(3/2)}*\Gamma[1/2, (-2*\text{I})*\text{ArcSin}[a*x]] + (-1 + (4*\text{I})*\text{ArcSin}[a*x] - 4*\text{Sqrt}[2]*E^{((2*\text{I})*\text{ArcSin}[a*x])}*(\text{I}*\text{ArcSin}[a*x])^{(3/2)}*\Gamma[1/2, (2*\text{I})*\text{ArcSin}[a*x]])/E^{((2*\text{I})*\text{ArcSin}[a*x])}) - 4*\text{ArcSin}[a*x]*(\text{I}*E^{((4*\text{I})*\text{ArcSin}[a*x])}*(\text{I} - 8*\text{ArcSin}[a*x]) - 16*((-\text{I})*\text{ArcSin}[a*x])^{(3/2)}*\Gamma[1/2, (-4*\text{I})*\text{ArcSin}[a*x]] + (-1 + (8*\text{I})*\text{ArcSin}[a*x] - 16*\text{E}^{((4*\text{I})*\text{ArcSin}[a*x])}*(\text{I}*\text{ArcSin}[a*x])^{(3/2)}*\Gamma[1/2, (4*\text{I})*\text{ArcSin}[a*x]])/E^{((4*\text{I})*\text{ArcSin}[a*x])}) - 6*\text{Sin}[2*$

$\text{ArcSin}[a*x] + 3*\text{Sin}[4*\text{ArcSin}[a*x]]/(60*a^4*\text{ArcSin}[a*x]^{(5/2)})$

Maple [A] time = 0.055, size = 139, normalized size = 0.7

$$\frac{1}{60a^4} \left(128\sqrt{2}\sqrt{\pi}\text{FresnelC}\left(2\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)(\arcsin(ax))^{5/2} - 64\sqrt{\pi}\text{FresnelC}\left(2\frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)(\arcsin(ax))^{5/2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3/arcsin(a*x)^(7/2),x)

[Out] 1/60/a^4*(128*2^(1/2)*Pi^(1/2)*FresnelC(2*2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))*arcsin(a*x)^(5/2)-64*Pi^(1/2)*FresnelC(2*arcsin(a*x)^(1/2)/Pi^(1/2))*arcsin(a*x)^(5/2)+32*sin(2*arcsin(a*x))*arcsin(a*x)^2-64*sin(4*arcsin(a*x))*arcsin(a*x)^2-8*arcsin(a*x)*cos(2*arcsin(a*x))+8*arcsin(a*x)*cos(4*arcsin(a*x))-6*sin(2*arcsin(a*x))+3*sin(4*arcsin(a*x)))/arcsin(a*x)^(5/2)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^(7/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3/arcsin(a*x)^(7/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3/asin(a*x)**(7/2),x)

[Out] Timed out

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^3}{\arcsin(ax)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3/arcsin(a*x)^(7/2),x, algorithm="giac")
```

```
[Out] integrate(x^3/arcsin(a*x)^(7/2), x)
```

$$3.115 \quad \int \frac{x^2}{\sin^{-1}(ax)^{7/2}} dx$$

Optimal. Leaf size=191

$$\frac{2\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a^3} - \frac{6\sqrt{6\pi}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{5a^3} + \frac{24x^2\sqrt{1-a^2x^2}}{5a\sqrt{\sin^{-1}(ax)}} - \frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{16\sqrt{1-a^2x^2}}{15a^3\sqrt{\sin^{-1}(ax)}} - \frac{1}{15a^2}$$

[Out] $(-2*x^2*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) - (8*x)/(15*a^2*\text{ArcSin}[a*x]^{(3/2)}) + (4*x^3)/(5*\text{ArcSin}[a*x]^{(3/2)}) - (16*\text{Sqrt}[1 - a^2*x^2])/(15*a^3*\text{Sqrt}[\text{ArcSin}[a*x]]) + (24*x^2*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (2*\text{Sqrt}[2*Pi]*\text{FresnelS}[\text{Sqrt}[2/Pi]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(15*a^3) - (6*\text{Sqrt}[6*Pi]*\text{FresnelS}[\text{Sqrt}[6/Pi]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(5*a^3)$

Rubi [A] time = 0.347694, antiderivative size = 191, normalized size of antiderivative = 1., number of steps used = 13, number of rules used = 7, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.583$, Rules used = {4633, 4719, 4631, 3305, 3351, 4621, 4723}

$$\frac{2\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a^3} - \frac{6\sqrt{6\pi}S\left(\sqrt{\frac{6}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{5a^3} + \frac{24x^2\sqrt{1-a^2x^2}}{5a\sqrt{\sin^{-1}(ax)}} - \frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{16\sqrt{1-a^2x^2}}{15a^3\sqrt{\sin^{-1}(ax)}} - \frac{1}{15a^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2/\text{ArcSin}[a*x]^{(7/2)}, x]$

[Out] $(-2*x^2*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) - (8*x)/(15*a^2*\text{ArcSin}[a*x]^{(3/2)}) + (4*x^3)/(5*\text{ArcSin}[a*x]^{(3/2)}) - (16*\text{Sqrt}[1 - a^2*x^2])/(15*a^3*\text{Sqrt}[\text{ArcSin}[a*x]]) + (24*x^2*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (2*\text{Sqrt}[2*Pi]*\text{FresnelS}[\text{Sqrt}[2/Pi]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(15*a^3) - (6*\text{Sqrt}[6*Pi]*\text{FresnelS}[\text{Sqrt}[6/Pi]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(5*a^3)$

Rule 4633

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^{(n)}*(x)^{(m)}, x_Symbol] := \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] + (\text{Dist}[(c*(m+1))/(b*(n+1)), \text{Int}[(x^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x] - \text{Dist}[m/(b*c*(n+1)), \text{Int}[(x^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x]) /; \text{FreeQ}\{a, b, c\}, x \&\& \text{IGtQ}[m, 0] \&\& \text{LtQ}[n, -2]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^{(n)}*((f*x)^{(m)})/\text{Sqrt}[d + (e*x)^2], x_Symbol] := \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{LtQ}[n, -1] \&\& \text{GtQ}[d, 0]$

Rule 4631

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^{(n)}*(x)^{(m)}, x_Symbol] := \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] - \text{Dist}[1/(b*c^{(m+1)}*(n+1)), \text{Subst}[\text{Int}[\text{ExpandTrigReduce}[(a + b*x)^{(n+1)}, \text{Sin}$

$[x]^{(m-1)}(m-(m+1)\sin[x]^2), x], x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{IGtQ}[m, 0] \&\& \text{GeQ}[n, -2] \&\& \text{LtQ}[n, -1]$

Rule 3305

$\text{Int}[\sin[(e_.) + (f_.)*(x_.)]/\text{Sqrt}[(c_.) + (d_.)*(x_.)], x_Symbol] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /; \text{FreeQ}\{c, d, e, f\}, x] \&\& \text{ComplexFreeQ}[f] \&\& \text{EqQ}[d*e - c*f, 0]$

Rule 3351

$\text{Int}[\text{Sin}[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Rt}[d, 2]*(e + f*x)])/(f*\text{Rt}[d, 2]), x] /; \text{FreeQ}\{d, e, f\}, x]$

Rule 4621

$\text{Int}[(a_.) + \text{ArcSin}[(c_.)*(x_.)]*(b_.)]^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] + \text{Dist}[c/(b*(n+1)), \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{LtQ}[n, -1]$

Rule 4723

$\text{Int}[(a_.) + \text{ArcSin}[(c_.)*(x_.)]*(b_.)]^{(n_.)}*(x_.)^{(m_.)}*((d_.) + (e_.)*(x_.)^2)^{(p_.)}, x_Symbol] \rightarrow \text{Dist}[d^p/c^{(m+1)}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x]^{(2*p+1)}, x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c, d, e, n\}, x] \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{IntegerQ}[2*p] \&\& \text{GtQ}[p, -1] \&\& \text{IGtQ}[m, 0] \&\& (\text{IntegerQ}[p] \parallel \text{GtQ}[d, 0])$

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sin^{-1}(ax)^{7/2}} dx &= -\frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} + \frac{4\int \frac{x}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx}{5a} - \frac{1}{5}(6a)\int \frac{x^3}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{8x}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^3}{5\sin^{-1}(ax)^{3/2}} - \frac{12}{5}\int \frac{x^2}{\sin^{-1}(ax)^{3/2}} dx + \frac{8\int \frac{1}{\sin^{-1}(ax)^{3/2}} dx}{15a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{8x}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^3}{5\sin^{-1}(ax)^{3/2}} - \frac{16\sqrt{1-a^2x^2}}{15a^3\sqrt{\sin^{-1}(ax)}} + \frac{24x^2\sqrt{1-a^2x^2}}{5a\sqrt{\sin^{-1}(ax)}} - \frac{24\text{Su}}{15a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{8x}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^3}{5\sin^{-1}(ax)^{3/2}} - \frac{16\sqrt{1-a^2x^2}}{15a^3\sqrt{\sin^{-1}(ax)}} + \frac{24x^2\sqrt{1-a^2x^2}}{5a\sqrt{\sin^{-1}(ax)}} - \frac{16\text{Su}}{15a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{8x}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^3}{5\sin^{-1}(ax)^{3/2}} - \frac{16\sqrt{1-a^2x^2}}{15a^3\sqrt{\sin^{-1}(ax)}} + \frac{24x^2\sqrt{1-a^2x^2}}{5a\sqrt{\sin^{-1}(ax)}} - \frac{32\text{Su}}{15a^2} \\ &= -\frac{2x^2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{8x}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{4x^3}{5\sin^{-1}(ax)^{3/2}} - \frac{16\sqrt{1-a^2x^2}}{15a^3\sqrt{\sin^{-1}(ax)}} + \frac{24x^2\sqrt{1-a^2x^2}}{5a\sqrt{\sin^{-1}(ax)}} + \frac{2\sqrt{2\pi}}{15a^2} \end{aligned}$$

Mathematica [C] time = 0.47627, size = 280, normalized size = 1.47

$$-4\sqrt{-i\sin^{-1}(ax)}\sin^{-1}(ax)^2\text{Gamma}\left(\frac{1}{2}, -i\sin^{-1}(ax)\right) + 36\sqrt{3}\sqrt{-i\sin^{-1}(ax)}\sin^{-1}(ax)^2\text{Gamma}\left(\frac{1}{2}, -3i\sin^{-1}(ax)\right) + e^{-i\sin^{-1}(ax)}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2/ArcSin[a*x]^(7/2),x]

[Out] (3*E^((3*I)*ArcSin[a*x])*(1 + (2*I)*ArcSin[a*x] - 12*ArcSin[a*x]^2) + E^(I*ArcSin[a*x])*(-3 - (2*I)*ArcSin[a*x] + 4*ArcSin[a*x]^2) - 4*Sqrt[(-I)*ArcSin[a*x]]*ArcSin[a*x]^2*Gamma[1/2, (-I)*ArcSin[a*x]] + (-3 + (2*I)*ArcSin[a*x] + 4*ArcSin[a*x]^2 + 4*E^(I*ArcSin[a*x])*(I*ArcSin[a*x])^(5/2)*Gamma[1/2, I*ArcSin[a*x]])/E^(I*ArcSin[a*x]) + 36*Sqrt[3]*Sqrt[(-I)*ArcSin[a*x]]*ArcSin[a*x]^2*Gamma[1/2, (-3*I)*ArcSin[a*x]] - (3*(-1 + (2*I)*ArcSin[a*x] + 12*ArcSin[a*x]^2 + 12*Sqrt[3]*E^((3*I)*ArcSin[a*x])*(I*ArcSin[a*x])^(5/2)*Gamma[1/2, (3*I)*ArcSin[a*x]]))/E^((3*I)*ArcSin[a*x]))/(60*a^3*ArcSin[a*x]^(5/2))

Maple [A] time = 0.055, size = 154, normalized size = 0.8

$$-\frac{1}{30a^3} \left(36\sqrt{2}\sqrt{\pi}\sqrt{3}\text{FresnelS}\left(\frac{\sqrt{2}\sqrt{3}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)(\arcsin(ax))^{5/2} - 4\sqrt{2}\sqrt{\pi}\text{FresnelS}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right)(\arcsin(ax))^{5/2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/arcsin(a*x)^(7/2),x)

[Out] -1/30/a^3*(36*2^(1/2)*Pi^(1/2)*3^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*3^(1/2)*arcsin(a*x)^(1/2))*arcsin(a*x)^(5/2)-4*2^(1/2)*Pi^(1/2)*FresnelS(2^(1/2)/Pi^(1/2)*arcsin(a*x)^(1/2))*arcsin(a*x)^(5/2)-4*arcsin(a*x)^2*(-a^2*x^2+1)^(1/2)+36*arcsin(a*x)^2*cos(3*arcsin(a*x))-2*a*x*arcsin(a*x)+6*arcsin(a*x)*sin(3*arcsin(a*x))+3*(-a^2*x^2+1)^(1/2)-3*cos(3*arcsin(a*x)))/arcsin(a*x)^(5/2)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(7/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(7/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/asin(a*x)**(7/2),x)

[Out] Timed out

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\arcsin(ax)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/arcsin(a*x)^(7/2),x, algorithm="giac")

[Out] integrate(x^2/arcsin(a*x)^(7/2), x)

$$3.116 \quad \int \frac{x}{\sin^{-1}(ax)^{7/2}} dx$$

Optimal. Leaf size=119

$$-\frac{32\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{15a^2} + \frac{32x\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{2x\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{8x^2}{15\sin^{-1}(ax)^{3/2}}$$

[Out] $(-2*x*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) - 4/(15*a^2*\text{ArcSin}[a*x]^{(3/2)}) + (8*x^2)/(15*\text{ArcSin}[a*x]^{(3/2)}) + (32*x*\text{Sqrt}[1 - a^2*x^2])/(15*a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (32*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(15*a^2)$

Rubi [A] time = 0.171635, antiderivative size = 119, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4633, 4719, 4631, 3304, 3352, 4641}

$$-\frac{32\sqrt{\pi}\text{FresnelC}\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{15a^2} + \frac{32x\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{2x\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{8x^2}{15\sin^{-1}(ax)^{3/2}}$$

Antiderivative was successfully verified.

[In] Int[x/ArcSin[a*x]^(7/2),x]

[Out] $(-2*x*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) - 4/(15*a^2*\text{ArcSin}[a*x]^{(3/2)}) + (8*x^2)/(15*\text{ArcSin}[a*x]^{(3/2)}) + (32*x*\text{Sqrt}[1 - a^2*x^2])/(15*a*\text{Sqrt}[\text{ArcSin}[a*x]]) - (32*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[\text{ArcSin}[a*x]])/\text{Sqrt}[\text{Pi}]])/(15*a^2)$

Rule 4633

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_.)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + (Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]

Rule 4719

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((f_.)*(x_.)^(m_.))/Sqrt[(d_.) + (e_.)*(x_.)^2], x_Symbol] := Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*Sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*Sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_.)^(m_.), x_Symbol] := Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a

, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] := Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rubi steps

$$\begin{aligned} \int \frac{x}{\sin^{-1}(ax)^{7/2}} dx &= -\frac{2x\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} + \frac{2\int \frac{1}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx}{5a} - \frac{1}{5}(4a) \int \frac{x^2}{\sqrt{1-a^2x^2}\sin^{-1}(ax)^{5/2}} dx \\ &= -\frac{2x\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{8x^2}{15\sin^{-1}(ax)^{3/2}} - \frac{16}{15} \int \frac{x}{\sin^{-1}(ax)^{3/2}} dx \\ &= -\frac{2x\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{8x^2}{15\sin^{-1}(ax)^{3/2}} + \frac{32x\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{32\text{Subst}\left(\int \frac{\cos(2x)}{\sqrt{x}} dx, \frac{\sin^{-1}(ax)}{a}\right)}{15a^2} \\ &= -\frac{2x\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{8x^2}{15\sin^{-1}(ax)^{3/2}} + \frac{32x\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{64\text{Subst}\left(\int \cos(2x^2) dx, \frac{\sin^{-1}(ax)}{a}\right)}{15a^2} \\ &= -\frac{2x\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} - \frac{4}{15a^2\sin^{-1}(ax)^{3/2}} + \frac{8x^2}{15\sin^{-1}(ax)^{3/2}} + \frac{32x\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{32\sqrt{\pi}C\left(\frac{2\sqrt{\sin^{-1}(ax)}}{\sqrt{\pi}}\right)}{15a^2} \end{aligned}$$

Mathematica [C] time = 0.411848, size = 146, normalized size = 1.23

$$\frac{3\sin\left(2\sin^{-1}(ax)\right) + \sin^{-1}(ax)\left(8\sqrt{2}\left(-i\sin^{-1}(ax)\right)^{3/2}\Gamma\left(\frac{1}{2}, -2i\sin^{-1}(ax)\right) + e^{-2i\sin^{-1}(ax)}\left(8\sqrt{2}e^{2i\sin^{-1}(ax)}\left(i\sin^{-1}(ax)\right)^{3/2}\Gamma\left(\frac{1}{2}, 2i\sin^{-1}(ax)\right) + 3\sin\left[2\sin^{-1}(ax)\right]\right)}{15a^2\sin^{-1}(ax)^{5/2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x/ArcSin[a*x]^(7/2), x]

[Out] -(ArcSin[a*x]*(2*E^((2*I)*ArcSin[a*x]))*(1 + (4*I)*ArcSin[a*x]) + 8*Sqrt[2]*((-I)*ArcSin[a*x])^(3/2)*Gamma[1/2, (-2*I)*ArcSin[a*x]] + (2 - (8*I)*ArcSin[a*x] + 8*Sqrt[2]*E^((2*I)*ArcSin[a*x]))*(I*ArcSin[a*x])^(3/2)*Gamma[1/2, (2*I)*ArcSin[a*x]])/E^((2*I)*ArcSin[a*x]) + 3*Sin[2*ArcSin[a*x]]/(15*a^2*ArcSin[a*x]^(5/2))

Maple [A] time = 0.038, size = 73, normalized size = 0.6

$$\frac{1}{15a^2} \left(-32\sqrt{\pi} \operatorname{FresnelC} \left(2 \frac{\sqrt{\arcsin(ax)}}{\sqrt{\pi}} \right) (\arcsin(ax))^{5/2} + 16 \sin(2 \arcsin(ax)) (\arcsin(ax))^2 - 4 \arcsin(ax) \cos(2 \arcsin(ax)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/arcsin(a*x)^(7/2),x)

[Out] 1/15/a^2*(-32*Pi^(1/2)*FresnelC(2*arcsin(a*x)^(1/2)/Pi^(1/2))*arcsin(a*x)^(5/2)+16*sin(2*arcsin(a*x))*arcsin(a*x)^2-4*arcsin(a*x)*cos(2*arcsin(a*x))-3*sin(2*arcsin(a*x)))/arcsin(a*x)^(5/2)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(7/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/arcsin(a*x)^(7/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/asin(a*x)**(7/2),x)

[Out] Timed out

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\arcsin(ax)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x/arcsin(a*x)^(7/2),x, algorithm="giac")
```

```
[Out] integrate(x/arcsin(a*x)^(7/2), x)
```

$$3.117 \quad \int \frac{1}{\sin^{-1}(ax)^{7/2}} dx$$

Optimal. Leaf size=105

$$\frac{8\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} + \frac{8\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a} + \frac{4x}{15\sin^{-1}(ax)^{3/2}}$$

[Out] $(-2*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) + (4*x)/(15*\text{ArcSin}[a*x]^{(3/2)}) + (8*\text{Sqrt}[1 - a^2*x^2])/(15*a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (8*\text{Sqrt}[2*\text{Pi}]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(15*a)$

Rubi [A] time = 0.165702, antiderivative size = 105, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4621, 4719, 4723, 3305, 3351}

$$\frac{8\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} - \frac{2\sqrt{1-a^2x^2}}{5a\sin^{-1}(ax)^{5/2}} + \frac{8\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a} + \frac{4x}{15\sin^{-1}(ax)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{ArcSin}[a*x]^{(-7/2)}, x]$

[Out] $(-2*\text{Sqrt}[1 - a^2*x^2])/(5*a*\text{ArcSin}[a*x]^{(5/2)}) + (4*x)/(15*\text{ArcSin}[a*x]^{(3/2)}) + (8*\text{Sqrt}[1 - a^2*x^2])/(15*a*\text{Sqrt}[\text{ArcSin}[a*x]]) + (8*\text{Sqrt}[2*\text{Pi}]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[\text{ArcSin}[a*x]]])/(15*a)$

Rule 4621

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^{(n)}, x_Symbol] \rightarrow \text{Simp}[(\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] + \text{Dist}[c/(b*(n+1)), \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c\}, x] \&\& \text{LtQ}[n, -1]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^{(n)}*(f*x)^{(m)}/\text{Sqrt}[d + (e*x)^2], x_Symbol] \rightarrow \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x] \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{LtQ}[n, -1] \&\& \text{GtQ}[d, 0]$

Rule 4723

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + \text{ArcSin}[c*x])^{(n)}*(x)^{(m)}*(d + (e*x)^2)^{(p)}, x_Symbol] \rightarrow \text{Dist}[d^p/c^{(m+1)}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x]^{(2*p+1)}, x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c, d, e, n\}, x] \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{IntegerQ}[2*p] \&\& \text{GtQ}[p, -1] \&\& \text{IGtQ}[m, 0] \&\& (\text{IntegerQ}[p] \parallel \text{GtQ}[d, 0])$

Rule 3305

$\text{Int}[\text{sin}[(e + (f*x))/\text{Sqrt}[c + d*x]], x_Symbol] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /; \text{FreeQ}\{c, d, e, f\}$

, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))²], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int \frac{1}{\sin^{-1}(ax)^{7/2}} dx &= -\frac{2\sqrt{1-a^2x^2}}{5a \sin^{-1}(ax)^{5/2}} - \frac{1}{5}(2a) \int \frac{x}{\sqrt{1-a^2x^2} \sin^{-1}(ax)^{5/2}} dx \\ &= -\frac{2\sqrt{1-a^2x^2}}{5a \sin^{-1}(ax)^{5/2}} + \frac{4x}{15 \sin^{-1}(ax)^{3/2}} - \frac{4}{15} \int \frac{1}{\sin^{-1}(ax)^{3/2}} dx \\ &= -\frac{2\sqrt{1-a^2x^2}}{5a \sin^{-1}(ax)^{5/2}} + \frac{4x}{15 \sin^{-1}(ax)^{3/2}} + \frac{8\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} + \frac{1}{15}(8a) \int \frac{x}{\sqrt{1-a^2x^2}\sqrt{\sin^{-1}(ax)}} dx \\ &= -\frac{2\sqrt{1-a^2x^2}}{5a \sin^{-1}(ax)^{5/2}} + \frac{4x}{15 \sin^{-1}(ax)^{3/2}} + \frac{8\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} + \frac{8 \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{x}} dx, x, \sin^{-1}(ax)\right)}{15a} \\ &= -\frac{2\sqrt{1-a^2x^2}}{5a \sin^{-1}(ax)^{5/2}} + \frac{4x}{15 \sin^{-1}(ax)^{3/2}} + \frac{8\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} + \frac{16 \operatorname{Subst}\left(\int \sin(x^2) dx, x, \sqrt{\sin^{-1}(ax)}\right)}{15a} \\ &= -\frac{2\sqrt{1-a^2x^2}}{5a \sin^{-1}(ax)^{5/2}} + \frac{4x}{15 \sin^{-1}(ax)^{3/2}} + \frac{8\sqrt{1-a^2x^2}}{15a\sqrt{\sin^{-1}(ax)}} + \frac{8\sqrt{2\pi}S\left(\sqrt{\frac{2}{\pi}}\sqrt{\sin^{-1}(ax)}\right)}{15a} \end{aligned}$$

Mathematica [C] time = 0.259962, size = 143, normalized size = 1.36

$$\frac{-8\sqrt{-i \sin^{-1}(ax)} \sin^{-1}(ax)^2 \operatorname{Gamma}\left(\frac{1}{2}, -i \sin^{-1}(ax)\right) + e^{-i \sin^{-1}(ax)} \left(8e^{i \sin^{-1}(ax)} (i \sin^{-1}(ax))^{5/2} \operatorname{Gamma}\left(\frac{1}{2}, i \sin^{-1}(ax)\right) + \dots\right)}{30a \sin^{-1}(ax)^{5/2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[ArcSin[a*x]^(-7/2), x]

[Out] (2*E^(I*ArcSin[a*x])*(-3 - (2*I)*ArcSin[a*x] + 4*ArcSin[a*x]²) - 8*Sqrt[(-I)*ArcSin[a*x]]*ArcSin[a*x]²*Gamma[1/2, (-I)*ArcSin[a*x]] + (-6 + (4*I)*ArcSin[a*x] + 8*ArcSin[a*x]² + 8*E^(I*ArcSin[a*x])*(I*ArcSin[a*x])^(5/2)*Gamma[1/2, I*ArcSin[a*x]])/E^(I*ArcSin[a*x]))/(30*a*ArcSin[a*x]^(5/2))

Maple [A] time = 0.04, size = 110, normalized size = 1.1

$$\frac{\sqrt{2}}{15a\sqrt{\pi}(\arcsin(ax))^3} \left(8(\arcsin(ax))^3 \pi \operatorname{FresnelS}\left(\frac{\sqrt{2}\sqrt{\arcsin(ax)}}{\sqrt{\pi}}\right) + 4(\arcsin(ax))^{5/2} \sqrt{2}\sqrt{\pi}\sqrt{-a^2x^2+1} + 2(\arcsin(ax))^{5/2} \sqrt{2}\sqrt{\pi}\sqrt{-a^2x^2+1} + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/arcsin(a*x)^(7/2), x)

```
[Out] 1/15/a*2^(1/2)/Pi^(1/2)/arcsin(a*x)^3*(8*arcsin(a*x)^3*Pi*FresnelS(2^(1/2)/
Pi^(1/2)*arcsin(a*x)^(1/2))+4*arcsin(a*x)^(5/2)*2^(1/2)*Pi^(1/2)*(-a^2*x^2+
1)^(1/2)+2*arcsin(a*x)^(3/2)*2^(1/2)*Pi^(1/2)*x*a-3*2^(1/2)*arcsin(a*x)^(1/
2)*Pi^(1/2)*(-a^2*x^2+1)^(1/2))
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/arcsin(a*x)^(7/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/arcsin(a*x)^(7/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/asin(a*x)**(7/2),x)
```

```
[Out] Timed out
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\arcsin(ax)^{\frac{7}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/arcsin(a*x)^(7/2),x, algorithm="giac")
```

```
[Out] integrate(arcsin(a*x)^(-7/2), x)
```

$$3.118 \quad \int \frac{1}{x \sin^{-1}(ax)^{7/2}} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{1}{x \sin^{-1}(ax)^{7/2}}, x\right)$$

[Out] Unintegrable[1/(x*ArcSin[a*x]^(7/2)), x]

Rubi [A] time = 0.0127218, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x \sin^{-1}(ax)^{7/2}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*ArcSin[a*x]^(7/2)), x]

[Out] Defer[Int][1/(x*ArcSin[a*x]^(7/2)), x]

Rubi steps

$$\int \frac{1}{x \sin^{-1}(ax)^{7/2}} dx = \int \frac{1}{x \sin^{-1}(ax)^{7/2}} dx$$

Mathematica [A] time = 0.46164, size = 0, normalized size = 0.

$$\int \frac{1}{x \sin^{-1}(ax)^{7/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*ArcSin[a*x]^(7/2)), x]

[Out] Integrate[1/(x*ArcSin[a*x]^(7/2)), x]

Maple [A] time = 0.066, size = 0, normalized size = 0.

$$\int \frac{1}{x} (\arcsin(ax))^{-\frac{7}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/arcsin(a*x)^(7/2), x)

[Out] int(1/x/arcsin(a*x)^(7/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(7/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(7/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/asin(a*x)**(7/2),x)

[Out] Timed out

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x \arcsin(ax)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/arcsin(a*x)^(7/2),x, algorithm="giac")

[Out] integrate(1/(x*arcsin(a*x)^(7/2)), x)

3.119 $\int (bx)^m \sin^{-1}(ax)^4 dx$

Optimal. Leaf size=64

$$\frac{\sin^{-1}(ax)^4 (bx)^{m+1}}{b(m+1)} - \frac{4a \text{Unintegrable}\left(\frac{\sin^{-1}(ax)^3 (bx)^{m+1}}{\sqrt{1-a^2x^2}}, x\right)}{b(m+1)}$$

[Out] $((b*x)^{(1+m)}*\text{ArcSin}[a*x]^4)/(b*(1+m)) - (4*a*\text{Unintegrable}[((b*x)^{(1+m)}*\text{ArcSin}[a*x]^3)/\text{Sqrt}[1 - a^2*x^2], x))/(b*(1+m))$

Rubi [A] time = 0.121914, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int (bx)^m \sin^{-1}(ax)^4 dx$$

Verification is Not applicable to the result.

[In] $\text{Int}[(b*x)^m*\text{ArcSin}[a*x]^4, x]$

[Out] $((b*x)^{(1+m)}*\text{ArcSin}[a*x]^4)/(b*(1+m)) - (4*a*\text{Defer}[\text{Int}][(b*x)^{(1+m)}*\text{ArcSin}[a*x]^3)/\text{Sqrt}[1 - a^2*x^2], x))/(b*(1+m))$

Rubi steps

$$\int (bx)^m \sin^{-1}(ax)^4 dx = \frac{(bx)^{1+m} \sin^{-1}(ax)^4}{b(1+m)} - \frac{(4a) \int \frac{(bx)^{1+m} \sin^{-1}(ax)^3}{\sqrt{1-a^2x^2}} dx}{b(1+m)}$$

Mathematica [A] time = 1.06375, size = 0, normalized size = 0.

$$\int (bx)^m \sin^{-1}(ax)^4 dx$$

Verification is Not applicable to the result.

[In] $\text{Integrate}[(b*x)^m*\text{ArcSin}[a*x]^4, x]$

[Out] $\text{Integrate}[(b*x)^m*\text{ArcSin}[a*x]^4, x]$

Maple [A] time = 0.828, size = 0, normalized size = 0.

$$\int (bx)^m (\arcsin(ax))^4 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((b*x)^m*\arcsin(a*x)^4, x)$

[Out] $\text{int}((b*x)^m*\arcsin(a*x)^4, x)$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^4,x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}((bx)^m \arcsin(ax)^4, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^4,x, algorithm="fricas")

[Out] integral((b*x)^m*arcsin(a*x)^4, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin^4(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m*asin(a*x)**4,x)

[Out] Integral((b*x)**m*asin(a*x)**4, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin(ax)^4 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^4,x, algorithm="giac")

[Out] integrate((b*x)^m*arcsin(a*x)^4, x)

3.120 $\int (bx)^m \sin^{-1}(ax)^3 dx$

Optimal. Leaf size=64

$$\frac{\sin^{-1}(ax)^3 (bx)^{m+1}}{b(m+1)} - \frac{3a \text{Unintegrable}\left(\frac{\sin^{-1}(ax)^2 (bx)^{m+1}}{\sqrt{1-a^2x^2}}, x\right)}{b(m+1)}$$

[Out] $((b*x)^{(1+m)}*ArcSin[a*x]^3)/(b*(1+m)) - (3*a*Unintegrable[((b*x)^{(1+m)}*ArcSin[a*x]^2)/Sqrt[1 - a^2*x^2], x])/(b*(1+m))$

Rubi [A] time = 0.118226, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int (bx)^m \sin^{-1}(ax)^3 dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m*ArcSin[a*x]^3,x]

[Out] $((b*x)^{(1+m)}*ArcSin[a*x]^3)/(b*(1+m)) - (3*a*Defer[Int](((b*x)^{(1+m)}*ArcSin[a*x]^2)/Sqrt[1 - a^2*x^2], x))/(b*(1+m))$

Rubi steps

$$\int (bx)^m \sin^{-1}(ax)^3 dx = \frac{(bx)^{1+m} \sin^{-1}(ax)^3}{b(1+m)} - \frac{(3a) \int \frac{(bx)^{1+m} \sin^{-1}(ax)^2}{\sqrt{1-a^2x^2}} dx}{b(1+m)}$$

Mathematica [A] time = 0.941219, size = 0, normalized size = 0.

$$\int (bx)^m \sin^{-1}(ax)^3 dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m*ArcSin[a*x]^3,x]

[Out] Integrate[(b*x)^m*ArcSin[a*x]^3, x]

Maple [A] time = 0.548, size = 0, normalized size = 0.

$$\int (bx)^m (\arcsin(ax))^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*arcsin(a*x)^3,x)

[Out] int((b*x)^m*arcsin(a*x)^3,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^3,x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}((bx)^m \arcsin(ax)^3, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^3,x, algorithm="fricas")

[Out] integral((b*x)^m*arcsin(a*x)^3, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin^3(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m*asin(a*x)**3,x)

[Out] Integral((b*x)**m*asin(a*x)**3, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin(ax)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^3,x, algorithm="giac")

[Out] integrate((b*x)^m*arcsin(a*x)^3, x)

3.121 $\int (bx)^m \sin^{-1}(ax)^2 dx$

Optimal. Leaf size=150

$$\frac{2a^2(bx)^{m+3} \text{HypergeometricPFQ}\left(\left\{1, \frac{m}{2} + \frac{3}{2}, \frac{m}{2} + \frac{3}{2}\right\}, \left\{\frac{m}{2} + 2, \frac{m}{2} + \frac{5}{2}\right\}, a^2x^2\right)}{b^3(m+1)(m+2)(m+3)} - \frac{2a \sin^{-1}(ax)(bx)^{m+2} \text{Hypergeometric2F1}\left[1/2, (2+m)/2, (4+m)/2, a^2x^2\right]}{b^2(m+1)(m+2)}$$

[Out] $((bx)^{(1+m)} \text{ArcSin}[ax]^2)/(b(1+m)) - (2a(bx)^{(2+m)} \text{ArcSin}[ax] * \text{Hypergeometric2F1}[1/2, (2+m)/2, (4+m)/2, a^2x^2])/(b^2(1+m)(2+m)) + (2a^2(bx)^{(3+m)} \text{HypergeometricPFQ}[\{1, 3/2 + m/2, 3/2 + m/2\}, \{2 + m/2, 5/2 + m/2\}, a^2x^2])/(b^3(1+m)(2+m)(3+m))$

Rubi [A] time = 0.114086, antiderivative size = 150, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {4627, 4711}

$$\frac{2a^2(bx)^{m+3} {}_3F_2\left(1, \frac{m}{2} + \frac{3}{2}, \frac{m}{2} + \frac{3}{2}; \frac{m}{2} + 2, \frac{m}{2} + \frac{5}{2}; a^2x^2\right)}{b^3(m+1)(m+2)(m+3)} - \frac{2a \sin^{-1}(ax)(bx)^{m+2} {}_2F_1\left(\frac{1}{2}, \frac{m+2}{2}; \frac{m+4}{2}; a^2x^2\right)}{b^2(m+1)(m+2)} + \frac{\sin^{-1}(ax)^2(bx)^{m+1}}{b(m+1)}$$

Antiderivative was successfully verified.

[In] Int[(b*x)^m*ArcSin[a*x]^2,x]

[Out] $((bx)^{(1+m)} \text{ArcSin}[ax]^2)/(b(1+m)) - (2a(bx)^{(2+m)} \text{ArcSin}[ax] * \text{Hypergeometric2F1}[1/2, (2+m)/2, (4+m)/2, a^2x^2])/(b^2(1+m)(2+m)) + (2a^2(bx)^{(3+m)} \text{HypergeometricPFQ}[\{1, 3/2 + m/2, 3/2 + m/2\}, \{2 + m/2, 5/2 + m/2\}, a^2x^2])/(b^3(1+m)(2+m)(3+m))$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((d_.)*(x_.))^(m_.), x_Symbol] := Simp[((d*x)^(m+1)*(a + b*ArcSin[c*x])^n)/(d*(m+1)), x] - Dist[(b*c*n)/(d*(m+1)), Int[((d*x)^(m+1)*(a + b*ArcSin[c*x])^(n-1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4711

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))*((f_.)*(x_.))^(m_.)/Sqrt[(d_.) + (e_.)*(x_.)^2], x_Symbol] := Simp[((f*x)^(m+1)*(a + b*ArcSin[c*x])*Hypergeometric2F1[1/2, (1+m)/2, (3+m)/2, c^2*x^2])/(Sqrt[d]*f*(m+1)), x] - Simp[(b*c*(f*x)^(m+2)*HypergeometricPFQ[\{1, 1 + m/2, 1 + m/2\}, \{3/2 + m/2, 2 + m/2\}, c^2*x^2])/(Sqrt[d]*f^2*(m+1)*(m+2)), x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int (bx)^m \sin^{-1}(ax)^2 dx &= \frac{(bx)^{1+m} \sin^{-1}(ax)^2}{b(1+m)} - \frac{(2a) \int \frac{(bx)^{1+m} \sin^{-1}(ax)}{\sqrt{1-a^2x^2}} dx}{b(1+m)} \\ &= \frac{(bx)^{1+m} \sin^{-1}(ax)^2}{b(1+m)} - \frac{2a(bx)^{2+m} \sin^{-1}(ax) {}_2F_1\left(\frac{1}{2}, \frac{2+m}{2}; \frac{4+m}{2}; a^2x^2\right)}{b^2(1+m)(2+m)} + \frac{2a^2(bx)^{3+m} {}_3F_2\left(1, \frac{3}{2} + \frac{m}{2}, \frac{3}{2} + \frac{m}{2}\right)}{b^3(1+m)(2+m)} \end{aligned}$$

Mathematica [A] time = 0.0431142, size = 122, normalized size = 0.81

$$\frac{x(bx)^m \left(2a^2x^2 \text{HypergeometricPFQ} \left(\left\{ 1, \frac{m}{2} + \frac{3}{2}, \frac{m}{2} + \frac{3}{2} \right\}, \left\{ \frac{m}{2} + 2, \frac{m}{2} + \frac{5}{2} \right\}, a^2x^2 \right) + (m+3) \sin^{-1}(ax) \right) \left((m+2) \sin^{-1}(ax) \right)}{(m+1)(m+2)(m+3)}$$

Antiderivative was successfully verified.

[In] Integrate[(b*x)^m*ArcSin[a*x]^2,x]

[Out] (x*(b*x)^m*((3 + m)*ArcSin[a*x]*((2 + m)*ArcSin[a*x] - 2*a*x*Hypergeometric2F1[1/2, (2 + m)/2, (4 + m)/2, a^2*x^2]) + 2*a^2*x^2*HypergeometricPFQ[{1, 3/2 + m/2, 3/2 + m/2}, {2 + m/2, 5/2 + m/2}, a^2*x^2]))/((1 + m)*(2 + m)*(3 + m))

Maple [F] time = 0.525, size = 0, normalized size = 0.

$$\int (bx)^m (\arcsin(ax))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*arcsin(a*x)^2,x)

[Out] int((b*x)^m*arcsin(a*x)^2,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^2,x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left((bx)^m \arcsin(ax)^2, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral((b*x)^m*arcsin(a*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \text{asin}^2(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)**m*asin(a*x)**2,x)
```

```
[Out] Integral((b*x)**m*asin(a*x)**2, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin(ax)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x)^2,x, algorithm="giac")
```

```
[Out] integrate((b*x)^m*arcsin(a*x)^2, x)
```

3.122 $\int (bx)^m \sin^{-1}(ax) dx$

Optimal. Leaf size=69

$$\frac{\sin^{-1}(ax)(bx)^{m+1}}{b(m+1)} - \frac{a(bx)^{m+2} \text{Hypergeometric2F1}\left(\frac{1}{2}, \frac{m+2}{2}, \frac{m+4}{2}, a^2x^2\right)}{b^2(m+1)(m+2)}$$

[Out] $((b*x)^{(1+m)*\text{ArcSin}[a*x]})/(b*(1+m)) - (a*(b*x)^{(2+m)*\text{Hypergeometric2F1}[1/2, (2+m)/2, (4+m)/2, a^2*x^2])/(b^2*(1+m)*(2+m))$

Rubi [A] time = 0.0252512, antiderivative size = 69, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.2$, Rules used = {4627, 364}

$$\frac{\sin^{-1}(ax)(bx)^{m+1}}{b(m+1)} - \frac{a(bx)^{m+2} {}_2F_1\left(\frac{1}{2}, \frac{m+2}{2}; \frac{m+4}{2}; a^2x^2\right)}{b^2(m+1)(m+2)}$$

Antiderivative was successfully verified.

[In] Int[(b*x)^m*ArcSin[a*x], x]

[Out] $((b*x)^{(1+m)*\text{ArcSin}[a*x]})/(b*(1+m)) - (a*(b*x)^{(2+m)*\text{Hypergeometric2F1}[1/2, (2+m)/2, (4+m)/2, a^2*x^2])/(b^2*(1+m)*(2+m))$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((d_.)*(x_.))^(m_.), x_Symbol] :> Simp[((d*x)^(m+1)*(a + b*ArcSin[c*x])^n)/(d*(m+1)), x] - Dist[(b*c*n)/(d*(m+1)), Int[((d*x)^(m+1)*(a + b*ArcSin[c*x])^(n-1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 364

Int[((c_.)*(x_.))^(m_.)*((a_.) + (b_.)*(x_.)^(n_.))^(p_.), x_Symbol] :> Simp[(a^p*(c*x)^(m+1)*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, -((b*x^n)/a)])/ (c*(m+1)), x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rubi steps

$$\begin{aligned} \int (bx)^m \sin^{-1}(ax) dx &= \frac{(bx)^{1+m} \sin^{-1}(ax)}{b(1+m)} - \frac{a \int \frac{(bx)^{1+m}}{\sqrt{1-a^2x^2}} dx}{b(1+m)} \\ &= \frac{(bx)^{1+m} \sin^{-1}(ax)}{b(1+m)} - \frac{a(bx)^{2+m} {}_2F_1\left(\frac{1}{2}, \frac{2+m}{2}; \frac{4+m}{2}; a^2x^2\right)}{b^2(1+m)(2+m)} \end{aligned}$$

Mathematica [A] time = 0.0203494, size = 56, normalized size = 0.81

$$\frac{x(bx)^m \left(ax \text{Hypergeometric2F1}\left(\frac{1}{2}, \frac{m+2}{2}, \frac{m+4}{2}, a^2x^2\right) - (m+2) \sin^{-1}(ax) \right)}{(m+1)(m+2)}$$

Antiderivative was successfully verified.

[In] Integrate[(b*x)^m*ArcSin[a*x],x]

[Out] $-\left(x(b*x)^m\left(-((2+m)*\text{ArcSin}[a*x]) + a*x*\text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{(2+m)}{2}, \frac{(4+m)}{2}, a^2*x^2\right]\right)\right)/((1+m)*(2+m))$

Maple [F] time = 0.531, size = 0, normalized size = 0.

$$\int (bx)^m \arcsin(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*arcsin(a*x),x)

[Out] int((b*x)^m*arcsin(a*x),x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x),x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left((bx)^m \arcsin(ax), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x),x, algorithm="fricas")

[Out] integral((b*x)^m*arcsin(a*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \text{asin}(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m*asin(a*x),x)

[Out] Integral((b*x)**m*asin(a*x), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x),x, algorithm="giac")
```

```
[Out] integrate((b*x)^m*arcsin(a*x), x)
```

$$3.123 \quad \int \frac{(bx)^m}{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{(bx)^m}{\sin^{-1}(ax)}, x\right)$$

[Out] Unintegrable[(b*x)^m/ArcSin[a*x], x]

Rubi [A] time = 0.0165568, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(bx)^m}{\sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m/ArcSin[a*x], x]

[Out] Defer[Int] [(b*x)^m/ArcSin[a*x], x]

Rubi steps

$$\int \frac{(bx)^m}{\sin^{-1}(ax)} dx = \int \frac{(bx)^m}{\sin^{-1}(ax)} dx$$

Mathematica [A] time = 0.561421, size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m/ArcSin[a*x], x]

[Out] Integrate[(b*x)^m/ArcSin[a*x], x]

Maple [A] time = 0.434, size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m/arcsin(a*x), x)

[Out] int((b*x)^m/arcsin(a*x), x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x),x, algorithm="maxima")

[Out] integrate((b*x)^m/arcsin(a*x), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{(bx)^m}{\arcsin(ax)}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x),x, algorithm="fricas")

[Out] integral((b*x)^m/arcsin(a*x), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\text{asin}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m/asin(a*x),x)

[Out] Integral((b*x)**m/asin(a*x), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x),x, algorithm="giac")

[Out] integrate((b*x)^m/arcsin(a*x), x)

$$3.124 \quad \int \frac{(bx)^m}{\sin^{-1}(ax)^2} dx$$

Optimal. Leaf size=14

$$\text{Unintegrable}\left(\frac{(bx)^m}{\sin^{-1}(ax)^2}, x\right)$$

[Out] Unintegrable[(b*x)^m/ArcSin[a*x]^2, x]

Rubi [A] time = 0.0153909, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(bx)^m}{\sin^{-1}(ax)^2} dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m/ArcSin[a*x]^2, x]

[Out] Defer[Int] [(b*x)^m/ArcSin[a*x]^2, x]

Rubi steps

$$\int \frac{(bx)^m}{\sin^{-1}(ax)^2} dx = \int \frac{(bx)^m}{\sin^{-1}(ax)^2} dx$$

Mathematica [A] time = 0.575555, size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\sin^{-1}(ax)^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m/ArcSin[a*x]^2, x]

[Out] Integrate[(b*x)^m/ArcSin[a*x]^2, x]

Maple [A] time = 0.434, size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{(\arcsin(ax))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m/arcsin(a*x)^2, x)

[Out] int((b*x)^m/arcsin(a*x)^2, x)

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x)^2,x, algorithm="maxima")

[Out] Timed out

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{(bx)^m}{\arcsin(ax)^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x)^2,x, algorithm="fricas")

[Out] integral((b*x)^m/arcsin(a*x)^2, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\arcsin^2(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m/asin(a*x)**2,x)

[Out] Integral((b*x)**m/asin(a*x)**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\arcsin(ax)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x)^2,x, algorithm="giac")

[Out] integrate((b*x)^m/arcsin(a*x)^2, x)

3.125 $\int (bx)^m \sin^{-1}(ax)^{3/2} dx$

Optimal. Leaf size=16

Unintegrable $(\sin^{-1}(ax)^{3/2}(bx)^m, x)$

[Out] Unintegrable[(b*x)^m*ArcSin[a*x]^(3/2), x]

Rubi [A] time = 0.016084, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int (bx)^m \sin^{-1}(ax)^{3/2} dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m*ArcSin[a*x]^(3/2), x]

[Out] Defer[Int] [(b*x)^m*ArcSin[a*x]^(3/2), x]

Rubi steps

$$\int (bx)^m \sin^{-1}(ax)^{3/2} dx = \int (bx)^m \sin^{-1}(ax)^{3/2} dx$$

Mathematica [A] time = 2.62588, size = 0, normalized size = 0.

$$\int (bx)^m \sin^{-1}(ax)^{3/2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m*ArcSin[a*x]^(3/2), x]

[Out] Integrate[(b*x)^m*ArcSin[a*x]^(3/2), x]

Maple [A] time = 0.07, size = 0, normalized size = 0.

$$\int (bx)^m (\arcsin(ax))^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*arcsin(a*x)^(3/2), x)

[Out] int((b*x)^m*arcsin(a*x)^(3/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x)^(3/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x)^(3/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)**m*asin(a*x)**(3/2),x)
```

```
[Out] Timed out
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin(ax)^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x)^(3/2),x, algorithm="giac")
```

```
[Out] integrate((b*x)^m*arcsin(a*x)^(3/2), x)
```

$$3.126 \quad \int (bx)^m \sqrt{\sin^{-1}(ax)} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable}\left(\sqrt{\sin^{-1}(ax)(bx)^m}, x\right)$$

[Out] Unintegrable[(b*x)^m*Sqrt[ArcSin[a*x]], x]

Rubi [A] time = 0.0152887, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int (bx)^m \sqrt{\sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m*Sqrt[ArcSin[a*x]], x]

[Out] Defer[Int] [(b*x)^m*Sqrt[ArcSin[a*x]], x]

Rubi steps

$$\int (bx)^m \sqrt{\sin^{-1}(ax)} dx = \int (bx)^m \sqrt{\sin^{-1}(ax)} dx$$

Mathematica [A] time = 2.9291, size = 0, normalized size = 0.

$$\int (bx)^m \sqrt{\sin^{-1}(ax)} dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m*Sqrt[ArcSin[a*x]], x]

[Out] Integrate[(b*x)^m*Sqrt[ArcSin[a*x]], x]

Maple [A] time = 0.062, size = 0, normalized size = 0.

$$\int (bx)^m \sqrt{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*arcsin(a*x)^(1/2), x)

[Out] int((b*x)^m*arcsin(a*x)^(1/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^(1/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \sqrt{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m*asin(a*x)**(1/2),x)

[Out] Integral((b*x)**m*sqrt(asin(a*x)), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \sqrt{\arcsin(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m*arcsin(a*x)^(1/2),x, algorithm="giac")

[Out] integrate((b*x)^m*sqrt(arcsin(a*x)), x)

$$3.127 \quad \int \frac{(bx)^m}{\sqrt{\sin^{-1}(ax)}} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable} \left(\frac{(bx)^m}{\sqrt{\sin^{-1}(ax)}}, x \right)$$

[Out] Unintegrable[(b*x)^m/Sqrt[ArcSin[a*x]], x]

Rubi [A] time = 0.0153915, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(bx)^m}{\sqrt{\sin^{-1}(ax)}} dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m/Sqrt[ArcSin[a*x]], x]

[Out] Defer[Int] [(b*x)^m/Sqrt[ArcSin[a*x]], x]

Rubi steps

$$\int \frac{(bx)^m}{\sqrt{\sin^{-1}(ax)}} dx = \int \frac{(bx)^m}{\sqrt{\sin^{-1}(ax)}} dx$$

Mathematica [A] time = 2.20408, size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\sqrt{\sin^{-1}(ax)}} dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m/Sqrt[ArcSin[a*x]], x]

[Out] Integrate[(b*x)^m/Sqrt[ArcSin[a*x]], x]

Maple [A] time = 0.066, size = 0, normalized size = 0.

$$\int (bx)^m \frac{1}{\sqrt{\arcsin(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m/arcsin(a*x)^(1/2), x)

```
[Out] int((b*x)^m/arcsin(a*x)^(1/2),x)
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m/arcsin(a*x)^(1/2),x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m/arcsin(a*x)^(1/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\sqrt{\operatorname{asin}(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)**m/asin(a*x)**(1/2),x)
```

```
[Out] Integral((b*x)**m/sqrt(asin(a*x)), x)
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\sqrt{\operatorname{arcsin}(ax)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m/arcsin(a*x)^(1/2),x, algorithm="giac")
```

```
[Out] integrate((b*x)^m/sqrt(arcsin(a*x)), x)
```

$$3.128 \quad \int \frac{(bx)^m}{\sin^{-1}(ax)^{3/2}} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable}\left(\frac{(bx)^m}{\sin^{-1}(ax)^{3/2}}, x\right)$$

[Out] Unintegrable[(b*x)^m/ArcSin[a*x]^(3/2), x]

Rubi [A] time = 0.0151034, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(bx)^m}{\sin^{-1}(ax)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m/ArcSin[a*x]^(3/2), x]

[Out] Defer[Int] [(b*x)^m/ArcSin[a*x]^(3/2), x]

Rubi steps

$$\int \frac{(bx)^m}{\sin^{-1}(ax)^{3/2}} dx = \int \frac{(bx)^m}{\sin^{-1}(ax)^{3/2}} dx$$

Mathematica [A] time = 2.19188, size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\sin^{-1}(ax)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m/ArcSin[a*x]^(3/2), x]

[Out] Integrate[(b*x)^m/ArcSin[a*x]^(3/2), x]

Maple [A] time = 0.059, size = 0, normalized size = 0.

$$\int (bx)^m (\arcsin(ax))^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m/arcsin(a*x)^(3/2), x)

[Out] int((b*x)^m/arcsin(a*x)^(3/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x)^(3/2),x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x)^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\operatorname{asin}^{\frac{3}{2}}(ax)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)**m/asin(a*x)**(3/2),x)

[Out] Integral((b*x)**m/asin(a*x)**(3/2), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(bx)^m}{\operatorname{arcsin}(ax)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((b*x)^m/arcsin(a*x)^(3/2),x, algorithm="giac")

[Out] integrate((b*x)^m/arcsin(a*x)^(3/2), x)

3.129 $\int (bx)^m \sin^{-1}(ax)^n dx$

Optimal. Leaf size=14

Unintegrable $((bx)^m \sin^{-1}(ax)^n, x)$

[Out] Unintegrable[(b*x)^m*ArcSin[a*x]^n, x]

Rubi [A] time = 0.0156084, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int (bx)^m \sin^{-1}(ax)^n dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^m*ArcSin[a*x]^n, x]

[Out] Defer[Int] [(b*x)^m*ArcSin[a*x]^n, x]

Rubi steps

$$\int (bx)^m \sin^{-1}(ax)^n dx = \int (bx)^m \sin^{-1}(ax)^n dx$$

Mathematica [A] time = 0.797716, size = 0, normalized size = 0.

$$\int (bx)^m \sin^{-1}(ax)^n dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^m*ArcSin[a*x]^n, x]

[Out] Integrate[(b*x)^m*ArcSin[a*x]^n, x]

Maple [A] time = 0.758, size = 0, normalized size = 0.

$$\int (bx)^m (\arcsin(ax))^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^m*arcsin(a*x)^n, x)

[Out] int((b*x)^m*arcsin(a*x)^n, x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x)^n,x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}((bx)^m \arcsin(ax)^n, x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x)^n,x, algorithm="fricas")
```

```
[Out] integral((b*x)^m*arcsin(a*x)^n, x)
```

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin^n(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)**m*asin(a*x)**n,x)
```

```
[Out] Integral((b*x)**m*asin(a*x)**n, x)
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^m \arcsin(ax)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^m*arcsin(a*x)^n,x, algorithm="giac")
```

```
[Out] integrate((b*x)^m*arcsin(a*x)^n, x)
```

3.130 $\int x^3 \sin^{-1}(ax)^n dx$

Optimal. Leaf size=167

$$\frac{2^{-n-4} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -2i \sin^{-1}(ax))}{a^4} + \frac{2^{-2(n+3)} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, 2i \sin^{-1}(ax))}{a^4}$$

```
[Out] -((2^(-4 - n)*ArcSin[a*x]^n*Gamma[1 + n, (-2*I)*ArcSin[a*x]])/(a^4*((-I)*ArcSin[a*x])^n)) - (2^(-4 - n)*ArcSin[a*x]^n*Gamma[1 + n, (2*I)*ArcSin[a*x]])/(a^4*(I*ArcSin[a*x])^n) + (ArcSin[a*x]^n*Gamma[1 + n, (-4*I)*ArcSin[a*x]])/(2^(2*(3 + n))*a^4*((-I)*ArcSin[a*x])^n) + (ArcSin[a*x]^n*Gamma[1 + n, (4*I)*ArcSin[a*x]])/(2^(2*(3 + n))*a^4*(I*ArcSin[a*x])^n)
```

Rubi [A] time = 0.176853, antiderivative size = 167, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4635, 4406, 3308, 2181}

$$\frac{2^{-n-4} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -2i \sin^{-1}(ax))}{a^4} + \frac{2^{-2(n+3)} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, 2i \sin^{-1}(ax))}{a^4}$$

Antiderivative was successfully verified.

```
[In] Int[x^3*ArcSin[a*x]^n,x]
```

```
[Out] -((2^(-4 - n)*ArcSin[a*x]^n*Gamma[1 + n, (-2*I)*ArcSin[a*x]])/(a^4*((-I)*ArcSin[a*x])^n)) - (2^(-4 - n)*ArcSin[a*x]^n*Gamma[1 + n, (2*I)*ArcSin[a*x]])/(a^4*(I*ArcSin[a*x])^n) + (ArcSin[a*x]^n*Gamma[1 + n, (-4*I)*ArcSin[a*x]])/(2^(2*(3 + n))*a^4*((-I)*ArcSin[a*x])^n) + (ArcSin[a*x]^n*Gamma[1 + n, (4*I)*ArcSin[a*x]])/(2^(2*(3 + n))*a^4*(I*ArcSin[a*x])^n)
```

Rule 4635

```
Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^n_*(x_)^m_., x_Symbol] :> Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_.)]^(p_.)*((c_.) + (d_.)*(x_.))^m_*Sin[(a_.) + (b_.)*(x_.)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3308

```
Int[((c_.) + (d_.)*(x_.))^m_*sin[(e_.) + (f_.)*(x_.)], x_Symbol] :> Dist[I/2, Int[(c + d*x)^m/E^(I*(e + f*x)), x], x] - Dist[I/2, Int[(c + d*x)^m*E^(I*(e + f*x)), x], x] /; FreeQ[{c, d, e, f, m}, x]
```

Rule 2181

```
Int[(F_)^((g_.)*((e_.) + (f_.)*(x_.)))*((c_.) + (d_.)*(x_.))^m_., x_Symbol] :> -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, (-((f*g*Log[F])/d))*(c + d*x])]/(d*(-((f*g*Log[F])/d))^(IntPart[m] + 1)*(-((f*g*Log[F])*(c + d*x))/d))^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !IntegerQ[m]
```


Rubi steps

$$\begin{aligned}
\int x^3 \sin^{-1}(ax)^n dx &= \frac{\text{Subst}\left(\int x^n \cos(x) \sin^3(x) dx, x, \sin^{-1}(ax)\right)}{a^4} \\
&= \frac{\text{Subst}\left(\int \left(\frac{1}{4}x^n \sin(2x) - \frac{1}{8}x^n \sin(4x)\right) dx, x, \sin^{-1}(ax)\right)}{a^4} \\
&= -\frac{\text{Subst}\left(\int x^n \sin(4x) dx, x, \sin^{-1}(ax)\right)}{8a^4} + \frac{\text{Subst}\left(\int x^n \sin(2x) dx, x, \sin^{-1}(ax)\right)}{4a^4} \\
&= -\frac{i \text{Subst}\left(\int e^{-4ix} x^n dx, x, \sin^{-1}(ax)\right)}{16a^4} + \frac{i \text{Subst}\left(\int e^{4ix} x^n dx, x, \sin^{-1}(ax)\right)}{16a^4} + \frac{i \text{Subst}\left(\int e^{-2ix} x^n dx, x, \sin^{-1}(ax)\right)}{8a^4} \\
&= -\frac{2^{-4-n} (-i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(1+n, -2i \sin^{-1}(ax))}{a^4} - \frac{2^{-4-n} (i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(1+n, 2i \sin^{-1}(ax))}{a^4}
\end{aligned}$$

Mathematica [A] time = 0.0876354, size = 132, normalized size = 0.79

$$\frac{4^{-n-3} \sin^{-1}(ax)^n (\sin^{-1}(ax)^2)^{-n} \left(-2^{n+2} (-i \sin^{-1}(ax))^n \text{Gamma}(n+1, 2i \sin^{-1}(ax)) + (-i \sin^{-1}(ax))^n \text{Gamma}(n+1, -2i \sin^{-1}(ax)) \right)}{a^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*ArcSin[a*x]^n,x]

[Out] (4^(-3 - n)*ArcSin[a*x]^n*(-(2^(2 + n)*(I*ArcSin[a*x])^n*Gamma[1 + n, (-2*I)*ArcSin[a*x]]) - 2^(2 + n)*((-I)*ArcSin[a*x])^n*Gamma[1 + n, (2*I)*ArcSin[a*x]]) + (I*ArcSin[a*x])^n*Gamma[1 + n, (-4*I)*ArcSin[a*x]] + ((-I)*ArcSin[a*x])^n*Gamma[1 + n, (4*I)*ArcSin[a*x]])/(a^4*(ArcSin[a*x]^2)^n)

Maple [F] time = 0.144, size = 0, normalized size = 0.

$$\int x^3 (\arcsin(ax))^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*arcsin(a*x)^n,x)

[Out] int(x^3*arcsin(a*x)^n,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^n,x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \arcsin(ax)^n, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^n,x, algorithm="fricas")

[Out] integral(x^3*arcsin(a*x)^n, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \arcsin^n(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*asin(a*x)**n,x)

[Out] Integral(x**3*asin(a*x)**n, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \arcsin(ax)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*arcsin(a*x)^n,x, algorithm="giac")

[Out] integrate(x^3*arcsin(a*x)^n, x)

3.131 $\int x^2 \sin^{-1}(ax)^n dx$

Optimal. Leaf size=171

$$\frac{i \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -i \sin^{-1}(ax))}{8a^3} + \frac{i 3^{-n-1} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -3i \sin^{-1}(ax))}{8a^3}$$

```
[Out] ((-I/8)*ArcSin[a*x]^n*Gamma[1 + n, (-I)*ArcSin[a*x]]/(a^3*((-I)*ArcSin[a*x])^n) + ((I/8)*ArcSin[a*x]^n*Gamma[1 + n, I*ArcSin[a*x]]/(a^3*(I*ArcSin[a*x])^n) + ((I/8)*3^(-1 - n)*ArcSin[a*x]^n*Gamma[1 + n, (-3*I)*ArcSin[a*x]]/(a^3*((-I)*ArcSin[a*x])^n) - ((I/8)*3^(-1 - n)*ArcSin[a*x]^n*Gamma[1 + n, (3*I)*ArcSin[a*x]]/(a^3*(I*ArcSin[a*x])^n)
```

Rubi [A] time = 0.166141, antiderivative size = 171, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4635, 4406, 3307, 2181}

$$\frac{i \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -i \sin^{-1}(ax))}{8a^3} + \frac{i 3^{-n-1} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -3i \sin^{-1}(ax))}{8a^3}$$

Antiderivative was successfully verified.

```
[In] Int[x^2*ArcSin[a*x]^n,x]
```

```
[Out] ((-I/8)*ArcSin[a*x]^n*Gamma[1 + n, (-I)*ArcSin[a*x]]/(a^3*((-I)*ArcSin[a*x])^n) + ((I/8)*ArcSin[a*x]^n*Gamma[1 + n, I*ArcSin[a*x]]/(a^3*(I*ArcSin[a*x])^n) + ((I/8)*3^(-1 - n)*ArcSin[a*x]^n*Gamma[1 + n, (-3*I)*ArcSin[a*x]]/(a^3*((-I)*ArcSin[a*x])^n) - ((I/8)*3^(-1 - n)*ArcSin[a*x]^n*Gamma[1 + n, (3*I)*ArcSin[a*x]]/(a^3*(I*ArcSin[a*x])^n)
```

Rule 4635

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*SIN[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3307

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + Pi*(k_.) + (f_.)*(x_)], x_Symbol] := Dist[I/2, Int[(c + d*x)^m/(E^(I*k*Pi)*E^(I*(e + f*x))), x], x] - Dist[I/2, Int[(c + d*x)^m*E^(I*k*Pi)*E^(I*(e + f*x)), x], x] /; FreeQ[{c, d, e, f, m}, x] && IntegerQ[2*k]
```

Rule 2181

```
Int[(F_)^((g_.)*((e_.) + (f_.)*(x_)))*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, (-((f*g*Log[F])/d))*(c + d*x])]/(d*(-((f*g*Log[F])/d))^(IntPart[m] + 1)*(-((f*g*Log[F])/d))^(FracPart[m])), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !I
```

ntegerQ [m]

Rubi steps

$$\begin{aligned}
 \int x^2 \sin^{-1}(ax)^n dx &= \frac{\text{Subst}\left(\int x^n \cos(x) \sin^2(x) dx, x, \sin^{-1}(ax)\right)}{a^3} \\
 &= \frac{\text{Subst}\left(\int \left(\frac{1}{4}x^n \cos(x) - \frac{1}{4}x^n \cos(3x)\right) dx, x, \sin^{-1}(ax)\right)}{a^3} \\
 &= \frac{\text{Subst}\left(\int x^n \cos(x) dx, x, \sin^{-1}(ax)\right)}{4a^3} - \frac{\text{Subst}\left(\int x^n \cos(3x) dx, x, \sin^{-1}(ax)\right)}{4a^3} \\
 &= \frac{\text{Subst}\left(\int e^{-ix} x^n dx, x, \sin^{-1}(ax)\right)}{8a^3} + \frac{\text{Subst}\left(\int e^{ix} x^n dx, x, \sin^{-1}(ax)\right)}{8a^3} - \frac{\text{Subst}\left(\int e^{-3ix} x^n dx, x, \sin^{-1}(ax)\right)}{8a^3} \\
 &= -\frac{i\left(-i \sin^{-1}(ax)\right)^{-n} \sin^{-1}(ax)^n \Gamma(1+n, -i \sin^{-1}(ax))}{8a^3} + \frac{i\left(i \sin^{-1}(ax)\right)^{-n} \sin^{-1}(ax)^n \Gamma(1+n, i \sin^{-1}(ax))}{8a^3}
 \end{aligned}$$

Mathematica [A] time = 0.0723912, size = 137, normalized size = 0.8

$$\frac{i3^{-n-1} \sin^{-1}(ax)^n (\sin^{-1}(ax)^2)^{-n} \left(3^{n+1} (-i \sin^{-1}(ax))^n \text{Gamma}(n+1, i \sin^{-1}(ax)) - (-i \sin^{-1}(ax))^n \text{Gamma}(n+1, 3i \sin^{-1}(ax))\right)}{8a^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*ArcSin[a*x]^n,x]

[Out] ((I/8)*3^(-1 - n)*ArcSin[a*x]^n*(-(3^(1 + n)*(I*ArcSin[a*x])^n*Gamma[1 + n, (-I)*ArcSin[a*x]]) + 3^(1 + n)*((-I)*ArcSin[a*x])^n*Gamma[1 + n, I*ArcSin[a*x]]) + (I*ArcSin[a*x])^n*Gamma[1 + n, (-3*I)*ArcSin[a*x]] - ((-I)*ArcSin[a*x])^n*Gamma[1 + n, (3*I)*ArcSin[a*x]]))/(a^3*(ArcSin[a*x]^2)^n)

Maple [F] time = 0.154, size = 0, normalized size = 0.

$$\int x^2 (\arcsin(ax))^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*arcsin(a*x)^n,x)

[Out] int(x^2*arcsin(a*x)^n,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^n,x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \arcsin(ax)^n, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^n,x, algorithm="fricas")

[Out] integral(x^2*arcsin(a*x)^n, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \arcsin^n(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*asin(a*x)**n,x)

[Out] Integral(x**2*asin(a*x)**n, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \arcsin(ax)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*arcsin(a*x)^n,x, algorithm="giac")

[Out] integrate(x^2*arcsin(a*x)^n, x)

3.132 $\int x \sin^{-1}(ax)^n dx$

Optimal. Leaf size=85

$$\frac{2^{-n-3} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -2i \sin^{-1}(ax))}{a^2} - \frac{2^{-n-3} (i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(n+1, 2i \sin^{-1}(ax))}{a^2}$$

[Out] -((2^(-3 - n)*ArcSin[a*x]^n*Gamma[1 + n, (-2*I)*ArcSin[a*x]])/(a^2*((-I)*ArcSin[a*x])^n)) - (2^(-3 - n)*ArcSin[a*x]^n*Gamma[1 + n, (2*I)*ArcSin[a*x]])/(a^2*(I*ArcSin[a*x])^n)

Rubi [A] time = 0.0819761, antiderivative size = 85, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4635, 4406, 12, 3308, 2181}

$$\frac{2^{-n-3} \sin^{-1}(ax)^n (-i \sin^{-1}(ax))^{-n} \Gamma(n+1, -2i \sin^{-1}(ax))}{a^2} - \frac{2^{-n-3} (i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(n+1, 2i \sin^{-1}(ax))}{a^2}$$

Antiderivative was successfully verified.

[In] Int[x*ArcSin[a*x]^n,x]

[Out] -((2^(-3 - n)*ArcSin[a*x]^n*Gamma[1 + n, (-2*I)*ArcSin[a*x]])/(a^2*((-I)*ArcSin[a*x])^n)) - (2^(-3 - n)*ArcSin[a*x]^n*Gamma[1 + n, (2*I)*ArcSin[a*x]])/(a^2*(I*ArcSin[a*x])^n)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n*(x_)^m, x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3308

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := Dist[I/2, Int[(c + d*x)^m/E^(I*(e + f*x)), x], x] - Dist[I/2, Int[(c + d*x)^m*E^(I*(e + f*x)), x], x] /; FreeQ[{c, d, e, f, m}, x]

Rule 2181

Int[(F_)^((g_.)*((e_.) + (f_.)*(x_)))*((c_.) + (d_.)*(x_))^(m_), x_Symbol] := -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, (-((f*g*Log[F])/d))*(c + d*x])]/(d*(-((f*g*Log[F])/d))^(IntPart[m] + 1)*(-((f*g*Log[F])*(c + d*x)/d))^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !I

ntegerQ[m]

Rubi steps

$$\begin{aligned} \int x \sin^{-1}(ax)^n dx &= \frac{\text{Subst}\left(\int x^n \cos(x) \sin(x) dx, x, \sin^{-1}(ax)\right)}{a^2} \\ &= \frac{\text{Subst}\left(\int \frac{1}{2}x^n \sin(2x) dx, x, \sin^{-1}(ax)\right)}{a^2} \\ &= \frac{\text{Subst}\left(\int x^n \sin(2x) dx, x, \sin^{-1}(ax)\right)}{2a^2} \\ &= \frac{i \text{Subst}\left(\int e^{-2ix} x^n dx, x, \sin^{-1}(ax)\right)}{4a^2} - \frac{i \text{Subst}\left(\int e^{2ix} x^n dx, x, \sin^{-1}(ax)\right)}{4a^2} \\ &= -\frac{2^{-3-n} (-i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(1+n, -2i \sin^{-1}(ax))}{a^2} - \frac{2^{-3-n} (i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(1+n, 2i \sin^{-1}(ax))}{a^2} \end{aligned}$$

Mathematica [A] time = 0.019394, size = 75, normalized size = 0.88

$$\frac{2^{-n-3} \sin^{-1}(ax)^n (\sin^{-1}(ax)^2)^{-n} \left((-i \sin^{-1}(ax))^n \text{Gamma}(n+1, 2i \sin^{-1}(ax)) + (i \sin^{-1}(ax))^n \text{Gamma}(n+1, -2i \sin^{-1}(ax)) \right)}{a^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*ArcSin[a*x]^n,x]

[Out] -((2^(-3 - n)*ArcSin[a*x]^n*((I*ArcSin[a*x])^n*Gamma[1 + n, (-2*I)*ArcSin[a*x]]) + ((-I)*ArcSin[a*x])^n*Gamma[1 + n, (2*I)*ArcSin[a*x]]))/(a^2*(ArcSin[a*x]^2)^n)

Maple [C] time = 0.117, size = 138, normalized size = 1.6

$$\frac{\sqrt{\pi}}{4a^2} \left(2 \frac{(\arcsin(ax))^{1+n} \sin(2 \arcsin(ax))}{\sqrt{\pi}(2+n)} - \frac{\sin(2 \arcsin(ax))}{\sqrt{\pi}(2+n)} 2^{\frac{1}{2}-n} \sqrt{\arcsin(ax)} \text{LommelS1}\left(n + \frac{3}{2}, \frac{3}{2}, 2 \arcsin(ax)\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*arcsin(a*x)^n,x)

[Out] 1/4*Pi^(1/2)/a^2*(2/Pi^(1/2)/(2+n)*arcsin(a*x)^(1+n)*sin(2*arcsin(a*x))-2^(1/2-n)/Pi^(1/2)/(2+n)*arcsin(a*x)^(1/2)*LommelS1(n+3/2,3/2,2*arcsin(a*x))*sin(2*arcsin(a*x))-3*2^(-3/2-n)/Pi^(1/2)/(2+n)/arcsin(a*x)^(1/2)*(4/3+2/3*n)*(2*arcsin(a*x)*cos(2*arcsin(a*x))-sin(2*arcsin(a*x)))*LommelS1(n+1/2,1/2,2*arcsin(a*x)))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*arcsin(a*x)^n,x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \arcsin(ax)^n, x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*arcsin(a*x)^n,x, algorithm="fricas")
```

```
[Out] integral(x*arcsin(a*x)^n, x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \arcsin^n(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*asin(a*x)**n,x)
```

```
[Out] Integral(x*asin(a*x)**n, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x \arcsin(ax)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*arcsin(a*x)^n,x, algorithm="giac")
```

```
[Out] integrate(x*arcsin(a*x)^n, x)
```


3.133 $\int \sin^{-1}(ax)^n dx$

Optimal. Leaf size=79

$$\frac{i(i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(n+1, i \sin^{-1}(ax))}{2a} - \frac{i(-i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(n+1, -i \sin^{-1}(ax))}{2a}$$

[Out] $((-I/2)*\text{ArcSin}[a*x]^n*\text{Gamma}[1+n, (-I)*\text{ArcSin}[a*x]])/(a*(-I)*\text{ArcSin}[a*x])^n + ((I/2)*\text{ArcSin}[a*x]^n*\text{Gamma}[1+n, I*\text{ArcSin}[a*x]])/(a*(I*\text{ArcSin}[a*x])^n)$

Rubi [A] time = 0.0546235, antiderivative size = 79, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4623, 3307, 2181}

$$\frac{i(i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(n+1, i \sin^{-1}(ax))}{2a} - \frac{i(-i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(n+1, -i \sin^{-1}(ax))}{2a}$$

Antiderivative was successfully verified.

[In] Int[ArcSin[a*x]^n, x]

[Out] $((-I/2)*\text{ArcSin}[a*x]^n*\text{Gamma}[1+n, (-I)*\text{ArcSin}[a*x]])/(a*(-I)*\text{ArcSin}[a*x])^n + ((I/2)*\text{ArcSin}[a*x]^n*\text{Gamma}[1+n, I*\text{ArcSin}[a*x]])/(a*(I*\text{ArcSin}[a*x])^n)$

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_), x_Symbol] :> Dist[1/(b*c), Subst[Int[x^n*cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3307

Int[((c_.) + (d_.)*(x_.))^(m_.)*sin[(e_.) + Pi*(k_.) + (f_.)*(x_.)], x_Symbol] :> Dist[I/2, Int[(c + d*x)^m/(E^(I*k*Pi)*E^(I*(e + f*x))), x], x] - Dist[I/2, Int[(c + d*x)^m*E^(I*k*Pi)*E^(I*(e + f*x)), x], x] /; FreeQ[{c, d, e, f, m}, x] && IntegerQ[2*k]

Rule 2181

Int[(F_)^((g_.)*((e_.) + (f_.)*(x_.)))*((c_.) + (d_.)*(x_.))^(m_), x_Symbol] :> -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, (-((f*g*Log[F])/d))*(c + d*x])]/(d*(-((f*g*Log[F])/d))^(IntPart[m] + 1)*(-((f*g*Log[F])*(c + d*x)/d))^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \sin^{-1}(ax)^n dx &= \frac{\text{Subst}\left(\int x^n \cos(x) dx, x, \sin^{-1}(ax)\right)}{a} \\ &= \frac{\text{Subst}\left(\int e^{-ix} x^n dx, x, \sin^{-1}(ax)\right)}{2a} + \frac{\text{Subst}\left(\int e^{ix} x^n dx, x, \sin^{-1}(ax)\right)}{2a} \\ &= -\frac{i(-i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(1+n, -i \sin^{-1}(ax))}{2a} + \frac{i(i \sin^{-1}(ax))^{-n} \sin^{-1}(ax)^n \Gamma(1+n, i \sin^{-1}(ax))}{2a} \end{aligned}$$

Mathematica [A] time = 0.035468, size = 73, normalized size = 0.92

$$\frac{i \sin^{-1}(ax)^n (\sin^{-1}(ax)^2)^{-n} \left((-i \sin^{-1}(ax))^n \Gamma(n+1, i \sin^{-1}(ax)) - (i \sin^{-1}(ax))^n \Gamma(n+1, -i \sin^{-1}(ax)) \right)}{2a}$$

Antiderivative was successfully verified.

[In] Integrate[ArcSin[a*x]^n,x]

[Out] $((I/2)*ArcSin[a*x]^n*(-((I*ArcSin[a*x])^n*Gamma[1+n,(-I)*ArcSin[a*x]])+((-I)*ArcSin[a*x])^n*Gamma[1+n,I*ArcSin[a*x]]))/(a*(ArcSin[a*x]^2)^n)$

Maple [C] time = 0.082, size = 240, normalized size = 3.

$$\frac{2^n \sqrt{\pi}}{a} \left(\frac{2^{-1-n} (\arcsin(ax))^n (6+2n) ax}{\sqrt{\pi} (1+n) (3+n)} + \frac{(\arcsin(ax))^n 2^{-n}}{\sqrt{\pi} (1+n) (a^2 x^2 - 1)} \sqrt{-a^2 x^2 + 1} (a^2 x^2 \arcsin(ax) - \arcsin(ax) + ax \sqrt{-a^2 x^2 + 1}) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^n,x)

[Out] $2^n \pi^{1/2} / a * (2^{(-1-n)} / \pi^{1/2} / (1+n) * \arcsin(a*x)^n * (6+2*n) / (3+n) * a*x + 1 / \pi^{1/2} / (1+n) * \arcsin(a*x)^n * 2^{(-n)} * (-a^2*x^2+1)^{1/2} / (a^2*x^2-1) * (a^2*x^2*\arcsin(a*x) - \arcsin(a*x) + a*x*(-a^2*x^2+1)^{1/2})) + 2^{(-n)} / \pi^{1/2} / (1+n) * \arcsin(a*x)^{1/2} * n * \text{LommelS1}(n+1/2, 3/2, \arcsin(a*x)) * a*x - 2^{(-n)} / \pi^{1/2} / (1+n) / \arcsin(a*x)^{1/2} * (-a^2*x^2+1)^{1/2} / (a^2*x^2-1) * (a^2*x^2*\arcsin(a*x) - \arcsin(a*x) + a*x*(-a^2*x^2+1)^{1/2})) * \text{LommelS1}(n+3/2, 1/2, \arcsin(a*x))$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n,x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\arcsin(ax)^n, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^n, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{asin}^n(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**n,x)

[Out] Integral(asin(a*x)**n, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{arcsin}(ax)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^n, x)

$$3.134 \quad \int \frac{\sin^{-1}(ax)^n}{x} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{\sin^{-1}(ax)^n}{x}, x\right)$$

[Out] Unintegrable[ArcSin[a*x]^n/x, x]

Rubi [A] time = 0.0147082, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin^{-1}(ax)^n}{x} dx$$

Verification is Not applicable to the result.

[In] Int[ArcSin[a*x]^n/x, x]

[Out] Defer[Int][ArcSin[a*x]^n/x, x]

Rubi steps

$$\int \frac{\sin^{-1}(ax)^n}{x} dx = \int \frac{\sin^{-1}(ax)^n}{x} dx$$

Mathematica [A] time = 0.278058, size = 0, normalized size = 0.

$$\int \frac{\sin^{-1}(ax)^n}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[ArcSin[a*x]^n/x, x]

[Out] Integrate[ArcSin[a*x]^n/x, x]

Maple [A] time = 0.102, size = 0, normalized size = 0.

$$\int \frac{(\arcsin(ax))^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^n/x, x)

[Out] int(arcsin(a*x)^n/x, x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/x,x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^n}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/x,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^n/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin^n(ax)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**n/x,x)

[Out] Integral(asin(a*x)**n/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^n}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/x,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^n/x, x)

$$3.135 \quad \int \frac{\sin^{-1}(ax)^n}{x^2} dx$$

Optimal. Leaf size=12

$$\text{Unintegrable}\left(\frac{\sin^{-1}(ax)^n}{x^2}, x\right)$$

[Out] Unintegrable[ArcSin[a*x]^n/x^2, x]

Rubi [A] time = 0.0159331, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin^{-1}(ax)^n}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[ArcSin[a*x]^n/x^2,x]

[Out] Defer[Int][ArcSin[a*x]^n/x^2, x]

Rubi steps

$$\int \frac{\sin^{-1}(ax)^n}{x^2} dx = \int \frac{\sin^{-1}(ax)^n}{x^2} dx$$

Mathematica [A] time = 0.525123, size = 0, normalized size = 0.

$$\int \frac{\sin^{-1}(ax)^n}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[ArcSin[a*x]^n/x^2,x]

[Out] Integrate[ArcSin[a*x]^n/x^2, x]

Maple [A] time = 0.072, size = 0, normalized size = 0.

$$\int \frac{(\arcsin(ax))^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^n/x^2,x)

[Out] int(arcsin(a*x)^n/x^2,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/x^2,x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\arcsin(ax)^n}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/x^2,x, algorithm="fricas")

[Out] integral(arcsin(a*x)^n/x^2, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin^n(ax)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**n/x**2,x)

[Out] Integral(asin(a*x)**n/x**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^n}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/x^2,x, algorithm="giac")

[Out] integrate(arcsin(a*x)^n/x^2, x)

3.136 $\int (bx)^{3/2} \sin^{-1}(ax)^n dx$

Optimal. Leaf size=16

Unintegrable $((bx)^{3/2} \sin^{-1}(ax)^n, x)$

[Out] Unintegrable[(b*x)^(3/2)*ArcSin[a*x]^n, x]

Rubi [A] time = 0.0214075, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int (bx)^{3/2} \sin^{-1}(ax)^n dx$$

Verification is Not applicable to the result.

[In] Int[(b*x)^(3/2)*ArcSin[a*x]^n, x]

[Out] Defer[Int] [(b*x)^(3/2)*ArcSin[a*x]^n, x]

Rubi steps

$$\int (bx)^{3/2} \sin^{-1}(ax)^n dx = \int (bx)^{3/2} \sin^{-1}(ax)^n dx$$

Mathematica [A] time = 3.57054, size = 0, normalized size = 0.

$$\int (bx)^{3/2} \sin^{-1}(ax)^n dx$$

Verification is Not applicable to the result.

[In] Integrate[(b*x)^(3/2)*ArcSin[a*x]^n, x]

[Out] Integrate[(b*x)^(3/2)*ArcSin[a*x]^n, x]

Maple [A] time = 0.089, size = 0, normalized size = 0.

$$\int (bx)^{\frac{3}{2}} (\arcsin(ax))^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^(3/2)*arcsin(a*x)^n, x)

[Out] int((b*x)^(3/2)*arcsin(a*x)^n, x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^(3/2)*arcsin(a*x)^n,x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\sqrt{bx}bx \arcsin(ax)^n, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^(3/2)*arcsin(a*x)^n,x, algorithm="fricas")
```

```
[Out] integral(sqrt(b*x)*b*x*arcsin(a*x)^n, x)
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)**(3/2)*asin(a*x)**n,x)
```

```
[Out] Timed out
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int (bx)^{\frac{3}{2}} \arcsin(ax)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^(3/2)*arcsin(a*x)^n,x, algorithm="giac")
```

```
[Out] integrate((b*x)^(3/2)*arcsin(a*x)^n, x)
```

3.137 $\int \sqrt{bx} \sin^{-1}(ax)^n dx$

Optimal. Leaf size=16

$$\text{Unintegrable}\left(\sqrt{bx} \sin^{-1}(ax)^n, x\right)$$

[Out] Unintegrable[Sqrt[b*x]*ArcSin[a*x]^n, x]

Rubi [A] time = 0.0174957, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \sqrt{bx} \sin^{-1}(ax)^n dx$$

Verification is Not applicable to the result.

[In] Int[Sqrt[b*x]*ArcSin[a*x]^n, x]

[Out] Defer[Int][Sqrt[b*x]*ArcSin[a*x]^n, x]

Rubi steps

$$\int \sqrt{bx} \sin^{-1}(ax)^n dx = \int \sqrt{bx} \sin^{-1}(ax)^n dx$$

Mathematica [A] time = 4.26913, size = 0, normalized size = 0.

$$\int \sqrt{bx} \sin^{-1}(ax)^n dx$$

Verification is Not applicable to the result.

[In] Integrate[Sqrt[b*x]*ArcSin[a*x]^n, x]

[Out] Integrate[Sqrt[b*x]*ArcSin[a*x]^n, x]

Maple [A] time = 0.07, size = 0, normalized size = 0.

$$\int \sqrt{bx} (\arcsin(ax))^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((b*x)^(1/2)*arcsin(a*x)^n, x)

[Out] int((b*x)^(1/2)*arcsin(a*x)^n, x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^(1/2)*arcsin(a*x)^n,x, algorithm="maxima")
```

```
[Out] Exception raised: RuntimeError
```

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\sqrt{bx} \arcsin(ax)^n, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^(1/2)*arcsin(a*x)^n,x, algorithm="fricas")
```

```
[Out] integral(sqrt(b*x)*arcsin(a*x)^n, x)
```

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{bx} \arcsin^n(ax) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)**(1/2)*asin(a*x)**n,x)
```

```
[Out] Integral(sqrt(b*x)*asin(a*x)**n, x)
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{bx} \arcsin(ax)^n dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((b*x)^(1/2)*arcsin(a*x)^n,x, algorithm="giac")
```

```
[Out] integrate(sqrt(b*x)*arcsin(a*x)^n, x)
```

$$3.138 \quad \int \frac{\sin^{-1}(ax)^n}{\sqrt{bx}} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable}\left(\frac{\sin^{-1}(ax)^n}{\sqrt{bx}}, x\right)$$

[Out] Unintegrable[ArcSin[a*x]^n/Sqrt[b*x], x]

Rubi [A] time = 0.0183719, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin^{-1}(ax)^n}{\sqrt{bx}} dx$$

Verification is Not applicable to the result.

[In] Int[ArcSin[a*x]^n/Sqrt[b*x], x]

[Out] Defer[Int][ArcSin[a*x]^n/Sqrt[b*x], x]

Rubi steps

$$\int \frac{\sin^{-1}(ax)^n}{\sqrt{bx}} dx = \int \frac{\sin^{-1}(ax)^n}{\sqrt{bx}} dx$$

Mathematica [A] time = 1.5516, size = 0, normalized size = 0.

$$\int \frac{\sin^{-1}(ax)^n}{\sqrt{bx}} dx$$

Verification is Not applicable to the result.

[In] Integrate[ArcSin[a*x]^n/Sqrt[b*x], x]

[Out] Integrate[ArcSin[a*x]^n/Sqrt[b*x], x]

Maple [A] time = 0.069, size = 0, normalized size = 0.

$$\int (\arcsin(ax))^n \frac{1}{\sqrt{bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^n/(b*x)^(1/2), x)

[Out] int(arcsin(a*x)^n/(b*x)^(1/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/(b*x)^(1/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{bx} \arcsin(ax)^n}{bx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/(b*x)^(1/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x)*arcsin(a*x)^n/(b*x), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin^n(ax)}{\sqrt{bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**n/(b*x)**(1/2), x)

[Out] Integral(asin(a*x)**n/sqrt(b*x), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^n}{\sqrt{bx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/(b*x)^(1/2), x, algorithm="giac")

[Out] integrate(arcsin(a*x)^n/sqrt(b*x), x)

$$3.139 \quad \int \frac{\sin^{-1}(ax)^n}{(bx)^{3/2}} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable} \left(\frac{\sin^{-1}(ax)^n}{(bx)^{3/2}}, x \right)$$

[Out] Unintegrable[ArcSin[a*x]^n/(b*x)^(3/2), x]

Rubi [A] time = 0.0207741, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin^{-1}(ax)^n}{(bx)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Int[ArcSin[a*x]^n/(b*x)^(3/2), x]

[Out] Defer[Int][ArcSin[a*x]^n/(b*x)^(3/2), x]

Rubi steps

$$\int \frac{\sin^{-1}(ax)^n}{(bx)^{3/2}} dx = \int \frac{\sin^{-1}(ax)^n}{(bx)^{3/2}} dx$$

Mathematica [A] time = 1.90002, size = 0, normalized size = 0.

$$\int \frac{\sin^{-1}(ax)^n}{(bx)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[ArcSin[a*x]^n/(b*x)^(3/2), x]

[Out] Integrate[ArcSin[a*x]^n/(b*x)^(3/2), x]

Maple [A] time = 0.069, size = 0, normalized size = 0.

$$\int (\arcsin(ax))^n (bx)^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(arcsin(a*x)^n/(b*x)^(3/2), x)

[Out] int(arcsin(a*x)^n/(b*x)^(3/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: RuntimeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/(b*x)^(3/2), x, algorithm="maxima")

[Out] Exception raised: RuntimeError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{bx} \arcsin(ax)^n}{b^2 x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/(b*x)^(3/2), x, algorithm="fricas")

[Out] integral(sqrt(b*x)*arcsin(a*x)^n/(b^2*x^2), x)

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(asin(a*x)**n/(b*x)**(3/2), x)

[Out] Timed out

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\arcsin(ax)^n}{(bx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(arcsin(a*x)^n/(b*x)^(3/2), x, algorithm="giac")

[Out] integrate(arcsin(a*x)^n/(b*x)^(3/2), x)

3.140 $\int x^3 (a + b \sin^{-1}(cx)) dx$

Optimal. Leaf size=76

$$\frac{1}{4}x^4(a + b \sin^{-1}(cx)) + \frac{bx^3\sqrt{1-c^2x^2}}{16c} + \frac{3bx\sqrt{1-c^2x^2}}{32c^3} - \frac{3b \sin^{-1}(cx)}{32c^4}$$

[Out] (3*b*x*Sqrt[1 - c^2*x^2])/(32*c^3) + (b*x^3*Sqrt[1 - c^2*x^2])/(16*c) - (3*b*ArcSin[c*x])/(32*c^4) + (x^4*(a + b*ArcSin[c*x]))/4

Rubi [A] time = 0.0345858, antiderivative size = 76, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4627, 321, 216}

$$\frac{1}{4}x^4(a + b \sin^{-1}(cx)) + \frac{bx^3\sqrt{1-c^2x^2}}{16c} + \frac{3bx\sqrt{1-c^2x^2}}{32c^3} - \frac{3b \sin^{-1}(cx)}{32c^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*(a + b*ArcSin[c*x]),x]

[Out] (3*b*x*Sqrt[1 - c^2*x^2])/(32*c^3) + (b*x^3*Sqrt[1 - c^2*x^2])/(16*c) - (3*b*ArcSin[c*x])/(32*c^4) + (x^4*(a + b*ArcSin[c*x]))/4

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^((n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 321

Int[((c_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_.))^(p_.), x_Symbol] :> Simp[(c^(n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), Int[(c*x)^(m - n)*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n - 1] && NeQ[m + n*p + 1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int x^3 (a + b \sin^{-1}(cx)) dx &= \frac{1}{4}x^4(a + b \sin^{-1}(cx)) - \frac{1}{4}(bc) \int \frac{x^4}{\sqrt{1-c^2x^2}} dx \\ &= \frac{bx^3\sqrt{1-c^2x^2}}{16c} + \frac{1}{4}x^4(a + b \sin^{-1}(cx)) - \frac{(3b) \int \frac{x^2}{\sqrt{1-c^2x^2}} dx}{16c} \\ &= \frac{3bx\sqrt{1-c^2x^2}}{32c^3} + \frac{bx^3\sqrt{1-c^2x^2}}{16c} + \frac{1}{4}x^4(a + b \sin^{-1}(cx)) - \frac{(3b) \int \frac{1}{\sqrt{1-c^2x^2}} dx}{32c^3} \\ &= \frac{3bx\sqrt{1-c^2x^2}}{32c^3} + \frac{bx^3\sqrt{1-c^2x^2}}{16c} - \frac{3b \sin^{-1}(cx)}{32c^4} + \frac{1}{4}x^4(a + b \sin^{-1}(cx)) \end{aligned}$$

Mathematica [A] time = 0.029848, size = 81, normalized size = 1.07

$$\frac{ax^4}{4} + \frac{bx^3\sqrt{1-c^2x^2}}{16c} + \frac{3bx\sqrt{1-c^2x^2}}{32c^3} - \frac{3b\sin^{-1}(cx)}{32c^4} + \frac{1}{4}bx^4\sin^{-1}(cx)$$

Antiderivative was successfully verified.

[In] Integrate[x^3*(a + b*ArcSin[c*x]),x]

[Out] (a*x^4)/4 + (3*b*x*Sqrt[1 - c^2*x^2])/(32*c^3) + (b*x^3*Sqrt[1 - c^2*x^2])/(16*c) - (3*b*ArcSin[c*x])/(32*c^4) + (b*x^4*ArcSin[c*x])/4

Maple [A] time = 0.005, size = 72, normalized size = 1.

$$\frac{1}{c^4} \left(\frac{c^4 x^4 a}{4} + b \left(\frac{c^4 x^4 \arcsin(cx)}{4} + \frac{c^3 x^3 \sqrt{-c^2 x^2 + 1}}{16} + \frac{3cx \sqrt{-c^2 x^2 + 1}}{32} - \frac{3 \arcsin(cx)}{32} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*(a+b*arcsin(c*x)),x)

[Out] 1/c^4*(1/4*c^4*x^4*a+b*(1/4*c^4*x^4*arcsin(c*x)+1/16*c^3*x^3*(-c^2*x^2+1)^(1/2)+3/32*c*x*(-c^2*x^2+1)^(1/2)-3/32*arcsin(c*x)))

Maxima [A] time = 1.59075, size = 111, normalized size = 1.46

$$\frac{1}{4}ax^4 + \frac{1}{32} \left(8x^4 \arcsin(cx) + \left(\frac{2\sqrt{-c^2x^2+1}x^3}{c^2} + \frac{3\sqrt{-c^2x^2+1}x}{c^4} - \frac{3\arcsin\left(\frac{c^2x}{\sqrt{c^2}}\right)}{\sqrt{c^2}c^4} \right) c \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] 1/4*a*x^4 + 1/32*(8*x^4*arcsin(c*x) + (2*sqrt(-c^2*x^2 + 1)*x^3/c^2 + 3*sqrt(-c^2*x^2 + 1)*x/c^4 - 3*arcsin(c^2*x/sqrt(c^2))/(sqrt(c^2)*c^4))*c)*b

Fricas [A] time = 1.43564, size = 139, normalized size = 1.83

$$\frac{8ac^4x^4 + (8bc^4x^4 - 3b)\arcsin(cx) + (2bc^3x^3 + 3bcx)\sqrt{-c^2x^2 + 1}}{32c^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] 1/32*(8*a*c^4*x^4 + (8*b*c^4*x^4 - 3*b)*arcsin(c*x) + (2*b*c^3*x^3 + 3*b*c*x)*sqrt(-c^2*x^2 + 1))/c^4

Sympy [A] time = 2.3713, size = 80, normalized size = 1.05

$$\begin{cases} \frac{ax^4}{4} + \frac{bx^4 \operatorname{asin}(cx)}{4} + \frac{bx^3 \sqrt{-c^2x^2+1}}{16c} + \frac{3bx \sqrt{-c^2x^2+1}}{32c^3} - \frac{3b \operatorname{asin}(cx)}{32c^4} & \text{for } c \neq 0 \\ \frac{ax^4}{4} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*(a+b*asin(c*x)),x)

[Out] Piecewise((a*x**4/4 + b*x**4*asin(c*x)/4 + b*x**3*sqrt(-c**2*x**2 + 1)/(16*c) + 3*b*x*sqrt(-c**2*x**2 + 1)/(32*c**3) - 3*b*asin(c*x)/(32*c**4), Ne(c, 0)), (a*x**4/4, True))

Giac [A] time = 1.37045, size = 163, normalized size = 2.14

$$-\frac{(-c^2x^2+1)^{\frac{3}{2}}bx}{16c^3} + \frac{(c^2x^2-1)^2b \operatorname{arcsin}(cx)}{4c^4} + \frac{5\sqrt{-c^2x^2+1}bx}{32c^3} + \frac{(c^2x^2-1)^2a}{4c^4} + \frac{(c^2x^2-1)b \operatorname{arcsin}(cx)}{2c^4} + \frac{(c^2x^2-1)a}{2c^4} +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] -1/16*(-c^2*x^2 + 1)^(3/2)*b*x/c^3 + 1/4*(c^2*x^2 - 1)^2*b*arcsin(c*x)/c^4 + 5/32*sqrt(-c^2*x^2 + 1)*b*x/c^3 + 1/4*(c^2*x^2 - 1)^2*a/c^4 + 1/2*(c^2*x^2 - 1)*b*arcsin(c*x)/c^4 + 1/2*(c^2*x^2 - 1)*a/c^4 + 5/32*b*arcsin(c*x)/c^4

3.141 $\int x^2 (a + b \sin^{-1}(cx)) dx$

Optimal. Leaf size=60

$$\frac{1}{3}x^3(a + b \sin^{-1}(cx)) - \frac{b(1 - c^2x^2)^{3/2}}{9c^3} + \frac{b\sqrt{1 - c^2x^2}}{3c^3}$$

[Out] (b*Sqrt[1 - c^2*x^2])/(3*c^3) - (b*(1 - c^2*x^2)^(3/2))/(9*c^3) + (x^3*(a + b*ArcSin[c*x]))/3

Rubi [A] time = 0.0391678, antiderivative size = 60, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4627, 266, 43}

$$\frac{1}{3}x^3(a + b \sin^{-1}(cx)) - \frac{b(1 - c^2x^2)^{3/2}}{9c^3} + \frac{b\sqrt{1 - c^2x^2}}{3c^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*ArcSin[c*x]),x]

[Out] (b*Sqrt[1 - c^2*x^2])/(3*c^3) - (b*(1 - c^2*x^2)^(3/2))/(9*c^3) + (x^3*(a + b*ArcSin[c*x]))/3

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 266

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]

Rule 43

Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_.), x_Symbol] :> Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0] || GtQ[m + n + 2, 0])

Rubi steps

$$\begin{aligned} \int x^2 (a + b \sin^{-1}(cx)) dx &= \frac{1}{3}x^3(a + b \sin^{-1}(cx)) - \frac{1}{3}(bc) \int \frac{x^3}{\sqrt{1 - c^2x^2}} dx \\ &= \frac{1}{3}x^3(a + b \sin^{-1}(cx)) - \frac{1}{6}(bc) \text{Subst}\left(\int \frac{x}{\sqrt{1 - c^2x}} dx, x, x^2\right) \\ &= \frac{1}{3}x^3(a + b \sin^{-1}(cx)) - \frac{1}{6}(bc) \text{Subst}\left(\int \left(\frac{1}{c^2\sqrt{1 - c^2x}} - \frac{\sqrt{1 - c^2x}}{c^2}\right) dx, x, x^2\right) \\ &= \frac{b\sqrt{1 - c^2x^2}}{3c^3} - \frac{b(1 - c^2x^2)^{3/2}}{9c^3} + \frac{1}{3}x^3(a + b \sin^{-1}(cx)) \end{aligned}$$

Mathematica [A] time = 0.0391751, size = 49, normalized size = 0.82

$$\frac{1}{9} \left(3ax^3 + \frac{b\sqrt{1-c^2x^2}(c^2x^2+2)}{c^3} + 3bx^3 \sin^{-1}(cx) \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*ArcSin[c*x]),x]

[Out] (3*a*x^3 + (b*Sqrt[1 - c^2*x^2]*(2 + c^2*x^2))/c^3 + 3*b*x^3*ArcSin[c*x])/9

Maple [A] time = 0.003, size = 64, normalized size = 1.1

$$\frac{1}{c^3} \left(\frac{c^3 x^3 a}{3} + b \left(\frac{c^3 x^3 \arcsin(cx)}{3} + \frac{c^2 x^2}{9} \sqrt{-c^2 x^2 + 1} + \frac{2}{9} \sqrt{-c^2 x^2 + 1} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a+b*arcsin(c*x)),x)

[Out] 1/c^3*(1/3*c^3*x^3*a+b*(1/3*c^3*x^3*arcsin(c*x)+1/9*c^2*x^2*(-c^2*x^2+1)^(1/2)+2/9*(-c^2*x^2+1)^(1/2)))

Maxima [A] time = 1.6864, size = 80, normalized size = 1.33

$$\frac{1}{3} ax^3 + \frac{1}{9} \left(3x^3 \arcsin(cx) + c \left(\frac{\sqrt{-c^2x^2+1}x^2}{c^2} + \frac{2\sqrt{-c^2x^2+1}}{c^4} \right) \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] 1/3*a*x^3 + 1/9*(3*x^3*arcsin(c*x) + c*(sqrt(-c^2*x^2 + 1)*x^2/c^2 + 2*sqrt(-c^2*x^2 + 1)/c^4))*b

Fricas [A] time = 1.52999, size = 119, normalized size = 1.98

$$\frac{3bc^3x^3 \arcsin(cx) + 3ac^3x^3 + (bc^2x^2 + 2b)\sqrt{-c^2x^2 + 1}}{9c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] 1/9*(3*b*c^3*x^3*arcsin(c*x) + 3*a*c^3*x^3 + (b*c^2*x^2 + 2*b)*sqrt(-c^2*x^2 + 1))/c^3

Sympy [A] time = 0.921519, size = 65, normalized size = 1.08

$$\begin{cases} \frac{ax^3}{3} + \frac{bx^3 \operatorname{asin}(cx)}{3} + \frac{bx^2 \sqrt{-c^2x^2+1}}{9c} + \frac{2b \sqrt{-c^2x^2+1}}{9c^3} & \text{for } c \neq 0 \\ \frac{ax^3}{3} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(a+b*asin(c*x)),x)

[Out] Piecewise((a*x**3/3 + b*x**3*asin(c*x)/3 + b*x**2*sqrt(-c**2*x**2 + 1)/(9*c) + 2*b*sqrt(-c**2*x**2 + 1)/(9*c**3), Ne(c, 0)), (a*x**3/3, True))

Giac [A] time = 1.34687, size = 100, normalized size = 1.67

$$\frac{1}{3}ax^3 + \frac{(c^2x^2 - 1)bx \operatorname{arcsin}(cx)}{3c^2} + \frac{bx \operatorname{arcsin}(cx)}{3c^2} - \frac{(-c^2x^2 + 1)^{\frac{3}{2}}b}{9c^3} + \frac{\sqrt{-c^2x^2 + 1}b}{3c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] 1/3*a*x^3 + 1/3*(c^2*x^2 - 1)*b*x*arcsin(c*x)/c^2 + 1/3*b*x*arcsin(c*x)/c^2 - 1/9*(-c^2*x^2 + 1)^(3/2)*b/c^3 + 1/3*sqrt(-c^2*x^2 + 1)*b/c^3

3.142 $\int x (a + b \sin^{-1}(cx)) dx$

Optimal. Leaf size=51

$$\frac{1}{2}x^2(a + b \sin^{-1}(cx)) + \frac{bx\sqrt{1-c^2x^2}}{4c} - \frac{b \sin^{-1}(cx)}{4c^2}$$

[Out] (b*x*Sqrt[1 - c^2*x^2])/(4*c) - (b*ArcSin[c*x])/(4*c^2) + (x^2*(a + b*ArcSin[c*x]))/2

Rubi [A] time = 0.0189604, antiderivative size = 51, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4627, 321, 216}

$$\frac{1}{2}x^2(a + b \sin^{-1}(cx)) + \frac{bx\sqrt{1-c^2x^2}}{4c} - \frac{b \sin^{-1}(cx)}{4c^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*ArcSin[c*x]),x]

[Out] (b*x*Sqrt[1 - c^2*x^2])/(4*c) - (b*ArcSin[c*x])/(4*c^2) + (x^2*(a + b*ArcSin[c*x]))/2

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_.*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 321

Int[((c_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(c^(n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), Int[(c*x)^(m - n)*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n - 1] && NeQ[m + n*p + 1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 216

Int[1/Sqrt[(a_.) + (b_.)*(x_)^2], x_Symbol] :> Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned} \int x (a + b \sin^{-1}(cx)) dx &= \frac{1}{2}x^2(a + b \sin^{-1}(cx)) - \frac{1}{2}(bc) \int \frac{x^2}{\sqrt{1-c^2x^2}} dx \\ &= \frac{bx\sqrt{1-c^2x^2}}{4c} + \frac{1}{2}x^2(a + b \sin^{-1}(cx)) - \frac{b \int \frac{1}{\sqrt{1-c^2x^2}} dx}{4c} \\ &= \frac{bx\sqrt{1-c^2x^2}}{4c} - \frac{b \sin^{-1}(cx)}{4c^2} + \frac{1}{2}x^2(a + b \sin^{-1}(cx)) \end{aligned}$$

Mathematica [A] time = 0.0193532, size = 56, normalized size = 1.1

$$\frac{ax^2}{2} + \frac{bx\sqrt{1-c^2x^2}}{4c} - \frac{b\sin^{-1}(cx)}{4c^2} + \frac{1}{2}bx^2\sin^{-1}(cx)$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*ArcSin[c*x]),x]

[Out] (a*x^2)/2 + (b*x*Sqrt[1 - c^2*x^2])/(4*c) - (b*ArcSin[c*x])/(4*c^2) + (b*x^2*ArcSin[c*x])/2

Maple [A] time = 0.003, size = 52, normalized size = 1.

$$\frac{1}{c^2} \left(\frac{c^2 x^2 a}{2} + b \left(\frac{c^2 x^2 \arcsin(cx)}{2} + \frac{cx}{4} \sqrt{-c^2 x^2 + 1} - \frac{\arcsin(cx)}{4} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a+b*arcsin(c*x)),x)

[Out] 1/c^2*(1/2*c^2*x^2*a+b*(1/2*c^2*x^2*arcsin(c*x)+1/4*c*x*(-c^2*x^2+1)^(1/2)-1/4*arcsin(c*x)))

Maxima [A] time = 1.59805, size = 82, normalized size = 1.61

$$\frac{1}{2} ax^2 + \frac{1}{4} \left(2x^2 \arcsin(cx) + c \left(\frac{\sqrt{-c^2x^2 + 1}x}{c^2} - \frac{\arcsin\left(\frac{cx}{\sqrt{c^2}}\right)}{\sqrt{c^2}c^2} \right) \right) b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] 1/2*a*x^2 + 1/4*(2*x^2*arcsin(c*x) + c*(sqrt(-c^2*x^2 + 1)*x/c^2 - arcsin(c^2*x/sqrt(c^2))/(sqrt(c^2)*c^2)))*b

Fricas [A] time = 1.48371, size = 111, normalized size = 2.18

$$\frac{2ac^2x^2 + \sqrt{-c^2x^2 + 1}bcx + (2bc^2x^2 - b)\arcsin(cx)}{4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] 1/4*(2*a*c^2*x^2 + sqrt(-c^2*x^2 + 1)*b*c*x + (2*b*c^2*x^2 - b)*arcsin(c*x))/c^2

Sympy [A] time = 0.435322, size = 54, normalized size = 1.06

$$\begin{cases} \frac{ax^2}{2} + \frac{bx^2 \operatorname{asin}(cx)}{2} + \frac{bx\sqrt{-c^2x^2+1}}{4c} - \frac{b \operatorname{asin}(cx)}{4c^2} & \text{for } c \neq 0 \\ \frac{ax^2}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*asin(c*x)),x)

[Out] Piecewise((a*x**2/2 + b*x**2*asin(c*x)/2 + b*x*sqrt(-c**2*x**2 + 1)/(4*c) - b*asin(c*x)/(4*c**2), Ne(c, 0)), (a*x**2/2, True))

Giac [A] time = 1.31596, size = 86, normalized size = 1.69

$$\frac{\sqrt{-c^2x^2+1}bx}{4c} + \frac{(c^2x^2-1)b \operatorname{arcsin}(cx)}{2c^2} + \frac{(c^2x^2-1)a}{2c^2} + \frac{b \operatorname{arcsin}(cx)}{4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] 1/4*sqrt(-c^2*x^2 + 1)*b*x/c + 1/2*(c^2*x^2 - 1)*b*arcsin(c*x)/c^2 + 1/2*(c^2*x^2 - 1)*a/c^2 + 1/4*b*arcsin(c*x)/c^2

3.143 $\int (a + b \sin^{-1}(cx)) dx$

Optimal. Leaf size=30

$$ax + \frac{b\sqrt{1-c^2x^2}}{c} + bx \sin^{-1}(cx)$$

[Out] a*x + (b*Sqrt[1 - c^2*x^2])/c + b*x*ArcSin[c*x]

Rubi [A] time = 0.0137527, antiderivative size = 30, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4619, 261}

$$ax + \frac{b\sqrt{1-c^2x^2}}{c} + bx \sin^{-1}(cx)$$

Antiderivative was successfully verified.

[In] Int[a + b*ArcSin[c*x], x]

[Out] a*x + (b*Sqrt[1 - c^2*x^2])/c + b*x*ArcSin[c*x]

Rule 4619

Int[((a_) + ArcSin[(c_)*(x_)])*(b_)^(n_), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 261

Int[(x_)^(m_)*((a_) + (b_)*(x_)^(n_))^(p_), x_Symbol] := Simp[(a + b*x^n)^(p + 1)/(b*n*(p + 1)), x] /; FreeQ[{a, b, m, n, p}, x] && EqQ[m, n - 1] && NeQ[p, -1]

Rubi steps

$$\begin{aligned} \int (a + b \sin^{-1}(cx)) dx &= ax + b \int \sin^{-1}(cx) dx \\ &= ax + bx \sin^{-1}(cx) - (bc) \int \frac{x}{\sqrt{1-c^2x^2}} dx \\ &= ax + \frac{b\sqrt{1-c^2x^2}}{c} + bx \sin^{-1}(cx) \end{aligned}$$

Mathematica [A] time = 0.0123389, size = 30, normalized size = 1.

$$ax + \frac{b\sqrt{1-c^2x^2}}{c} + bx \sin^{-1}(cx)$$

Antiderivative was successfully verified.

[In] Integrate[a + b*ArcSin[c*x], x]

[Out] a*x + (b*Sqrt[1 - c^2*x^2])/c + b*x*ArcSin[c*x]

Maple [A] time = 0.003, size = 30, normalized size = 1.

$$ax + \frac{b}{c} \left(cx \arcsin(cx) + \sqrt{-c^2x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(a+b*arcsin(c*x),x)

[Out] a*x+b/c*(c*x*arcsin(c*x)+(-c^2*x^2+1)^(1/2))

Maxima [A] time = 1.51728, size = 39, normalized size = 1.3

$$ax + \frac{\left(cx \arcsin(cx) + \sqrt{-c^2x^2 + 1} \right) b}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(a+b*arcsin(c*x),x, algorithm="maxima")

[Out] a*x + (c*x*arcsin(c*x) + sqrt(-c^2*x^2 + 1))*b/c

Fricas [A] time = 1.45936, size = 73, normalized size = 2.43

$$\frac{bcx \arcsin(cx) + acx + \sqrt{-c^2x^2 + 1}b}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(a+b*arcsin(c*x),x, algorithm="fricas")

[Out] (b*c*x*arcsin(c*x) + a*c*x + sqrt(-c^2*x^2 + 1)*b)/c

Sympy [A] time = 0.170436, size = 26, normalized size = 0.87

$$ax + b \left(\begin{cases} x \arcsin(cx) + \frac{\sqrt{-c^2x^2+1}}{c} & \text{for } c \neq 0 \\ 0 & \text{otherwise} \end{cases} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(a+b*asin(c*x),x)

[Out] a*x + b*Piecewise((x*asin(c*x) + sqrt(-c**2*x**2 + 1)/c, Ne(c, 0)), (0, True))

Giac [A] time = 1.28599, size = 39, normalized size = 1.3

$$ax + \frac{(cx \arcsin(cx) + \sqrt{-c^2x^2 + 1})b}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(a+b*arcsin(c*x),x, algorithm="giac")
```

```
[Out] a*x + (c*x*arcsin(c*x) + sqrt(-c^2*x^2 + 1))*b/c
```

3.144 $\int \frac{a+b \sin^{-1}(cx)}{x} dx$

Optimal. Leaf size=63

$$-\frac{1}{2}ib \operatorname{PolyLog}\left(2, e^{2i \sin^{-1}(cx)}\right) - \frac{i(a+b \sin^{-1}(cx))^2}{2b} + \log\left(1 - e^{2i \sin^{-1}(cx)}\right)(a+b \sin^{-1}(cx))$$

[Out] $((-I/2)*(a + b*\operatorname{ArcSin}[c*x])^2)/b + (a + b*\operatorname{ArcSin}[c*x])* \operatorname{Log}[1 - E^{((2*I)*\operatorname{ArcSin}[c*x])}] - (I/2)*b*\operatorname{PolyLog}[2, E^{((2*I)*\operatorname{ArcSin}[c*x])}]$

Rubi [A] time = 0.069963, antiderivative size = 63, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4625, 3717, 2190, 2279, 2391}

$$-\frac{1}{2}ib \operatorname{PolyLog}\left(2, e^{2i \sin^{-1}(cx)}\right) - \frac{i(a+b \sin^{-1}(cx))^2}{2b} + \log\left(1 - e^{2i \sin^{-1}(cx)}\right)(a+b \sin^{-1}(cx))$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])/x, x]$

[Out] $((-I/2)*(a + b*\operatorname{ArcSin}[c*x])^2)/b + (a + b*\operatorname{ArcSin}[c*x])* \operatorname{Log}[1 - E^{((2*I)*\operatorname{ArcSin}[c*x])}] - (I/2)*b*\operatorname{PolyLog}[2, E^{((2*I)*\operatorname{ArcSin}[c*x])}]$

Rule 4625

$\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])/x, x]$ \rightarrow $\operatorname{Subst}[\operatorname{Int}[(a + b*x)^n/\operatorname{Tan}[x], x], x, \operatorname{ArcSin}[c*x]]$ /; $\operatorname{FreeQ}\{a, b, c, x\}$ && $\operatorname{IGtQ}[n, 0]$

Rule 3717

$\operatorname{Int}[(c + d*x)^m*\tan[e + \operatorname{Pi}*k + f*x], x]$ \rightarrow $\operatorname{Simp}[(c + d*x)^{m+1}/(d*(m+1)), x] - \operatorname{Dist}[2*I, \operatorname{Int}[(c + d*x)^m*\operatorname{E}^{(2*I*k*\operatorname{Pi})}*\operatorname{E}^{(2*I*(e + f*x))}/(1 + \operatorname{E}^{(2*I*k*\operatorname{Pi})}*\operatorname{E}^{(2*I*(e + f*x))}), x], x]$ /; $\operatorname{FreeQ}\{c, d, e, f, x\}$ && $\operatorname{IntegerQ}[4*k]$ && $\operatorname{IGtQ}[m, 0]$

Rule 2190

$\operatorname{Int}[(c + d*x)^m*\operatorname{Log}[1 + (b*(F^{g*(e + f*x)})^n)/a], x] - \operatorname{Dist}[(d*m)/(b*f*g*n*\operatorname{Log}[F]), \operatorname{Int}[(c + d*x)^{m-1}*\operatorname{Log}[1 + (b*(F^{g*(e + f*x)})^n)/a], x], x]$ /; $\operatorname{FreeQ}\{F, a, b, c, d, e, f, g, n, x\}$ && $\operatorname{IGtQ}[m, 0]$

Rule 2279

$\operatorname{Int}[\operatorname{Log}[a + b*x]/x, x]$ \rightarrow $\operatorname{Dist}[1/(d*e*n*\operatorname{Log}[F]), \operatorname{Subst}[\operatorname{Int}[\operatorname{Log}[a + b*x]/x, x], x, (F^{e*(c + d*x)})^n], x]$ /; $\operatorname{FreeQ}\{F, a, b, c, d, e, n, x\}$ && $\operatorname{GtQ}[a, 0]$

Rule 2391

$\operatorname{Int}[\operatorname{Log}[(c + d*x)^n]/x, x]$ \rightarrow $-\operatorname{Simp}[\operatorname{PolyLog}[2, -(c*e*x^n)]/n, x]$ /; $\operatorname{FreeQ}\{c, d, e, n, x\}$ && $\operatorname{EqQ}[c*d, 1]$

Rubi steps

$$\begin{aligned}
\int \frac{a + b \sin^{-1}(cx)}{x} dx &= \text{Subst} \left(\int (a + bx) \cot(x) dx, x, \sin^{-1}(cx) \right) \\
&= -\frac{i(a + b \sin^{-1}(cx))^2}{2b} - 2i \text{Subst} \left(\int \frac{e^{2ix}(a + bx)}{1 - e^{2ix}} dx, x, \sin^{-1}(cx) \right) \\
&= -\frac{i(a + b \sin^{-1}(cx))^2}{2b} + (a + b \sin^{-1}(cx)) \log(1 - e^{2i \sin^{-1}(cx)}) - b \text{Subst} \left(\int \log(1 - e^{2ix}) dx, x \right) \\
&= -\frac{i(a + b \sin^{-1}(cx))^2}{2b} + (a + b \sin^{-1}(cx)) \log(1 - e^{2i \sin^{-1}(cx)}) + \frac{1}{2}(ib) \text{Subst} \left(\int \frac{\log(1 - x)}{x} dx, x \right) \\
&= -\frac{i(a + b \sin^{-1}(cx))^2}{2b} + (a + b \sin^{-1}(cx)) \log(1 - e^{2i \sin^{-1}(cx)}) - \frac{1}{2} ib \text{Li}_2(e^{2i \sin^{-1}(cx)})
\end{aligned}$$

Mathematica [A] time = 0.0321451, size = 52, normalized size = 0.83

$$-\frac{1}{2} ib \left(\sin^{-1}(cx)^2 + \text{PolyLog} \left(2, e^{2i \sin^{-1}(cx)} \right) \right) + a \log(x) + b \sin^{-1}(cx) \log(1 - e^{2i \sin^{-1}(cx)})$$

Warning: Unable to verify antiderivative.

[In] Integrate[(a + b*ArcSin[c*x])/x,x]

[Out] b*ArcSin[c*x]*Log[1 - E^((2*I)*ArcSin[c*x])] + a*Log[x] - (I/2)*b*(ArcSin[c*x]^2 + PolyLog[2, E^((2*I)*ArcSin[c*x])])

Maple [A] time = 0.03, size = 122, normalized size = 1.9

$$a \ln(cx) - \frac{i}{2} b (\arcsin(cx))^2 + b \arcsin(cx) \ln(1 + icx + \sqrt{-c^2x^2 + 1}) + b \arcsin(cx) \ln(1 - icx - \sqrt{-c^2x^2 + 1}) - ib \text{polylog}(2, e^{2i \arcsin(cx)})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))/x,x)

[Out] a*ln(c*x)-1/2*I*b*arcsin(c*x)^2+b*arcsin(c*x)*ln(1+I*c*x+(-c^2*x^2+1)^(1/2))+b*arcsin(c*x)*ln(1-I*c*x-(-c^2*x^2+1)^(1/2))-I*b*polylog(2,I*c*x+(-c^2*x^2+1)^(1/2))-I*b*polylog(2,-I*c*x-(-c^2*x^2+1)^(1/2))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$b \int \frac{\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})}{x} dx + a \log(x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x,x, algorithm="maxima")

[Out] b*integrate(arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))/x, x) + a*log(x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{b \arcsin(cx) + a}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x,x, algorithm="fricas")

[Out] integral((b*arcsin(c*x) + a)/x, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{a + b \arcsin(cx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))/x,x)

[Out] Integral((a + b*asin(c*x))/x, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{b \arcsin(cx) + a}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x,x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)/x, x)

$$3.145 \quad \int \frac{a+b \sin^{-1}(cx)}{x^2} dx$$

Optimal. Leaf size=33

$$-\frac{a+b \sin^{-1}(cx)}{x} - bc \tanh^{-1}\left(\sqrt{1-c^2x^2}\right)$$

[Out] -((a + b*ArcSin[c*x])/x) - b*c*ArcTanh[Sqrt[1 - c^2*x^2]]

Rubi [A] time = 0.0265272, antiderivative size = 33, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4627, 266, 63, 208}

$$-\frac{a+b \sin^{-1}(cx)}{x} - bc \tanh^{-1}\left(\sqrt{1-c^2x^2}\right)$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])/x^2,x]

[Out] -((a + b*ArcSin[c*x])/x) - b*c*ArcTanh[Sqrt[1 - c^2*x^2]]

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 266

```
Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Dist[1/n, Subst[
Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b
, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]
```

Rule 63

```
Int[((a_.) + (b_.)*(x_))^(m_.)*((c_.) + (d_.)*(x_))^(n_), x_Symbol] := With[
{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b +
(d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ
[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Den
ominator[m]] && IntLinearQ[a, b, c, d, m, n, x]
```

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{a + b \sin^{-1}(cx)}{x^2} dx &= -\frac{a + b \sin^{-1}(cx)}{x} + (bc) \int \frac{1}{x\sqrt{1 - c^2x^2}} dx \\
&= -\frac{a + b \sin^{-1}(cx)}{x} + \frac{1}{2}(bc) \operatorname{Subst} \left(\int \frac{1}{x\sqrt{1 - c^2x}} dx, x, x^2 \right) \\
&= -\frac{a + b \sin^{-1}(cx)}{x} - \frac{b \operatorname{Subst} \left(\int \frac{1}{\frac{1}{c^2} - x^2} dx, x, \sqrt{1 - c^2x^2} \right)}{c} \\
&= -\frac{a + b \sin^{-1}(cx)}{x} - bc \tanh^{-1} \left(\sqrt{1 - c^2x^2} \right)
\end{aligned}$$

Mathematica [A] time = 0.0027337, size = 36, normalized size = 1.09

$$-\frac{a}{x} - bc \tanh^{-1} \left(\sqrt{1 - c^2x^2} \right) - \frac{b \sin^{-1}(cx)}{x}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])/x^2,x]

[Out] -(a/x) - (b*ArcSin[c*x])/x - b*c*ArcTanh[Sqrt[1 - c^2*x^2]]

Maple [A] time = 0.004, size = 43, normalized size = 1.3

$$c \left(-\frac{a}{cx} + b \left(-\frac{\arcsin(cx)}{cx} - \operatorname{Artanh} \left(\frac{1}{\sqrt{-c^2x^2 + 1}} \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))/x^2,x)

[Out] c*(-a/c/x+b*(-1/c/x*arcsin(c*x)-arctanh(1/(-c^2*x^2+1)^(1/2))))

Maxima [A] time = 1.50488, size = 63, normalized size = 1.91

$$-\left(c \log \left(\frac{2\sqrt{-c^2x^2 + 1}}{|x|} + \frac{2}{|x|} \right) + \frac{\arcsin(cx)}{x} \right) b - \frac{a}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^2,x, algorithm="maxima")

[Out] -(c*log(2*sqrt(-c^2*x^2 + 1)/abs(x) + 2/abs(x)) + arcsin(c*x)/x)*b - a/x

Fricas [A] time = 1.55218, size = 140, normalized size = 4.24

$$-\frac{bcx \log \left(\sqrt{-c^2x^2 + 1} + 1 \right) - bcx \log \left(\sqrt{-c^2x^2 + 1} - 1 \right) + 2b \arcsin(cx) + 2a}{2x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^2,x, algorithm="fricas")

[Out] -1/2*(b*c*x*log(sqrt(-c^2*x^2 + 1) + 1) - b*c*x*log(sqrt(-c^2*x^2 + 1) - 1) + 2*b*arcsin(c*x) + 2*a)/x

Sympy [A] time = 3.3225, size = 39, normalized size = 1.18

$$-\frac{a}{x} + bc \left(\begin{cases} -\operatorname{acosh}\left(\frac{1}{cx}\right) & \text{for } \frac{1}{|c^2x^2|} > 1 \\ i \operatorname{asin}\left(\frac{1}{cx}\right) & \text{otherwise} \end{cases} \right) - \frac{b \operatorname{asin}(cx)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))/x**2,x)

[Out] -a/x + b*c*Piecewise((-acosh(1/(c*x)), 1/Abs(c**2*x**2) > 1), (I*asin(1/(c*x)), True)) - b*asin(c*x)/x

Giac [B] time = 1.58261, size = 439, normalized size = 13.3

$$\frac{\sqrt{-c^2x^2 + 1}bc^2x \operatorname{arcsin}(cx)}{2\left(\sqrt{-c^2x^2 + 1} + 1\right)^2} - \frac{bc^2x \operatorname{arcsin}(cx)}{2\left(\sqrt{-c^2x^2 + 1} + 1\right)^2} - \frac{\sqrt{-c^2x^2 + 1}ac^2x}{2\left(\sqrt{-c^2x^2 + 1} + 1\right)^2} + \frac{\sqrt{-c^2x^2 + 1}bc \log(|c||x|)}{\sqrt{-c^2x^2 + 1} + 1} - \frac{\sqrt{-c^2x^2 + 1}}{\sqrt{-c^2x^2 + 1} + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^2,x, algorithm="giac")

[Out] -1/2*sqrt(-c^2*x^2 + 1)*b*c^2*x*arcsin(c*x)/(sqrt(-c^2*x^2 + 1) + 1)^2 - 1/2*b*c^2*x*arcsin(c*x)/(sqrt(-c^2*x^2 + 1) + 1)^2 - 1/2*sqrt(-c^2*x^2 + 1)*a*c^2*x/(sqrt(-c^2*x^2 + 1) + 1)^2 + sqrt(-c^2*x^2 + 1)*b*c*log(abs(c)*abs(x))/(sqrt(-c^2*x^2 + 1) + 1) - sqrt(-c^2*x^2 + 1)*b*c*log(sqrt(-c^2*x^2 + 1) + 1)/(sqrt(-c^2*x^2 + 1) + 1) - 1/2*a*c^2*x/(sqrt(-c^2*x^2 + 1) + 1)^2 + b*c*log(abs(c)*abs(x))/(sqrt(-c^2*x^2 + 1) + 1) - b*c*log(sqrt(-c^2*x^2 + 1) + 1)/(sqrt(-c^2*x^2 + 1) + 1) - 1/2*sqrt(-c^2*x^2 + 1)*b*arcsin(c*x)/x - 1/2*b*arcsin(c*x)/x - 1/2*sqrt(-c^2*x^2 + 1)*a/x - 1/2*a/x

$$3.146 \quad \int \frac{a+b \sin^{-1}(cx)}{x^3} dx$$

Optimal. Leaf size=39

$$-\frac{a+b \sin^{-1}(cx)}{2x^2} - \frac{bc\sqrt{1-c^2x^2}}{2x}$$

[Out] $-(b*c*\text{Sqrt}[1 - c^2*x^2])/(2*x) - (a + b*\text{ArcSin}[c*x])/(2*x^2)$

Rubi [A] time = 0.0189224, antiderivative size = 39, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {4627, 264}

$$-\frac{a+b \sin^{-1}(cx)}{2x^2} - \frac{bc\sqrt{1-c^2x^2}}{2x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*\text{ArcSin}[c*x])/x^3, x]$

[Out] $-(b*c*\text{Sqrt}[1 - c^2*x^2])/(2*x) - (a + b*\text{ArcSin}[c*x])/(2*x^2)$

Rule 4627

$\text{Int}[(a_.) + \text{ArcSin}[(c_.)*(x_)]*(b_.)^{(n_.)}*((d_.)*(x_))^{(m_.)}, x_Symbol]$
 $:\> \text{Simp}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ $\text{FreeQ}\{a, b, c, d, m\}, x$ && $\text{IGtQ}[n, 0]$ && $\text{NeQ}[m, -1]$

Rule 264

$\text{Int}[(c_.)*(x_))^{(m_.)}*((a_.) + (b_.)*(x_))^{(n_.)}^{(p_.)}, x_Symbol]$ $:\> \text{Simp}[(c*x)^{(m+1)}*(a + b*x^n)^{(p+1)}/(a*c*(m+1)), x] /;$ $\text{FreeQ}\{a, b, c, m, n, p\}, x$ && $\text{EqQ}[(m+1)/n + p + 1, 0]$ && $\text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int \frac{a+b \sin^{-1}(cx)}{x^3} dx &= -\frac{a+b \sin^{-1}(cx)}{2x^2} + \frac{1}{2}(bc) \int \frac{1}{x^2\sqrt{1-c^2x^2}} dx \\ &= -\frac{bc\sqrt{1-c^2x^2}}{2x} - \frac{a+b \sin^{-1}(cx)}{2x^2} \end{aligned}$$

Mathematica [A] time = 0.013428, size = 44, normalized size = 1.13

$$-\frac{a}{2x^2} - \frac{bc\sqrt{1-c^2x^2}}{2x} - \frac{b \sin^{-1}(cx)}{2x^2}$$

Antiderivative was successfully verified.

[In] $\text{Integrate}[(a + b*\text{ArcSin}[c*x])/x^3, x]$

[Out] $-a/(2*x^2) - (b*c*\text{Sqrt}[1 - c^2*x^2])/(2*x) - (b*\text{ArcSin}[c*x])/(2*x^2)$

Maple [A] time = 0.004, size = 50, normalized size = 1.3

$$c^2 \left(-\frac{a}{2c^2x^2} + b \left(-\frac{\arcsin(cx)}{2c^2x^2} - \frac{1}{2cx} \sqrt{-c^2x^2 + 1} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))/x^3,x)

[Out] c^2*(-1/2*a/c^2/x^2+b*(-1/2/c^2/x^2*arcsin(c*x)-1/2/c/x*(-c^2*x^2+1)^(1/2))
)

Maxima [A] time = 1.53808, size = 49, normalized size = 1.26

$$-\frac{1}{2}b \left(\frac{\sqrt{-c^2x^2 + 1}c}{x} + \frac{\arcsin(cx)}{x^2} \right) - \frac{a}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^3,x, algorithm="maxima")

[Out] -1/2*b*(sqrt(-c^2*x^2 + 1)*c/x + arcsin(c*x)/x^2) - 1/2*a/x^2

Fricas [A] time = 1.48941, size = 88, normalized size = 2.26

$$\frac{\sqrt{-c^2x^2 + 1}bcx - ax^2 + b \arcsin(cx) + a}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^3,x, algorithm="fricas")

[Out] -1/2*(sqrt(-c^2*x^2 + 1)*b*c*x - a*x^2 + b*arcsin(c*x) + a)/x^2

Sympy [A] time = 2.89605, size = 61, normalized size = 1.56

$$-\frac{a}{2x^2} + \frac{bc \left(\begin{cases} -\frac{i\sqrt{c^2x^2-1}}{x} & \text{for } |c^2x^2| > 1 \\ -\frac{\sqrt{-c^2x^2+1}}{x} & \text{otherwise} \end{cases} \right)}{2} - \frac{b \operatorname{asin}(cx)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))/x**3,x)

[Out] -a/(2*x**2) + b*c*Piecewise((-I*sqrt(c**2*x**2 - 1)/x, Abs(c**2*x**2) > 1),
(-sqrt(-c**2*x**2 + 1)/x, True))/2 - b*asin(c*x)/(2*x**2)

Giac [B] time = 1.40209, size = 220, normalized size = 5.64

$$\frac{bc^4x^2 \arcsin(cx)}{8\left(\sqrt{-c^2x^2+1}+1\right)^2} - \frac{ac^4x^2}{8\left(\sqrt{-c^2x^2+1}+1\right)^2} + \frac{bc^3x}{4\left(\sqrt{-c^2x^2+1}+1\right)} - \frac{1}{4}bc^2 \arcsin(cx) - \frac{1}{4}ac^2 - \frac{bc\left(\sqrt{-c^2x^2+1}+1\right)}{4x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^3,x, algorithm="giac")

[Out] -1/8*b*c^4*x^2*arcsin(c*x)/(sqrt(-c^2*x^2 + 1) + 1)^2 - 1/8*a*c^4*x^2/(sqrt(-c^2*x^2 + 1) + 1)^2 + 1/4*b*c^3*x/(sqrt(-c^2*x^2 + 1) + 1) - 1/4*b*c^2*arcsin(c*x) - 1/4*a*c^2 - 1/4*b*c*(sqrt(-c^2*x^2 + 1) + 1)/x - 1/8*b*(sqrt(-c^2*x^2 + 1) + 1)^2*arcsin(c*x)/x^2 - 1/8*a*(sqrt(-c^2*x^2 + 1) + 1)^2/x^2

$$3.147 \quad \int \frac{a+b \sin^{-1}(cx)}{x^4} dx$$

Optimal. Leaf size=62

$$-\frac{a+b \sin^{-1}(cx)}{3x^3} - \frac{bc\sqrt{1-c^2x^2}}{6x^2} - \frac{1}{6}bc^3 \tanh^{-1}\left(\sqrt{1-c^2x^2}\right)$$

[Out] $-(b*c*\text{Sqrt}[1 - c^2*x^2])/(6*x^2) - (a + b*\text{ArcSin}[c*x])/(3*x^3) - (b*c^3*\text{ArcTanh}[\text{Sqrt}[1 - c^2*x^2]])/6$

Rubi [A] time = 0.0382465, antiderivative size = 62, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4627, 266, 51, 63, 208}

$$-\frac{a+b \sin^{-1}(cx)}{3x^3} - \frac{bc\sqrt{1-c^2x^2}}{6x^2} - \frac{1}{6}bc^3 \tanh^{-1}\left(\sqrt{1-c^2x^2}\right)$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])/x^4,x]

[Out] $-(b*c*\text{Sqrt}[1 - c^2*x^2])/(6*x^2) - (a + b*\text{ArcSin}[c*x])/(3*x^3) - (b*c^3*\text{ArcTanh}[\text{Sqrt}[1 - c^2*x^2]])/6$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^(n_.)*((d_.)*(x_)^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 266

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]

Rule 51

Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] :> Simp[((a + b*x)^(m + 1)*(c + d*x)^(n + 1))/((b*c - a*d)*(m + 1)), x] - Dist[(d*(m + n + 2))/((b*c - a*d)*(m + 1)), Int[(a + b*x)^(m + 1)*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && LtQ[m, -1] && !(LtQ[n, -1] && (EqQ[a, 0] || (NeQ[c, 0] && LtQ[m - n, 0] && IntegerQ[n]))) && IntLinearQ[a, b, c, d, m, n, x]

Rule 63

Int[((a_.) + (b_.)*(x_)^(m_))*((c_.) + (d_.)*(x_)^(n_)), x_Symbol] :> With[{p = Denominator[m]}, Dist[p/b, Subst[Int[x^(p*(m + 1) - 1)*(c - (a*d)/b + (d*x^p)/b)^n, x], x, (a + b*x)^(1/p)], x]] /; FreeQ[{a, b, c, d}, x] && NeQ[b*c - a*d, 0] && LtQ[-1, m, 0] && LeQ[-1, n, 0] && LeQ[Denominator[n], Denominator[m]] && IntLinearQ[a, b, c, d, m, n, x]

Rule 208

```
Int[((a_) + (b_.)*(x_)^2)^(-1), x_Symbol] := Simp[(Rt[-(a/b), 2]*ArcTanh[x/
Rt[-(a/b), 2]])/a, x] /; FreeQ[{a, b}, x] && NegQ[a/b]
```

Rubi steps

$$\begin{aligned}
\int \frac{a + b \sin^{-1}(cx)}{x^4} dx &= -\frac{a + b \sin^{-1}(cx)}{3x^3} + \frac{1}{3}(bc) \int \frac{1}{x^3 \sqrt{1 - c^2 x^2}} dx \\
&= -\frac{a + b \sin^{-1}(cx)}{3x^3} + \frac{1}{6}(bc) \operatorname{Subst} \left(\int \frac{1}{x^2 \sqrt{1 - c^2 x}} dx, x, x^2 \right) \\
&= -\frac{bc \sqrt{1 - c^2 x^2}}{6x^2} - \frac{a + b \sin^{-1}(cx)}{3x^3} + \frac{1}{12}(bc^3) \operatorname{Subst} \left(\int \frac{1}{x \sqrt{1 - c^2 x}} dx, x, x^2 \right) \\
&= -\frac{bc \sqrt{1 - c^2 x^2}}{6x^2} - \frac{a + b \sin^{-1}(cx)}{3x^3} - \frac{1}{6}(bc) \operatorname{Subst} \left(\int \frac{1}{\frac{1}{c^2} - \frac{x^2}{c^2}} dx, x, \sqrt{1 - c^2 x^2} \right) \\
&= -\frac{bc \sqrt{1 - c^2 x^2}}{6x^2} - \frac{a + b \sin^{-1}(cx)}{3x^3} - \frac{1}{6} bc^3 \tanh^{-1} \left(\sqrt{1 - c^2 x^2} \right)
\end{aligned}$$

Mathematica [A] time = 0.0183823, size = 67, normalized size = 1.08

$$-\frac{a}{3x^3} - \frac{bc\sqrt{1-c^2x^2}}{6x^2} - \frac{1}{6}bc^3 \tanh^{-1}\left(\sqrt{1-c^2x^2}\right) - \frac{b \sin^{-1}(cx)}{3x^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*ArcSin[c*x])/x^4,x]
```

```
[Out] -a/(3*x^3) - (b*c*Sqrt[1 - c^2*x^2])/(6*x^2) - (b*ArcSin[c*x])/(3*x^3) - (b
*c^3*ArcTanh[Sqrt[1 - c^2*x^2]])/6
```

Maple [A] time = 0.003, size = 65, normalized size = 1.1

$$c^3 \left(-\frac{a}{3c^3x^3} + b \left(-\frac{\arcsin(cx)}{3c^3x^3} - \frac{1}{6c^2x^2} \sqrt{-c^2x^2 + 1} - \frac{1}{6} \operatorname{Arctanh} \left(\frac{1}{\sqrt{-c^2x^2 + 1}} \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a+b*arcsin(c*x))/x^4,x)
```

```
[Out] c^3*(-1/3*a/c^3/x^3+b*(-1/3/c^3/x^3*arcsin(c*x)-1/6/c^2/x^2*(-c^2*x^2+1)^(1
/2)-1/6*arctanh(1/(-c^2*x^2+1)^(1/2))))
```

Maxima [A] time = 1.54952, size = 93, normalized size = 1.5

$$-\frac{1}{6} \left(\left(c^2 \log \left(\frac{2 \sqrt{-c^2 x^2 + 1}}{|x|} + \frac{2}{|x|} \right) + \frac{\sqrt{-c^2 x^2 + 1}}{x^2} \right) c + \frac{2 \arcsin(cx)}{x^3} \right) b - \frac{a}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))/x^4,x, algorithm="maxima")
```

[Out] $-1/6*((c^2*\log(2*\sqrt{-c^2*x^2 + 1})/abs(x) + 2/abs(x)) + \sqrt{-c^2*x^2 + 1}/x^2)*c + 2*\arcsin(cx)/x^3*b - 1/3*a/x^3$

Fricas [A] time = 1.66349, size = 194, normalized size = 3.13

$$\frac{bc^3x^3 \log\left(\sqrt{-c^2x^2+1}+1\right) - bc^3x^3 \log\left(\sqrt{-c^2x^2+1}-1\right) + 2\sqrt{-c^2x^2+1}bcx + 4b \arcsin(cx) + 4a}{12x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^4,x, algorithm="fricas")

[Out] $-1/12*(b*c^3*x^3*\log(\sqrt{-c^2*x^2 + 1} + 1) - b*c^3*x^3*\log(\sqrt{-c^2*x^2 + 1} - 1) + 2*\sqrt{-c^2*x^2 + 1}*b*c*x + 4*b*\arcsin(c*x) + 4*a)/x^3$

Sympy [A] time = 5.74433, size = 119, normalized size = 1.92

$$-\frac{a}{3x^3} + \frac{bc \left(\begin{array}{l} \frac{c^2 \operatorname{acosh}\left(\frac{1}{cx}\right) - c\sqrt{-1+\frac{1}{c^2x^2}}}{2} - \frac{c\sqrt{-1+\frac{1}{c^2x^2}}}{2x} \quad \text{for } \frac{1}{|c^2x^2|} > 1 \\ \frac{ic^2 \operatorname{asin}\left(\frac{1}{cx}\right)}{2} - \frac{ic}{2x\sqrt{1-\frac{1}{c^2x^2}}} + \frac{i}{2cx^3\sqrt{1-\frac{1}{c^2x^2}}} \quad \text{otherwise} \end{array} \right)}{3} - \frac{b \operatorname{asin}(cx)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))/x**4,x)

[Out] $-a/(3*x**3) + b*c*\operatorname{Piecewise}((-c**2*\operatorname{acosh}(1/(c*x)))/2 - c*\sqrt{-1 + 1/(c**2*x**2)})/(2*x), 1/\operatorname{Abs}(c**2*x**2) > 1), (I*c**2*\operatorname{asin}(1/(c*x)))/2 - I*c/(2*x*\sqrt{1 - 1/(c**2*x**2)}) + I/(2*c*x**3*\sqrt{1 - 1/(c**2*x**2)}), \operatorname{True}))/3 - b*a*\operatorname{asin}(c*x)/(3*x**3)$

Giac [B] time = 2.03371, size = 383, normalized size = 6.18

$$-\frac{bc^6x^3 \arcsin(cx)}{24\left(\sqrt{-c^2x^2+1}+1\right)^3} - \frac{ac^6x^3}{24\left(\sqrt{-c^2x^2+1}+1\right)^3} + \frac{bc^5x^2}{24\left(\sqrt{-c^2x^2+1}+1\right)^2} - \frac{bc^4x \arcsin(cx)}{8\left(\sqrt{-c^2x^2+1}+1\right)} - \frac{ac^4x}{8\left(\sqrt{-c^2x^2+1}+1\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/x^4,x, algorithm="giac")

[Out] $-1/24*b*c^6*x^3*\arcsin(c*x)/(\sqrt{-c^2*x^2 + 1} + 1)^3 - 1/24*a*c^6*x^3/(\sqrt{-c^2*x^2 + 1} + 1)^3 + 1/24*b*c^5*x^2/(\sqrt{-c^2*x^2 + 1} + 1)^2 - 1/8*b*c^4*x*\arcsin(c*x)/(\sqrt{-c^2*x^2 + 1} + 1) - 1/8*a*c^4*x/(\sqrt{-c^2*x^2 + 1} + 1) + 1/6*b*c^3*\log(abs(c)*abs(x)) - 1/6*b*c^3*\log(\sqrt{-c^2*x^2 + 1} + 1) - 1/8*b*c^2*(\sqrt{-c^2*x^2 + 1} + 1)*\arcsin(c*x)/x - 1/8*a*c^2*(\sqrt{-c^2*x^2 + 1} + 1)/x - 1/24*b*c*(\sqrt{-c^2*x^2 + 1} + 1)^2/x^2 - 1/24*b*(\sqrt{-c^2*x^2 + 1} + 1)^3*\arcsin(c*x)/x^3 - 1/24*a*(\sqrt{-c^2*x^2 + 1} + 1)^3/x^3$

3.148 $\int x^2 (a + b \sin^{-1}(cx))^2 dx$

Optimal. Leaf size=102

$$\frac{2bx^2\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{9c} + \frac{4b\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{9c^3} + \frac{1}{3}x^3(a+b\sin^{-1}(cx))^2 - \frac{4b^2x}{9c^2} - \frac{2}{27}b^2x^3$$

[Out] $(-4*b^2*x)/(9*c^2) - (2*b^2*x^3)/27 + (4*b*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]))/(9*c^3) + (2*b*x^2*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]))/(9*c) + (x^3*(a + b*ArcSin[c*x])^2)/3$

Rubi [A] time = 0.153869, antiderivative size = 102, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {4627, 4707, 4677, 8, 30}

$$\frac{2bx^2\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{9c} + \frac{4b\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{9c^3} + \frac{1}{3}x^3(a+b\sin^{-1}(cx))^2 - \frac{4b^2x}{9c^2} - \frac{2}{27}b^2x^3$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*ArcSin[c*x])^2,x]

[Out] $(-4*b^2*x)/(9*c^2) - (2*b^2*x^3)/27 + (4*b*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]))/(9*c^3) + (2*b*x^2*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]))/(9*c) + (x^3*(a + b*ArcSin[c*x])^2)/3$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_.)*((f_.)*(x_))^(m_)]/Sqrt[(d_ + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d*IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rule 30

$\text{Int}[(x_)^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[x^{(m + 1)}/(m + 1), x] /; \text{FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int x^2 (a + b \sin^{-1}(cx))^2 dx &= \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^2 - \frac{1}{3} (2bc) \int \frac{x^3 (a + b \sin^{-1}(cx))}{\sqrt{1 - c^2 x^2}} dx \\ &= \frac{2bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{9c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^2 - \frac{1}{9} (2b^2) \int x^2 dx - \frac{(4b) \int x^3 (a + b \sin^{-1}(cx))}{9c} \\ &= -\frac{2}{27} b^2 x^3 + \frac{4b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{9c^3} + \frac{2bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{9c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^2 \\ &= -\frac{4b^2 x}{9c^2} - \frac{2b^2 x^3}{27} + \frac{4b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{9c^3} + \frac{2bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{9c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^2 \end{aligned}$$

Mathematica [A] time = 0.188787, size = 95, normalized size = 0.93

$$\frac{1}{3} \left(x^3 (a + b \sin^{-1}(cx))^2 - \frac{2b \left(-3c^2 x^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx)) - 6 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx)) + bc^3 x^3 + 6bcx \right)}{9c^3} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*ArcSin[c*x])^2,x]

[Out] (x^3*(a + b*ArcSin[c*x])^2 - (2*b*(6*b*c*x + b*c^3*x^3 - 6*Sqrt[1 - c^2*x^2])*(a + b*ArcSin[c*x]) - 3*c^2*x^2*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])))/(9*c^3)/3

Maple [A] time = 0.025, size = 126, normalized size = 1.2

$$\frac{1}{c^3} \left(\frac{a^2 c^3 x^3}{3} + b^2 \left(\frac{c^3 x^3 (\arcsin(cx))^2}{3} + \frac{2 \arcsin(cx) (c^2 x^2 + 2)}{9} \sqrt{-c^2 x^2 + 1} - \frac{2 c^3 x^3}{27} - \frac{4 cx}{9} \right) + 2 ab \left(\frac{1}{3} c^3 x^3 \arcsin(cx) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a+b*arcsin(c*x))^2,x)

[Out] 1/c^3*(1/3*a^2*c^3*x^3+b^2*(1/3*c^3*x^3*arcsin(c*x)^2+2/9*arcsin(c*x)*(c^2*x^2+2)*(-c^2*x^2+1)^(1/2)-2/27*c^3*x^3-4/9*c*x)+2*a*b*(1/3*c^3*x^3*arcsin(c*x)+1/9*c^2*x^2*(-c^2*x^2+1)^(1/2)+2/9*(-c^2*x^2+1)^(1/2))

Maxima [A] time = 1.54948, size = 192, normalized size = 1.88

$$\frac{1}{3} b^2 x^3 \arcsin(cx)^2 + \frac{1}{3} a^2 x^3 + \frac{2}{9} \left(3 x^3 \arcsin(cx) + c \left(\frac{\sqrt{-c^2 x^2 + 1} x^2}{c^2} + \frac{2 \sqrt{-c^2 x^2 + 1}}{c^4} \right) \right) ab + \frac{2}{27} \left(3 c \left(\frac{\sqrt{-c^2 x^2 + 1} x^2}{c^2} + \frac{2 \sqrt{-c^2 x^2 + 1}}{c^4} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] $\frac{1}{3}b^2x^3\arcsin(cx)^2 + \frac{1}{3}a^2x^3 + \frac{2}{9}(3x^3\arcsin(cx) + c(\sqrt{-c^2x^2 + 1})x^2/c^2 + 2\sqrt{-c^2x^2 + 1}/c^4))ab + \frac{2}{27}(3c(\sqrt{-c^2x^2 + 1})x^2/c^2 + 2\sqrt{-c^2x^2 + 1}/c^4)\arcsin(cx) - (c^2x^3 + 6x)/c^2)b^2$

Fricas [A] time = 1.43564, size = 255, normalized size = 2.5

$$\frac{9b^2c^3x^3 \arcsin(cx)^2 + 18abc^3x^3 \arcsin(cx) + (9a^2 - 2b^2)c^3x^3 - 12b^2cx + 6(abc^2x^2 + 2ab + (b^2c^2x^2 + 2b^2)\arcsin(cx))\sqrt{-c^2x^2 + 1}}{27c^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] $\frac{1}{27}(9b^2c^3x^3\arcsin(cx)^2 + 18a^2b^2c^3x^3\arcsin(cx) + (9a^2 - 2b^2)c^3x^3 - 12b^2cx + 6(a^2b^2c^2x^2 + 2a^2b + (b^2c^2x^2 + 2b^2)\arcsin(cx))\sqrt{-c^2x^2 + 1})/c^3$

Sympy [A] time = 2.05873, size = 170, normalized size = 1.67

$$\left\{ \begin{array}{l} \frac{a^2x^3}{3} + \frac{2abx^3 \arcsin(cx)}{3} + \frac{2abx^2\sqrt{-c^2x^2+1}}{9c} + \frac{4ab\sqrt{-c^2x^2+1}}{9c^3} + \frac{b^2x^3 \arcsin^2(cx)}{3} - \frac{2b^2x^3}{27} + \frac{2b^2x^2\sqrt{-c^2x^2+1} \arcsin(cx)}{9c} - \frac{4b^2x}{9c^2} + \frac{4b^2\sqrt{-c^2x^2+1} \arcsin(cx)}{9c^3} \\ \frac{a^2x^3}{3} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(a+b*asin(c*x))**2,x)

[Out] Piecewise((a**2*x**3/3 + 2*a*b*x**3*asin(c*x)/3 + 2*a*b*x**2*sqrt(-c**2*x**2 + 1)/(9*c) + 4*a*b*sqrt(-c**2*x**2 + 1)/(9*c**3) + b**2*x**3*asin(c*x)**2/3 - 2*b**2*x**3/27 + 2*b**2*x**2*sqrt(-c**2*x**2 + 1)*asin(c*x)/(9*c) - 4*b**2*x/(9*c**2) + 4*b**2*sqrt(-c**2*x**2 + 1)*asin(c*x)/(9*c**3), Ne(c, 0)), (a**2*x**3/3, True))

Giac [B] time = 1.34679, size = 262, normalized size = 2.57

$$\frac{1}{3}a^2x^3 + \frac{(c^2x^2 - 1)b^2x \arcsin(cx)^2}{3c^2} + \frac{2(c^2x^2 - 1)abx \arcsin(cx)}{3c^2} + \frac{b^2x \arcsin(cx)^2}{3c^2} - \frac{2(c^2x^2 - 1)b^2x}{27c^2} + \frac{2abx \arcsin(cx)}{3c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^2,x, algorithm="giac")

[Out] $\frac{1}{3}a^2x^3 + \frac{1}{3}(c^2x^2 - 1)b^2x\arcsin(cx)^2/c^2 + \frac{2}{3}(c^2x^2 - 1)a^2b^2x\arcsin(cx)/c^2 + \frac{1}{3}b^2x\arcsin(cx)^2/c^2 - \frac{2}{27}(c^2x^2 - 1)b^2x/c^2 + \frac{2}{3}a^2b^2x\arcsin(cx)/c^2 - \frac{2}{9}(-c^2x^2 + 1)^{(3/2)}b^2\arcsin(cx)/c^3 - \frac{14}{27}b^2x/c^2 - \frac{2}{9}(-c^2x^2 + 1)^{(3/2)}a^2b/c^3 + \frac{2}{3}\sqrt{-c^2x^2 + 1}b^2\arcsin(cx)/c^3 + \frac{2}{3}\sqrt{-c^2x^2 + 1}a^2b/c^3$

3.149 $\int x \left(a + b \sin^{-1}(cx) \right)^2 dx$

Optimal. Leaf size=76

$$\frac{bx\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{2c} - \frac{(a+b\sin^{-1}(cx))^2}{4c^2} + \frac{1}{2}x^2(a+b\sin^{-1}(cx))^2 - \frac{1}{4}b^2x^2$$

[Out] $-(b^2x^2)/4 + (bx\sqrt{1-c^2x^2}(a+b\text{ArcSin}[c*x]))/(2*c) - (a+b*\text{ArcSin}[c*x])^2/(4*c^2) + (x^2*(a+b*\text{ArcSin}[c*x])^2)/2$

Rubi [A] time = 0.118784, antiderivative size = 76, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4627, 4707, 4641, 30}

$$\frac{bx\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{2c} - \frac{(a+b\sin^{-1}(cx))^2}{4c^2} + \frac{1}{2}x^2(a+b\sin^{-1}(cx))^2 - \frac{1}{4}b^2x^2$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*(a + b*\text{ArcSin}[c*x])^2, x]$

[Out] $-(b^2x^2)/4 + (bx\sqrt{1-c^2x^2}(a+b\text{ArcSin}[c*x]))/(2*c) - (a+b*\text{ArcSin}[c*x])^2/(4*c^2) + (x^2*(a+b*\text{ArcSin}[c*x])^2)/2$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(d*x)^m, x_Symbol] \rightarrow \text{Simp}[(d*x)^{m+1}(a+b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c^n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}(a+b*\text{ArcSin}[c*x])^{n-1}]/\text{Sqrt}[1-c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 4707

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(f*x)^m/\text{Sqrt}[d + e*x^2], x_Symbol] \rightarrow \text{Simp}[(f*(f*x)^{m-1}*\text{Sqrt}[d + e*x^2]*(a+b*\text{ArcSin}[c*x])^n)/(e*m), x] + (\text{Dist}[(f^2*(m-1))/(c^2*m), \text{Int}[(f*x)^{m-2}*(a+b*\text{ArcSin}[c*x])^n]/\text{Sqrt}[d + e*x^2], x], x] + \text{Dist}[(b*f*n*\text{Sqrt}[1-c^2*x^2])/(c*m*\text{Sqrt}[d + e*x^2]), \text{Int}[(f*x)^{m-1}*(a+b*\text{ArcSin}[c*x])^{n-1}], x], x] /; \text{FreeQ}\{a, b, c, d, e, f\}, x \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[n, 0] \ \&\& \ \text{GtQ}[m, 1] \ \&\& \ \text{IntegerQ}[m]$

Rule 4641

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n/\text{Sqrt}[d + e*x^2], x_Symbol] \rightarrow \text{Simp}[(a+b*\text{ArcSin}[c*x])^{n+1}/(b*c*\text{Sqrt}[d]*(n+1)), x] /; \text{FreeQ}\{a, b, c, d, e, n\}, x \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[d, 0] \ \&\& \ \text{NeQ}[n, -1]$

Rule 30

$\text{Int}[x^m, x_Symbol] \rightarrow \text{Simp}[x^{m+1}/(m+1), x] /; \text{FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rubi steps

$$\begin{aligned} \int x(a + b \sin^{-1}(cx))^2 dx &= \frac{1}{2}x^2(a + b \sin^{-1}(cx))^2 - (bc) \int \frac{x^2(a + b \sin^{-1}(cx))}{\sqrt{1 - c^2x^2}} dx \\ &= \frac{bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))}{2c} + \frac{1}{2}x^2(a + b \sin^{-1}(cx))^2 - \frac{1}{2}b^2 \int x dx - \frac{b \int \frac{a + b \sin^{-1}(cx)}{\sqrt{1 - c^2x^2}} dx}{2c} \\ &= -\frac{1}{4}b^2x^2 + \frac{bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))}{2c} - \frac{(a + b \sin^{-1}(cx))^2}{4c^2} + \frac{1}{2}x^2(a + b \sin^{-1}(cx))^2 \end{aligned}$$

Mathematica [A] time = 0.0734169, size = 73, normalized size = 0.96

$$-\frac{-2c^2x^2(a + b \sin^{-1}(cx))^2 - 2bcx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx)) + (a + b \sin^{-1}(cx))^2 + b^2c^2x^2}{4c^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*ArcSin[c*x])^2,x]

[Out] -(b^2*c^2*x^2 - 2*b*c*x*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]) + (a + b*ArcSin[c*x])^2 - 2*c^2*x^2*(a + b*ArcSin[c*x])^2)/(4*c^2)

Maple [A] time = 0.023, size = 120, normalized size = 1.6

$$\frac{1}{c^2} \left(\frac{a^2c^2x^2}{2} + b^2 \left(\frac{(c^2x^2 - 1)(\arcsin(cx))^2}{2} + \frac{\arcsin(cx)}{2} (cx\sqrt{-c^2x^2 + 1} + \arcsin(cx)) - \frac{(\arcsin(cx))^2}{4} - \frac{c^2x^2}{4} \right) + 2ab \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a+b*arcsin(c*x))^2,x)

[Out] 1/c^2*(1/2*a^2*c^2*x^2+b^2*(1/2*(c^2*x^2-1)*arcsin(c*x)^2+1/2*arcsin(c*x)*(c*x*(-c^2*x^2+1)^(1/2)+arcsin(c*x))-1/4*arcsin(c*x)^2-1/4*c^2*x^2)+2*a*b*(1/2*c^2*x^2*arcsin(c*x)+1/4*c*x*(-c^2*x^2+1)^(1/2)-1/4*arcsin(c*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{2}a^2x^2 + \frac{1}{2} \left(2x^2 \arcsin(cx) + c \left(\frac{\sqrt{-c^2x^2 + 1}x}{c^2} - \frac{\arcsin\left(\frac{cx}{\sqrt{c^2}}\right)}{\sqrt{c^2c^2}} \right) \right) ab + \frac{1}{2} \left(x^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^2 + 2c \int \frac{\sqrt{cx}}{\sqrt{1-c^2x^2}} dx \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] 1/2*a^2*x^2 + 1/2*(2*x^2*arcsin(c*x) + c*(sqrt(-c^2*x^2 + 1)*x/c^2 - arcsin(c^2*x/sqrt(c^2))/(sqrt(c^2)*c^2))*a*b + 1/2*(x^2*arctan2(c*x, sqrt(c*x + 1))*sqrt(-c*x + 1))^2 + 2*c*integrate(sqrt(c*x + 1)*sqrt(-c*x + 1)*x^2*arctan2(c*x, sqrt(c*x + 1))*sqrt(-c*x + 1)/(c^2*x^2 - 1), x)*b^2

Fricas [A] time = 1.48231, size = 221, normalized size = 2.91

$$\frac{(2a^2 - b^2)c^2x^2 + (2b^2c^2x^2 - b^2)\arcsin(cx)^2 + 2(2abc^2x^2 - ab)\arcsin(cx) + 2(b^2cx\arcsin(cx) + abcx)\sqrt{-c^2x^2 + 1}}{4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] 1/4*((2*a^2 - b^2)*c^2*x^2 + (2*b^2*c^2*x^2 - b^2)*arcsin(c*x)^2 + 2*(2*a*b*c^2*x^2 - a*b)*arcsin(c*x) + 2*(b^2*c*x*arcsin(c*x) + a*b*c*x)*sqrt(-c^2*x^2 + 1))/c^2

Sympy [A] time = 1.17421, size = 126, normalized size = 1.66

$$\begin{cases} \frac{a^2x^2}{2} + abx^2\arcsin(cx) + \frac{abx\sqrt{-c^2x^2+1}}{2c} - \frac{ab\arcsin(cx)}{2c^2} + \frac{b^2x^2\arcsin^2(cx)}{2} - \frac{b^2x^2}{4} + \frac{b^2x\sqrt{-c^2x^2+1}\arcsin(cx)}{2c} - \frac{b^2\arcsin^2(cx)}{4c^2} & \text{for } c \neq 0 \\ \frac{a^2x^2}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*asin(c*x))**2,x)

[Out] Piecewise((a**2*x**2/2 + a*b*x**2*asin(c*x) + a*b*x*sqrt(-c**2*x**2 + 1)/(2*c) - a*b*asin(c*x)/(2*c**2) + b**2*x**2*asin(c*x)**2/2 - b**2*x**2/4 + b**2*x*sqrt(-c**2*x**2 + 1)*asin(c*x)/(2*c) - b**2*asin(c*x)**2/(4*c**2), Ne(c, 0)), (a**2*x**2/2, True))

Giac [B] time = 1.29979, size = 209, normalized size = 2.75

$$\frac{\sqrt{-c^2x^2 + 1}b^2x\arcsin(cx)}{2c} + \frac{(c^2x^2 - 1)b^2\arcsin(cx)^2}{2c^2} + \frac{\sqrt{-c^2x^2 + 1}abx}{2c} + \frac{(c^2x^2 - 1)ab\arcsin(cx)}{c^2} + \frac{b^2\arcsin(cx)^2}{4c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^2,x, algorithm="giac")

[Out] 1/2*sqrt(-c^2*x^2 + 1)*b^2*x*arcsin(c*x)/c + 1/2*(c^2*x^2 - 1)*b^2*arcsin(c*x)^2/c^2 + 1/2*sqrt(-c^2*x^2 + 1)*a*b*x/c + (c^2*x^2 - 1)*a*b*arcsin(c*x)/c^2 + 1/4*b^2*arcsin(c*x)^2/c^2 + 1/2*(c^2*x^2 - 1)*a^2/c^2 - 1/4*(c^2*x^2 - 1)*b^2/c^2 + 1/2*a*b*arcsin(c*x)/c^2 - 1/8*b^2/c^2

3.150 $\int (a + b \sin^{-1}(cx))^2 dx$

Optimal. Leaf size=47

$$\frac{2b\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{c} + x(a+b\sin^{-1}(cx))^2 - 2b^2x$$

[Out] $-2*b^2*x + (2*b*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]))/c + x*(a + b*ArcSin[c*x])^2$

Rubi [A] time = 0.0602799, antiderivative size = 47, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4619, 4677, 8}

$$\frac{2b\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{c} + x(a+b\sin^{-1}(cx))^2 - 2b^2x$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^2, x]

[Out] $-2*b^2*x + (2*b*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]))/c + x*(a + b*ArcSin[c*x])^2$

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^n, x_Symbol] :> Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x]))^(n - 1)]/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^n*(x_)*((d_.) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1)], x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 8

Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]

Rubi steps

$$\begin{aligned} \int (a + b \sin^{-1}(cx))^2 dx &= x(a + b \sin^{-1}(cx))^2 - (2bc) \int \frac{x(a + b \sin^{-1}(cx))}{\sqrt{1 - c^2x^2}} dx \\ &= \frac{2b\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))}{c} + x(a + b \sin^{-1}(cx))^2 - (2b^2) \int 1 dx \\ &= -2b^2x + \frac{2b\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))}{c} + x(a + b \sin^{-1}(cx))^2 \end{aligned}$$

Mathematica [A] time = 0.0401299, size = 47, normalized size = 1.

$$\frac{2b\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))}{c} + x(a+b\sin^{-1}(cx))^2 - 2b^2x$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])^2,x]

[Out] -2*b^2*x + (2*b*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x]))/c + x*(a + b*ArcSin[c*x])^2

Maple [A] time = 0.023, size = 72, normalized size = 1.5

$$\frac{1}{c} \left(cxa^2 + b^2 \left(cx \arcsin(cx)^2 - 2cx + 2 \arcsin(cx) \sqrt{-c^2x^2 + 1} \right) + 2ab \left(cx \arcsin(cx) + \sqrt{-c^2x^2 + 1} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^2,x)

[Out] 1/c*(c*x*a^2+b^2*(c*x*arcsin(c*x)^2-2*c*x+2*arcsin(c*x)*(-c^2*x^2+1)^(1/2))+2*a*b*(c*x*arcsin(c*x)+(-c^2*x^2+1)^(1/2)))

Maxima [A] time = 1.56612, size = 97, normalized size = 2.06

$$b^2x \arcsin(cx)^2 - 2b^2 \left(x - \frac{\sqrt{-c^2x^2 + 1} \arcsin(cx)}{c} \right) + a^2x + \frac{2 \left(cx \arcsin(cx) + \sqrt{-c^2x^2 + 1} \right) ab}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] b^2*x*arcsin(c*x)^2 - 2*b^2*(x - sqrt(-c^2*x^2 + 1)*arcsin(c*x)/c) + a^2*x + 2*(c*x*arcsin(c*x) + sqrt(-c^2*x^2 + 1))*a*b/c

Fricas [A] time = 1.55504, size = 159, normalized size = 3.38

$$\frac{b^2cx \arcsin(cx)^2 + 2abcx \arcsin(cx) + (a^2 - 2b^2)cx + 2\sqrt{-c^2x^2 + 1}(b^2 \arcsin(cx) + ab)}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] (b^2*c*x*arcsin(c*x)^2 + 2*a*b*c*x*arcsin(c*x) + (a^2 - 2*b^2)*c*x + 2*sqrt(-c^2*x^2 + 1)*(b^2*arcsin(c*x) + a*b))/c

Sympy [A] time = 0.528404, size = 82, normalized size = 1.74

$$\begin{cases} a^2x + 2abx \operatorname{asin}(cx) + \frac{2ab\sqrt{-c^2x^2+1}}{c} + b^2x \operatorname{asin}^2(cx) - 2b^2x + \frac{2b^2\sqrt{-c^2x^2+1}\operatorname{asin}(cx)}{c} & \text{for } c \neq 0 \\ a^2x & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**2,x)

[Out] Piecewise((a**2*x + 2*a*b*x*asin(c*x) + 2*a*b*sqrt(-c**2*x**2 + 1)/c + b**2*x*asin(c*x)**2 - 2*b**2*x + 2*b**2*sqrt(-c**2*x**2 + 1)*asin(c*x)/c, Ne(c, 0)), (a**2*x, True))

Giac [A] time = 1.35122, size = 101, normalized size = 2.15

$$b^2x \operatorname{arcsin}(cx)^2 + 2abx \operatorname{arcsin}(cx) + a^2x - 2b^2x + \frac{2\sqrt{-c^2x^2+1}b^2 \operatorname{arcsin}(cx)}{c} + \frac{2\sqrt{-c^2x^2+1}ab}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2,x, algorithm="giac")

[Out] b^2*x*arcsin(c*x)^2 + 2*a*b*x*arcsin(c*x) + a^2*x - 2*b^2*x + 2*sqrt(-c^2*x^2 + 1)*b^2*arcsin(c*x)/c + 2*sqrt(-c^2*x^2 + 1)*a*b/c

$$3.151 \quad \int \frac{(a+b \sin^{-1}(cx))^2}{x} dx$$

Optimal. Leaf size=90

$$-ib \operatorname{PolyLog}\left(2, e^{2i \sin^{-1}(cx)}\right) (a+b \sin^{-1}(cx)) + \frac{1}{2} b^2 \operatorname{PolyLog}\left(3, e^{2i \sin^{-1}(cx)}\right) - \frac{i(a+b \sin^{-1}(cx))^3}{3b} + \log\left(1 - e^{2i \sin^{-1}(cx)}\right)$$

[Out] $((-I/3)*(a + b*\operatorname{ArcSin}[c*x])^3)/b + (a + b*\operatorname{ArcSin}[c*x])^2*\operatorname{Log}[1 - E^{((2*I)*\operatorname{ArcSin}[c*x])}] - I*b*(a + b*\operatorname{ArcSin}[c*x])* \operatorname{PolyLog}[2, E^{((2*I)*\operatorname{ArcSin}[c*x])}] + (b^2*\operatorname{PolyLog}[3, E^{((2*I)*\operatorname{ArcSin}[c*x])}])/2$

Rubi [A] time = 0.122593, antiderivative size = 90, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.429$, Rules used = {4625, 3717, 2190, 2531, 2282, 6589}

$$-ib \operatorname{PolyLog}\left(2, e^{2i \sin^{-1}(cx)}\right) (a+b \sin^{-1}(cx)) + \frac{1}{2} b^2 \operatorname{PolyLog}\left(3, e^{2i \sin^{-1}(cx)}\right) - \frac{i(a+b \sin^{-1}(cx))^3}{3b} + \log\left(1 - e^{2i \sin^{-1}(cx)}\right)$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])^2/x, x]$

[Out] $((-I/3)*(a + b*\operatorname{ArcSin}[c*x])^3)/b + (a + b*\operatorname{ArcSin}[c*x])^2*\operatorname{Log}[1 - E^{((2*I)*\operatorname{ArcSin}[c*x])}] - I*b*(a + b*\operatorname{ArcSin}[c*x])* \operatorname{PolyLog}[2, E^{((2*I)*\operatorname{ArcSin}[c*x])}] + (b^2*\operatorname{PolyLog}[3, E^{((2*I)*\operatorname{ArcSin}[c*x])}])/2$

Rule 4625

$\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])^2/x, x]$ \rightarrow $\operatorname{Subst}[\operatorname{Int}[(a + b*x)^n/\operatorname{Tan}[x], x], x, \operatorname{ArcSin}[c*x]]$ /; $\operatorname{FreeQ}\{a, b, c, x\}$ && $\operatorname{IGtQ}[n, 0]$

Rule 3717

$\operatorname{Int}[(c + d*x)^m*\operatorname{tan}[(e + \operatorname{Pi}*k) + (f + g*x)], x]$ \rightarrow $\operatorname{Simp}[(I*(c + d*x)^{m+1})/(d*(m+1)), x] - \operatorname{Dist}[2*I, \operatorname{Int}[(c + d*x)^m*\operatorname{E}^{(2*I*k*\operatorname{Pi})}*\operatorname{E}^{(2*I*(e + f*x))}/(1 + \operatorname{E}^{(2*I*k*\operatorname{Pi})}*\operatorname{E}^{(2*I*(e + f*x))}), x]$ /; $\operatorname{FreeQ}\{c, d, e, f, x\}$ && $\operatorname{IntegerQ}[4*k]$ && $\operatorname{IGtQ}[m, 0]$

Rule 2190

$\operatorname{Int}[(F + (g + d*x)^m*(e + f*x))^n*(c + d*x)^m, x]$ \rightarrow $\operatorname{Simp}[(c + d*x)^m*\operatorname{Log}[1 + (b*(F + (g + d*x)^m*(e + f*x))^n/a]/(b*f*g*n*\operatorname{Log}[F]), x] - \operatorname{Dist}[(d*m)/(b*f*g*n*\operatorname{Log}[F]), \operatorname{Int}[(c + d*x)^{m-1}*\operatorname{Log}[1 + (b*(F + (g + d*x)^m*(e + f*x))^n/a], x], x]$ /; $\operatorname{FreeQ}\{F, a, b, c, d, e, f, g, n, x\}$ && $\operatorname{IGtQ}[m, 0]$

Rule 2531

$\operatorname{Int}[\operatorname{Log}[1 + (e + g*x)^m*(F + (c + d*x)^n*(a + b*x))]^n, x]$ \rightarrow $-\operatorname{Simp}[(f + g*x)^m*\operatorname{PolyLog}[2, -(e*(F + (c + d*x)^n*(a + b*x)))^n]/(b*c*n*\operatorname{Log}[F]), x] + \operatorname{Dist}[(g*m)/(b*c*n*\operatorname{Log}[F]), \operatorname{Int}[(f + g*x)^{m-1}*\operatorname{PolyLog}[2, -(e*(F + (c + d*x)^n*(a + b*x)))^n], x], x]$ /; $\operatorname{FreeQ}\{F, a, b, c, e, f, g, n, x\}$ && $\operatorname{GtQ}[m, 0]$

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_)] /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int \frac{(a + b \sin^{-1}(cx))^2}{x} dx &= \text{Subst} \left(\int (a + bx)^2 \cot(x) dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{i(a + b \sin^{-1}(cx))^3}{3b} - 2i \text{Subst} \left(\int \frac{e^{2ix}(a + bx)^2}{1 - e^{2ix}} dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{i(a + b \sin^{-1}(cx))^3}{3b} + (a + b \sin^{-1}(cx))^2 \log(1 - e^{2i \sin^{-1}(cx)}) - (2b) \text{Subst} \left(\int (a + bx) \log(1 - e^{2ix}) dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{i(a + b \sin^{-1}(cx))^3}{3b} + (a + b \sin^{-1}(cx))^2 \log(1 - e^{2i \sin^{-1}(cx)}) - ib(a + b \sin^{-1}(cx)) \text{Li}_2(e^{2i \sin^{-1}(cx)}) \\ &= -\frac{i(a + b \sin^{-1}(cx))^3}{3b} + (a + b \sin^{-1}(cx))^2 \log(1 - e^{2i \sin^{-1}(cx)}) - ib(a + b \sin^{-1}(cx)) \text{Li}_2(e^{2i \sin^{-1}(cx)}) \\ &= -\frac{i(a + b \sin^{-1}(cx))^3}{3b} + (a + b \sin^{-1}(cx))^2 \log(1 - e^{2i \sin^{-1}(cx)}) - ib(a + b \sin^{-1}(cx)) \text{Li}_2(e^{2i \sin^{-1}(cx)}) \end{aligned}$$

Mathematica [A] time = 0.155712, size = 143, normalized size = 1.59

$$2ab \left(\sin^{-1}(cx) \log(1 - e^{2i \sin^{-1}(cx)}) - \frac{1}{2} i \left(\sin^{-1}(cx)^2 + \text{PolyLog}\left(2, e^{2i \sin^{-1}(cx)}\right) \right) \right) + b^2 \left(i \sin^{-1}(cx) \text{PolyLog}\left(2, e^{-2i \sin^{-1}(cx)}\right) \right)$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[(a + b*ArcSin[c*x])^2/x, x]
```

```
[Out] a^2*Log[c*x] + 2*a*b*(ArcSin[c*x]*Log[1 - E^((2*I)*ArcSin[c*x])]) - (I/2)*(A
rcSin[c*x]^2 + PolyLog[2, E^((2*I)*ArcSin[c*x])]) + b^2*((-I/24)*Pi^3 + (I
/3)*ArcSin[c*x]^3 + ArcSin[c*x]^2*Log[1 - E^((-2*I)*ArcSin[c*x])]) + I*ArcSi
n[c*x]*PolyLog[2, E^((-2*I)*ArcSin[c*x])] + PolyLog[3, E^((-2*I)*ArcSin[c*x
])]/2)
```

Maple [B] time = 0.03, size = 319, normalized size = 3.5

$$a^2 \ln(cx) - \frac{i}{3} b^2 (\arcsin(cx))^3 + b^2 (\arcsin(cx))^2 \ln(1 + icx + \sqrt{-c^2x^2 + 1}) - 2ib^2 \arcsin(cx) \text{polylog}\left(2, -icx - \sqrt{-c^2x^2 + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a+b*arcsin(c*x))^2/x, x)
```

```
[Out] a^2*ln(c*x)-1/3*I*b^2*arcsin(c*x)^3+b^2*arcsin(c*x)^2*ln(1+I*c*x+(-c^2*x^2+1)^(1/2))-2*I*b^2*arcsin(c*x)*polylog(2,-I*c*x-(-c^2*x^2+1)^(1/2))+2*b^2*polylog(3,-I*c*x-(-c^2*x^2+1)^(1/2))+b^2*arcsin(c*x)^2*ln(1-I*c*x-(-c^2*x^2+1)^(1/2))-2*I*b^2*arcsin(c*x)*polylog(2,I*c*x+(-c^2*x^2+1)^(1/2))+2*b^2*polylog(3,I*c*x+(-c^2*x^2+1)^(1/2))-I*a*b*arcsin(c*x)^2-2*I*a*b*polylog(2,I*c*x+(-c^2*x^2+1)^(1/2))-2*I*a*b*polylog(2,-I*c*x-(-c^2*x^2+1)^(1/2))+2*a*b*arcsin(c*x)*ln(1-I*c*x-(-c^2*x^2+1)^(1/2))+2*a*b*arcsin(c*x)*ln(1+I*c*x+(-c^2*x^2+1)^(1/2))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$a^2 \log(x) + \int \frac{b^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^2 + 2ab \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))^2/x,x, algorithm="maxima")
```

```
[Out] a^2*log(x) + integrate((b^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^2 + 2*a*b*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)))/x, x)
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))^2/x,x, algorithm="fricas")
```

```
[Out] integral((b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2)/x, x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(a + b \arcsin(cx))^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*asin(c*x))**2/x,x)
```

```
[Out] Integral((a + b*asin(c*x))**2/x, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))^2/x,x, algorithm="giac")
```

```
[Out] integrate((b*arcsin(c*x) + a)^2/x, x)
```

$$3.152 \quad \int \frac{(a+b \sin^{-1}(cx))^2}{x^2} dx$$

Optimal. Leaf size=81

$$2ib^2c \operatorname{PolyLog}\left(2, -e^{i \sin^{-1}(cx)}\right) - 2ib^2c \operatorname{PolyLog}\left(2, e^{i \sin^{-1}(cx)}\right) - \frac{(a+b \sin^{-1}(cx))^2}{x} - 4bc \tanh^{-1}\left(e^{i \sin^{-1}(cx)}\right)(a+b \sin^{-1}(cx))$$

[Out] -((a + b*ArcSin[c*x])^2/x) - 4*b*c*(a + b*ArcSin[c*x])*ArcTanh[E^(I*ArcSin[c*x])] + (2*I)*b^2*c*PolyLog[2, -E^(I*ArcSin[c*x])] - (2*I)*b^2*c*PolyLog[2, E^(I*ArcSin[c*x])]

Rubi [A] time = 0.128171, antiderivative size = 81, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {4627, 4709, 4183, 2279, 2391}

$$2ib^2c \operatorname{PolyLog}\left(2, -e^{i \sin^{-1}(cx)}\right) - 2ib^2c \operatorname{PolyLog}\left(2, e^{i \sin^{-1}(cx)}\right) - \frac{(a+b \sin^{-1}(cx))^2}{x} - 4bc \tanh^{-1}\left(e^{i \sin^{-1}(cx)}\right)(a+b \sin^{-1}(cx))$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^2/x^2,x]

[Out] -((a + b*ArcSin[c*x])^2/x) - 4*b*c*(a + b*ArcSin[c*x])*ArcTanh[E^(I*ArcSin[c*x])] + (2*I)*b^2*c*PolyLog[2, -E^(I*ArcSin[c*x])] - (2*I)*b^2*c*PolyLog[2, E^(I*ArcSin[c*x])]

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_.)*((d_.)*(x_)^ (m_.)), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4709

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_.)*(x_)^ (m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Dist[1/(c^(m + 1)*Sqrt[d]), Subst[Int[(a + b*x)^n*Sin[x]^m, x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && IGtQ[n, 0] && IntegerQ[m]

Rule 4183

Int[csc[(e_.) + (f_.)*(x_)]*((c_.) + (d_.)*(x_)^ (m_.)), x_Symbol] :> Simp[(-2*(c + d*x)^m*ArcTanh[E^(I*(e + f*x))])/f, x] + (-Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Log[1 - E^(I*(e + f*x))], x], x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Log[1 + E^(I*(e + f*x))], x], x]) /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]

Rule 2279

Int[Log[(a_) + (b_.)*((F_)^((e_.)*((c_.) + (d_.)*(x_))))^ (n_.)], x_Symbol] :> Dist[1/(d*e*n*Log[F]), Subst[Int[Log[a + b*x]/x, x], x, (F^(e*(c + d*x)))^n], x] /; FreeQ[{F, a, b, c, d, e, n}, x] && GtQ[a, 0]

Rule 2391

Int [Log[(c_.)*((d_) + (e_.)*(x_)^(n_.))]/(x_), x_Symbol] := -Simp [PolyLog [2, -(c*e*x^n)]/n, x] /; FreeQ[{c, d, e, n}, x] && EqQ[c*d, 1]

Rubi steps

$$\begin{aligned} \int \frac{(a + b \sin^{-1}(cx))^2}{x^2} dx &= -\frac{(a + b \sin^{-1}(cx))^2}{x} + (2bc) \int \frac{a + b \sin^{-1}(cx)}{x\sqrt{1-c^2x^2}} dx \\ &= -\frac{(a + b \sin^{-1}(cx))^2}{x} + (2bc) \text{Subst} \left(\int (a + bx) \csc(x) dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{(a + b \sin^{-1}(cx))^2}{x} - 4bc(a + b \sin^{-1}(cx)) \tanh^{-1}(e^{i \sin^{-1}(cx)}) - (2b^2c) \text{Subst} \left(\int \log(1 - e^{ix}) dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{(a + b \sin^{-1}(cx))^2}{x} - 4bc(a + b \sin^{-1}(cx)) \tanh^{-1}(e^{i \sin^{-1}(cx)}) + (2ib^2c) \text{Subst} \left(\int \frac{\log(1 - x)}{x} dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{(a + b \sin^{-1}(cx))^2}{x} - 4bc(a + b \sin^{-1}(cx)) \tanh^{-1}(e^{i \sin^{-1}(cx)}) + 2ib^2c \text{Li}_2(-e^{i \sin^{-1}(cx)}) - 2ib^2c \text{Li}_2(e^{i \sin^{-1}(cx)}) \end{aligned}$$

Mathematica [A] time = 0.225321, size = 126, normalized size = 1.56

$$\frac{-ib^2 \left(2cx \text{PolyLog} \left(2, -e^{i \sin^{-1}(cx)} \right) - 2cx \text{PolyLog} \left(2, e^{i \sin^{-1}(cx)} \right) + i \sin^{-1}(cx) \left(\sin^{-1}(cx) + 2cx \left(\log \left(1 + e^{i \sin^{-1}(cx)} \right) - \log \left(1 - e^{i \sin^{-1}(cx)} \right) \right) \right) \right)}{x}$$

Warning: Unable to verify antiderivative.

[In] Integrate[(a + b*ArcSin[c*x])^2/x^2,x]

[Out] -((a^2 + 2*a*b*(ArcSin[c*x] + c*x*ArcTanh[Sqrt[1 - c^2*x^2]]) - I*b^2*(I*ArcSin[c*x]*(ArcSin[c*x] + 2*c*x*(-Log[1 - E^(I*ArcSin[c*x]])] + Log[1 + E^(I*ArcSin[c*x]]))) + 2*c*x*PolyLog[2, -E^(I*ArcSin[c*x])] - 2*c*x*PolyLog[2, E^(I*ArcSin[c*x])]))/x

Maple [A] time = 0.056, size = 171, normalized size = 2.1

$$-\frac{a^2}{x} - \frac{b^2 (\arcsin(cx))^2}{x} + 2cb^2 \arcsin(cx) \ln \left(1 - icx - \sqrt{-c^2x^2 + 1} \right) - 2cb^2 \arcsin(cx) \ln \left(1 + icx + \sqrt{-c^2x^2 + 1} \right) - 2ib^2 \text{Li}_2(-e^{i \arcsin(cx)}) + 2ib^2 \text{Li}_2(e^{i \arcsin(cx)})$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^2/x^2,x)

[Out] -a^2/x - b^2/x*arcsin(c*x)^2 + 2*c*b^2*arcsin(c*x)*ln(1-I*c*x - (-c^2*x^2+1)^(1/2)) - 2*c*b^2*arcsin(c*x)*ln(1+I*c*x + (-c^2*x^2+1)^(1/2)) - 2*I*b^2*c*polylog(2, I*c*x + (-c^2*x^2+1)^(1/2)) + 2*I*b^2*c*polylog(2, -I*c*x - (-c^2*x^2+1)^(1/2)) - 2*a*b/x*arcsin(c*x) - 2*c*a*b*arctanh(1/(-c^2*x^2+1)^(1/2))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$-2 \left(c \log \left(\frac{2\sqrt{-c^2x^2+1}}{|x|} + \frac{2}{|x|} \right) + \frac{\arcsin(cx)}{x} \right) ab - \frac{\left(2cx \int \frac{\sqrt{-cx+1} \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}}{\sqrt{cx+1}(cx-1)x} dx + \arctan \left(cx, \sqrt{cx+1}\sqrt{-cx+1} \right) \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/x^2,x, algorithm="maxima")

[Out] $-2*(c*\log(2*\sqrt{-c^2*x^2 + 1})/\text{abs}(x) + 2/\text{abs}(x)) + \arcsin(c*x)/x)*a*b - (2*c*x*\int(\sqrt{c*x + 1}*\sqrt{-c*x + 1}*\arctan2(c*x, \sqrt{c*x + 1}*\sqrt{-c*x + 1}))/(\text{c}^2*x^3 - x), x) + \arctan2(c*x, \sqrt{c*x + 1}*\sqrt{-c*x + 1})^2)*b^2/x - a^2/x$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\int \left(\frac{b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2}{x^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/x^2,x, algorithm="fricas")

[Out] integral((b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2)/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(a + b \arcsin(cx))^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**2/x**2,x)

[Out] Integral((a + b*asin(c*x))**2/x**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/x^2,x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)^2/x^2, x)

3.153 $\int x^2 (a + b \sin^{-1}(cx))^3 dx$

Optimal. Leaf size=178

$$-\frac{4ab^2x}{3c^2} - \frac{2}{9}b^2x^3(a + b \sin^{-1}(cx)) + \frac{bx^2\sqrt{1-c^2x^2}(a + b \sin^{-1}(cx))^2}{3c} + \frac{2b\sqrt{1-c^2x^2}(a + b \sin^{-1}(cx))^2}{3c^3} + \frac{1}{3}x^3(a + b \sin^{-1}(cx))^3$$

[Out] $(-4*a*b^2*x)/(3*c^2) - (14*b^3*sqrt[1 - c^2*x^2])/(9*c^3) + (2*b^3*(1 - c^2*x^2)^{(3/2)})/(27*c^3) - (4*b^3*x*ArcSin[c*x])/(3*c^2) - (2*b^2*x^3*(a + b*ArcSin[c*x]))/9 + (2*b*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2)/(3*c^3) + (b*x^2*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2)/(3*c) + (x^3*(a + b*ArcSin[c*x])^3)/3$

Rubi [A] time = 0.296877, antiderivative size = 178, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 7, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4627, 4707, 4677, 4619, 261, 266, 43}

$$-\frac{4ab^2x}{3c^2} - \frac{2}{9}b^2x^3(a + b \sin^{-1}(cx)) + \frac{bx^2\sqrt{1-c^2x^2}(a + b \sin^{-1}(cx))^2}{3c} + \frac{2b\sqrt{1-c^2x^2}(a + b \sin^{-1}(cx))^2}{3c^3} + \frac{1}{3}x^3(a + b \sin^{-1}(cx))^3$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*ArcSin[c*x])^3,x]

[Out] $(-4*a*b^2*x)/(3*c^2) - (14*b^3*sqrt[1 - c^2*x^2])/(9*c^3) + (2*b^3*(1 - c^2*x^2)^{(3/2)})/(27*c^3) - (4*b^3*x*ArcSin[c*x])/(3*c^2) - (2*b^2*x^3*(a + b*ArcSin[c*x]))/9 + (2*b*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2)/(3*c^3) + (b*x^2*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2)/(3*c) + (x^3*(a + b*ArcSin[c*x])^3)/3$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((f_.)*(x_))^(m_)]/sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m], Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/sqrt[d + e*x^2], x], x] + Dist[(b*f*n*sqrt[1 - c^2*x^2])/(c*m*sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] :> Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d*IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^n, x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 261

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_.))^p, x_Symbol] := Simp[(a + b*x^n)^(p + 1)/(b*n*(p + 1)), x] /; FreeQ[{a, b, m, n, p}, x] && EqQ[m, n - 1] && NeQ[p, -1]

Rule 266

Int[(x_)^(m_.)*((a_) + (b_.)*(x_)^(n_.))^p, x_Symbol] := Dist[1/n, Subst[Int[x^(Simplify[(m + 1)/n] - 1)*(a + b*x)^p, x], x, x^n], x] /; FreeQ[{a, b, m, n, p}, x] && IntegerQ[Simplify[(m + 1)/n]]

Rule 43

Int[((a_.) + (b_.)*(x_.))^(m_.)*((c_.) + (d_.)*(x_.))^n, x_Symbol] := Int[ExpandIntegrand[(a + b*x)^m*(c + d*x)^n, x], x] /; FreeQ[{a, b, c, d, n}, x] && NeQ[b*c - a*d, 0] && IGtQ[m, 0] && (!IntegerQ[n] || (EqQ[c, 0] && LeQ[7*m + 4*n + 4, 0]) || LtQ[9*m + 5*(n + 1), 0]) || GtQ[m + n + 2, 0]

Rubi steps

$$\begin{aligned} \int x^2 (a + b \sin^{-1}(cx))^3 dx &= \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^3 - (bc) \int \frac{x^3 (a + b \sin^{-1}(cx))^2}{\sqrt{1 - c^2 x^2}} dx \\ &= \frac{bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2}{3c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^3 - \frac{1}{3} (2b^2) \int x^2 (a + b \sin^{-1}(cx))^2 dx \\ &= -\frac{2}{9} b^2 x^3 (a + b \sin^{-1}(cx)) + \frac{2b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{3c} \\ &= -\frac{4ab^2 x}{3c^2} - \frac{2}{9} b^2 x^3 (a + b \sin^{-1}(cx)) + \frac{2b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{3c} \\ &= -\frac{4ab^2 x}{3c^2} - \frac{4b^3 x \sin^{-1}(cx)}{3c^2} - \frac{2}{9} b^2 x^3 (a + b \sin^{-1}(cx)) + \frac{2b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))}{3c} \\ &= -\frac{4ab^2 x}{3c^2} - \frac{14b^3 \sqrt{1 - c^2 x^2}}{9c^3} + \frac{2b^3 (1 - c^2 x^2)^{3/2}}{27c^3} - \frac{4b^3 x \sin^{-1}(cx)}{3c^2} - \frac{2}{9} b^2 x^3 (a + b \sin^{-1}(cx)) \end{aligned}$$

Mathematica [A] time = 0.40945, size = 163, normalized size = 0.92

$$\frac{1}{27} \left(\frac{b \left(9c^2 x^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2 - 2b \left(3c^3 x^3 (a + b \sin^{-1}(cx)) + b \sqrt{1 - c^2 x^2} (c^2 x^2 + 2) \right) + 18 \left(\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx)) \right)^2 \right)}{c^3} \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*(a + b*ArcSin[c*x])^3,x]

[Out] (9*x^3*(a + b*ArcSin[c*x])^3 + (b*(9*c^2*x^2*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2 - 2*b*(b*Sqrt[1 - c^2*x^2]*(2 + c^2*x^2) + 3*c^3*x^3*(a + b*ArcSi

$n[c*x])) + 18*(\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^2 - 2*b*(a*c*x + b*\text{Sqrt}[1 - c^2*x^2] + b*c*x*\text{ArcSin}[c*x])))/c^3)/27$

Maple [A] time = 0.029, size = 235, normalized size = 1.3

$$\frac{1}{c^3} \left(\frac{a^3 c^3 x^3}{3} + b^3 \left(\frac{c^3 x^3 (\arcsin(cx))^3}{3} + \frac{(\arcsin(cx))^2 (c^2 x^2 + 2)}{3} \sqrt{-c^2 x^2 + 1} - \frac{4}{3} \sqrt{-c^2 x^2 + 1} - \frac{4cx \arcsin(cx)}{3} - \frac{2c^3 x^3 a}{3} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(a+b*arcsin(c*x))^3,x)`

[Out] $\frac{1}{c^3} * (\frac{1}{3} * a^3 * c^3 * x^3 + b^3 * (\frac{1}{3} * c^3 * x^3 * \arcsin(c*x)^3 + \frac{1}{3} * \arcsin(c*x)^2 * (c^2 * x^2 + 2) * (-c^2 * x^2 + 1)^{(1/2)} - \frac{4}{3} * (-c^2 * x^2 + 1)^{(1/2)} - \frac{4}{3} * c * x * \arcsin(c*x) - \frac{2}{9} * c^3 * x^3 * \arcsin(c*x) - \frac{2}{27} * (c^2 * x^2 + 2) * (-c^2 * x^2 + 1)^{(1/2)}) + 3 * a * b^2 * (\frac{1}{3} * c^3 * x^3 * \arcsin(c*x)^2 + \frac{2}{9} * \arcsin(c*x) * (c^2 * x^2 + 2) * (-c^2 * x^2 + 1)^{(1/2)} - \frac{2}{27} * c^3 * x^3 - \frac{4}{9} * c * x) + 3 * a^2 * b * (\frac{1}{3} * c^3 * x^3 * \arcsin(c*x) + \frac{1}{9} * c^2 * x^2 * (-c^2 * x^2 + 1)^{(1/2)} + \frac{2}{9} * (-c^2 * x^2 + 1)^{(1/2)}))$

Maxima [A] time = 1.88801, size = 369, normalized size = 2.07

$$\frac{1}{3} b^3 x^3 \arcsin(cx)^3 + ab^2 x^3 \arcsin(cx)^2 + \frac{1}{3} a^3 x^3 + \frac{1}{3} \left(3x^3 \arcsin(cx) + c \left(\frac{\sqrt{-c^2 x^2 + 1} x^2}{c^2} + \frac{2\sqrt{-c^2 x^2 + 1}}{c^4} \right) \right) a^2 b + \frac{2}{9} \left(3c^3 x^3 \arcsin(cx)^2 + 2c^2 x^2 \arcsin(cx) + c \sqrt{-c^2 x^2 + 1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(a+b*arcsin(c*x))^3,x, algorithm="maxima")`

[Out] $\frac{1}{3} * b^3 * x^3 * \arcsin(c*x)^3 + a * b^2 * x^3 * \arcsin(c*x)^2 + \frac{1}{3} * a^3 * x^3 + \frac{1}{3} * (3 * x^3 * \arcsin(c*x) + c * (\text{sqrt}(-c^2 * x^2 + 1) * x^2 / c^2 + 2 * \text{sqrt}(-c^2 * x^2 + 1) / c^4)) * a^2 * b + \frac{2}{9} * (3 * c * (\text{sqrt}(-c^2 * x^2 + 1) * x^2 / c^2 + 2 * \text{sqrt}(-c^2 * x^2 + 1) / c^4) * \arcsin(c*x) - (c^2 * x^3 + 6 * x) / c^2 * a * b^2 + \frac{1}{27} * (9 * c * (\text{sqrt}(-c^2 * x^2 + 1) * x^2 / c^2 + 2 * \text{sqrt}(-c^2 * x^2 + 1) / c^4) * \arcsin(c*x)^2 - 2 * c * ((\text{sqrt}(-c^2 * x^2 + 1) * x^2 + 20 * \text{sqrt}(-c^2 * x^2 + 1) / c^2) / c^2 + 3 * (c^2 * x^3 + 6 * x) * \arcsin(c*x) / c^3)) * b^3$

Fricas [A] time = 1.80444, size = 441, normalized size = 2.48

$$9b^3c^3x^3 \arcsin(cx)^3 + 27ab^2c^3x^3 \arcsin(cx)^2 + 3(3a^3 - 2ab^2)c^3x^3 - 36ab^2cx + 3((9a^2b - 2b^3)c^3x^3 - 12b^3cx) \arcsin(cx)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(a+b*arcsin(c*x))^3,x, algorithm="fricas")`

[Out] $\frac{1}{27} * (9 * b^3 * c^3 * x^3 * \arcsin(c*x)^3 + 27 * a * b^2 * c^3 * x^3 * \arcsin(c*x)^2 + 3 * (3 * a^3 - 2 * a * b^2) * c^3 * x^3 - 36 * a * b^2 * c * x + 3 * ((9 * a^2 * b - 2 * b^3) * c^3 * x^3 - 12 * b^3 * c * x) * \arcsin(c*x) + ((9 * a^2 * b - 2 * b^3) * c^2 * x^2 + 18 * a^2 * b - 40 * b^3 + 9 * (b^3 * c^2 * x^2 + 2 * b^3) * \arcsin(c*x)^2 + 18 * (a * b^2 * c^2 * x^2 + 2 * a * b^2) * \arcsin(c*x)) * \text{sqrt}(-c^2 * x^2 + 1)) / c^3$

Sympy [A] time = 3.74468, size = 328, normalized size = 1.84

$$\left\{ \begin{array}{l} \frac{a^3 x^3}{3} + a^2 b x^3 \operatorname{asin}(cx) + \frac{a^2 b x^2 \sqrt{-c^2 x^2 + 1}}{3c} + \frac{2a^2 b \sqrt{-c^2 x^2 + 1}}{3c^3} + ab^2 x^3 \operatorname{asin}^2(cx) - \frac{2ab^2 x^3}{9} + \frac{2ab^2 x^2 \sqrt{-c^2 x^2 + 1} \operatorname{asin}(cx)}{3c} - \frac{4ab^2 x}{3c^2} + \frac{4ab^2}{3} \end{array} \right.$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(a+b*asin(c*x))**3,x)

[Out] Piecewise((a**3*x**3/3 + a**2*b*x**3*asin(c*x) + a**2*b*x**2*sqrt(-c**2*x**2 + 1)/(3*c) + 2*a**2*b*sqrt(-c**2*x**2 + 1)/(3*c**3) + a*b**2*x**3*asin(c*x)**2 - 2*a*b**2*x**3/9 + 2*a*b**2*x**2*sqrt(-c**2*x**2 + 1)*asin(c*x)/(3*c) - 4*a*b**2*x/(3*c**2) + 4*a*b**2*sqrt(-c**2*x**2 + 1)*asin(c*x)/(3*c**3) + b**3*x**3*asin(c*x)**3/3 - 2*b**3*x**3*asin(c*x)/9 + b**3*x**2*sqrt(-c**2*x**2 + 1)*asin(c*x)**2/(3*c) - 2*b**3*x**2*sqrt(-c**2*x**2 + 1)/(27*c) - 4*b**3*x*asin(c*x)/(3*c**2) + 2*b**3*sqrt(-c**2*x**2 + 1)*asin(c*x)**2/(3*c**3) - 40*b**3*sqrt(-c**2*x**2 + 1)/(27*c**3), Ne(c, 0)), (a**3*x**3/3, True))

Giac [B] time = 1.45838, size = 497, normalized size = 2.79

$$\frac{1}{3} a^3 x^3 + \frac{(c^2 x^2 - 1) b^3 x \operatorname{arcsin}(cx)^3}{3c^2} + \frac{(c^2 x^2 - 1) ab^2 x \operatorname{arcsin}(cx)^2}{c^2} + \frac{b^3 x \operatorname{arcsin}(cx)^3}{3c^2} + \frac{(c^2 x^2 - 1) a^2 b x \operatorname{arcsin}(cx)}{c^2} -$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^3,x, algorithm="giac")

[Out] 1/3*a^3*x^3 + 1/3*(c^2*x^2 - 1)*b^3*x*arcsin(c*x)^3/c^2 + (c^2*x^2 - 1)*a*b^2*x*arcsin(c*x)^2/c^2 + 1/3*b^3*x*arcsin(c*x)^3/c^2 + (c^2*x^2 - 1)*a^2*b*x*arcsin(c*x)/c^2 - 2/9*(c^2*x^2 - 1)*b^3*x*arcsin(c*x)/c^2 + a*b^2*x*arcsin(c*x)^2/c^2 - 1/3*(-c^2*x^2 + 1)^(3/2)*b^3*arcsin(c*x)^2/c^3 - 2/9*(c^2*x^2 - 1)*a*b^2*x/c^2 + a^2*b*x*arcsin(c*x)/c^2 - 14/9*b^3*x*arcsin(c*x)/c^2 - 2/3*(-c^2*x^2 + 1)^(3/2)*a*b^2*arcsin(c*x)/c^3 + sqrt(-c^2*x^2 + 1)*b^3*arcsin(c*x)^2/c^3 - 14/9*a*b^2*x/c^2 - 1/3*(-c^2*x^2 + 1)^(3/2)*a^2*b/c^3 + 2/27*(-c^2*x^2 + 1)^(3/2)*b^3/c^3 + 2*sqrt(-c^2*x^2 + 1)*a*b^2*arcsin(c*x)/c^3 + sqrt(-c^2*x^2 + 1)*a^2*b/c^3 - 14/9*sqrt(-c^2*x^2 + 1)*b^3/c^3

3.154 $\int x \left(a + b \sin^{-1}(cx) \right)^3 dx$

Optimal. Leaf size=125

$$-\frac{3}{4}b^2x^2(a + b \sin^{-1}(cx)) + \frac{3bx\sqrt{1-c^2x^2}(a + b \sin^{-1}(cx))^2}{4c} - \frac{(a + b \sin^{-1}(cx))^3}{4c^2} + \frac{1}{2}x^2(a + b \sin^{-1}(cx))^3 - \frac{3b^3x\sqrt{1-c^2x^2}}{8c}$$

[Out] $(-3*b^3*x*sqrt[1 - c^2*x^2])/(8*c) + (3*b^3*ArcSin[c*x])/(8*c^2) - (3*b^2*x^2*(a + b*ArcSin[c*x]))/4 + (3*b*x*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2)/(4*c) - (a + b*ArcSin[c*x])^3/(4*c^2) + (x^2*(a + b*ArcSin[c*x])^3)/2$

Rubi [A] time = 0.204622, antiderivative size = 125, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {4627, 4707, 4641, 321, 216}

$$-\frac{3}{4}b^2x^2(a + b \sin^{-1}(cx)) + \frac{3bx\sqrt{1-c^2x^2}(a + b \sin^{-1}(cx))^2}{4c} - \frac{(a + b \sin^{-1}(cx))^3}{4c^2} + \frac{1}{2}x^2(a + b \sin^{-1}(cx))^3 - \frac{3b^3x\sqrt{1-c^2x^2}}{8c}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*ArcSin[c*x])^3,x]

[Out] $(-3*b^3*x*sqrt[1 - c^2*x^2])/(8*c) + (3*b^3*ArcSin[c*x])/(8*c^2) - (3*b^2*x^2*(a + b*ArcSin[c*x]))/4 + (3*b*x*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2)/(4*c) - (a + b*ArcSin[c*x])^3/(4*c^2) + (x^2*(a + b*ArcSin[c*x])^3)/2$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)*((f_.)*(x_))^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 321

Int[((c_.)*(x_))^(m_)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(c^(n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), Int[(c*x)^(m - n)*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n - 1] && NeQ[m + n*p

+ 1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 216

Int[1/Sqrt[(a_) + (b_.)*(x_)^2], x_Symbol] := Simp[ArcSin[(Rt[-b, 2]*x)/Sqrt[a]]/Rt[-b, 2], x] /; FreeQ[{a, b}, x] && GtQ[a, 0] && NegQ[b]

Rubi steps

$$\begin{aligned}
 \int x(a + b \sin^{-1}(cx))^3 dx &= \frac{1}{2}x^2(a + b \sin^{-1}(cx))^3 - \frac{1}{2}(3bc) \int \frac{x^2(a + b \sin^{-1}(cx))^2}{\sqrt{1 - c^2x^2}} dx \\
 &= \frac{3bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{4c} + \frac{1}{2}x^2(a + b \sin^{-1}(cx))^3 - \frac{1}{2}(3b^2) \int x(a + b \sin^{-1}(cx))^2 dx \\
 &= -\frac{3}{4}b^2x^2(a + b \sin^{-1}(cx)) + \frac{3bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{4c} - \frac{(a + b \sin^{-1}(cx))^3}{4c^2} + \frac{1}{2}x^2(a + b \sin^{-1}(cx))^3 \\
 &= -\frac{3b^3x\sqrt{1 - c^2x^2}}{8c} - \frac{3}{4}b^2x^2(a + b \sin^{-1}(cx)) + \frac{3bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{4c} - \frac{(a + b \sin^{-1}(cx))^3}{4c^2} \\
 &= -\frac{3b^3x\sqrt{1 - c^2x^2}}{8c} + \frac{3b^3 \sin^{-1}(cx)}{8c^2} - \frac{3}{4}b^2x^2(a + b \sin^{-1}(cx)) + \frac{3bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{4c}
 \end{aligned}$$

Mathematica [A] time = 0.14751, size = 114, normalized size = 0.91

$$\frac{-3b^2 \left(cx \left(2acx + b\sqrt{1 - c^2x^2} \right) + b \left(2c^2x^2 - 1 \right) \sin^{-1}(cx) \right) + 4c^2x^2 \left(a + b \sin^{-1}(cx) \right)^3 + 6bcx\sqrt{1 - c^2x^2} \left(a + b \sin^{-1}(cx) \right)^2}{8c^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*(a + b*ArcSin[c*x])^3,x]

[Out] (6*b*c*x*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2 - 2*(a + b*ArcSin[c*x])^3 + 4*c^2*x^2*(a + b*ArcSin[c*x])^3 - 3*b^2*(c*x*(2*a*c*x + b*Sqrt[1 - c^2*x^2]) + b*(-1 + 2*c^2*x^2)*ArcSin[c*x]))/(8*c^2)

Maple [A] time = 0.027, size = 219, normalized size = 1.8

$$\frac{1}{c^2} \left(\frac{c^2x^2a^3}{2} + b^3 \left(\frac{(c^2x^2 - 1)(\arcsin(cx))^3}{2} + \frac{3(\arcsin(cx))^2}{4} \left(cx\sqrt{-c^2x^2 + 1} + \arcsin(cx) \right) - \frac{(3c^2x^2 - 3)\arcsin(cx)}{4} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a+b*arcsin(c*x))^3,x)

[Out] 1/c^2*(1/2*c^2*x^2*a^3+b^3*(1/2*(c^2*x^2-1)*arcsin(c*x)^3+3/4*arcsin(c*x)^2*(c*x*(-c^2*x^2+1)^(1/2)+arcsin(c*x))-3/4*(c^2*x^2-1)*arcsin(c*x)-3/8*c*x*(-c^2*x^2+1)^(1/2)-3/8*arcsin(c*x)-1/2*arcsin(c*x)^3)+3*a*b^2*(1/2*(c^2*x^2-1)*arcsin(c*x)^2+1/2*arcsin(c*x)*(c*x*(-c^2*x^2+1)^(1/2)+arcsin(c*x))-1/4*arcsin(c*x)^2-1/4*c^2*x^2)+3*a^2*b*(1/2*c^2*x^2*arcsin(c*x)+1/4*c*x*(-c^2*x^2+1)^(1/2)-1/4*arcsin(c*x)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{1}{2} b^3 x^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^3 + \frac{1}{2} a^3 x^2 + \frac{3}{4} \left(2x^2 \arcsin(cx) + c \left(\frac{\sqrt{-c^2x^2+1}x}{c^2} - \frac{\arcsin\left(\frac{c^2x}{\sqrt{c^2}}\right)}{\sqrt{c^2c^2}} \right) \right) a^2 b + \int \frac{3(\sqrt{c^2x^2+1})}{c^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^3,x, algorithm="maxima")

[Out] 1/2*b^3*x^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^3 + 1/2*a^3*x^2 + 3/4*(2*x^2*arcsin(c*x) + c*(sqrt(-c^2*x^2 + 1)*x/c^2 - arcsin(c^2*x/sqrt(c^2))/(sqrt(c^2)*c^2))*a^2*b + integrate(3/2*(sqrt(c*x + 1)*sqrt(-c*x + 1)*b^3*c*x^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^2 + 2*(a*b^2*c^2*x^3 - a*b^2*x)*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^2)/(c^2*x^2 - 1), x)

Fricas [A] time = 1.68147, size = 378, normalized size = 3.02

$$\frac{2(2a^3 - 3ab^2)c^2x^2 + 2(2b^3c^2x^2 - b^3)\arcsin(cx)^3 + 6(2ab^2c^2x^2 - ab^2)\arcsin(cx)^2 + 3(2(2a^2b - b^3)c^2x^2 - 2a^2b + b^3)}{8c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^3,x, algorithm="fricas")

[Out] 1/8*(2*(2*a^3 - 3*a*b^2)*c^2*x^2 + 2*(2*b^3*c^2*x^2 - b^3)*arcsin(c*x)^3 + 6*(2*a*b^2*c^2*x^2 - a*b^2)*arcsin(c*x)^2 + 3*(2*(2*a^2*b - b^3)*c^2*x^2 - 2*a^2*b + b^3)*arcsin(c*x) + 3*(2*b^3*c*x*arcsin(c*x)^2 + 4*a*b^2*c*x*arcsin(c*x) + (2*a^2*b - b^3)*c*x)*sqrt(-c^2*x^2 + 1))/c^2

Sympy [A] time = 1.89282, size = 264, normalized size = 2.11

$$\frac{\frac{a^3x^2}{2} + \frac{3a^2bx^2\arcsin(cx)}{2} + \frac{3a^2bx\sqrt{-c^2x^2+1}}{4c} - \frac{3a^2b\arcsin(cx)}{4c^2} + \frac{3ab^2x^2\arcsin^2(cx)}{2} - \frac{3ab^2x^2}{4} + \frac{3ab^2x\sqrt{-c^2x^2+1}\arcsin(cx)}{2c} - \frac{3ab^2\arcsin^2(cx)}{4c^2} + \frac{b^3x^2\arcsin^3(cx)}{2}}{\frac{a^3x^2}{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*asin(c*x))**3,x)

[Out] Piecewise((a**3*x**2/2 + 3*a**2*b*x**2*asin(c*x)/2 + 3*a**2*b*x*sqrt(-c**2*x**2 + 1)/(4*c) - 3*a**2*b*asin(c*x)/(4*c**2) + 3*a*b**2*x**2*asin(c*x)**2/2 - 3*a*b**2*x**2/4 + 3*a*b**2*x*sqrt(-c**2*x**2 + 1)*asin(c*x)/(2*c) - 3*a*b**2*asin(c*x)**2/(4*c**2) + b**3*x**2*asin(c*x)**3/2 - 3*b**3*x**2*asin(c*x)/4 + 3*b**3*x*sqrt(-c**2*x**2 + 1)*asin(c*x)**2/(4*c) - 3*b**3*x*sqrt(-c**2*x**2 + 1)/(8*c) - b**3*asin(c*x)**3/(4*c**2) + 3*b**3*asin(c*x)/(8*c**2), Ne(c, 0)), (a**3*x**2/2, True))

Giac [B] time = 1.47751, size = 385, normalized size = 3.08

$$\frac{3\sqrt{-c^2x^2+1}b^3x\arcsin(cx)^2}{4c} + \frac{(c^2x^2-1)b^3\arcsin(cx)^3}{2c^2} + \frac{3\sqrt{-c^2x^2+1}ab^2x\arcsin(cx)}{2c} + \frac{3(c^2x^2-1)ab^2\arcsin(cx)^2}{2c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(a+b*arcsin(c*x))^3,x, algorithm="giac")
```

```
[Out] 3/4*sqrt(-c^2*x^2 + 1)*b^3*x*arcsin(c*x)^2/c + 1/2*(c^2*x^2 - 1)*b^3*arcsin
(c*x)^3/c^2 + 3/2*sqrt(-c^2*x^2 + 1)*a*b^2*x*arcsin(c*x)/c + 3/2*(c^2*x^2 -
1)*a*b^2*arcsin(c*x)^2/c^2 + 1/4*b^3*arcsin(c*x)^3/c^2 + 3/4*sqrt(-c^2*x^2
+ 1)*a^2*b*x/c - 3/8*sqrt(-c^2*x^2 + 1)*b^3*x/c + 3/2*(c^2*x^2 - 1)*a^2*b*
arcsin(c*x)/c^2 - 3/4*(c^2*x^2 - 1)*b^3*arcsin(c*x)/c^2 + 3/4*a*b^2*arcsin(
c*x)^2/c^2 + 1/2*(c^2*x^2 - 1)*a^3/c^2 - 3/4*(c^2*x^2 - 1)*a*b^2/c^2 + 3/4*
a^2*b*arcsin(c*x)/c^2 - 3/8*b^3*arcsin(c*x)/c^2 - 3/8*a*b^2/c^2
```

3.155 $\int (a + b \sin^{-1}(cx))^3 dx$

Optimal. Leaf size=82

$$-6ab^2x + \frac{3b\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))^2}{c} + x(a+b\sin^{-1}(cx))^3 - \frac{6b^3\sqrt{1-c^2x^2}}{c} - 6b^3x\sin^{-1}(cx)$$

[Out] $-6*a*b^2*x - (6*b^3*\text{Sqrt}[1 - c^2*x^2])/c - 6*b^3*x*\text{ArcSin}[c*x] + (3*b*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^2)/c + x*(a + b*\text{ArcSin}[c*x])^3$

Rubi [A] time = 0.108703, antiderivative size = 82, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 3, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.3$, Rules used = {4619, 4677, 261}

$$-6ab^2x + \frac{3b\sqrt{1-c^2x^2}(a+b\sin^{-1}(cx))^2}{c} + x(a+b\sin^{-1}(cx))^3 - \frac{6b^3\sqrt{1-c^2x^2}}{c} - 6b^3x\sin^{-1}(cx)$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*\text{ArcSin}[c*x])^3, x]$

[Out] $-6*a*b^2*x - (6*b^3*\text{Sqrt}[1 - c^2*x^2])/c - 6*b^3*x*\text{ArcSin}[c*x] + (3*b*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^2)/c + x*(a + b*\text{ArcSin}[c*x])^3$

Rule 4619

$\text{Int}[(a + \text{ArcSin}[c*x])^n, x] := \text{Simp}[x*(a + b*\text{ArcSin}[c*x])^n, x] - \text{Dist}[b*c^n, \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{n-1})/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4677

$\text{Int}[(a + \text{ArcSin}[c*x])^n * (d + e*x^2)^p, x] := \text{Simp}[(d + e*x^2)^{p+1} * (a + b*\text{ArcSin}[c*x])^n / (2*e*(p+1)), x] + \text{Dist}[b*n*d^{\text{IntPart}[p]} * (d + e*x^2)^{\text{FracPart}[p]} / (2*c*(p+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(1 - c^2*x^2)^{p+1/2} * (a + b*\text{ArcSin}[c*x])^{n-1}, x], x] /;$ FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 261

$\text{Int}[x^m * (a + b*x^n)^p, x] := \text{Simp}[(a + b*x^n)^{p+1} / (b*n*(p+1)), x] /;$ FreeQ[{a, b, m, n, p}, x] && EqQ[m, n-1] && NeQ[p, -1]

Rubi steps

$$\begin{aligned}
\int (a + b \sin^{-1}(cx))^3 dx &= x(a + b \sin^{-1}(cx))^3 - (3bc) \int \frac{x(a + b \sin^{-1}(cx))^2}{\sqrt{1 - c^2x^2}} dx \\
&= \frac{3b\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{c} + x(a + b \sin^{-1}(cx))^3 - (6b^2) \int (a + b \sin^{-1}(cx)) dx \\
&= -6ab^2x + \frac{3b\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{c} + x(a + b \sin^{-1}(cx))^3 - (6b^3) \int \sin^{-1}(cx) dx \\
&= -6ab^2x - 6b^3x \sin^{-1}(cx) + \frac{3b\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{c} + x(a + b \sin^{-1}(cx))^3 + (6b^3c) \int \frac{1}{\sqrt{1 - c^2x^2}} dx \\
&= -6ab^2x - \frac{6b^3\sqrt{1 - c^2x^2}}{c} - 6b^3x \sin^{-1}(cx) + \frac{3b\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^2}{c} + x(a + b \sin^{-1}(cx))^3 + (6b^3c) \int \frac{1}{\sqrt{1 - c^2x^2}} dx
\end{aligned}$$

Mathematica [A] time = 0.0881327, size = 77, normalized size = 0.94

$$\frac{3b \left(\sqrt{1 - c^2x^2} (a + b \sin^{-1}(cx))^2 - 2b (acx + b\sqrt{1 - c^2x^2} + bcx \sin^{-1}(cx)) \right)}{c} + x(a + b \sin^{-1}(cx))^3$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])^3,x]

[Out] x*(a + b*ArcSin[c*x])^3 + (3*b*(Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^2 - 2*b*(a*c*x + b*Sqrt[1 - c^2*x^2] + b*c*x*ArcSin[c*x])))/c

Maple [A] time = 0.024, size = 132, normalized size = 1.6

$$\frac{1}{c} \left(cxa^3 + b^3 \left(cx (\arcsin(cx))^3 + 3 (\arcsin(cx))^2 \sqrt{-c^2x^2 + 1} - 6 \sqrt{-c^2x^2 + 1} - 6 cx \arcsin(cx) \right) + 3ab^2 \left(cx (\arcsin(cx))^2 + 3 (\arcsin(cx))^2 \sqrt{-c^2x^2 + 1} - 6 \sqrt{-c^2x^2 + 1} - 6 cx \arcsin(cx) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^3,x)

[Out] 1/c*(c*x*a^3+b^3*(c*x*arcsin(c*x)^3+3*arcsin(c*x)^2*(-c^2*x^2+1)^(1/2))-6*(-c^2*x^2+1)^(1/2)-6*c*x*arcsin(c*x))+3*a*b^2*(c*x*arcsin(c*x)^2-2*c*x+2*arcsin(c*x)*(-c^2*x^2+1)^(1/2))+3*a^2*b*(c*x*arcsin(c*x)+(-c^2*x^2+1)^(1/2))

Maxima [A] time = 1.86907, size = 190, normalized size = 2.32

$$b^3x \arcsin(cx)^3 + 3ab^2x \arcsin(cx)^2 + 3 \left(\frac{\sqrt{-c^2x^2 + 1} \arcsin(cx)^2}{c} - \frac{2 \left(cx \arcsin(cx) + \sqrt{-c^2x^2 + 1} \right)}{c} \right) b^3 - 6ab^2 \left(x - \frac{1}{c} \arcsin(cx) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3,x, algorithm="maxima")

[Out] b^3*x*arcsin(c*x)^3 + 3*a*b^2*x*arcsin(c*x)^2 + 3*(sqrt(-c^2*x^2 + 1)*arcsin(c*x)^2/c - 2*(c*x*arcsin(c*x) + sqrt(-c^2*x^2 + 1))/c)*b^3 - 6*a*b^2*(x - 1/c*arcsin(c*x))

$\sqrt{-c^2x^2 + 1} \arcsin(cx)/c + a^3x + 3(c x \arcsin(cx) + \sqrt{-c^2x^2 + 1})a^2b/c$

Fricas [A] time = 1.79325, size = 262, normalized size = 3.2

$$\frac{b^3cx \arcsin(cx)^3 + 3ab^2cx \arcsin(cx)^2 + 3(a^2b - 2b^3)cx \arcsin(cx) + (a^3 - 6ab^2)cx + 3(b^3 \arcsin(cx)^2 + 2ab^2 \arcsin(cx))}{c}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3,x, algorithm="fricas")

[Out] $(b^3cx \arcsin(cx)^3 + 3a^2b^2cx \arcsin(cx)^2 + 3(a^2b - 2b^3)cx \arcsin(cx) + (a^3 - 6a^2b^2)cx + 3(b^3 \arcsin(cx)^2 + 2a^2b^2 \arcsin(cx)) + a^2b - 2b^3) \sqrt{-c^2x^2 + 1} / c$

Sympy [A] time = 1.2092, size = 160, normalized size = 1.95

$$\begin{cases} a^3x + 3a^2bx \arcsin(cx) + \frac{3a^2b\sqrt{-c^2x^2+1}}{c} + 3ab^2x \arcsin^2(cx) - 6ab^2x + \frac{6ab^2\sqrt{-c^2x^2+1} \arcsin(cx)}{c} + b^3x \arcsin^3(cx) - 6b^3x \arcsin(cx) + a^3x \\ a^3x \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**3,x)

[Out] Piecewise((a**3*x + 3*a**2*b*x*asin(c*x) + 3*a**2*b*sqrt(-c**2*x**2 + 1)/c + 3*a*b**2*x*asin(c*x)**2 - 6*a*b**2*x + 6*a*b**2*sqrt(-c**2*x**2 + 1)*asin(c*x)/c + b**3*x*asin(c*x)**3 - 6*b**3*x*asin(c*x) + 3*b**3*sqrt(-c**2*x**2 + 1)*asin(c*x)**2/c - 6*b**3*sqrt(-c**2*x**2 + 1)/c, Ne(c, 0)), (a**3*x, True))

Giac [A] time = 1.37369, size = 203, normalized size = 2.48

$$b^3x \arcsin(cx)^3 + 3ab^2x \arcsin(cx)^2 + 3a^2bx \arcsin(cx) - 6b^3x \arcsin(cx) + \frac{3\sqrt{-c^2x^2 + 1}b^3 \arcsin(cx)^2}{c} + a^3x - 6ab^2x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3,x, algorithm="giac")

[Out] $b^3x \arcsin(cx)^3 + 3a^2b^2x \arcsin(cx)^2 + 3a^2bx \arcsin(cx) - 6b^3x \arcsin(cx) + 3\sqrt{-c^2x^2 + 1}b^3 \arcsin(cx)^2/c + a^3x - 6a^2b^2x + 6\sqrt{-c^2x^2 + 1}a^2b^2 \arcsin(cx)/c + 3\sqrt{-c^2x^2 + 1}a^2b^2/c - 6\sqrt{-c^2x^2 + 1}b^3/c$

$$3.156 \quad \int \frac{(a+b \sin^{-1}(cx))^3}{x} dx$$

Optimal. Leaf size=123

$$\frac{3}{2}b^2 \text{PolyLog}\left(3, e^{2i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) - \frac{3}{2}ib \text{PolyLog}\left(2, e^{2i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx))^2 + \frac{3}{4}ib^3 \text{PolyLog}\left(4, e^{2i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx))^3$$

```
[Out] ((-I/4)*(a + b*ArcSin[c*x])^4)/b + (a + b*ArcSin[c*x])^3*Log[1 - E^((2*I)*ArcSin[c*x])] - ((3*I)/2)*b*(a + b*ArcSin[c*x])^2*PolyLog[2, E^((2*I)*ArcSin[c*x])] + (3*b^2*(a + b*ArcSin[c*x])*PolyLog[3, E^((2*I)*ArcSin[c*x])])/2 + ((3*I)/4)*b^3*PolyLog[4, E^((2*I)*ArcSin[c*x])]
```

Rubi [A] time = 0.146619, antiderivative size = 123, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4625, 3717, 2190, 2531, 6609, 2282, 6589}

$$\frac{3}{2}b^2 \text{PolyLog}\left(3, e^{2i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) - \frac{3}{2}ib \text{PolyLog}\left(2, e^{2i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx))^2 + \frac{3}{4}ib^3 \text{PolyLog}\left(4, e^{2i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx))^3$$

Antiderivative was successfully verified.

```
[In] Int[(a + b*ArcSin[c*x])^3/x, x]
```

```
[Out] ((-I/4)*(a + b*ArcSin[c*x])^4)/b + (a + b*ArcSin[c*x])^3*Log[1 - E^((2*I)*ArcSin[c*x])] - ((3*I)/2)*b*(a + b*ArcSin[c*x])^2*PolyLog[2, E^((2*I)*ArcSin[c*x])] + (3*b^2*(a + b*ArcSin[c*x])*PolyLog[3, E^((2*I)*ArcSin[c*x])])/2 + ((3*I)/4)*b^3*PolyLog[4, E^((2*I)*ArcSin[c*x])]
```

Rule 4625

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^n_/(x_), x_Symbol] := Subst[Int[(a + b*x)^n/Tan[x], x], x, ArcSin[c*x]] /; FreeQ[{a, b, c}, x] && IGtQ[n, 0]
```

Rule 3717

```
Int[((c_.) + (d_.)*(x_)^m_)*tan[(e_.) + Pi*(k_.) + (f_.)*(x_)], x_Symbol] := Simp[(I*(c + d*x)^(m + 1))/(d*(m + 1)), x] - Dist[2*I, Int[((c + d*x)^m * E^(2*I*k*Pi) * E^(2*I*(e + f*x)))/(1 + E^(2*I*k*Pi) * E^(2*I*(e + f*x))), x], x] /; FreeQ[{c, d, e, f}, x] && IntegerQ[4*k] && IGtQ[m, 0]
```

Rule 2190

```
Int[(((F_)^((g_.)*((e_.) + (f_.)*(x_))))^n_)*((c_.) + (d_.)*(x_)^m_)/((a_.) + (b_.)*(F_)^((g_.)*((e_.) + (f_.)*(x_))))^n_, x_Symbol] := Simp[((c + d*x)^m * Log[1 + (b*(F^(g*(e + f*x)))^n)/a])/(b*f*g*n*Log[F]), x] - Dist[(d*m)/(b*f*g*n*Log[F]), Int[(c + d*x)^(m - 1) * Log[1 + (b*(F^(g*(e + f*x)))^n)/a], x], x] /; FreeQ[{F, a, b, c, d, e, f, g, n}, x] && IGtQ[m, 0]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_))))^n_]*((f_.) + (g_.)*(x_)^m_), x_Symbol] := -Simp[((f + g*x)^m * PolyLog[2, -(e*(F^(c*(a + b*x))))^n])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^(m - 1) * PolyLog[2, -(e*(F^(c*(a + b*x))))^n], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && IGtQ[m, 0]
```

, g, n}, x] && GtQ[m, 0]

Rule 6609

```
Int[((e_.) + (f_.)*(x_))^(m_.)*PolyLog[n_, (d_.)*((F_)^((c_.)*((a_.) + (b_.
)*(x_)))^(p_.)], x_Symbol] := Simp[((e + f*x)^m*PolyLog[n + 1, d*(F^(c*(a
+ b*x)))^p])/(b*c*p*Log[F]), x] - Dist[(f*m)/(b*c*p*Log[F]), Int[(e + f*x)^(
m - 1)*PolyLog[n + 1, d*(F^(c*(a + b*x)))^p], x], x] /; FreeQ[{F, a, b, c,
d, e, f, n, p}, x] && GtQ[m, 0]
```

Rule 2282

```
Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x]
, Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x]] /; Functi
onOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[
{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*
(F_) [v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]
```

Rule 6589

```
Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_S
ymbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d
, e, n, p}, x] && EqQ[b*d, a*e]
```

Rubi steps

$$\begin{aligned} \int \frac{(a + b \sin^{-1}(cx))^3}{x} dx &= \text{Subst} \left(\int (a + bx)^3 \cot(x) dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{i(a + b \sin^{-1}(cx))^4}{4b} - 2i \text{Subst} \left(\int \frac{e^{2ix}(a + bx)^3}{1 - e^{2ix}} dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{i(a + b \sin^{-1}(cx))^4}{4b} + (a + b \sin^{-1}(cx))^3 \log(1 - e^{2i \sin^{-1}(cx)}) - (3b) \text{Subst} \left(\int (a + bx)^2 \log(1 - e^{2ix}) dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{i(a + b \sin^{-1}(cx))^4}{4b} + (a + b \sin^{-1}(cx))^3 \log(1 - e^{2i \sin^{-1}(cx)}) - \frac{3}{2} ib (a + b \sin^{-1}(cx))^2 \text{Li}_2(e^{2i \sin^{-1}(cx)}) \\ &= -\frac{i(a + b \sin^{-1}(cx))^4}{4b} + (a + b \sin^{-1}(cx))^3 \log(1 - e^{2i \sin^{-1}(cx)}) - \frac{3}{2} ib (a + b \sin^{-1}(cx))^2 \text{Li}_2(e^{2i \sin^{-1}(cx)}) \\ &= -\frac{i(a + b \sin^{-1}(cx))^4}{4b} + (a + b \sin^{-1}(cx))^3 \log(1 - e^{2i \sin^{-1}(cx)}) - \frac{3}{2} ib (a + b \sin^{-1}(cx))^2 \text{Li}_2(e^{2i \sin^{-1}(cx)}) \\ &= -\frac{i(a + b \sin^{-1}(cx))^4}{4b} + (a + b \sin^{-1}(cx))^3 \log(1 - e^{2i \sin^{-1}(cx)}) - \frac{3}{2} ib (a + b \sin^{-1}(cx))^2 \text{Li}_2(e^{2i \sin^{-1}(cx)}) \end{aligned}$$

Mathematica [A] time = 0.238776, size = 244, normalized size = 1.98

$$3a^2b \left(\sin^{-1}(cx) \log(1 - e^{2i \sin^{-1}(cx)}) - \frac{1}{2} i \left(\sin^{-1}(cx)^2 + \text{PolyLog}(2, e^{2i \sin^{-1}(cx)}) \right) \right) + \frac{1}{8} ab^2 \left(24i \sin^{-1}(cx) \text{PolyLog}(2, e^{-2i \sin^{-1}(cx)}) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[(a + b*ArcSin[c*x])^3/x, x]

[Out] a^3*Log[c*x] + 3*a^2*b*(ArcSin[c*x]*Log[1 - E^((2*I)*ArcSin[c*x])] - (I/2)*(ArcSin[c*x]^2 + PolyLog[2, E^((2*I)*ArcSin[c*x])])) + (a*b^2*((-I)*Pi^3 +

$$(8*I)*\text{ArcSin}[c*x]^3 + 24*\text{ArcSin}[c*x]^2*\text{Log}[1 - E^{((-2*I)*\text{ArcSin}[c*x])}] + (24*I)*\text{ArcSin}[c*x]*\text{PolyLog}[2, E^{((-2*I)*\text{ArcSin}[c*x])}] + 12*\text{PolyLog}[3, E^{((-2*I)*\text{ArcSin}[c*x])}))/8 - (I/64)*b^3*(\text{Pi}^4 - 16*\text{ArcSin}[c*x]^4 + (64*I)*\text{ArcSin}[c*x]^3*\text{Log}[1 - E^{((-2*I)*\text{ArcSin}[c*x])}] - 96*\text{ArcSin}[c*x]^2*\text{PolyLog}[2, E^{((-2*I)*\text{ArcSin}[c*x])}] + (96*I)*\text{ArcSin}[c*x]*\text{PolyLog}[3, E^{((-2*I)*\text{ArcSin}[c*x])}] + 48*\text{PolyLog}[4, E^{((-2*I)*\text{ArcSin}[c*x])}])$$

Maple [B] time = 0.026, size = 592, normalized size = 4.8

$$a^3 \ln(cx) - 3ia^2b \text{polylog}\left(2, -icx - \sqrt{-c^2x^2 + 1}\right) + b^3 (\arcsin(cx))^3 \ln\left(1 + icx + \sqrt{-c^2x^2 + 1}\right) + 6ib^3 \text{polylog}\left(4, icx\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^3/x,x)

[Out] $a^3*\ln(c*x) - 3*I*a^2*b*\text{polylog}(2, -I*c*x - (-c^2*x^2+1)^{(1/2)}) + b^3*\arcsin(c*x)^3*\ln(1+I*c*x + (-c^2*x^2+1)^{(1/2)}) + 6*I*b^3*\text{polylog}(4, I*c*x + (-c^2*x^2+1)^{(1/2)}) + 6*b^3*\arcsin(c*x)*\text{polylog}(3, -I*c*x - (-c^2*x^2+1)^{(1/2)}) + 6*I*b^3*\text{polylog}(4, -I*c*x - (-c^2*x^2+1)^{(1/2)}) + b^3*\arcsin(c*x)^3*\ln(1-I*c*x - (-c^2*x^2+1)^{(1/2)}) - 6*I*a*b^2*\arcsin(c*x)*\text{polylog}(2, -I*c*x - (-c^2*x^2+1)^{(1/2)}) + 6*b^3*\arcsin(c*x)*\text{polylog}(3, I*c*x + (-c^2*x^2+1)^{(1/2)}) - 6*I*a*b^2*\arcsin(c*x)*\text{polylog}(2, I*c*x + (-c^2*x^2+1)^{(1/2)}) - 1/4*I*b^3*\arcsin(c*x)^4 - 3*I*b^3*\arcsin(c*x)^2*\text{polylog}(2, -I*c*x - (-c^2*x^2+1)^{(1/2)}) - 3/2*I*a^2*b*\arcsin(c*x)^2 + 3*a*b^2*\arcsin(c*x)^2*\ln(1+I*c*x + (-c^2*x^2+1)^{(1/2)}) + 3*a*b^2*\arcsin(c*x)^2*\ln(1-I*c*x - (-c^2*x^2+1)^{(1/2)}) + 6*a*b^2*\text{polylog}(3, -I*c*x - (-c^2*x^2+1)^{(1/2)}) + 6*a*b^2*\text{polylog}(3, I*c*x + (-c^2*x^2+1)^{(1/2)}) - 3*I*a^2*b*\text{polylog}(2, I*c*x + (-c^2*x^2+1)^{(1/2)}) + 3*a^2*b*\arcsin(c*x)*\ln(1+I*c*x + (-c^2*x^2+1)^{(1/2)}) + 3*a^2*b*\arcsin(c*x)*\ln(1-I*c*x - (-c^2*x^2+1)^{(1/2)}) - 3*I*b^3*\arcsin(c*x)^2*\text{polylog}(2, I*c*x + (-c^2*x^2+1)^{(1/2)}) - I*a*b^2*\arcsin(c*x)^3$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$a^3 \log(x) + \int \frac{b^3 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^3 + 3ab^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^2 + 3a^2b \arctan\left(cx, \sqrt{cx+1}\right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3/x,x, algorithm="maxima")

[Out] $a^3*\log(x) + \text{integrate}((b^3*\arctan2(c*x, \text{sqrt}(c*x + 1))*\text{sqrt}(-c*x + 1))^3 + 3*a*b^2*\arctan2(c*x, \text{sqrt}(c*x + 1))*\text{sqrt}(-c*x + 1))^2 + 3*a^2*b*\arctan2(c*x, \text{sqrt}(c*x + 1))*\text{sqrt}(-c*x + 1))/x, x)$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3/x,x, algorithm="fricas")

[Out] `integral((b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) + a^3)/x, x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(a + b \operatorname{asin}(cx))^3}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**3/x,x)`

[Out] `Integral((a + b*asin(c*x))**3/x, x)`

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \operatorname{arcsin}(cx) + a)^3}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/x,x, algorithm="giac")`

[Out] `integrate((b*arcsin(c*x) + a)^3/x, x)`

$$3.157 \quad \int \frac{(a+b \sin^{-1}(cx))^3}{x^2} dx$$

Optimal. Leaf size=137

$$6ib^2c \operatorname{PolyLog}\left(2, -e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) - 6ib^2c \operatorname{PolyLog}\left(2, e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) - 6b^3c \operatorname{PolyLog}\left(3, -e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) + 6b^3c \operatorname{PolyLog}\left(3, e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx))$$

```
[Out] -((a + b*ArcSin[c*x])^3/x) - 6*b*c*(a + b*ArcSin[c*x])^2*ArcTanh[E^(I*ArcSin[c*x])] + (6*I)*b^2*c*(a + b*ArcSin[c*x])*PolyLog[2, -E^(I*ArcSin[c*x])] - (6*I)*b^2*c*(a + b*ArcSin[c*x])*PolyLog[2, E^(I*ArcSin[c*x])] - 6*b^3*c*PolyLog[3, -E^(I*ArcSin[c*x])] + 6*b^3*c*PolyLog[3, E^(I*ArcSin[c*x])]
```

Rubi [A] time = 0.212895, antiderivative size = 137, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 6, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.429$, Rules used = {4627, 4709, 4183, 2531, 2282, 6589}

$$6ib^2c \operatorname{PolyLog}\left(2, -e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) - 6ib^2c \operatorname{PolyLog}\left(2, e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) - 6b^3c \operatorname{PolyLog}\left(3, -e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx)) + 6b^3c \operatorname{PolyLog}\left(3, e^{i \sin^{-1}(cx)}\right) (a + b \sin^{-1}(cx))$$

Antiderivative was successfully verified.

```
[In] Int[(a + b*ArcSin[c*x])^3/x^2, x]
```

```
[Out] -((a + b*ArcSin[c*x])^3/x) - 6*b*c*(a + b*ArcSin[c*x])^2*ArcTanh[E^(I*ArcSin[c*x])] + (6*I)*b^2*c*(a + b*ArcSin[c*x])*PolyLog[2, -E^(I*ArcSin[c*x])] - (6*I)*b^2*c*(a + b*ArcSin[c*x])*PolyLog[2, E^(I*ArcSin[c*x])] - 6*b^3*c*PolyLog[3, -E^(I*ArcSin[c*x])] + 6*b^3*c*PolyLog[3, E^(I*ArcSin[c*x])]
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_.)*((d_.)*(x_)^ (m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 4709

```
Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_.)*(x_)^ (m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol]
:> Dist[1/(c^(m + 1)*Sqrt[d]), Subst[Int[(a + b*x)^n*Sin[x]^m, x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && IGtQ[n, 0] && IntegerQ[m]
```

Rule 4183

```
Int[csc[(e_.) + (f_.)*(x_)]*((c_.) + (d_.)*(x_)^ (m_.), x_Symbol]
:> Simp[(-2*(c + d*x)^m*ArcTanh[E^(I*(e + f*x))])/f, x] + (-Dist[(d*m)/f, Int[(c + d*x)^ (m - 1)*Log[1 - E^(I*(e + f*x))], x], x] + Dist[(d*m)/f, Int[(c + d*x)^ (m - 1)*Log[1 + E^(I*(e + f*x))], x], x]) /; FreeQ[{c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 2531

```
Int[Log[1 + (e_.)*((F_)^((c_.)*((a_.) + (b_.)*(x_)))]^ (n_.)]*((f_.) + (g_.)*(x_)^ (m_.), x_Symbol]
:> -Simp[((f + g*x)^m*PolyLog[2, -(e*(F^(c*(a + b*x))))^n])/(b*c*n*Log[F]), x] + Dist[(g*m)/(b*c*n*Log[F]), Int[(f + g*x)^ (m -
```

1)*PolyLog[2, -(e*(F^(c*(a + b*x)))^n)], x], x] /; FreeQ[{F, a, b, c, e, f, g, n}, x] && GtQ[m, 0]

Rule 2282

Int[u_, x_Symbol] := With[{v = FunctionOfExponential[u, x]}, Dist[v/D[v, x], Subst[Int[FunctionOfExponentialFunction[u, x]/x, x], x, v], x] /; FunctionOfExponentialQ[u, x] && !MatchQ[u, (w_)*((a_.)*(v_)^(n_))^(m_) /; FreeQ[{a, m, n}, x] && IntegerQ[m*n]] && !MatchQ[u, E^((c_.)*((a_.) + (b_.)*x))*(F_)[v_] /; FreeQ[{a, b, c}, x] && InverseFunctionQ[F[x]]]

Rule 6589

Int[PolyLog[n_, (c_.)*((a_.) + (b_.)*(x_))^(p_.)]/((d_.) + (e_.)*(x_)), x_Symbol] := Simp[PolyLog[n + 1, c*(a + b*x)^p]/(e*p), x] /; FreeQ[{a, b, c, d, e, n, p}, x] && EqQ[b*d, a*e]

Rubi steps

$$\begin{aligned} \int \frac{(a + b \sin^{-1}(cx))^3}{x^2} dx &= -\frac{(a + b \sin^{-1}(cx))^3}{x} + (3bc) \int \frac{(a + b \sin^{-1}(cx))^2}{x\sqrt{1 - c^2x^2}} dx \\ &= -\frac{(a + b \sin^{-1}(cx))^3}{x} + (3bc) \text{Subst} \left(\int (a + bx)^2 \csc(x) dx, x, \sin^{-1}(cx) \right) \\ &= -\frac{(a + b \sin^{-1}(cx))^3}{x} - 6bc (a + b \sin^{-1}(cx))^2 \tanh^{-1} \left(e^{i \sin^{-1}(cx)} \right) - (6b^2c) \text{Subst} \left(\int (a + bx) \log \right) \\ &= -\frac{(a + b \sin^{-1}(cx))^3}{x} - 6bc (a + b \sin^{-1}(cx))^2 \tanh^{-1} \left(e^{i \sin^{-1}(cx)} \right) + 6ib^2c (a + b \sin^{-1}(cx)) \text{Li}_2 \left(\right) \\ &= -\frac{(a + b \sin^{-1}(cx))^3}{x} - 6bc (a + b \sin^{-1}(cx))^2 \tanh^{-1} \left(e^{i \sin^{-1}(cx)} \right) + 6ib^2c (a + b \sin^{-1}(cx)) \text{Li}_2 \left(\right) \\ &= -\frac{(a + b \sin^{-1}(cx))^3}{x} - 6bc (a + b \sin^{-1}(cx))^2 \tanh^{-1} \left(e^{i \sin^{-1}(cx)} \right) + 6ib^2c (a + b \sin^{-1}(cx)) \text{Li}_2 \left(\right) \end{aligned}$$

Mathematica [B] time = 0.314443, size = 283, normalized size = 2.07

$$3ab^2c \left(2i \text{PolyLog} \left(2, -e^{i \sin^{-1}(cx)} \right) - 2i \text{PolyLog} \left(2, e^{i \sin^{-1}(cx)} \right) - \sin^{-1}(cx) \left(\frac{\sin^{-1}(cx)}{cx} - 2 \log \left(1 - e^{i \sin^{-1}(cx)} \right) + 2 \log \left(1 + e^{i \sin^{-1}(cx)} \right) \right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[(a + b*ArcSin[c*x])^3/x^2, x]

[Out] -(a^3/x) - (3*a^2*b*ArcSin[c*x])/x + 3*a^2*b*c*Log[x] - 3*a^2*b*c*Log[1 + Sqrt[1 - c^2*x^2]] + 3*a*b^2*c*(-(ArcSin[c*x]*(ArcSin[c*x]/(c*x) - 2*Log[1 - E^(I*ArcSin[c*x]])] + 2*Log[1 + E^(I*ArcSin[c*x]])]) + (2*I)*PolyLog[2, -E^(I*ArcSin[c*x])] - (2*I)*PolyLog[2, E^(I*ArcSin[c*x])] + b^3*c*(-(ArcSin[c*x]^3/(c*x)) + 3*ArcSin[c*x]^2*Log[1 - E^(I*ArcSin[c*x])] - 3*ArcSin[c*x]^2*Log[1 + E^(I*ArcSin[c*x])] + (6*I)*ArcSin[c*x]*PolyLog[2, -E^(I*ArcSin[c*x])] - (6*I)*ArcSin[c*x]*PolyLog[2, E^(I*ArcSin[c*x])] - 6*PolyLog[3, -E^(I*ArcSin[c*x])] + 6*PolyLog[3, E^(I*ArcSin[c*x])])

Maple [B] time = 0.042, size = 378, normalized size = 2.8

$$-\frac{a^3}{x} - \frac{b^3 (\arcsin(cx))^3}{x} - 3cb^3 (\arcsin(cx))^2 \ln\left(1 + icx + \sqrt{-c^2x^2 + 1}\right) + 6icb^3 \arcsin(cx) \operatorname{polylog}\left(2, -icx - \sqrt{-c^2x^2 + 1}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^3/x^2,x)

[Out] $-a^3/x - b^3/x * \arcsin(c*x)^3 - 3*c*b^3 * \arcsin(c*x)^2 * \ln(1 + I*c*x + (-c^2*x^2 + 1)^{(1/2)}) + 6*I*c*b^3 * \arcsin(c*x) * \operatorname{polylog}(2, -I*c*x - (-c^2*x^2 + 1)^{(1/2)}) - 6*b^3 * c * \operatorname{polylog}(3, -I*c*x - (-c^2*x^2 + 1)^{(1/2)}) + 3*c*b^3 * \arcsin(c*x)^2 * \ln(1 - I*c*x - (-c^2*x^2 + 1)^{(1/2)}) - 6*I*c*b^3 * \arcsin(c*x) * \operatorname{polylog}(2, I*c*x + (-c^2*x^2 + 1)^{(1/2)}) + 6*b^3 * c * \operatorname{polylog}(3, I*c*x + (-c^2*x^2 + 1)^{(1/2)}) - 3*a*b^2/x * \arcsin(c*x)^2 + 6*c*a*b^2 * \arcsin(c*x) * \ln(1 - I*c*x - (-c^2*x^2 + 1)^{(1/2)}) - 6*c*a*b^2 * \arcsin(c*x) * \ln(1 + I*c*x + (-c^2*x^2 + 1)^{(1/2)}) - 6*I*c*a*b^2 * \operatorname{polylog}(2, I*c*x + (-c^2*x^2 + 1)^{(1/2)}) + 6*I*c*a*b^2 * \operatorname{polylog}(2, -I*c*x - (-c^2*x^2 + 1)^{(1/2)}) - 3*a^2*b/x * \arcsin(c*x) - 3*c*a^2*b * \operatorname{arctanh}(1/(-c^2*x^2 + 1)^{(1/2)})$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$-3 \left(c \log\left(\frac{2\sqrt{-c^2x^2+1}}{|x|} + \frac{2}{|x|}\right) + \frac{\arcsin(cx)}{x} \right) a^2 b - \frac{a^3}{x} - \frac{b^3 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^3 + \frac{3}{2} \left(ab^2 c^2 \left(\frac{\log(cx+1)}{c} - \log \right) \right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3/x^2,x, algorithm="maxima")

[Out] $-3*(c*\log(2*\sqrt{-c^2*x^2+1}/\operatorname{abs}(x) + 2/\operatorname{abs}(x)) + \arcsin(c*x)/x)*a^2*b - a^3/x - (b^3*\arctan2(c*x, \sqrt{c*x+1}*\sqrt{-c*x+1})^3 + x*\operatorname{integrate}(3*(\sqrt{c*x+1}*\sqrt{-c*x+1}*b^3*c*x*\arctan2(c*x, \sqrt{c*x+1}*\sqrt{-c*x+1}))^2 - (a*b^2*c^2*x^2 - a*b^2)*\arctan2(c*x, \sqrt{c*x+1}*\sqrt{-c*x+1})^2)/(c^2*x^4 - x^2), x))/x$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3/x^2,x, algorithm="fricas")

[Out] $\operatorname{integral}((b^3*\arcsin(c*x)^3 + 3*a*b^2*\arcsin(c*x)^2 + 3*a^2*b*\arcsin(c*x) + a^3)/x^2, x)$

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(a + b \operatorname{asin}(cx))^3}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**3/x**2,x)

[Out] Integral((a + b*asin(c*x))**3/x**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^3}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^3/x^2,x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)^3/x^2, x)

$$3.158 \quad \int \frac{x^2}{a+b \sin^{-1}(cx)} dx$$

Optimal. Leaf size=121

$$\frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{4bc^3} - \frac{\cos\left(\frac{3a}{b}\right) \operatorname{CosIntegral}\left(\frac{3(a+b \sin^{-1}(cx))}{b}\right)}{4bc^3} + \frac{\sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{4bc^3} - \frac{\sin\left(\frac{3a}{b}\right) \operatorname{Si}\left(\frac{3(a+b \sin^{-1}(cx))}{b}\right)}{4bc^3}$$

[Out] (Cos[a/b]*CosIntegral[(a + b*ArcSin[c*x])/b])/(4*b*c^3) - (Cos[(3*a)/b]*CosIntegral[(3*(a + b*ArcSin[c*x]))/b])/(4*b*c^3) + (Sin[a/b]*SinIntegral[(a + b*ArcSin[c*x])/b])/(4*b*c^3) - (Sin[(3*a)/b]*SinIntegral[(3*(a + b*ArcSin[c*x]))/b])/(4*b*c^3)

Rubi [A] time = 0.253727, antiderivative size = 117, normalized size of antiderivative = 0.97, number of steps used = 9, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {4635, 4406, 3303, 3299, 3302}

$$\frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{4bc^3} - \frac{\cos\left(\frac{3a}{b}\right) \operatorname{CosIntegral}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4bc^3} + \frac{\sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{4bc^3} - \frac{\sin\left(\frac{3a}{b}\right) \operatorname{Si}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4bc^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*ArcSin[c*x]),x]

[Out] (Cos[a/b]*CosIntegral[a/b + ArcSin[c*x]])/(4*b*c^3) - (Cos[(3*a)/b]*CosIntegral[(3*a)/b + 3*ArcSin[c*x]])/(4*b*c^3) + (Sin[a/b]*SinIntegral[a/b + ArcSin[c*x]])/(4*b*c^3) - (Sin[(3*a)/b]*SinIntegral[(3*a)/b + 3*ArcSin[c*x]])/(4*b*c^3)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_.)*(x_)^ (m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{x^2}{a + b \sin^{-1}(cx)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x) \sin^2(x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{c^3} \\ &= \frac{\text{Subst}\left(\int \left(\frac{\cos(x)}{4(a+bx)} - \frac{\cos(3x)}{4(a+bx)}\right) dx, x, \sin^{-1}(cx)\right)}{c^3} \\ &= \frac{\text{Subst}\left(\int \frac{\cos(x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4c^3} - \frac{\text{Subst}\left(\int \frac{\cos(3x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4c^3} \\ &= \frac{\cos\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{a}{b}+x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4c^3} - \frac{\cos\left(\frac{3a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{3a}{b}+3x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4c^3} + \frac{\sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right) - \sin\left(\frac{3a}{b}\right) \text{Si}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4bc^3} \\ &= \frac{\cos\left(\frac{a}{b}\right) \text{Ci}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{4bc^3} - \frac{\cos\left(\frac{3a}{b}\right) \text{Ci}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4bc^3} + \frac{\sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{4bc^3} - \frac{\sin\left(\frac{3a}{b}\right) \text{Si}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4bc^3} \end{aligned}$$

Mathematica [A] time = 0.19952, size = 91, normalized size = 0.75

$$\frac{\cos\left(\frac{a}{b}\right) \text{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right) - \cos\left(\frac{3a}{b}\right) \text{CosIntegral}\left(3\left(\frac{a}{b} + \sin^{-1}(cx)\right)\right) + \sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right) - \sin\left(\frac{3a}{b}\right) \text{Si}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4bc^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2/(a + b*ArcSin[c*x]),x]
```

```
[Out] (Cos[a/b]*CosIntegral[a/b + ArcSin[c*x]] - Cos[(3*a)/b]*CosIntegral[3*(a/b + ArcSin[c*x])] + Sin[a/b]*SinIntegral[a/b + ArcSin[c*x]] - Sin[(3*a)/b]*SinIntegral[3*(a/b + ArcSin[c*x])])/(4*b*c^3)
```

Maple [A] time = 0.025, size = 102, normalized size = 0.8

$$\frac{1}{c^3} \left(\frac{1}{4b} \text{Si}\left(\arcsin(cx) + \frac{a}{b}\right) \sin\left(\frac{a}{b}\right) + \frac{1}{4b} \text{Ci}\left(\arcsin(cx) + \frac{a}{b}\right) \cos\left(\frac{a}{b}\right) - \frac{1}{4b} \text{Si}\left(3 \arcsin(cx) + 3 \frac{a}{b}\right) \sin\left(3 \frac{a}{b}\right) - \frac{1}{4b} \text{Ci}\left(3 \arcsin(cx) + 3 \frac{a}{b}\right) \cos\left(3 \frac{a}{b}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2/(a+b*arcsin(c*x)),x)
```

```
[Out] 1/c^3*(1/4*Si(arcsin(c*x)+a/b)*sin(a/b)/b+1/4*Ci(arcsin(c*x)+a/b)*cos(a/b)/b-1/4*Si(3*arcsin(c*x)+3*a/b)*sin(3*a/b)/b-1/4*Ci(3*arcsin(c*x)+3*a/b)*cos(3*a/b)/b)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate(x^2/(b*arcsin(c*x) + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^2}{b \arcsin(cx) + a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(x^2/(b*arcsin(c*x) + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{a + b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(a+b*asin(c*x)),x)

[Out] Integral(x**2/(a + b*asin(c*x)), x)

Giac [A] time = 1.30241, size = 234, normalized size = 1.93

$$-\frac{\cos\left(\frac{a}{b}\right)^3 \text{Ci}\left(\frac{3a}{b} + 3 \arcsin(cx)\right)}{bc^3} - \frac{\cos\left(\frac{a}{b}\right)^2 \sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{3a}{b} + 3 \arcsin(cx)\right)}{bc^3} + \frac{3 \cos\left(\frac{a}{b}\right) \text{Ci}\left(\frac{3a}{b} + 3 \arcsin(cx)\right)}{4bc^3} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] -cos(a/b)^3*cos_integral(3*a/b + 3*arcsin(c*x))/(b*c^3) - cos(a/b)^2*sin(a/b)*sin_integral(3*a/b + 3*arcsin(c*x))/(b*c^3) + 3/4*cos(a/b)*cos_integral(3*a/b + 3*arcsin(c*x))/(b*c^3) + 1/4*cos(a/b)*cos_integral(a/b + arcsin(c*x))/(b*c^3) + 1/4*sin(a/b)*sin_integral(3*a/b + 3*arcsin(c*x))/(b*c^3) + 1/4*sin(a/b)*sin_integral(a/b + arcsin(c*x))/(b*c^3)

$$3.159 \quad \int \frac{x}{a+b \sin^{-1}(cx)} dx$$

Optimal. Leaf size=63

$$\frac{\cos\left(\frac{2a}{b}\right) \operatorname{Si}\left(\frac{2(a+b \sin^{-1}(cx))}{b}\right)}{2bc^2} - \frac{\sin\left(\frac{2a}{b}\right) \operatorname{CosIntegral}\left(\frac{2(a+b \sin^{-1}(cx))}{b}\right)}{2bc^2}$$

[Out] $-(\operatorname{CosIntegral}[(2*(a + b*\operatorname{ArcSin}[c*x]))/b]*\operatorname{Sin}[(2*a)/b])/(2*b*c^2) + (\operatorname{Cos}[(2*a)/b]*\operatorname{SinIntegral}[(2*(a + b*\operatorname{ArcSin}[c*x]))/b])/(2*b*c^2)$

Rubi [A] time = 0.131864, antiderivative size = 63, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4635, 4406, 12, 3303, 3299, 3302}

$$\frac{\cos\left(\frac{2a}{b}\right) \operatorname{Si}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{2bc^2} - \frac{\sin\left(\frac{2a}{b}\right) \operatorname{CosIntegral}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{2bc^2}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[x/(a + b*\operatorname{ArcSin}[c*x]), x]$

[Out] $-(\operatorname{CosIntegral}[(2*a)/b + 2*\operatorname{ArcSin}[c*x]]*\operatorname{Sin}[(2*a)/b])/(2*b*c^2) + (\operatorname{Cos}[(2*a)/b]*\operatorname{SinIntegral}[(2*a)/b + 2*\operatorname{ArcSin}[c*x]])/(2*b*c^2)$

Rule 4635

$\operatorname{Int}[(a + \operatorname{ArcSin}(c*x))*(b*x)^n*(x)^m, x_Symbol] \rightarrow \operatorname{Dist}[1/c^{m+1}, \operatorname{Subst}[\operatorname{Int}[(a + b*x)^n*\operatorname{Sin}[x]^m*\operatorname{Cos}[x], x], x, \operatorname{ArcSin}[c*x]], x] /;$ $\operatorname{FreeQ}\{a, b, c, n, x\} \ \&\& \ \operatorname{IGtQ}[m, 0]$

Rule 4406

$\operatorname{Int}[\operatorname{Cos}(a + b*x)^p*(c + d*x)^m*\operatorname{Sin}(a + b*x)^n, x_Symbol] \rightarrow \operatorname{Int}[\operatorname{ExpandTrigReduce}[(c + d*x)^m, \operatorname{Sin}[a + b*x]^n*\operatorname{Cos}[a + b*x]^p, x], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, m, x\} \ \&\& \ \operatorname{IGtQ}[n, 0] \ \&\& \ \operatorname{IGtQ}[p, 0]$

Rule 12

$\operatorname{Int}(a*u, x_Symbol) \rightarrow \operatorname{Dist}[a, \operatorname{Int}[u, x], x] /;$ $\operatorname{FreeQ}[a, x] \ \&\& \ !\operatorname{MatchQ}[u, (b)*v] /;$ $\operatorname{FreeQ}[b, x]$

Rule 3303

$\operatorname{Int}[\operatorname{sin}(e + f*x)/(c + d*x), x_Symbol] \rightarrow \operatorname{Dist}[\operatorname{Cos}[(d*e - c*f)/d], \operatorname{Int}[\operatorname{Sin}[(c*f)/d + f*x]/(c + d*x), x], x] + \operatorname{Dist}[\operatorname{Sin}[(d*e - c*f)/d], \operatorname{Int}[\operatorname{Cos}[(c*f)/d + f*x]/(c + d*x), x], x] /;$ $\operatorname{FreeQ}\{c, d, e, f, x\} \ \&\& \ \operatorname{NeQ}[d*e - c*f, 0]$

Rule 3299

$\operatorname{Int}[\operatorname{sin}(e + f*x)/(c + d*x), x_Symbol] \rightarrow \operatorname{Simp}[\operatorname{SinIntegral}[e + f*x]/d, x] /;$ $\operatorname{FreeQ}\{c, d, e, f, x\} \ \&\& \ \operatorname{EqQ}[d*e - c*f, 0]$

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{x}{a + b \sin^{-1}(cx)} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x) \sin(x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{c^2} \\ &= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{2(a+bx)} dx, x, \sin^{-1}(cx)\right)}{c^2} \\ &= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{2c^2} \\ &= \frac{\cos\left(\frac{2a}{b}\right) \text{Subst}\left(\int \frac{\sin\left(\frac{2a}{b}+2x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{2c^2} - \frac{\sin\left(\frac{2a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{2a}{b}+2x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{2c^2} \\ &= -\frac{\text{Ci}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right) \sin\left(\frac{2a}{b}\right)}{2bc^2} + \frac{\cos\left(\frac{2a}{b}\right) \text{Si}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{2bc^2} \end{aligned}$$

Mathematica [A] time = 0.079123, size = 56, normalized size = 0.89

$$\frac{\cos\left(\frac{2a}{b}\right) \text{Si}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right) - \sin\left(\frac{2a}{b}\right) \text{CosIntegral}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{2bc^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x/(a + b*ArcSin[c*x]), x]
```

```
[Out] -(CosIntegral[(2*a)/b + 2*ArcSin[c*x]]*Sin[(2*a)/b]) + Cos[(2*a)/b]*SinIntegral[(2*a)/b + 2*ArcSin[c*x]]/(2*b*c^2)
```

Maple [A] time = 0.023, size = 58, normalized size = 0.9

$$\frac{1}{c^2} \left(\frac{1}{2b} \text{Si}\left(2 \arcsin(cx) + 2 \frac{a}{b}\right) \cos\left(2 \frac{a}{b}\right) - \frac{1}{2b} \text{Ci}\left(2 \arcsin(cx) + 2 \frac{a}{b}\right) \sin\left(2 \frac{a}{b}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x/(a+b*arcsin(c*x)), x)
```

```
[Out] 1/c^2*(1/2*Si(2*arcsin(c*x)+2*a/b)*cos(2*a/b)/b-1/2*Ci(2*arcsin(c*x)+2*a/b)*sin(2*a/b)/b)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate(x/(b*arcsin(c*x) + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x}{b \arcsin(cx) + a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(x/(b*arcsin(c*x) + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{a + b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*asin(c*x)),x)

[Out] Integral(x/(a + b*asin(c*x)), x)

Giac [A] time = 1.28797, size = 116, normalized size = 1.84

$$-\frac{\cos\left(\frac{a}{b}\right) \text{Ci}\left(\frac{2a}{b} + 2 \arcsin(cx)\right) \sin\left(\frac{a}{b}\right)}{bc^2} + \frac{\cos\left(\frac{a}{b}\right)^2 \text{Si}\left(\frac{2a}{b} + 2 \arcsin(cx)\right)}{bc^2} - \frac{\text{Si}\left(\frac{2a}{b} + 2 \arcsin(cx)\right)}{2bc^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] -cos(a/b)*cos_integral(2*a/b + 2*arcsin(c*x))*sin(a/b)/(b*c^2) + cos(a/b)^2
*sin_integral(2*a/b + 2*arcsin(c*x))/(b*c^2) - 1/2*sin_integral(2*a/b + 2*a
rksin(c*x))/(b*c^2)

$$3.160 \quad \int \frac{1}{a+b \sin^{-1}(cx)} dx$$

Optimal. Leaf size=53

$$\frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{bc} + \frac{\sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{bc}$$

[Out] (Cos[a/b]*CosIntegral[(a + b*ArcSin[c*x])/b])/(b*c) + (Sin[a/b]*SinIntegral[(a + b*ArcSin[c*x])/b])/(b*c)

Rubi [A] time = 0.066952, antiderivative size = 53, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.4$, Rules used = {4623, 3303, 3299, 3302}

$$\frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{bc} + \frac{\sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{bc}$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^(-1), x]

[Out] (Cos[a/b]*CosIntegral[(a + b*ArcSin[c*x])/b])/(b*c) + (Sin[a/b]*SinIntegral[(a + b*ArcSin[c*x])/b])/(b*c)

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)]^(n_), x_Symbol] :> Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{a + b \sin^{-1}(cx)} dx &= \frac{\text{Subst}\left(\int \frac{\cos\left(\frac{a-x}{b}\right)}{x} dx, x, a + b \sin^{-1}(cx)\right)}{bc} \\ &= \frac{\cos\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{x}{b}\right)}{x} dx, x, a + b \sin^{-1}(cx)\right)}{bc} + \frac{\sin\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\sin\left(\frac{x}{b}\right)}{x} dx, x, a + b \sin^{-1}(cx)\right)}{bc} \\ &= \frac{\cos\left(\frac{a}{b}\right) \text{Ci}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{bc} + \frac{\sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{bc} \end{aligned}$$

Mathematica [A] time = 0.0648763, size = 44, normalized size = 0.83

$$\frac{\cos\left(\frac{a}{b}\right) \text{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right) + \sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{bc}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])^(-1), x]

[Out] (Cos[a/b]*CosIntegral[a/b + ArcSin[c*x]] + Sin[a/b]*SinIntegral[a/b + ArcSin[c*x]])/(b*c)

Maple [A] time = 0.023, size = 48, normalized size = 0.9

$$\frac{1}{c} \left(\frac{1}{b} \text{Si}\left(\arcsin(cx) + \frac{a}{b}\right) \sin\left(\frac{a}{b}\right) + \frac{1}{b} \text{Ci}\left(\arcsin(cx) + \frac{a}{b}\right) \cos\left(\frac{a}{b}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a+b*arcsin(c*x)), x)

[Out] 1/c*(Si(arcsin(c*x)+a/b)*sin(a/b)/b+Ci(arcsin(c*x)+a/b)*cos(a/b)/b)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x)), x, algorithm="maxima")

[Out] integrate(1/(b*arcsin(c*x) + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{b \arcsin(cx) + a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(1/(b*arcsin(c*x) + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{a + b \operatorname{asin}(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*asin(c*x)),x)

[Out] Integral(1/(a + b*asin(c*x)), x)

Giac [A] time = 1.41228, size = 66, normalized size = 1.25

$$\frac{\cos\left(\frac{a}{b}\right) \operatorname{Ci}\left(\frac{a}{b} + \operatorname{arcsin}(cx)\right)}{bc} + \frac{\sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a}{b} + \operatorname{arcsin}(cx)\right)}{bc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] cos(a/b)*cos_integral(a/b + arcsin(c*x))/(b*c) + sin(a/b)*sin_integral(a/b + arcsin(c*x))/(b*c)

$$3.161 \quad \int \frac{1}{x(a+b \sin^{-1}(cx))} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable} \left(\frac{1}{x(a+b \sin^{-1}(cx))}, x \right)$$

[Out] Unintegrable[1/(x*(a + b*ArcSin[c*x])), x]

Rubi [A] time = 0.0237117, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x(a+b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*(a + b*ArcSin[c*x])),x]

[Out] Defer[Int][1/(x*(a + b*ArcSin[c*x])), x]

Rubi steps

$$\int \frac{1}{x(a+b \sin^{-1}(cx))} dx = \int \frac{1}{x(a+b \sin^{-1}(cx))} dx$$

Mathematica [A] time = 0.245207, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*(a + b*ArcSin[c*x])),x]

[Out] Integrate[1/(x*(a + b*ArcSin[c*x])), x]

Maple [A] time = 0.145, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \arcsin(cx))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(a+b*arcsin(c*x)),x)

[Out] int(1/x/(a+b*arcsin(c*x)),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate(1/((b*arcsin(c*x) + a)*x), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{bx \arcsin(cx) + ax}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(1/(b*x*arcsin(c*x) + a*x), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x(a + b \arcsin(cx))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(a+b*asin(c*x)),x)

[Out] Integral(1/(x*(a + b*asin(c*x))), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] integrate(1/((b*arcsin(c*x) + a)*x), x)

$$3.162 \quad \int \frac{1}{x^2(a+b \sin^{-1}(cx))} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable}\left(\frac{1}{x^2(a+b \sin^{-1}(cx))}, x\right)$$

[Out] Unintegrable[1/(x^2*(a + b*ArcSin[c*x])), x]

Rubi [A] time = 0.0245967, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*(a + b*ArcSin[c*x])),x]

[Out] Defer[Int][1/(x^2*(a + b*ArcSin[c*x])), x]

Rubi steps

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))} dx = \int \frac{1}{x^2(a+b \sin^{-1}(cx))} dx$$

Mathematica [A] time = 2.16653, size = 0, normalized size = 0.

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*(a + b*ArcSin[c*x])),x]

[Out] Integrate[1/(x^2*(a + b*ArcSin[c*x])), x]

Maple [A] time = 0.243, size = 0, normalized size = 0.

$$\int \frac{1}{x^2(a+b \arcsin(cx))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(a+b*arcsin(c*x)),x)

[Out] int(1/x^2/(a+b*arcsin(c*x)),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate(1/((b*arcsin(c*x) + a)*x^2), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{bx^2 \arcsin(cx) + ax^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(1/(b*x^2*arcsin(c*x) + a*x^2), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (a + b \arcsin(cx))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x**2/(a+b*asin(c*x)),x)

[Out] Integral(1/(x**2*(a + b*asin(c*x))), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/x^2/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] integrate(1/((b*arcsin(c*x) + a)*x^2), x)

$$3.163 \quad \int \frac{x^2}{(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=156

$$\frac{\sin\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{4b^2c^3} - \frac{3 \sin\left(\frac{3a}{b}\right) \operatorname{CosIntegral}\left(\frac{3(a+b \sin^{-1}(cx))}{b}\right)}{4b^2c^3} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{4b^2c^3} + \frac{3 \cos\left(\frac{3a}{b}\right) \operatorname{Si}\left(\frac{3(a+b \sin^{-1}(cx))}{b}\right)}{4b^2c^3}$$

[Out] $-\left(\frac{x^2 \sqrt{1-c^2 x^2}}{b c (a+b \operatorname{ArcSin}[c x])}\right) + \left(\frac{\operatorname{CosIntegral}\left[\frac{a+b \operatorname{ArcSin}[c x]}{b}\right] \sin\left[\frac{a}{b}\right]}{4 b^2 c^3} - \left(\frac{3 \operatorname{CosIntegral}\left[\frac{3(a+b \operatorname{ArcSin}[c x])}{b}\right] \sin\left[\frac{3 a}{b}\right]}{4 b^2 c^3} - \left(\frac{\cos\left[\frac{a}{b}\right] \operatorname{SinIntegral}\left[\frac{a+b \operatorname{ArcSin}[c x]}{b}\right]}{4 b^2 c^3} + \left(\frac{3 \cos\left[\frac{3 a}{b}\right] \operatorname{SinIntegral}\left[\frac{3(a+b \operatorname{ArcSin}[c x])}{b}\right]}{4 b^2 c^3}\right)}\right)\right)$

Rubi [A] time = 0.18189, antiderivative size = 152, normalized size of antiderivative = 0.97, number of steps used = 8, number of rules used = 4, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.286$, Rules used = {4631, 3303, 3299, 3302}

$$\frac{\sin\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{4b^2c^3} - \frac{3 \sin\left(\frac{3a}{b}\right) \operatorname{CosIntegral}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4b^2c^3} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{4b^2c^3} + \frac{3 \cos\left(\frac{3a}{b}\right) \operatorname{Si}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4b^2c^3}$$

Antiderivative was successfully verified.

[In] Int[x^2/(a + b*ArcSin[c*x])^2,x]

[Out] $-\left(\frac{x^2 \sqrt{1-c^2 x^2}}{b c (a+b \operatorname{ArcSin}[c x])}\right) + \left(\frac{\operatorname{CosIntegral}\left[\frac{a}{b} + \operatorname{ArcSin}[c x]\right] \sin\left[\frac{a}{b}\right]}{4 b^2 c^3} - \left(\frac{3 \operatorname{CosIntegral}\left[\frac{3 a}{b} + 3 \operatorname{ArcSin}[c x]\right] \sin\left[\frac{3 a}{b}\right]}{4 b^2 c^3} - \left(\frac{\cos\left[\frac{a}{b}\right] \operatorname{SinIntegral}\left[\frac{a}{b} + \operatorname{ArcSin}[c x]\right]}{4 b^2 c^3} + \left(\frac{3 \cos\left[\frac{3 a}{b}\right] \operatorname{SinIntegral}\left[\frac{3 a}{b} + 3 \operatorname{ArcSin}[c x]\right]}{4 b^2 c^3}\right)}\right)\right)$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^(n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^m*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -

c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a + b \sin^{-1}(cx))^2} dx &= -\frac{x^2 \sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} + \frac{\text{Subst}\left(\int \left(-\frac{\sin(x)}{4(a+bx)} + \frac{3 \sin(3x)}{4(a+bx)}\right) dx, x, \sin^{-1}(cx)\right)}{bc^3} \\ &= -\frac{x^2 \sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} - \frac{\text{Subst}\left(\int \frac{\sin(x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4bc^3} + \frac{3 \text{Subst}\left(\int \frac{\sin(3x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4bc^3} \\ &= -\frac{x^2 \sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} - \frac{\cos\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\sin\left(\frac{a}{b}+x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4bc^3} + \frac{\left(3 \cos\left(\frac{3a}{b}\right)\right) \text{Subst}\left(\int \frac{\sin\left(\frac{3a}{b}+x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{4bc^3} \\ &= -\frac{x^2 \sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} + \frac{\text{Ci}\left(\frac{a}{b} + \sin^{-1}(cx)\right) \sin\left(\frac{a}{b}\right)}{4b^2 c^3} - \frac{3 \text{Ci}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right) \sin\left(\frac{3a}{b}\right)}{4b^2 c^3} - \frac{\cos\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{4b^2 c^3} + \frac{3 \cos\left(\frac{3a}{b}\right) \text{Si}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{4b^2 c^3} \end{aligned}$$

Mathematica [A] time = 0.531093, size = 125, normalized size = 0.8

$$\frac{-\frac{4bc^2x^2\sqrt{1-c^2x^2}}{a+b\sin^{-1}(cx)} + \sin\left(\frac{a}{b}\right) \text{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right) - 3 \sin\left(\frac{3a}{b}\right) \text{CosIntegral}\left(3\left(\frac{a}{b} + \sin^{-1}(cx)\right)\right) - \cos\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right) + 3 \cos\left(\frac{3a}{b}\right) \text{Si}\left(3\left(\frac{a}{b} + \sin^{-1}(cx)\right)\right)}{4b^2c^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*ArcSin[c*x])^2,x]

[Out] ((-4*b*c^2*x^2*Sqrt[1 - c^2*x^2])/(a + b*ArcSin[c*x]) + CosIntegral[a/b + ArcSin[c*x]]*Sin[a/b] - 3*CosIntegral[3*(a/b + ArcSin[c*x])]*Sin[(3*a)/b] - Cos[a/b]*SinIntegral[a/b + ArcSin[c*x]] + 3*Cos[(3*a)/b]*SinIntegral[3*(a/b + ArcSin[c*x])])/(4*b^2*c^3)

Maple [A] time = 0.037, size = 149, normalized size = 1.

$$\frac{1}{c^3} \left(-\frac{1}{(4a + 4b \arcsin(cx))b} \sqrt{-c^2x^2 + 1} - \frac{1}{4b^2} \left(\text{Si}\left(\arcsin(cx) + \frac{a}{b}\right) \cos\left(\frac{a}{b}\right) - \text{Ci}\left(\arcsin(cx) + \frac{a}{b}\right) \sin\left(\frac{a}{b}\right) \right) + \frac{\cos\left(\frac{a}{b}\right) \text{Si}\left(3\arcsin(cx) + \frac{3a}{b}\right) - \sin\left(\frac{a}{b}\right) \text{Ci}\left(3\arcsin(cx) + \frac{3a}{b}\right)}{4b^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a+b*arcsin(c*x))^2,x)

[Out] 1/c^3*(-1/4*(-c^2*x^2+1)^(1/2)/(a+b*arcsin(c*x))/b-1/4*(Si(arcsin(c*x)+a/b)*cos(a/b)-Ci(arcsin(c*x)+a/b)*sin(a/b))/b^2+1/4*cos(3*arcsin(c*x))/(a+b*arcsin(c*x))/b+3/4*(Si(3*arcsin(c*x)+3*a/b)*cos(3*a/b)-Ci(3*arcsin(c*x)+3*a/b)*sin(3*a/b))/b^2)

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^2}{b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] integral(x^2/(b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(a + b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(a+b*asin(c*x))**2,x)

[Out] Integral(x**2/(a + b*asin(c*x))**2, x)

Giac [B] time = 1.40317, size = 872, normalized size = 5.59

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^2,x, algorithm="giac")

[Out]
$$\begin{aligned} & -3*b*\arcsin(c*x)*\cos(a/b)^2*\cos_integral(3*a/b + 3*\arcsin(c*x))*\sin(a/b)/(b \\ & ^3*c^3*\arcsin(c*x) + a*b^2*c^3) + 3*b*\arcsin(c*x)*\cos(a/b)^3*\sin_integral(3 \\ & *a/b + 3*\arcsin(c*x))/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) - 3*a*\cos(a/b)^2*co \\ & s_integral(3*a/b + 3*\arcsin(c*x))*\sin(a/b)/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3 \\ &) + 3*a*\cos(a/b)^3*\sin_integral(3*a/b + 3*\arcsin(c*x))/(b^3*c^3*\arcsin(c*x) \\ & + a*b^2*c^3) + 3/4*b*\arcsin(c*x)*\cos_integral(3*a/b + 3*\arcsin(c*x))*\sin(a \\ & /b)/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) + 1/4*b*\arcsin(c*x)*\cos_integral(a/b \\ & + \arcsin(c*x))*\sin(a/b)/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) - 9/4*b*\arcsin(c* \\ & x)*\cos(a/b)*\sin_integral(3*a/b + 3*\arcsin(c*x))/(b^3*c^3*\arcsin(c*x) + a*b^ \\ & 2*c^3) - 1/4*b*\arcsin(c*x)*\cos(a/b)*\sin_integral(a/b + \arcsin(c*x))/(b^3*c^ \\ & 3*\arcsin(c*x) + a*b^2*c^3) + 3/4*a*\cos_integral(3*a/b + 3*\arcsin(c*x))*\sin \\ & (a/b)/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) + 1/4*a*\cos_integral(a/b + \arcsin(c* \\ & x))*\sin(a/b)/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) - 9/4*a*\cos(a/b)*\sin_integra \\ & l(3*a/b + 3*\arcsin(c*x))/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) - 1/4*a*\cos(a/b) \\ & *\sin_integral(a/b + \arcsin(c*x))/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) + (-c^2* \\ & x^2 + 1)^(3/2)*b/(b^3*c^3*\arcsin(c*x) + a*b^2*c^3) - \sqrt{-c^2*x^2 + 1}*b/(\\ & b^3*c^3*\arcsin(c*x) + a*b^2*c^3) \end{aligned}$$

$$3.164 \quad \int \frac{x}{(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=90

$$\frac{\cos\left(\frac{2a}{b}\right) \text{CosIntegral}\left(\frac{2(a+b \sin^{-1}(cx))}{b}\right)}{b^2 c^2} + \frac{\sin\left(\frac{2a}{b}\right) \text{Si}\left(\frac{2(a+b \sin^{-1}(cx))}{b}\right)}{b^2 c^2} - \frac{x\sqrt{1-c^2 x^2}}{bc(a+b \sin^{-1}(cx))}$$

[Out] $-\left(\frac{x\sqrt{1-c^2 x^2}}{b c (a+b \text{ArcSin}[c x])}\right) + \left(\frac{\text{Cos}\left[\frac{2 a}{b}\right] \text{CosIntegral}\left[\frac{2(a+b \text{ArcSin}[c x])}{b}\right]}{b^2 c^2} + \frac{\text{Sin}\left[\frac{2 a}{b}\right] \text{SinIntegral}\left[\frac{2(a+b \text{ArcSin}[c x])}{b}\right]}{b^2 c^2}\right)$

Rubi [A] time = 0.10033, antiderivative size = 90, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {4631, 3303, 3299, 3302}

$$\frac{\cos\left(\frac{2a}{b}\right) \text{CosIntegral}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{b^2 c^2} + \frac{\sin\left(\frac{2a}{b}\right) \text{Si}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{b^2 c^2} - \frac{x\sqrt{1-c^2 x^2}}{bc(a+b \sin^{-1}(cx))}$$

Antiderivative was successfully verified.

[In] Int[x/(a + b*ArcSin[c*x])^2,x]

[Out] $-\left(\frac{x\sqrt{1-c^2 x^2}}{b c (a+b \text{ArcSin}[c x])}\right) + \left(\frac{\text{Cos}\left[\frac{2 a}{b}\right] \text{CosIntegral}\left[\frac{2 a}{b} + 2 \text{ArcSin}[c x]\right]}{b^2 c^2} + \frac{\text{Sin}\left[\frac{2 a}{b}\right] \text{SinIntegral}\left[\frac{2 a}{b} + 2 \text{ArcSin}[c x]\right]}{b^2 c^2}\right)$

Rule 4631

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] - Dist[1/(b*c^(m + 1)*(n + 1)), Subst[Int[ExpandTrigReduce[(a + b*x)^(n + 1), Sin[x]^(m - 1)*(m - (m + 1)*Sin[x]^2), x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GeQ[n, -2] && LtQ[n, -1]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{x}{(a + b \sin^{-1}(cx))^2} dx &= -\frac{x\sqrt{1-c^2x^2}}{bc(a + b \sin^{-1}(cx))} + \frac{\text{Subst}\left(\int \frac{\cos(2x)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{bc^2} \\ &= -\frac{x\sqrt{1-c^2x^2}}{bc(a + b \sin^{-1}(cx))} + \frac{\cos\left(\frac{2a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{2a}{b}+2x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{bc^2} + \frac{\sin\left(\frac{2a}{b}\right) \text{Subst}\left(\int \frac{\sin\left(\frac{2a}{b}+2x\right)}{a+bx} dx, x, \sin^{-1}(cx)\right)}{bc^2} \\ &= -\frac{x\sqrt{1-c^2x^2}}{bc(a + b \sin^{-1}(cx))} + \frac{\cos\left(\frac{2a}{b}\right) \text{Ci}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{b^2c^2} + \frac{\sin\left(\frac{2a}{b}\right) \text{Si}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{b^2c^2} \end{aligned}$$

Mathematica [A] time = 0.265858, size = 79, normalized size = 0.88

$$\frac{-\frac{bcx\sqrt{1-c^2x^2}}{a+b\sin^{-1}(cx)} + \cos\left(\frac{2a}{b}\right) \text{CosIntegral}\left(2\left(\frac{a}{b} + \sin^{-1}(cx)\right)\right) + \sin\left(\frac{2a}{b}\right) \text{Si}\left(2\left(\frac{a}{b} + \sin^{-1}(cx)\right)\right)}{b^2c^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*ArcSin[c*x])^2,x]

[Out] $\left(-\frac{(b*c*x*\text{Sqrt}[1 - c^2*x^2])}{(a + b*\text{ArcSin}[c*x])} + \text{Cos}[(2*a)/b]*\text{CosIntegral}[2*(a/b + \text{ArcSin}[c*x])] + \text{Sin}[(2*a)/b]*\text{SinIntegral}[2*(a/b + \text{ArcSin}[c*x])]\right)/(b^2*c^2)$

Maple [A] time = 0.027, size = 77, normalized size = 0.9

$$\frac{1}{c^2} \left(-\frac{\sin(2 \arcsin(cx))}{(2a + 2b \arcsin(cx))b} + \frac{1}{b^2} \left(\text{Si}\left(2 \arcsin(cx) + 2\frac{a}{b}\right) \sin\left(2\frac{a}{b}\right) + \text{Ci}\left(2 \arcsin(cx) + 2\frac{a}{b}\right) \cos\left(2\frac{a}{b}\right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(a+b*arcsin(c*x))^2,x)

[Out] $\frac{1}{c^2} \left(-\frac{\sin(2 \arcsin(cx))}{(2a + 2b \arcsin(cx))b} + \frac{1}{b^2} \left(\text{Si}\left(2 \arcsin(cx) + 2\frac{a}{b}\right) \sin\left(2\frac{a}{b}\right) + \text{Ci}\left(2 \arcsin(cx) + 2\frac{a}{b}\right) \cos\left(2\frac{a}{b}\right) \right) \right)$

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x}{b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] integral(x/(b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(a + b \operatorname{asin}(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*asin(c*x))**2,x)

[Out] Integral(x/(a + b*asin(c*x))**2, x)

Giac [B] time = 1.41347, size = 440, normalized size = 4.89

$$\frac{2 b \operatorname{arcsin}(cx) \cos\left(\frac{a}{b}\right)^2 \operatorname{Ci}\left(\frac{2a}{b} + 2 \operatorname{arcsin}(cx)\right)}{b^3 c^2 \operatorname{arcsin}(cx) + ab^2 c^2} + \frac{2 b \operatorname{arcsin}(cx) \cos\left(\frac{a}{b}\right) \sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{2a}{b} + 2 \operatorname{arcsin}(cx)\right)}{b^3 c^2 \operatorname{arcsin}(cx) + ab^2 c^2} + \frac{2 a \cos\left(\frac{a}{b}\right)}{b^3 c^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^2,x, algorithm="giac")

[Out] 2*b*arcsin(c*x)*cos(a/b)^2*cos_integral(2*a/b + 2*arcsin(c*x))/(b^3*c^2*arcsin(c*x) + a*b^2*c^2) + 2*b*arcsin(c*x)*cos(a/b)*sin(a/b)*sin_integral(2*a/b + 2*arcsin(c*x))/(b^3*c^2*arcsin(c*x) + a*b^2*c^2) + 2*a*cos(a/b)^2*cos_integral(2*a/b + 2*arcsin(c*x))/(b^3*c^2*arcsin(c*x) + a*b^2*c^2) + 2*a*cos(a/b)*sin(a/b)*sin_integral(2*a/b + 2*arcsin(c*x))/(b^3*c^2*arcsin(c*x) + a*b^2*c^2) - sqrt(-c^2*x^2 + 1)*b*c*x/(b^3*c^2*arcsin(c*x) + a*b^2*c^2) - b*arcsin(c*x)*cos_integral(2*a/b + 2*arcsin(c*x))/(b^3*c^2*arcsin(c*x) + a*b^2*c^2) - a*cos_integral(2*a/b + 2*arcsin(c*x))/(b^3*c^2*arcsin(c*x) + a*b^2*c^2)

$$3.165 \quad \int \frac{1}{(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=86

$$\frac{\sin\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{b^2 c} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{b^2 c} - \frac{\sqrt{1-c^2 x^2}}{bc(a+b \sin^{-1}(cx))}$$

[Out] -(Sqrt[1 - c^2*x^2]/(b*c*(a + b*ArcSin[c*x]))) + (CosIntegral[(a + b*ArcSin[c*x])/b]*Sin[a/b])/(b^2*c) - (Cos[a/b]*SinIntegral[(a + b*ArcSin[c*x])/b])/(b^2*c)

Rubi [A] time = 0.168647, antiderivative size = 82, normalized size of antiderivative = 0.95, number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4621, 4723, 3303, 3299, 3302}

$$\frac{\sin\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{b^2 c} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{b^2 c} - \frac{\sqrt{1-c^2 x^2}}{bc(a+b \sin^{-1}(cx))}$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^(-2), x]

[Out] -(Sqrt[1 - c^2*x^2]/(b*c*(a + b*ArcSin[c*x]))) + (CosIntegral[a/b + ArcSin[c*x]]*Sin[a/b])/(b^2*c) - (Cos[a/b]*SinIntegral[a/b + ArcSin[c*x]])/(b^2*c)

Rule 4621

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_.), x_Symbol] :> Simp[(Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + Dist[c/(b*(n + 1)), Int[(x*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && LtQ[n, -1]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^ (n_.)*(x_)^ (m_.)*((d_.) + (e_.)*(x_)^2)^ (p_.), x_Symbol] :> Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{(a + b \sin^{-1}(cx))^2} dx &= -\frac{\sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} - \frac{c \int \frac{x}{\sqrt{1 - c^2 x^2}(a + b \sin^{-1}(cx))} dx}{b} \\ &= -\frac{\sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} - \frac{\text{Subst}\left(\int \frac{\sin(x)}{a + bx} dx, x, \sin^{-1}(cx)\right)}{bc} \\ &= -\frac{\sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} - \frac{\cos\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\sin\left(\frac{a}{b} + x\right)}{a + bx} dx, x, \sin^{-1}(cx)\right)}{bc} + \frac{\sin\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{a}{b} + x\right)}{a + bx} dx, x, \sin^{-1}(cx)\right)}{bc} \\ &= -\frac{\sqrt{1 - c^2 x^2}}{bc(a + b \sin^{-1}(cx))} + \frac{\text{Ci}\left(\frac{a}{b} + \sin^{-1}(cx)\right) \sin\left(\frac{a}{b}\right)}{b^2 c} - \frac{\cos\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{b^2 c} \end{aligned}$$

Mathematica [A] time = 0.155814, size = 72, normalized size = 0.84

$$\frac{-\frac{b\sqrt{1-c^2x^2}}{a+b\sin^{-1}(cx)} + \sin\left(\frac{a}{b}\right) \text{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right) - \cos\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{b^2 c}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*ArcSin[c*x])^(-2), x]
```

```
[Out] (-(b*Sqrt[1 - c^2*x^2])/(a + b*ArcSin[c*x])) + CosIntegral[a/b + ArcSin[c*x]]*Sin[a/b] - Cos[a/b]*SinIntegral[a/b + ArcSin[c*x]]/(b^2*c)
```

Maple [A] time = 0.03, size = 76, normalized size = 0.9

$$\frac{1}{c} \left(-\frac{1}{(a + b \arcsin(cx))b} \sqrt{-c^2 x^2 + 1} - \frac{1}{b^2} \left(\text{Si}\left(\arcsin(cx) + \frac{a}{b}\right) \cos\left(\frac{a}{b}\right) - \text{Ci}\left(\arcsin(cx) + \frac{a}{b}\right) \sin\left(\frac{a}{b}\right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(a+b*arcsin(c*x))^2,x)
```

```
[Out] 1/c*(-(-c^2*x^2+1)^(1/2)/(a+b*arcsin(c*x))/b-(Si(arcsin(c*x)+a/b)*cos(a/b)-Ci(arcsin(c*x)+a/b)*sin(a/b))/b^2)
```

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a+b*arcsin(c*x))^2,x, algorithm="maxima")
```

[Out] Timed out

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] integral(1/(b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(a + b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*asin(c*x))**2,x)

[Out] Integral((a + b*asin(c*x))**(-2), x)

Giac [B] time = 1.35946, size = 259, normalized size = 3.01

$$\frac{b \arcsin(cx) \operatorname{Ci}\left(\frac{a}{b} + \arcsin(cx)\right) \sin\left(\frac{a}{b}\right)}{b^3 c \arcsin(cx) + ab^2 c} - \frac{b \arcsin(cx) \cos\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a}{b} + \arcsin(cx)\right)}{b^3 c \arcsin(cx) + ab^2 c} + \frac{a \operatorname{Ci}\left(\frac{a}{b} + \arcsin(cx)\right) \sin\left(\frac{a}{b}\right)}{b^3 c \arcsin(cx) + ab^2 c} - \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^2,x, algorithm="giac")

[Out] b*arcsin(c*x)*cos_integral(a/b + arcsin(c*x))*sin(a/b)/(b^3*c*arcsin(c*x) + a*b^2*c) - b*arcsin(c*x)*cos(a/b)*sin_integral(a/b + arcsin(c*x))/(b^3*c*arcsin(c*x) + a*b^2*c) + a*cos_integral(a/b + arcsin(c*x))*sin(a/b)/(b^3*c*arcsin(c*x) + a*b^2*c) - a*cos(a/b)*sin_integral(a/b + arcsin(c*x))/(b^3*c*arcsin(c*x) + a*b^2*c) - sqrt(-c^2*x^2 + 1)*b/(b^3*c*arcsin(c*x) + a*b^2*c)

$$3.166 \quad \int \frac{1}{x(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable} \left(\frac{1}{x(a+b \sin^{-1}(cx))^2}, x \right)$$

[Out] Unintegrable[1/(x*(a + b*ArcSin[c*x])^2), x]

Rubi [A] time = 0.0226791, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*(a + b*ArcSin[c*x])^2), x]

[Out] Defer[Int][1/(x*(a + b*ArcSin[c*x])^2), x]

Rubi steps

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^2} dx = \int \frac{1}{x(a+b \sin^{-1}(cx))^2} dx$$

Mathematica [A] time = 3.98478, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*(a + b*ArcSin[c*x])^2), x]

[Out] Integrate[1/(x*(a + b*ArcSin[c*x])^2), x]

Maple [A] time = 0.184, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(a+b*arcsin(c*x))^2,x)

[Out] `int(1/x/(a+b*arcsin(c*x))^2,x)`

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^2,x, algorithm="maxima")`

[Out] Timed out

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{b^2x \arcsin(cx)^2 + 2abx \arcsin(cx) + a^2x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^2,x, algorithm="fricas")`

[Out] `integral(1/(b^2*x*arcsin(c*x)^2 + 2*a*b*x*arcsin(c*x) + a^2*x), x)`

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x(a + b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*asin(c*x))**2,x)`

[Out] `Integral(1/(x*(a + b*asin(c*x))**2), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^2 x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^2,x, algorithm="giac")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^2*x), x)`

$$3.167 \quad \int \frac{1}{x^2(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable}\left(\frac{1}{x^2(a+b \sin^{-1}(cx))^2}, x\right)$$

[Out] Unintegrable[1/(x^2*(a + b*ArcSin[c*x])^2), x]

Rubi [A] time = 0.0228626, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*(a + b*ArcSin[c*x])^2), x]

[Out] Defer[Int][1/(x^2*(a + b*ArcSin[c*x])^2), x]

Rubi steps

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^2} dx = \int \frac{1}{x^2(a+b \sin^{-1}(cx))^2} dx$$

Mathematica [A] time = 33.3234, size = 0, normalized size = 0.

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*(a + b*ArcSin[c*x])^2), x]

[Out] Integrate[1/(x^2*(a + b*ArcSin[c*x])^2), x]

Maple [A] time = 0.339, size = 0, normalized size = 0.

$$\int \frac{1}{x^2(a+b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(a+b*arcsin(c*x))^2, x)

[Out] `int(1/x^2/(a+b*arcsin(c*x))^2,x)`

Maxima [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^2,x, algorithm="maxima")`

[Out] Timed out

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{b^2x^2\arcsin(cx)^2 + 2abx^2\arcsin(cx) + a^2x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^2,x, algorithm="fricas")`

[Out] `integral(1/(b^2*x^2*arcsin(c*x)^2 + 2*a*b*x^2*arcsin(c*x) + a^2*x^2), x)`

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2(a + b\arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(a+b*asin(c*x))**2,x)`

[Out] `Integral(1/(x**2*(a + b*asin(c*x))**2), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b\arcsin(cx) + a)^2x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^2,x, algorithm="giac")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^2*x^2), x)`

$$3.168 \quad \int \frac{x^2}{(a+b \sin^{-1}(cx))^3} dx$$

Optimal. Leaf size=197

$$-\frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{8b^3c^3} + \frac{9 \cos\left(\frac{3a}{b}\right) \operatorname{CosIntegral}\left(\frac{3(a+b \sin^{-1}(cx))}{b}\right)}{8b^3c^3} - \frac{\sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{8b^3c^3} + \frac{9 \sin\left(\frac{3a}{b}\right) \operatorname{Si}\left(\frac{3(a+b \sin^{-1}(cx))}{b}\right)}{8b^3c^3}$$

```
[Out] -(x^2*sqrt[1 - c^2*x^2])/(2*b*c*(a + b*ArcSin[c*x])^2) - x/(b^2*c^2*(a + b*
ArcSin[c*x])) + (3*x^3)/(2*b^2*(a + b*ArcSin[c*x])) - (Cos[a/b]*CosIntegral
[(a + b*ArcSin[c*x])/b])/(8*b^3*c^3) + (9*Cos[(3*a)/b]*CosIntegral[(3*(a +
b*ArcSin[c*x]))/b])/(8*b^3*c^3) - (Sin[a/b]*SinIntegral[(a + b*ArcSin[c*x])
/b])/(8*b^3*c^3) + (9*Ssin[(3*a)/b]*SinIntegral[(3*(a + b*ArcSin[c*x]))/b])/(
(8*b^3*c^3))
```

Rubi [A] time = 0.542489, antiderivative size = 245, normalized size of antiderivative = 1.24, number of steps used = 16, number of rules used = 8, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.571$, Rules used = {4633, 4719, 4635, 4406, 3303, 3299, 3302, 4623}

$$-\frac{9 \cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{8b^3c^3} + \frac{9 \cos\left(\frac{3a}{b}\right) \operatorname{CosIntegral}\left(\frac{3a}{b} + 3 \sin^{-1}(cx)\right)}{8b^3c^3} + \frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{b^3c^3}$$

Antiderivative was successfully verified.

```
[In] Int[x^2/(a + b*ArcSin[c*x])^3,x]
```

```
[Out] -(x^2*sqrt[1 - c^2*x^2])/(2*b*c*(a + b*ArcSin[c*x])^2) - x/(b^2*c^2*(a + b*
ArcSin[c*x])) + (3*x^3)/(2*b^2*(a + b*ArcSin[c*x])) - (9*Cos[a/b]*CosIntegr
al[a/b + ArcSin[c*x]])/(8*b^3*c^3) + (9*Cos[(3*a)/b]*CosIntegral[(3*a)/b +
3*ArcSin[c*x]])/(8*b^3*c^3) + (Cos[a/b]*CosIntegral[(a + b*ArcSin[c*x])/b])
/(b^3*c^3) - (9*Ssin[a/b]*SinIntegral[a/b + ArcSin[c*x]])/(8*b^3*c^3) + (9*S
sin[(3*a)/b]*SinIntegral[(3*a)/b + 3*ArcSin[c*x]])/(8*b^3*c^3) + (Sin[a/b]*S
inIntegral[(a + b*ArcSin[c*x])/b])/(b^3*c^3)
```

Rule 4633

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)^m_., x_Symbol] := Simp[(x^m*sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + (Dist[(c*(m + 1))/(b*(n + 1)), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n + 1))/sqrt[1 - c^2*x^2], x], x] - Dist[m/(b*c*(n + 1)), Int[(x^(m - 1)*(a + b*ArcSin[c*x])^(n + 1))/sqrt[1 - c^2*x^2], x], x]) /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && LtQ[n, -2]
```

Rule 4719

```
Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_)*((f_.)*(x_)^m_)/sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]
```

Rule 4635

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x]
/; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 4623

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^ (n_), x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]
```

Rubi steps

$$\begin{aligned}
\int \frac{x^2}{(a + b \sin^{-1}(cx))^3} dx &= -\frac{x^2 \sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} + \frac{\int \frac{x}{\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2} dx}{bc} - \frac{(3c) \int \frac{x^3}{\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2} dx}{2b} \\
&= -\frac{x^2 \sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} - \frac{x}{b^2 c^2 (a + b \sin^{-1}(cx))} + \frac{3x^3}{2b^2 (a + b \sin^{-1}(cx))} - \frac{9 \int \frac{x^2}{a + b \sin^{-1}(cx)} dx}{2b^2} \\
&= -\frac{x^2 \sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} - \frac{x}{b^2 c^2 (a + b \sin^{-1}(cx))} + \frac{3x^3}{2b^2 (a + b \sin^{-1}(cx))} + \frac{\text{Subst} \left(\int \frac{\cos(\frac{a}{b})}{x} dx \right)}{b^2} \\
&= -\frac{x^2 \sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} - \frac{x}{b^2 c^2 (a + b \sin^{-1}(cx))} + \frac{3x^3}{2b^2 (a + b \sin^{-1}(cx))} - \frac{9 \text{Subst} \left(\int \left(\frac{\cos(\frac{a}{b})}{4(a + b \sin^{-1}(cx))} \right) dx \right)}{b^2} \\
&= -\frac{x^2 \sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} - \frac{x}{b^2 c^2 (a + b \sin^{-1}(cx))} + \frac{3x^3}{2b^2 (a + b \sin^{-1}(cx))} + \frac{\cos(\frac{a}{b}) \text{Ci} \left(\frac{a + b \sin^{-1}(cx)}{b} \right)}{b^3 c^3} \\
&= -\frac{x^2 \sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} - \frac{x}{b^2 c^2 (a + b \sin^{-1}(cx))} + \frac{3x^3}{2b^2 (a + b \sin^{-1}(cx))} + \frac{\cos(\frac{a}{b}) \text{Ci} \left(\frac{a + b \sin^{-1}(cx)}{b} \right)}{b^3 c^3} \\
&= -\frac{x^2 \sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} - \frac{x}{b^2 c^2 (a + b \sin^{-1}(cx))} + \frac{3x^3}{2b^2 (a + b \sin^{-1}(cx))} - \frac{9 \cos(\frac{a}{b}) \text{Ci} \left(\frac{a + b \sin^{-1}(cx)}{b} \right)}{8b^3 c^3}
\end{aligned}$$

Mathematica [A] time = 0.861159, size = 168, normalized size = 0.85

$$\frac{4b^2 x^2 \sqrt{1 - c^2 x^2}}{c(a + b \sin^{-1}(cx))^2} + \frac{\cos(\frac{a}{b}) \text{CosIntegral}(\frac{a}{b} + \sin^{-1}(cx))}{c^3} - \frac{9 \cos(\frac{3a}{b}) \text{CosIntegral}(3(\frac{a}{b} + \sin^{-1}(cx)))}{c^3} + \frac{\sin(\frac{a}{b}) \text{Si}(\frac{a}{b} + \sin^{-1}(cx))}{c^3} - \frac{9 \sin(\frac{3a}{b}) \text{Si}(3(\frac{a}{b} + \sin^{-1}(cx)))}{c^3}$$

$$8b^3$$

Antiderivative was successfully verified.

[In] Integrate[x^2/(a + b*ArcSin[c*x])^3,x]

[Out] -((4*b^2*x^2*sqrt[1 - c^2*x^2])/(c*(a + b*ArcSin[c*x])^2) + (8*b*x)/(c^2*(a + b*ArcSin[c*x])) - (12*b*x^3)/(a + b*ArcSin[c*x]) + (Cos[a/b]*CosIntegral[a/b + ArcSin[c*x]])/c^3 - (9*cos[(3*a)/b]*CosIntegral[3*(a/b + ArcSin[c*x])])/c^3 + (Sin[a/b]*SinIntegral[a/b + ArcSin[c*x]])/c^3 - (9*sin[(3*a)/b]*SinIntegral[3*(a/b + ArcSin[c*x])])/c^3)/(8*b^3)

Maple [A] time = 0.034, size = 290, normalized size = 1.5

$$\frac{1}{c^3} \left(-\frac{1}{8(a + b \arcsin(cx))^2 b} \sqrt{-c^2 x^2 + 1} - \frac{1}{(8a + 8b \arcsin(cx)) b^3} \left(\arcsin(cx) \text{Si} \left(\arcsin(cx) + \frac{a}{b} \right) \sin \left(\frac{a}{b} \right) b + \arcsin \left(\arcsin(cx) + \frac{a}{b} \right) \cos \left(\frac{a}{b} \right) b + \text{Si} \left(\arcsin(cx) + \frac{a}{b} \right) \cos \left(\frac{a}{b} \right) b \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a+b*arcsin(c*x))^3,x)

[Out] 1/c^3*(-1/8*(-c^2*x^2+1)^(1/2)/(a+b*arcsin(c*x))^2/b-1/8*(arcsin(c*x)*Si(arcsin(c*x)+a/b)*sin(a/b)*b+arcsin(c*x)*Ci(arcsin(c*x)+a/b)*cos(a/b)*b+Si(arcsin(c*x)+a/b)*cos(a/b)*b+Si(arcsin(c*x)+a/b)*sin(a/b)*b)/(8*b^3)

$$\frac{\sin(cx) + a/b \sin(a/b) a + \text{Ci}(\arcsin(cx) + a/b) \cos(a/b) a - x b c}{(a + b \arcsin(cx)) / b^3 + 1/8 \cos(3 \arcsin(cx)) / (a + b \arcsin(cx))^2 / b^3 + 3/8 (3 \arcsin(cx) \sin(3 \arcsin(cx) + 3a/b) \sin(3a/b) b + 3 \arcsin(cx) \text{Ci}(3 \arcsin(cx) + 3a/b) \cos(3a/b) b + 3 \text{Si}(3 \arcsin(cx) + 3a/b) \sin(3a/b) a + 3 \text{Ci}(3 \arcsin(cx) + 3a/b) \cos(3a/b) a - \sin(3 \arcsin(cx)) b} / (a + b \arcsin(cx)) / b^3$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{3ac^2x^3 - \sqrt{cx+1}\sqrt{-cx+1}bcx^2 - 2ax + (3bc^2x^3 - 2bx) \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) - (b^4c^2 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) - b^4c^2 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}))^2 + 2ab^3c^2 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})}{2(b^4c^2 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})^2 + 2ab^3c^2 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}))}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^3,x, algorithm="maxima")

[Out] 1/2*(3*a*c^2*x^3 - sqrt(c*x + 1)*sqrt(-c*x + 1)*b*c*x^2 - 2*a*x + (3*b*c^2*x^3 - 2*b*x)*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) - 2*(b^4*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^2 + 2*a*b^3*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) + a^2*b^2*c^2)*integrate(1/2*(9*c^2*x^2 - 2)/(b^3*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) + a*b^2*c^2), x))/(b^4*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^2 + 2*a*b^3*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) + a^2*b^2*c^2)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x^2}{b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^3,x, algorithm="fricas")

[Out] integral(x^2/(b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) + a^3), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(a + b \arcsin(cx))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(a+b*asin(c*x))**3,x)

[Out] Integral(x**2/(a + b*asin(c*x))**3, x)

Giac [B] time = 1.7048, size = 2078, normalized size = 10.55

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^3,x, algorithm="giac")

[Out]
$$\frac{9}{2}b^2\arcsin(cx)^2\cos(a/b)^3\cos_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{9}{2}b^2\arcsin(cx)^2\cos(a/b)^2\sin(a/b)\sin_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + 9ab\arcsin(cx)\cos(a/b)^3\cos_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + 9ab\arcsin(cx)\cos(a/b)^2\sin(a/b)\sin_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{3}{2}(c^2x^2 - 1)b^2cx\arcsin(cx)/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{27}{8}b^2\arcsin(cx)^2\cos(a/b)\cos_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{9}{2}a^2\cos(a/b)^3\cos_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{1}{8}b^2\arcsin(cx)^2\cos(a/b)\cos_integral(a/b + \arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{9}{8}b^2\arcsin(cx)^2\sin(a/b)\sin_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{9}{2}a^2\cos(a/b)^2\sin(a/b)\sin_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{1}{8}b^2\arcsin(cx)^2\sin(a/b)\sin_integral(a/b + \arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{3}{2}(c^2x^2 - 1)abcx/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{1}{2}b^2cx\arcsin(cx)/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{27}{4}ab\arcsin(cx)\cos(a/b)\cos_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{1}{4}ab\arcsin(cx)\cos(a/b)\cos_integral(a/b + \arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{9}{4}ab\arcsin(cx)\sin(a/b)\sin_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{1}{4}ab\arcsin(cx)\sin(a/b)\sin_integral(a/b + \arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{1}{2}abcx/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{27}{8}a^2\cos(a/b)\cos_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{1}{8}a^2\cos(a/b)\cos_integral(a/b + \arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{9}{8}a^2\sin(a/b)\sin_integral(3a/b + 3\arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{1}{8}a^2\sin(a/b)\sin_integral(a/b + \arcsin(cx))/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) + \frac{1}{2}(-c^2x^2 + 1)^{(3/2)}b^2/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3) - \frac{1}{2}\sqrt{-c^2x^2 + 1}b^2/(b^5c^3\arcsin(cx)^2 + 2ab^4c^3\arcsin(cx) + a^2b^3c^3)$$

$$3.169 \quad \int \frac{x}{(a+b \sin^{-1}(cx))^3} dx$$

Optimal. Leaf size=130

$$\frac{\sin\left(\frac{2a}{b}\right) \text{CosIntegral}\left(\frac{2(a+b \sin^{-1}(cx))}{b}\right)}{b^3 c^2} - \frac{\cos\left(\frac{2a}{b}\right) \text{Si}\left(\frac{2(a+b \sin^{-1}(cx))}{b}\right)}{b^3 c^2} - \frac{1}{2b^2 c^2 (a+b \sin^{-1}(cx))} + \frac{x^2}{b^2 (a+b \sin^{-1}(cx))} - \frac{1}{2}$$

[Out] $-(x*\text{Sqrt}[1 - c^2*x^2])/(2*b*c*(a + b*\text{ArcSin}[c*x])^2) - 1/(2*b^2*c^2*(a + b*\text{ArcSin}[c*x])) + x^2/(b^2*(a + b*\text{ArcSin}[c*x])) + (\text{CosIntegral}[(2*(a + b*\text{ArcSin}[c*x]))/b]*\text{Sin}[(2*a)/b])/(b^3*c^2) - (\text{Cos}[(2*a)/b]*\text{SinIntegral}[(2*(a + b*\text{ArcSin}[c*x]))/b])/(b^3*c^2)$

Rubi [A] time = 0.322832, antiderivative size = 130, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 9, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.75$, Rules used = {4633, 4719, 4635, 4406, 12, 3303, 3299, 3302, 4641}

$$\frac{\sin\left(\frac{2a}{b}\right) \text{CosIntegral}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{b^3 c^2} - \frac{\cos\left(\frac{2a}{b}\right) \text{Si}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{b^3 c^2} - \frac{1}{2b^2 c^2 (a+b \sin^{-1}(cx))} + \frac{x^2}{b^2 (a+b \sin^{-1}(cx))} - \frac{1}{2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x/(a + b*\text{ArcSin}[c*x])^3, x]$

[Out] $-(x*\text{Sqrt}[1 - c^2*x^2])/(2*b*c*(a + b*\text{ArcSin}[c*x])^2) - 1/(2*b^2*c^2*(a + b*\text{ArcSin}[c*x])) + x^2/(b^2*(a + b*\text{ArcSin}[c*x])) + (\text{CosIntegral}[(2*a)/b + 2*\text{ArcSin}[c*x]]*\text{Sin}[(2*a)/b])/(b^3*c^2) - (\text{Cos}[(2*a)/b]*\text{SinIntegral}[(2*a)/b + 2*\text{ArcSin}[c*x]])/(b^3*c^2)$

Rule 4633

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + x)^n*(x)^m, x_Symbol] \rightarrow \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{n+1})/(b*c*(n+1)), x] + (\text{Dist}[(c*(m+1))/(b*(n+1)), \text{Int}[(x^{m+1}*(a + b*\text{ArcSin}[c*x])^{n+1})/\text{Sqrt}[1 - c^2*x^2], x], x] - \text{Dist}[m/(b*c*(n+1)), \text{Int}[(x^{m-1}*(a + b*\text{ArcSin}[c*x])^{n+1})/\text{Sqrt}[1 - c^2*x^2], x], x]) /; \text{FreeQ}\{a, b, c\}, x \&\& \text{IGtQ}[m, 0] \&\& \text{LtQ}[n, -2]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + x)^n*((f + x)^m)/\text{Sqrt}[d + (e + x)^2], x_Symbol] \rightarrow \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{n+1})/(b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{m-1}*(a + b*\text{ArcSin}[c*x])^{n+1}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{LtQ}[n, -1] \&\& \text{GtQ}[d, 0]$

Rule 4635

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + x)^n*(x)^m, x_Symbol] \rightarrow \text{Dist}[1/c^{m+1}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x], x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c, n\}, x \&\& \text{IGtQ}[m, 0]$

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 4641

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] := Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{x}{(a + b \sin^{-1}(cx))^3} dx &= -\frac{x\sqrt{1-c^2x^2}}{2bc(a + b \sin^{-1}(cx))^2} + \frac{\int \frac{1}{\sqrt{1-c^2x^2}(a+b \sin^{-1}(cx))^2} dx}{2bc} - \frac{c \int \frac{x^2}{\sqrt{1-c^2x^2}(a+b \sin^{-1}(cx))^2} dx}{b} \\
&= -\frac{x\sqrt{1-c^2x^2}}{2bc(a + b \sin^{-1}(cx))^2} - \frac{1}{2b^2c^2(a + b \sin^{-1}(cx))} + \frac{x^2}{b^2(a + b \sin^{-1}(cx))} - \frac{2 \int \frac{x}{a+b \sin^{-1}(cx)} dx}{b^2} \\
&= -\frac{x\sqrt{1-c^2x^2}}{2bc(a + b \sin^{-1}(cx))^2} - \frac{1}{2b^2c^2(a + b \sin^{-1}(cx))} + \frac{x^2}{b^2(a + b \sin^{-1}(cx))} - \frac{2 \operatorname{Subst}\left(\int \frac{\cos(x) \sin}{a+bx} dx\right)}{b^2} \\
&= -\frac{x\sqrt{1-c^2x^2}}{2bc(a + b \sin^{-1}(cx))^2} - \frac{1}{2b^2c^2(a + b \sin^{-1}(cx))} + \frac{x^2}{b^2(a + b \sin^{-1}(cx))} - \frac{2 \operatorname{Subst}\left(\int \frac{\sin(2x)}{2(a+bx)} dx\right)}{b^2c^2} \\
&= -\frac{x\sqrt{1-c^2x^2}}{2bc(a + b \sin^{-1}(cx))^2} - \frac{1}{2b^2c^2(a + b \sin^{-1}(cx))} + \frac{x^2}{b^2(a + b \sin^{-1}(cx))} - \frac{\operatorname{Subst}\left(\int \frac{\sin(2x)}{a+bx} dx\right)}{b^2c^2} \\
&= -\frac{x\sqrt{1-c^2x^2}}{2bc(a + b \sin^{-1}(cx))^2} - \frac{1}{2b^2c^2(a + b \sin^{-1}(cx))} + \frac{x^2}{b^2(a + b \sin^{-1}(cx))} - \frac{\cos\left(\frac{2a}{b}\right) \operatorname{Subst}\left(\int \frac{\sin(2x)}{a+bx} dx\right)}{b^2c^2} \\
&= -\frac{x\sqrt{1-c^2x^2}}{2bc(a + b \sin^{-1}(cx))^2} - \frac{1}{2b^2c^2(a + b \sin^{-1}(cx))} + \frac{x^2}{b^2(a + b \sin^{-1}(cx))} + \frac{\operatorname{Ci}\left(\frac{2a}{b} + 2 \sin^{-1}(cx)\right)}{b^3c^2}
\end{aligned}$$

Mathematica [A] time = 0.330467, size = 108, normalized size = 0.83

$$\frac{-\frac{b^2cx\sqrt{1-c^2x^2}}{(a+b \sin^{-1}(cx))^2} + \frac{b(2c^2x^2-1)}{a+b \sin^{-1}(cx)} + 2 \sin\left(\frac{2a}{b}\right) \operatorname{CosIntegral}\left(2\left(\frac{a}{b} + \sin^{-1}(cx)\right)\right) - 2 \cos\left(\frac{2a}{b}\right) \operatorname{Si}\left(2\left(\frac{a}{b} + \sin^{-1}(cx)\right)\right)}{2b^3c^2}$$

Antiderivative was successfully verified.

[In] Integrate[x/(a + b*ArcSin[c*x])^3,x]

[Out] (-((b^2*c*x*Sqrt[1 - c^2*x^2])/(a + b*ArcSin[c*x])^2) + (b*(-1 + 2*c^2*x^2))/(a + b*ArcSin[c*x]) + 2*CosIntegral[2*(a/b + ArcSin[c*x])]*Sin[(2*a)/b] - 2*Cos[(2*a)/b]*SinIntegral[2*(a/b + ArcSin[c*x])])/(2*b^3*c^2)

Maple [A] time = 0.027, size = 157, normalized size = 1.2

$$\frac{1}{c^2} \left(-\frac{\sin(2 \arcsin(cx))}{4(a + b \arcsin(cx))^2 b} - \frac{1}{(2a + 2b \arcsin(cx)) b^3} \left(2 \arcsin(cx) \operatorname{Si}\left(2 \arcsin(cx) + 2 \frac{a}{b}\right) \cos\left(2 \frac{a}{b}\right) b - 2 \arcsin(cx) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(a+b*arcsin(c*x))^3,x)

[Out] 1/c^2*(-1/4*sin(2*arcsin(c*x))/(a+b*arcsin(c*x))^2/b-1/2*(2*arcsin(c*x)*Si(2*arcsin(c*x)+2*a/b)*cos(2*a/b)*b-2*arcsin(c*x)*Ci(2*arcsin(c*x)+2*a/b)*sin(2*a/b)*b+2*Si(2*arcsin(c*x)+2*a/b)*cos(2*a/b)*a-2*Ci(2*arcsin(c*x)+2*a/b)*sin(2*a/b)*a+cos(2*arcsin(c*x))*b)/(a+b*arcsin(c*x))/b^3)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{2ac^2x^2 - \sqrt{cx+1}\sqrt{-cx+1}bcx + (2bc^2x^2 - b)\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) - a - \frac{4(b^4c^2\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})^2 + 2ab^3c^2)}{2(b^4c^2\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})^2 + 2ab^3c^2\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})}}{2(b^4c^2\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})^2 + 2ab^3c^2\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^3,x, algorithm="maxima")

[Out] 1/2*(2*a*c^2*x^2 - sqrt(c*x + 1)*sqrt(-c*x + 1)*b*c*x + (2*b*c^2*x^2 - b)*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) - 4*(b^4*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^2 + 2*a*b^3*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) + a^2*b^2*c^2)*integrate(x/(b^3*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) + a*b^2), x) - a)/(b^4*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1))^2 + 2*a*b^3*c^2*arctan2(c*x, sqrt(c*x + 1)*sqrt(-c*x + 1)) + a^2*b^2*c^2)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{x}{b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^3,x, algorithm="fricas")

[Out] integral(x/(b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) + a^3), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(a + b \arcsin(cx))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*asin(c*x))**3,x)

[Out] Integral(x/(a + b*asin(c*x))**3, x)

Giac [B] time = 1.68654, size = 1166, normalized size = 8.97

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^3,x, algorithm="giac")

[Out] 2*b^2*arcsin(c*x)^2*cos(a/b)*cos_integral(2*a/b + 2*arcsin(c*x))*sin(a/b)/(b^5*c^2*arcsin(c*x)^2 + 2*a*b^4*c^2*arcsin(c*x) + a^2*b^3*c^2) - 2*b^2*arcs

$$\begin{aligned}
& \sin(cx)^2 \cos(a/b)^2 \sin_{\text{integral}}(2a/b + 2\arcsin(cx)) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + 4ab \arcsin(cx) \cos(a/b) \cos_{\text{integral}}(2a/b + 2\arcsin(cx)) \sin(a/b) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) - 4ab \arcsin(cx) \cos(a/b)^2 \sin_{\text{integral}}(2a/b + 2\arcsin(cx)) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + 2a^2 \cos(a/b) \cos_{\text{integral}}(2a/b + 2\arcsin(cx)) \sin(a/b) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + b^2 \arcsin(cx)^2 \sin_{\text{integral}}(2a/b + 2\arcsin(cx)) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) - 2a^2 \cos(a/b)^2 \sin_{\text{integral}}(2a/b + 2\arcsin(cx)) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) - 1/2 \sqrt{-c^2 x^2 + 1} b^2 c x / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + (c^2 x^2 - 1) b^2 \arcsin(cx) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + 2ab \arcsin(cx) \sin_{\text{integral}}(2a/b + 2\arcsin(cx)) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + (c^2 x^2 - 1) a b / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + 1/2 b^2 \arcsin(cx) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + a^2 \sin_{\text{integral}}(2a/b + 2\arcsin(cx)) / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2) + 1/2 a b / (b^5 c^2 \arcsin(cx)^2 + 2ab^4 c^2 \arcsin(cx) + a^2 b^3 c^2)
\end{aligned}$$

$$3.170 \quad \int \frac{1}{(a+b \sin^{-1}(cx))^3} dx$$

Optimal. Leaf size=111

$$\frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right) - \sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{2b^3c} + \frac{x}{2b^2(a+b \sin^{-1}(cx))} - \frac{\sqrt{1-c^2x^2}}{2bc(a+b \sin^{-1}(cx))^2}$$

[Out] -Sqrt[1 - c^2*x^2]/(2*b*c*(a + b*ArcSin[c*x])^2) + x/(2*b^2*(a + b*ArcSin[c*x])) - (Cos[a/b]*CosIntegral[(a + b*ArcSin[c*x])/b])/(2*b^3*c) - (Sin[a/b]*SinIntegral[(a + b*ArcSin[c*x])/b])/(2*b^3*c)

Rubi [A] time = 0.172366, antiderivative size = 111, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {4621, 4719, 4623, 3303, 3299, 3302}

$$\frac{\cos\left(\frac{a}{b}\right) \operatorname{CosIntegral}\left(\frac{a+b \sin^{-1}(cx)}{b}\right) - \sin\left(\frac{a}{b}\right) \operatorname{Si}\left(\frac{a+b \sin^{-1}(cx)}{b}\right)}{2b^3c} + \frac{x}{2b^2(a+b \sin^{-1}(cx))} - \frac{\sqrt{1-c^2x^2}}{2bc(a+b \sin^{-1}(cx))^2}$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^(-3), x]

[Out] -Sqrt[1 - c^2*x^2]/(2*b*c*(a + b*ArcSin[c*x])^2) + x/(2*b^2*(a + b*ArcSin[c*x])) - (Cos[a/b]*CosIntegral[(a + b*ArcSin[c*x])/b])/(2*b^3*c) - (Sin[a/b]*SinIntegral[(a + b*ArcSin[c*x])/b])/(2*b^3*c)

Rule 4621

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_), x_Symbol] :> Simp[(Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(n + 1))/(b*c*(n + 1)), x] + Dist[c/(b*(n + 1)), Int[(x*(a + b*ArcSin[c*x])^(n + 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && LtQ[n, -1]

Rule 4719

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_))*((f_.)*(x_)^ (m_.))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[((f*x)^m*(a + b*ArcSin[c*x])^(n + 1))/(b*c*Sqrt[d]*(n + 1)), x] - Dist[(f*m)/(b*c*Sqrt[d]*(n + 1)), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n + 1), x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_), x_Symbol] :> Dist[1/(b*c), Subst[Int[x^n * Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] &&

NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{1}{(a + b \sin^{-1}(cx))^3} dx &= -\frac{\sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} - \frac{c \int \frac{x}{\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^2} dx}{2b} \\ &= -\frac{\sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} + \frac{x}{2b^2 (a + b \sin^{-1}(cx))} - \frac{\int \frac{1}{a + b \sin^{-1}(cx)} dx}{2b^2} \\ &= -\frac{\sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} + \frac{x}{2b^2 (a + b \sin^{-1}(cx))} - \frac{\text{Subst}\left(\int \frac{\cos\left(\frac{a-x}{b}\right)}{x} dx, x, a + b \sin^{-1}(cx)\right)}{2b^3 c} \\ &= -\frac{\sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} + \frac{x}{2b^2 (a + b \sin^{-1}(cx))} - \frac{\cos\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{x}{b}\right)}{x} dx, x, a + b \sin^{-1}(cx)\right)}{2b^3 c} \\ &= -\frac{\sqrt{1 - c^2 x^2}}{2bc (a + b \sin^{-1}(cx))^2} + \frac{x}{2b^2 (a + b \sin^{-1}(cx))} - \frac{\cos\left(\frac{a}{b}\right) \text{Ci}\left(\frac{a + b \sin^{-1}(cx)}{b}\right)}{2b^3 c} - \frac{\sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a + b \sin^{-1}(cx)}{b}\right)}{2b^3 c} \end{aligned}$$

Mathematica [A] time = 0.417795, size = 93, normalized size = 0.84

$$\frac{b \left(\frac{b \sqrt{1 - c^2 x^2}}{c} - x (a + b \sin^{-1}(cx)) \right)}{(a + b \sin^{-1}(cx))^2} + \frac{\cos\left(\frac{a}{b}\right) \text{CosIntegral}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{c} + \frac{\sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \sin^{-1}(cx)\right)}{c}$$

$$2b^3$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])^(-3), x]

[Out] -((b*((b*Sqrt[1 - c^2*x^2])/c - x*(a + b*ArcSin[c*x])))/(a + b*ArcSin[c*x])^2 + (Cos[a/b]*CosIntegral[a/b + ArcSin[c*x]])/c + (Sin[a/b]*SinIntegral[a/b + ArcSin[c*x]])/c)/(2*b^3)

Maple [A] time = 0.03, size = 138, normalized size = 1.2

$$\frac{1}{c} \left(-\frac{1}{2(a + b \arcsin(cx))^2 b} \sqrt{-c^2 x^2 + 1} - \frac{1}{(2a + 2b \arcsin(cx)) b^3} \left(\arcsin(cx) \text{Si}\left(\arcsin(cx) + \frac{a}{b}\right) \sin\left(\frac{a}{b}\right) b + \arcsin\left(\frac{a + b \arcsin(cx)}{b}\right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a+b*arcsin(c*x))^3,x)

[Out] $\frac{1}{c} \cdot \frac{-1/2 \cdot (-c^2 x^2 + 1)^{1/2}}{(a + b \arcsin(c x))^2 / b - 1/2 \cdot (\arcsin(c x) \cdot \text{Si}(\arcsin(c x) + a/b) \cdot \sin(a/b) \cdot b + \arcsin(c x) \cdot \text{Ci}(\arcsin(c x) + a/b) \cdot \cos(a/b) \cdot b + \text{Si}(\arcsin(c x) + a/b) \cdot \sin(a/b) \cdot a + \text{Ci}(\arcsin(c x) + a/b) \cdot \cos(a/b) \cdot a - x \cdot b \cdot c)}{(a + b \arcsin(c x))^3 / b^3}$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\frac{bcx \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right) + acx - \sqrt{cx+1}\sqrt{-cx+1}b - \left(b^4c \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^2 + 2ab^3c \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)\right)}{2\left(b^4c \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^2 + 2ab^3c \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^3,x, algorithm="maxima")

[Out] $\frac{1/2 \cdot (b \cdot c \cdot x \cdot \arctan2(c \cdot x, \sqrt{c \cdot x + 1} \cdot \sqrt{-c \cdot x + 1})) + a \cdot c \cdot x - \sqrt{c \cdot x + 1} \cdot \sqrt{-c \cdot x + 1} \cdot b - 2 \cdot (b^4 \cdot c \cdot \arctan2(c \cdot x, \sqrt{c \cdot x + 1} \cdot \sqrt{-c \cdot x + 1}))^2 + 2 \cdot a \cdot b^3 \cdot c \cdot \arctan2(c \cdot x, \sqrt{c \cdot x + 1} \cdot \sqrt{-c \cdot x + 1}) + a^2 \cdot b^2 \cdot c}{(b^4 \cdot c \cdot \arctan2(c \cdot x, \sqrt{c \cdot x + 1} \cdot \sqrt{-c \cdot x + 1}))^2 + 2 \cdot a \cdot b^3 \cdot c \cdot \arctan2(c \cdot x, \sqrt{c \cdot x + 1} \cdot \sqrt{-c \cdot x + 1}) + a^2 \cdot b^2 \cdot c}$

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^3,x, algorithm="fricas")

[Out] integral(1/(b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) + a^3), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(a + b \arcsin(cx))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*asin(c*x))**3,x)

[Out] Integral((a + b*asin(c*x))**(-3), x)

Giac [B] time = 1.42593, size = 651, normalized size = 5.86

$$\frac{b^2 \arcsin(cx)^2 \cos\left(\frac{a}{b}\right) \text{Ci}\left(\frac{a}{b} + \arcsin(cx)\right)}{2\left(b^5c \arcsin(cx)^2 + 2ab^4c \arcsin(cx) + a^2b^3c\right)} - \frac{b^2 \arcsin(cx)^2 \sin\left(\frac{a}{b}\right) \text{Si}\left(\frac{a}{b} + \arcsin(cx)\right)}{2\left(b^5c \arcsin(cx)^2 + 2ab^4c \arcsin(cx) + a^2b^3c\right)} + \frac{b^2 \arcsin(cx)^2}{2\left(b^5c \arcsin(cx)^2 + 2ab^4c \arcsin(cx) + a^2b^3c\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^3,x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/2*b^2*\arcsin(c*x)^2*\cos(a/b)*\cos_integral(a/b + \arcsin(c*x))/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) - 1/2*b^2*\arcsin(c*x)^2*\sin(a/b)*\sin_integral(a/b + \arcsin(c*x))/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) \\ & + 1/2*b^2*c*x*\arcsin(c*x)/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) - a*b*\arcsin(c*x)*\cos(a/b)*\cos_integral(a/b + \arcsin(c*x))/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) \\ & - a*b*\arcsin(c*x)*\sin(a/b)*\sin_integral(a/b + \arcsin(c*x))/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) \\ & + 1/2*a*b*c*x/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) - 1/2*a^2*\cos(a/b)*\cos_integral(a/b + \arcsin(c*x))/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) \\ & - 1/2*a^2*\sin(a/b)*\sin_integral(a/b + \arcsin(c*x))/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) \\ & - 1/2*\sqrt{-c^2*x^2 + 1}*b^2/(b^5*c*\arcsin(c*x)^2 + 2*a*b^4*c*\arcsin(c*x) + a^2*b^3*c) \end{aligned}$$

$$3.171 \quad \int \frac{1}{x(a+b \sin^{-1}(cx))^3} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable} \left(\frac{1}{x(a+b \sin^{-1}(cx))^3}, x \right)$$

[Out] Unintegrable[1/(x*(a + b*ArcSin[c*x])^3), x]

Rubi [A] time = 0.0229314, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^3} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*(a + b*ArcSin[c*x])^3), x]

[Out] Defer[Int][1/(x*(a + b*ArcSin[c*x])^3), x]

Rubi steps

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^3} dx = \int \frac{1}{x(a+b \sin^{-1}(cx))^3} dx$$

Mathematica [A] time = 2.12791, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*(a + b*ArcSin[c*x])^3), x]

[Out] Integrate[1/(x*(a + b*ArcSin[c*x])^3), x]

Maple [A] time = 0.276, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \arcsin(cx))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(a+b*arcsin(c*x))^3,x)

[Out] $\int (1/x/(a+b*\arcsin(c*x))^3, x)$

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{\sqrt{cx+1}\sqrt{-cx+1}bcx - b \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right) - a - \frac{2\left(b^4c^2x^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^2 + 2ab^3c^2x^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)\right)}{b^2c^2}}{2\left(b^4c^2x^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)^2 + 2ab^3c^2x^2 \arctan\left(cx, \sqrt{cx+1}\sqrt{-cx+1}\right)\right) + a^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x/(a+b*\arcsin(c*x))^3, x, \text{algorithm}="maxima")$

[Out] $-1/2*(\sqrt{cx+1}\sqrt{-cx+1}*b*c*x - b*\arctan2(c*x, \sqrt{cx+1}\sqrt{-cx+1})) - 2*(b^4*c^2*x^2*\arctan2(c*x, \sqrt{cx+1}\sqrt{-cx+1})^2 + 2*a*b^3*c^2*x^2*\arctan2(c*x, \sqrt{cx+1}\sqrt{-cx+1}) + a^2*b^2*c^2*x^2)*\text{integrate}(1/(b^3*c^2*x^3*\arctan2(c*x, \sqrt{cx+1}\sqrt{-cx+1}) + a*b^2*c^2*x^3), x) - a)/(b^4*c^2*x^2*\arctan2(c*x, \sqrt{cx+1}\sqrt{-cx+1})^2 + 2*a*b^3*c^2*x^2*\arctan2(c*x, \sqrt{cx+1}\sqrt{-cx+1}) + a^2*b^2*c^2*x^2)$

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{b^3x \arcsin(cx)^3 + 3ab^2x \arcsin(cx)^2 + 3a^2bx \arcsin(cx) + a^3x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x/(a+b*\arcsin(c*x))^3, x, \text{algorithm}="fricas")$

[Out] $\text{integral}(1/(b^3*x*\arcsin(c*x)^3 + 3*a*b^2*x*\arcsin(c*x)^2 + 3*a^2*b*x*\arcsin(c*x) + a^3*x), x)$

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x(a + b \arcsin(cx))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x/(a+b*\arcsin(c*x))**3, x)$

[Out] $\text{Integral}(1/(x*(a + b*\arcsin(c*x))**3), x)$

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^3 x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x/(a+b*arcsin(c*x))^3,x, algorithm="giac")
```

```
[Out] integrate(1/((b*arcsin(c*x) + a)^3*x), x)
```

$$3.172 \quad \int \frac{1}{x^2(a+b \sin^{-1}(cx))^3} dx$$

Optimal. Leaf size=16

$$\text{Unintegrable} \left(\frac{1}{x^2(a+b \sin^{-1}(cx))^3}, x \right)$$

[Out] Unintegrable[1/(x^2*(a + b*ArcSin[c*x])^3), x]

Rubi [A] time = 0.0229158, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^3} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*(a + b*ArcSin[c*x])^3), x]

[Out] Defer[Int][1/(x^2*(a + b*ArcSin[c*x])^3), x]

Rubi steps

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^3} dx = \int \frac{1}{x^2(a+b \sin^{-1}(cx))^3} dx$$

Mathematica [A] time = 17.8547, size = 0, normalized size = 0.

$$\int \frac{1}{x^2(a+b \sin^{-1}(cx))^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*(a + b*ArcSin[c*x])^3), x]

[Out] Integrate[1/(x^2*(a + b*ArcSin[c*x])^3), x]

Maple [A] time = 0.5, size = 0, normalized size = 0.

$$\int \frac{1}{x^2(a+b \arcsin(cx))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(a+b*arcsin(c*x))^3, x)

[Out] $\int (1/x^2/(a+b*\arcsin(c*x)))^3, x$

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{ac^2x^2 + \sqrt{cx+1}\sqrt{-cx+1}bcx + (bc^2x^2 - 2b) \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) + (b^4c^2x^3 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})}{2(b^4c^2x^3 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})^2 + 2ab^3c^2x^3 \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^2/(a+b*\arcsin(c*x))^3, x, \text{algorithm}="maxima")$

[Out] $-1/2*(a*c^2*x^2 + \text{sqrt}(c*x + 1)*\text{sqrt}(-c*x + 1)*b*c*x + (b*c^2*x^2 - 2*b)*\arctan2(c*x, \text{sqrt}(c*x + 1)*\text{sqrt}(-c*x + 1)) + 2*(b^4*c^2*x^3*\arctan2(c*x, \text{sqrt}(c*x + 1)*\text{sqrt}(-c*x + 1))^2 + 2*a*b^3*c^2*x^3*\arctan2(c*x, \text{sqrt}(c*x + 1)*\text{sqrt}(-c*x + 1)) + a^2*b^2*c^2*x^3)*\text{integrate}(1/2*(c^2*x^2 - 6)/(b^3*c^2*x^4*\arctan2(c*x, \text{sqrt}(c*x + 1)*\text{sqrt}(-c*x + 1)) + a*b^2*c^2*x^4), x) - 2*a)/(b^4*c^2*x^3*\arctan2(c*x, \text{sqrt}(c*x + 1)*\text{sqrt}(-c*x + 1))^2 + 2*a*b^3*c^2*x^3*\arctan2(c*x, \text{sqrt}(c*x + 1)*\text{sqrt}(-c*x + 1)) + a^2*b^2*c^2*x^3)$

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{1}{b^3x^2 \arcsin(cx)^3 + 3ab^2x^2 \arcsin(cx)^2 + 3a^2bx^2 \arcsin(cx) + a^3x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x^2/(a+b*\arcsin(c*x))^3, x, \text{algorithm}="fricas")$

[Out] $\text{integral}(1/(b^3*x^2*\arcsin(c*x)^3 + 3*a*b^2*x^2*\arcsin(c*x)^2 + 3*a^2*b*x^2*\arcsin(c*x) + a^3*x^2), x)$

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (a + b \arcsin(cx))^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/x**2/(a+b*\arcsin(c*x))**3, x)$

[Out] $\text{Integral}(1/(x**2*(a + b*\arcsin(c*x))**3), x)$

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^3 x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/x^2/(a+b*arcsin(c*x))^3,x, algorithm="giac")
```

```
[Out] integrate(1/((b*arcsin(c*x) + a)^3*x^2), x)
```


3.173 $\int x^2 \sqrt{a + b \sin^{-1}(cx)} dx$

Optimal. Leaf size=242

$$\frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \sin\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c^3} - \frac{\sqrt{\frac{\pi}{6}} \sqrt{b} \sin\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{12c^3} - \frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c^3}$$

[Out] $(x^3 \sqrt{a + b \text{ArcSin}[c x]})/3 - (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/2] \text{Cos}[a/b] \text{FresnelS}[(\text{Sqrt}[2/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]])/(4 c^3) + (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/6] \text{Cos}[(3 a)/b] \text{FresnelS}[(\text{Sqrt}[6/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]])/(12 c^3) + (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/2] \text{FresnelC}[(\text{Sqrt}[2/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]] \text{Sin}[a/b])/(4 c^3) - (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/6] \text{FresnelC}[(\text{Sqrt}[6/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]] \text{Sin}[(3 a)/b])/(12 c^3)$

Rubi [A] time = 0.755672, antiderivative size = 242, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 8, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4629, 4723, 3312, 3306, 3305, 3351, 3304, 3352}

$$\frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \sin\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c^3} - \frac{\sqrt{\frac{\pi}{6}} \sqrt{b} \sin\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{12c^3} - \frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2 \sqrt{a + b \text{ArcSin}[c x]}, x]$

[Out] $(x^3 \sqrt{a + b \text{ArcSin}[c x]})/3 - (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/2] \text{Cos}[a/b] \text{FresnelS}[(\text{Sqrt}[2/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]])/(4 c^3) + (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/6] \text{Cos}[(3 a)/b] \text{FresnelS}[(\text{Sqrt}[6/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]])/(12 c^3) + (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/2] \text{FresnelC}[(\text{Sqrt}[2/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]] \text{Sin}[a/b])/(4 c^3) - (\text{Sqrt}[b] \text{Sqrt}[\text{Pi}/6] \text{FresnelC}[(\text{Sqrt}[6/\text{Pi}] \text{Sqrt}[a + b \text{ArcSin}[c x]])/\text{Sqrt}[b]] \text{Sin}[(3 a)/b])/(12 c^3)$

Rule 4629

$\text{Int}[(a + \text{ArcSin}[c x])^n (b + x)^m, x] \rightarrow \text{Simp}[(x^{m+1} (a + b \text{ArcSin}[c x])^n)/(m+1), x] - \text{Dist}[(b c^n)/(m+1), \text{Int}[x^{m+1} (a + b \text{ArcSin}[c x])^{n-1}/\text{Sqrt}[1 - c^2 x^2], x], x] /;$ FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4723

$\text{Int}[(a + \text{ArcSin}[c x])^n (b + x)^m ((d + e x)^2)^p, x] \rightarrow \text{Dist}[d^p/c^{m+1}, \text{Subst}[\text{Int}[(a + b x)^n \text{Sin}[x]^m \text{Cos}[x]^{2p+1}, x], x, \text{ArcSin}[c x]], x] /;$ FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2 d + e, 0] && IntegerQ[2p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3312

$\text{Int}[(c + d x)^m \sin[e + f x]^n, x] \rightarrow \text{Int}[\text{ExpandTrigReduce}[(c + d x)^m, \text{Sin}[e + f x]^n, x], x] /;$ FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3306

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos
[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d
*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d,
e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d
, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}
, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := D
ist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d
, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned}
\int x^2 \sqrt{a + b \sin^{-1}(cx)} dx &= \frac{1}{3} x^3 \sqrt{a + b \sin^{-1}(cx)} - \frac{1}{6} (bc) \int \frac{x^3}{\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}} dx \\
&= \frac{1}{3} x^3 \sqrt{a + b \sin^{-1}(cx)} - \frac{b \operatorname{Subst}\left(\int \frac{\sin^3(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{6c^3} \\
&= \frac{1}{3} x^3 \sqrt{a + b \sin^{-1}(cx)} - \frac{b \operatorname{Subst}\left(\int \left(\frac{3 \sin(x)}{4\sqrt{a+bx}} - \frac{\sin(3x)}{4\sqrt{a+bx}}\right) dx, x, \sin^{-1}(cx)\right)}{6c^3} \\
&= \frac{1}{3} x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{b \operatorname{Subst}\left(\int \frac{\sin(3x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{24c^3} - \frac{b \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{8c^3} \\
&= \frac{1}{3} x^3 \sqrt{a + b \sin^{-1}(cx)} - \frac{\left(b \cos\left(\frac{a}{b}\right)\right) \operatorname{Subst}\left(\int \frac{\sin\left(\frac{a}{b}+x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{8c^3} + \frac{\left(b \cos\left(\frac{3a}{b}\right)\right) \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{8c^3} \\
&= \frac{1}{3} x^3 \sqrt{a + b \sin^{-1}(cx)} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Subst}\left(\int \sin\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{4c^3} + \frac{\cos\left(\frac{3a}{b}\right) \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{8c^3} \\
&= \frac{1}{3} x^3 \sqrt{a + b \sin^{-1}(cx)} - \frac{\sqrt{b} \sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c^3} + \frac{\sqrt{b} \sqrt{\frac{\pi}{6}} \cos\left(\frac{3a}{b}\right) S\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{12c^3}
\end{aligned}$$

Mathematica [C] time = 0.30403, size = 246, normalized size = 1.02

$$ie^{-\frac{3ia}{b}}\sqrt{a+b\sin^{-1}(cx)}\left(9e^{\frac{2ia}{b}}\sqrt{\frac{i(a+b\sin^{-1}(cx))}{b}}\Gamma\left(\frac{3}{2},-\frac{i(a+b\sin^{-1}(cx))}{b}\right)-9e^{\frac{4ia}{b}}\sqrt{-\frac{i(a+b\sin^{-1}(cx))}{b}}\Gamma\left(\frac{3}{2},\frac{i(a+b\sin^{-1}(cx))}{b}\right)\right)$$

$$72c^3\sqrt{\frac{(a+bs)}{b}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2*Sqrt[a + b*ArcSin[c*x]],x]

[Out] $((-I/72)*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]*(9*E^{((2*I)*a)/b}*\text{Sqrt}[(I*(a + b*\text{ArcSin}[c*x]))/b]*\Gamma[3/2, ((-I)*(a + b*\text{ArcSin}[c*x]))/b] - 9*E^{((4*I)*a)/b}*\text{Sqrt}[(I*(a + b*\text{ArcSin}[c*x]))/b]*\Gamma[3/2, (I*(a + b*\text{ArcSin}[c*x]))/b] + \text{Sqrt}[3]*(-(\text{Sqrt}[(I*(a + b*\text{ArcSin}[c*x]))/b]*\Gamma[3/2, ((-3*I)*(a + b*\text{ArcSin}[c*x]))/b]) + E^{((6*I)*a)/b}*\text{Sqrt}[(I*(a + b*\text{ArcSin}[c*x]))/b]*\Gamma[3/2, ((3*I)*(a + b*\text{ArcSin}[c*x]))/b]))/(c^3*E^{((3*I)*a)/b}*\text{Sqrt}[(a + b*\text{ArcSin}[c*x])^2/b^2])$

Maple [A] time = 0.083, size = 356, normalized size = 1.5

$$\frac{1}{72c^3}\left(-\sqrt{3}\sqrt{2}\sqrt{\pi}\sqrt{b^{-1}}\sqrt{a+b\arcsin(cx)}\text{FresnelC}\left(\frac{\sqrt{3}\sqrt{2}}{\sqrt{\pi b}}\sqrt{a+b\arcsin(cx)}\frac{1}{\sqrt{b^{-1}}}\right)\sin\left(3\frac{a}{b}\right)b + \sqrt{3}\sqrt{2}\sqrt{\pi}\sqrt{b^{-1}}\sqrt{a+b\arcsin(cx)}\text{FresnelS}\left(\frac{\sqrt{3}\sqrt{2}}{\sqrt{\pi b}}\sqrt{a+b\arcsin(cx)}\frac{1}{\sqrt{b^{-1}}}\right)\cos\left(3\frac{a}{b}\right)b$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*(a+b*arcsin(c*x))^(1/2),x)

[Out] $1/72/c^3/(a+b*\arcsin(c*x))^{(1/2)}*(-3^{(1/2)}*2^{(1/2)}*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)}*3^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*\sin(3*a/b)*b+3^{(1/2)}*2^{(1/2)}*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\cos(3*a/b)*\text{FresnelS}(2^{(1/2)}/\text{Pi}^{(1/2)}*3^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*b-9*2^{(1/2)}*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\cos(a/b)*\text{FresnelS}(2^{(1/2)}/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*b+9*2^{(1/2)}*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\sin(a/b)*\text{FresnelC}(2^{(1/2)}/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*b+18*\arcsin(c*x)*\sin((a+b*\arcsin(c*x))/b-a/b)*b+18*\sin((a+b*\arcsin(c*x))/b-a/b)*a-6*\arcsin(c*x)*\sin(3*(a+b*\arcsin(c*x))/b-3*a/b)*b-6*\sin(3*(a+b*\arcsin(c*x))/b-3*a/b)*a$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{b \arcsin(cx) + ax^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")

[Out] integrate(sqrt(b*arcsin(c*x) + a)*x^2, x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \sqrt{a + b \operatorname{asin}(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(a+b*asin(c*x))**(1/2),x)

[Out] Integral(x**2*sqrt(a + b*asin(c*x)), x)

Giac [C] time = 2.10463, size = 531, normalized size = 2.19

$$\frac{i\sqrt{2}\sqrt{\pi}b \operatorname{erf}\left(-\frac{i\sqrt{2}\sqrt{b\operatorname{arcsin}(cx)+a}}{2\sqrt{|b|}} - \frac{\sqrt{2}\sqrt{b\operatorname{arcsin}(cx)+a}\sqrt{|b|}}{2b}\right) e^{\left(\frac{ia}{b}\right)}}{16c^3\left(\frac{ib}{\sqrt{|b|}} + \sqrt{|b|}\right)} - \frac{i\sqrt{2}\sqrt{\pi}b \operatorname{erf}\left(\frac{i\sqrt{2}\sqrt{b\operatorname{arcsin}(cx)+a}}{2\sqrt{|b|}} - \frac{\sqrt{2}\sqrt{b\operatorname{arcsin}(cx)+a}\sqrt{|b|}}{2b}\right) e^{\left(-\frac{ia}{b}\right)}}{16c^3\left(-\frac{ib}{\sqrt{|b|}} + \sqrt{|b|}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^(1/2),x, algorithm="giac")

[Out] 1/16*I*sqrt(2)*sqrt(pi)*b*erf(-1/2*I*sqrt(2)*sqrt(b*arcsin(c*x) + a)/sqrt(abs(b)) - 1/2*sqrt(2)*sqrt(b*arcsin(c*x) + a)*sqrt(abs(b))/b)*e^(I*a/b)/(c^3*(I*b/sqrt(abs(b)) + sqrt(abs(b)))) - 1/16*I*sqrt(2)*sqrt(pi)*b*erf(1/2*I*sqrt(2)*sqrt(b*arcsin(c*x) + a)/sqrt(abs(b)) - 1/2*sqrt(2)*sqrt(b*arcsin(c*x) + a)*sqrt(abs(b))/b)*e^(-I*a/b)/(c^3*(-I*b/sqrt(abs(b)) + sqrt(abs(b)))) - 1/24*I*sqrt(pi)*sqrt(b)*erf(-1/2*sqrt(6)*sqrt(b*arcsin(c*x) + a)/sqrt(b) - 1/2*I*sqrt(6)*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(3*I*a/b)/(c^3*(sqrt(6) + I*sqrt(6)*b/abs(b))) + 1/24*I*sqrt(pi)*sqrt(b)*erf(-1/2*sqrt(6)*sqrt(b*arcsin(c*x) + a)/sqrt(b) + 1/2*I*sqrt(6)*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-3*I*a/b)/(c^3*(sqrt(6) - I*sqrt(6)*b/abs(b))) + 1/24*I*sqrt(b*arcsin(c*x) + a)*e^(3*I*arcsin(c*x))/c^3 - 1/8*I*sqrt(b*arcsin(c*x) + a)*e^(I*arcsin(c*x))/c^3 + 1/8*I*sqrt(b*arcsin(c*x) + a)*e^(-I*arcsin(c*x))/c^3 - 1/24*I*sqrt(b*arcsin(c*x) + a)*e^(-3*I*arcsin(c*x))/c^3

3.174 $\int x \sqrt{a + b \sin^{-1}(cx)} dx$

Optimal. Leaf size=137

$$\frac{\sqrt{\pi}\sqrt{b} \cos\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{8c^2} + \frac{\sqrt{\pi}\sqrt{b} \sin\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{8c^2} - \frac{\sqrt{a + b \sin^{-1}(cx)}}{4c^2} + \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)}$$

[Out] $-\text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]] / (4 \cdot c^2) + (x^2 \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]]) / 2 + (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}] \cdot \text{Cos}[(2 \cdot a) / b] \cdot \text{FresnelC}[(2 \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]])] / (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}]]) / (8 \cdot c^2) + (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}] \cdot \text{FresnelS}[(2 \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]])] / (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}]) \cdot \text{Sin}[(2 \cdot a) / b]) / (8 \cdot c^2)$

Rubi [A] time = 0.453424, antiderivative size = 137, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 8, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.571$, Rules used = {4629, 4723, 3312, 3306, 3305, 3351, 3304, 3352}

$$\frac{\sqrt{\pi}\sqrt{b} \cos\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{8c^2} + \frac{\sqrt{\pi}\sqrt{b} \sin\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{8c^2} - \frac{\sqrt{a + b \sin^{-1}(cx)}}{4c^2} + \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]], x]$

[Out] $-\text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]] / (4 \cdot c^2) + (x^2 \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]]) / 2 + (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}] \cdot \text{Cos}[(2 \cdot a) / b] \cdot \text{FresnelC}[(2 \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]])] / (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}])) / (8 \cdot c^2) + (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}] \cdot \text{FresnelS}[(2 \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]])] / (\text{Sqrt}[b] \cdot \text{Sqrt}[\text{Pi}]) \cdot \text{Sin}[(2 \cdot a) / b]) / (8 \cdot c^2)$

Rule 4629

$\text{Int}[(a + \text{ArcSin}[c \cdot x]) \cdot (b \cdot x)^n \cdot x^m, x_Symbol] \rightarrow \text{Simp}[(x^{m+1} \cdot (a + b \cdot \text{ArcSin}[c \cdot x])^n) / (m+1), x] - \text{Dist}[(b \cdot c \cdot n) / (m+1), \text{Int}[x^{m+1} \cdot (a + b \cdot \text{ArcSin}[c \cdot x])^{n-1} / \text{Sqrt}[1 - c^2 \cdot x^2], x], x] /;$ FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4723

$\text{Int}[(a + \text{ArcSin}[c \cdot x]) \cdot (b \cdot x)^n \cdot x^m \cdot ((d + e \cdot x)^2)^p, x_Symbol] \rightarrow \text{Dist}[d^p / c^{m+1}, \text{Subst}[\text{Int}[(a + b \cdot x)^n \cdot \text{Sin}[x]^m \cdot \text{Cos}[x]^{2p+1}, x], x, \text{ArcSin}[c \cdot x]], x] /;$ FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2 \cdot d + e, 0] && IntegerQ[2 \cdot p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3312

$\text{Int}[(c + d \cdot x)^m \cdot \text{Sin}[e + f \cdot x]^n, x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigReduce}[(c + d \cdot x)^m, \text{Sin}[e + f \cdot x]^n, x], x] /;$ FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3306

$\text{Int}[\text{Sin}[e + f \cdot x] / \text{Sqrt}[c + d \cdot x], x_Symbol] \rightarrow \text{Dist}[\text{Cos}[(d \cdot e - c \cdot f) / d], \text{Int}[\text{Sin}[c \cdot f / d + f \cdot x] / \text{Sqrt}[c + d \cdot x], x], x] + \text{Dist}[\text{Sin}[(d$

$*e - c*f)/d]$, $\text{Int}[\text{Cos}[(c*f)/d + f*x]/\text{Sqrt}[c + d*x], x], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x]$ && $\text{ComplexFreeQ}[f]$ && $\text{NeQ}[d*e - c*f, 0]$

Rule 3305

$\text{Int}[\sin[(e_.) + (f_.)*(x_.)]/\text{Sqrt}[(c_.) + (d_.)*(x_.)], x_Symbol] := \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x]$ && $\text{ComplexFreeQ}[f]$ && $\text{EqQ}[d*e - c*f, 0]$

Rule 3351

$\text{Int}[\text{Sin}[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] := \text{Simp}[(\text{Sqrt}[\text{Pi}/2]*\text{FresnelS}[\text{Sqrt}[2/\text{Pi}]*\text{Rt}[d, 2]*(e + f*x)])/(f*\text{Rt}[d, 2]), x] /;$ $\text{FreeQ}\{d, e, f\}, x]$

Rule 3304

$\text{Int}[\sin[\text{Pi}/2 + (e_.) + (f_.)*(x_.)]/\text{Sqrt}[(c_.) + (d_.)*(x_.)], x_Symbol] := \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Cos}[(f*x^2)/d], x], x, \text{Sqrt}[c + d*x]], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x]$ && $\text{ComplexFreeQ}[f]$ && $\text{EqQ}[d*e - c*f, 0]$

Rule 3352

$\text{Int}[\text{Cos}[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] := \text{Simp}[(\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[\text{Sqrt}[2/\text{Pi}]*\text{Rt}[d, 2]*(e + f*x)])/(f*\text{Rt}[d, 2]), x] /;$ $\text{FreeQ}\{d, e, f\}, x]$

Rubi steps

$$\begin{aligned} \int x\sqrt{a + b \sin^{-1}(cx)} dx &= \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)} - \frac{1}{4}(bc) \int \frac{x^2}{\sqrt{1 - c^2x^2}\sqrt{a + b \sin^{-1}(cx)}} dx \\ &= \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)} - \frac{b \text{Subst}\left(\int \frac{\sin^2(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{4c^2} \\ &= \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)} - \frac{b \text{Subst}\left(\int \left(\frac{1}{2\sqrt{a+bx}} - \frac{\cos(2x)}{2\sqrt{a+bx}}\right) dx, x, \sin^{-1}(cx)\right)}{4c^2} \\ &= -\frac{\sqrt{a + b \sin^{-1}(cx)}}{4c^2} + \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{b \text{Subst}\left(\int \frac{\cos(2x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{8c^2} \\ &= -\frac{\sqrt{a + b \sin^{-1}(cx)}}{4c^2} + \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{\left(b \cos\left(\frac{2a}{b}\right)\right) \text{Subst}\left(\int \frac{\cos\left(\frac{2a}{b} + 2x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{8c^2} \\ &= -\frac{\sqrt{a + b \sin^{-1}(cx)}}{4c^2} + \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{\cos\left(\frac{2a}{b}\right) \text{Subst}\left(\int \cos\left(\frac{2x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{4c^2} \\ &= -\frac{\sqrt{a + b \sin^{-1}(cx)}}{4c^2} + \frac{1}{2}x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{\sqrt{b}\sqrt{\pi} \cos\left(\frac{2a}{b}\right) C\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{8c^2} + \frac{\sqrt{b}\sqrt{\pi} S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{8c^2} \end{aligned}$$

Mathematica [C] time = 0.0722514, size = 141, normalized size = 1.03

$$\frac{e^{-\frac{2ia}{b}} \sqrt{a + b \sin^{-1}(cx)} \left(\sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{3}{2}, -\frac{2i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{4ia}{b}} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{3}{2}, \frac{2i(a+b \sin^{-1}(cx))}{b}\right) \right)}{8\sqrt{2}c^2 \sqrt{\frac{(a+b \sin^{-1}(cx))^2}{b^2}}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*Sqrt[a + b*ArcSin[c*x]],x]

[Out] $-(\text{Sqrt}[a + b\text{ArcSin}[c*x]] * (\text{Sqrt}[(I*(a + b\text{ArcSin}[c*x]))/b] * \text{Gamma}[3/2, ((-2*I)*(a + b\text{ArcSin}[c*x]))/b] + E^{((4*I)*a)/b} * \text{Sqrt}[((-I)*(a + b\text{ArcSin}[c*x]))/b] * \text{Gamma}[3/2, ((2*I)*(a + b\text{ArcSin}[c*x]))/b]) / (8*\text{Sqrt}[2]*c^2 * E^{((2*I)*a)/b} * \text{Sqrt}[(a + b\text{ArcSin}[c*x])^2/b^2])$

Maple [A] time = 0.052, size = 173, normalized size = 1.3

$$-\frac{1}{8c^2} \left(-\sqrt{\pi}\sqrt{b^{-1}}\sqrt{a + b \arcsin(cx)} \sin\left(2\frac{a}{b}\right) \text{FresnelS}\left(2\frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{\pi}\sqrt{b^{-1}}b}\right) b - \sqrt{\pi}\sqrt{b^{-1}}\sqrt{a + b \arcsin(cx)} \text{FresnelC}\left(2\frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{\pi}\sqrt{b^{-1}}b}\right) b \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a+b*arcsin(c*x))^(1/2),x)

[Out] $-1/8/c^2/(a+b*\arcsin(c*x))^{1/2} * (-\text{Pi}^{1/2} * (1/b)^{1/2} * (a+b*\arcsin(c*x))^{1/2} * \sin(2*a/b) * \text{FresnelS}(2/\text{Pi}^{1/2}/(1/b)^{1/2} * (a+b*\arcsin(c*x))^{1/2}/b) * b - \text{Pi}^{1/2} * (1/b)^{1/2} * (a+b*\arcsin(c*x))^{1/2} * \text{FresnelC}(2/\text{Pi}^{1/2}/(1/b)^{1/2} * (a+b*\arcsin(c*x))^{1/2}/b) * \cos(2*a/b) * b + 2*\arcsin(c*x) * \cos(2*(a+b*\arcsin(c*x))/b - 2*a/b) * b + 2*\cos(2*(a+b*\arcsin(c*x))/b - 2*a/b) * a$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{b \arcsin(cx) + ax} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")

[Out] integrate(sqrt(b*arcsin(c*x) + a)*x, x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x\sqrt{a + b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*asin(c*x))**(1/2),x)

[Out] Integral(x*sqrt(a + b*asin(c*x)), x)

Giac [C] time = 1.80531, size = 236, normalized size = 1.72

$$\frac{\sqrt{\pi}\sqrt{b} \operatorname{erf}\left(-\frac{\sqrt{b}\arcsin(cx)+a}{\sqrt{b}} - \frac{i\sqrt{b}\arcsin(cx)+a\sqrt{b}}{|b|}\right) e^{\left(\frac{2ia}{b}\right)}}{16c^2\left(\frac{ib}{|b|} + 1\right)} - \frac{\sqrt{\pi}\sqrt{b} \operatorname{erf}\left(-\frac{\sqrt{b}\arcsin(cx)+a}{\sqrt{b}} + \frac{i\sqrt{b}\arcsin(cx)+a\sqrt{b}}{|b|}\right) e^{\left(-\frac{2ia}{b}\right)}}{16c^2\left(-\frac{ib}{|b|} + 1\right)} - \sqrt{b} \arcsin(cx)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^(1/2),x, algorithm="giac")

[Out] -1/16*sqrt(pi)*sqrt(b)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/(c^2*(I*b/abs(b) + 1)) - 1/16*sqrt(pi)*sqrt(b)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/(c^2*(-I*b/abs(b) + 1)) - 1/8*sqrt(b*arcsin(c*x) + a)*e^(2*I*arcsin(c*x))/c^2 - 1/8*sqrt(b*arcsin(c*x) + a)*e^(-2*I*arcsin(c*x))/c^2

3.175 $\int \sqrt{a + b \sin^{-1}(cx)} dx$

Optimal. Leaf size=120

$$\frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \sin\left(\frac{a}{b}\right) \operatorname{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{c} - \frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{c} + x \sqrt{a + b \sin^{-1}(cx)}$$

[Out] x*Sqrt[a + b*ArcSin[c*x]] - (Sqrt[b]*Sqrt[Pi/2]*Cos[a/b]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/c + (Sqrt[b]*Sqrt[Pi/2]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/c

Rubi [A] time = 0.331121, antiderivative size = 120, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.583$, Rules used = {4619, 4723, 3306, 3305, 3351, 3304, 3352}

$$\frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \sin\left(\frac{a}{b}\right) \operatorname{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{c} - \frac{\sqrt{\frac{\pi}{2}} \sqrt{b} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{c} + x \sqrt{a + b \sin^{-1}(cx)}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[a + b*ArcSin[c*x]], x]

[Out] x*Sqrt[a + b*ArcSin[c*x]] - (Sqrt[b]*Sqrt[Pi/2]*Cos[a/b]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/c + (Sqrt[b]*Sqrt[Pi/2]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/c

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c^n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.)*((d_.) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^(2)], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^(2)], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned} \int \sqrt{a + b \sin^{-1}(cx)} dx &= x\sqrt{a + b \sin^{-1}(cx)} - \frac{1}{2}(bc) \int \frac{x}{\sqrt{1 - c^2x^2}\sqrt{a + b \sin^{-1}(cx)}} dx \\ &= x\sqrt{a + b \sin^{-1}(cx)} - \frac{b \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2c} \\ &= x\sqrt{a + b \sin^{-1}(cx)} - \frac{(b \cos\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \frac{\sin\left(\frac{a}{b}+x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2c} + \frac{(b \sin\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \frac{\cos(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2c} \\ &= x\sqrt{a + b \sin^{-1}(cx)} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Subst}\left(\int \sin\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{c} + \frac{\sin\left(\frac{a}{b}\right) \operatorname{Subst}\left(\int \cos\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{c} \\ &= x\sqrt{a + b \sin^{-1}(cx)} - \frac{\sqrt{b}\sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{c} + \frac{\sqrt{b}\sqrt{\frac{\pi}{2}} C\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right) \sin\left(\frac{a}{b}\right)}{c} \end{aligned}$$

Mathematica [C] time = 0.0891791, size = 119, normalized size = 0.99

$$\frac{be^{-\frac{ia}{b}} \left(\sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{3}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{2ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{3}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) \right)}{2c\sqrt{a + b \sin^{-1}(cx)}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[Sqrt[a + b*ArcSin[c*x]], x]
```

```
[Out] (b*(Sqrt[(-I)*(a + b*ArcSin[c*x])]/b)*Gamma[3/2, ((-I)*(a + b*ArcSin[c*x])/b]) + E^(((2*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x])/b)*Gamma[3/2, (I*(a + b*ArcSin[c*x])/b)])/((2*c)*E^((I*a)/b)*Sqrt[a + b*ArcSin[c*x]])
```

Maple [A] time = 0.043, size = 178, normalized size = 1.5

$$\frac{1}{2c} \left(-\sqrt{2}\sqrt{\pi}\sqrt{b^{-1}}\sqrt{a + b \arcsin(cx)} \cos\left(\frac{a}{b}\right) \operatorname{FresnelS}\left(\frac{\sqrt{2}}{\sqrt{\pi b}}\sqrt{a + b \arcsin(cx)}\frac{1}{\sqrt{b^{-1}}}\right) b + \sqrt{2}\sqrt{\pi}\sqrt{b^{-1}}\sqrt{a + b \arcsin(cx)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*arcsin(c*x))^(1/2),x)`

[Out] $\frac{1}{2} \frac{1}{c} \frac{1}{(a+b \arcsin(cx))^{1/2}} \left(-2^{1/2} \frac{\pi^{1/2}}{(1/b)^{1/2}} (a+b \arcsin(cx))^{1/2} \cos(a/b) \operatorname{FresnelS}\left(\frac{2^{1/2}}{\pi^{1/2}} \frac{1}{(1/b)^{1/2}} (a+b \arcsin(cx))^{1/2} / b\right) + 2^{1/2} \frac{\pi^{1/2}}{(1/b)^{1/2}} (a+b \arcsin(cx))^{1/2} \sin(a/b) \operatorname{FresnelC}\left(\frac{2^{1/2}}{\pi^{1/2}} \frac{1}{(1/b)^{1/2}} (a+b \arcsin(cx))^{1/2} / b\right) + 2 \arcsin(cx) \sin\left(\frac{a+b \arcsin(cx)}{b-a/b}\right) + 2 \sin\left(\frac{a+b \arcsin(cx)}{b-a/b}\right) a \right)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")`

[Out] `integrate(sqrt(b*arcsin(c*x) + a), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{a + b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**(1/2),x)`

[Out] `Integral(sqrt(a + b*asin(c*x)), x)`

Giac [C] time = 1.6868, size = 266, normalized size = 2.22

$$\frac{i \sqrt{2} \sqrt{\pi} b \operatorname{erf}\left(-\frac{i \sqrt{2} \sqrt{b \arcsin(cx)+a}}{2 \sqrt{|b|}} - \frac{\sqrt{2} \sqrt{b \arcsin(cx)+a} \sqrt{|b|}}{2b}\right) e^{\left(\frac{ia}{b}\right)} - i \sqrt{2} \sqrt{\pi} b \operatorname{erf}\left(\frac{i \sqrt{2} \sqrt{b \arcsin(cx)+a}}{2 \sqrt{|b|}} - \frac{\sqrt{2} \sqrt{b \arcsin(cx)+a} \sqrt{|b|}}{2b}\right) e^{\left(-\frac{ia}{b}\right)}}{4c \left(\frac{ib}{\sqrt{|b|}} + \sqrt{|b|}\right)} - \frac{i \sqrt{2} \sqrt{\pi} b \operatorname{erf}\left(\frac{i \sqrt{2} \sqrt{b \arcsin(cx)+a}}{2 \sqrt{|b|}} - \frac{\sqrt{2} \sqrt{b \arcsin(cx)+a} \sqrt{|b|}}{2b}\right) e^{\left(-\frac{ia}{b}\right)} - i \sqrt{2} \sqrt{\pi} b \operatorname{erf}\left(-\frac{i \sqrt{2} \sqrt{b \arcsin(cx)+a}}{2 \sqrt{|b|}} - \frac{\sqrt{2} \sqrt{b \arcsin(cx)+a} \sqrt{|b|}}{2b}\right) e^{\left(\frac{ia}{b}\right)}}{4c \left(-\frac{ib}{\sqrt{|b|}} + \sqrt{|b|}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))^(1/2),x, algorithm="giac")
```

```
[Out] 1/4*I*sqrt(2)*sqrt(pi)*b*erf(-1/2*I*sqrt(2)*sqrt(b*arcsin(c*x) + a)/sqrt(abs(b)) - 1/2*sqrt(2)*sqrt(b*arcsin(c*x) + a)*sqrt(abs(b))/b)*e^(I*a/b)/(c*(I*b/sqrt(abs(b)) + sqrt(abs(b)))) - 1/4*I*sqrt(2)*sqrt(pi)*b*erf(1/2*I*sqrt(2)*sqrt(b*arcsin(c*x) + a)/sqrt(abs(b)) - 1/2*sqrt(2)*sqrt(b*arcsin(c*x) + a)*sqrt(abs(b))/b)*e^(-I*a/b)/(c*(-I*b/sqrt(abs(b)) + sqrt(abs(b)))) - 1/2*I*sqrt(b*arcsin(c*x) + a)*e^(I*arcsin(c*x))/c + 1/2*I*sqrt(b*arcsin(c*x) + a)*e^(-I*arcsin(c*x))/c
```

$$3.176 \quad \int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{\sqrt{a+b \sin^{-1}(cx)}}{x}, x \right)$$

[Out] Unintegrable[Sqrt[a + b*ArcSin[c*x]]/x, x]

Rubi [A] time = 0.0463406, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x} dx$$

Verification is Not applicable to the result.

[In] Int[Sqrt[a + b*ArcSin[c*x]]/x,x]

[Out] Defer[Int][Sqrt[a + b*ArcSin[c*x]]/x, x]

Rubi steps

$$\int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x} dx = \int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x} dx$$

Mathematica [A] time = 3.25393, size = 0, normalized size = 0.

$$\int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[Sqrt[a + b*ArcSin[c*x]]/x,x]

[Out] Integrate[Sqrt[a + b*ArcSin[c*x]]/x, x]

Maple [A] time = 0.128, size = 0, normalized size = 0.

$$\int \frac{1}{x} \sqrt{a+b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(1/2)/x,x)

[Out] `int((a+b*arcsin(c*x))^(1/2)/x,x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{b \arcsin(cx) + a}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2)/x,x, algorithm="maxima")`

[Out] `integrate(sqrt(b*arcsin(c*x) + a)/x, x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2)/x,x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{a + b \arcsin(cx)}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**(1/2)/x,x)`

[Out] `Integral(sqrt(a + b*asin(c*x))/x, x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{b \arcsin(cx) + a}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2)/x,x, algorithm="giac")`

[Out] `integrate(sqrt(b*arcsin(c*x) + a)/x, x)`

$$3.177 \quad \int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x^2} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{\sqrt{a+b \sin^{-1}(cx)}}{x^2}, x \right)$$

[Out] Unintegrable[Sqrt[a + b*ArcSin[c*x]]/x^2, x]

Rubi [A] time = 0.0373746, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[Sqrt[a + b*ArcSin[c*x]]/x^2,x]

[Out] Defer[Int][Sqrt[a + b*ArcSin[c*x]]/x^2, x]

Rubi steps

$$\int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x^2} dx = \int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x^2} dx$$

Mathematica [A] time = 11.4003, size = 0, normalized size = 0.

$$\int \frac{\sqrt{a+b \sin^{-1}(cx)}}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[Sqrt[a + b*ArcSin[c*x]]/x^2,x]

[Out] Integrate[Sqrt[a + b*ArcSin[c*x]]/x^2, x]

Maple [A] time = 0.165, size = 0, normalized size = 0.

$$\int \frac{1}{x^2} \sqrt{a+b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(1/2)/x^2,x)

[Out] `int((a+b*arcsin(c*x))^(1/2)/x^2,x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{b \arcsin(cx) + a}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2)/x^2,x, algorithm="maxima")`

[Out] `integrate(sqrt(b*arcsin(c*x) + a)/x^2, x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2)/x^2,x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{a + b \arcsin(cx)}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**(1/2)/x**2,x)`

[Out] `Integral(sqrt(a + b*asin(c*x))/x**2, x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{b \arcsin(cx) + a}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^(1/2)/x^2,x, algorithm="giac")`

[Out] `integrate(sqrt(b*arcsin(c*x) + a)/x^2, x)`

3.178 $\int x^2 \left(a + b \sin^{-1}(cx)\right)^{3/2} dx$

Optimal. Leaf size=313

$$\frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\cos\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{8c^3} + \frac{\sqrt{\frac{\pi}{6}}b^{3/2}\cos\left(\frac{3a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{24c^3} - \frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\sin\left(\frac{a}{b}\right)S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{8c^3}$$

[Out] (b*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(3*c^3) + (b*x^2*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(6*c) + (x^3*(a + b*ArcSin[c*x])^(3/2))/3 - (3*b^(3/2)*Sqrt[Pi/2]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(8*c^3) + (b^(3/2)*Sqrt[Pi/6]*Cos[(3*a)/b]*FresnelC[(Sqrt[6/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(24*c^3) - (3*b^(3/2)*Sqrt[Pi/2]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(8*c^3) + (b^(3/2)*Sqrt[Pi/6]*FresnelS[(Sqrt[6/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[(3*a)/b])/(24*c^3)

Rubi [A] time = 1.04618, antiderivative size = 313, normalized size of antiderivative = 1., number of steps used = 22, number of rules used = 11, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.688$, Rules used = {4629, 4707, 4677, 4623, 3306, 3305, 3351, 3304, 3352, 4635, 4406}

$$\frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\cos\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{8c^3} + \frac{\sqrt{\frac{\pi}{6}}b^{3/2}\cos\left(\frac{3a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{24c^3} - \frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\sin\left(\frac{a}{b}\right)S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{8c^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*(a + b*ArcSin[c*x])^(3/2), x]

[Out] (b*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(3*c^3) + (b*x^2*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(6*c) + (x^3*(a + b*ArcSin[c*x])^(3/2))/3 - (3*b^(3/2)*Sqrt[Pi/2]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(8*c^3) + (b^(3/2)*Sqrt[Pi/6]*Cos[(3*a)/b]*FresnelC[(Sqrt[6/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(24*c^3) - (3*b^(3/2)*Sqrt[Pi/2]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(8*c^3) + (b^(3/2)*Sqrt[Pi/6]*FresnelS[(Sqrt[6/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[(3*a)/b])/(24*c^3)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)^(m_.), x_Symbol] := Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_.)*((f_.)*(x_))^(m_.)/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] := Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4677

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]
```

Rule 4623

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_), x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]
```

Rule 3306

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 4635

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rubi steps

$$\begin{aligned}
\int x^2 (a + b \sin^{-1}(cx))^{3/2} dx &= \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2} - \frac{1}{2} (bc) \int \frac{x^3 \sqrt{a + b \sin^{-1}(cx)}}{\sqrt{1 - c^2 x^2}} dx \\
&= \frac{bx^2 \sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{6c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2} - \frac{1}{12} b^2 \int \frac{x^2}{\sqrt{a + b \sin^{-1}(cx)}} dx \\
&= \frac{b\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{6c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2} \\
&= \frac{b\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{6c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2} \\
&= \frac{b\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{6c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2} \\
&= \frac{b\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{6c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2} \\
&= \frac{b\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{6c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2} \\
&= \frac{b\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{3c^3} + \frac{bx^2 \sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{6c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{3/2}
\end{aligned}$$

Mathematica [C] time = 0.285122, size = 245, normalized size = 0.78

$$\frac{be^{-\frac{3ia}{b}} \sqrt{a + b \sin^{-1}(cx)} \left(27e^{\frac{2ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{5}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) + 27e^{\frac{4ia}{b}} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{5}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) \right)}{216c^3 \sqrt{(a+b \sin^{-1}(cx))^2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2*(a + b*ArcSin[c*x])^(3/2), x]

[Out] (b*Sqrt[a + b*ArcSin[c*x]]*(27*E^(((2*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[5/2, ((-I)*(a + b*ArcSin[c*x]))/b] + 27*E^(((4*I)*a)/b)*Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[5/2, (I*(a + b*ArcSin[c*x]))/b] - Sqrt[3]*(Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[5/2, ((-3*I)*(a + b*ArcSin[c*x]))/b] + E^(((6*I)*a)/b)*Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[5/2, ((3*I)*(a + b*ArcSin[c*x]))/b]))/(216*c^3*E^(((3*I)*a)/b)*Sqrt[(a + b*ArcSin[c*x])^2/b^2])

Maple [B] time = 0.105, size = 540, normalized size = 1.7

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(a+b*arcsin(c*x))^(3/2),x)`

[Out] $\frac{1}{144} \frac{1}{c^3} (a+b \arcsin(cx))^{1/2} (3^{1/2} (1/b)^{1/2} \pi^{1/2} (a+b \arcsin(cx))^{1/2} \cos(3a/b) \operatorname{FresnelC}(2^{1/2}/\pi^{1/2} 3^{1/2}/(1/b)^{1/2} (a+b \arcsin(cx))^{1/2}/b) + 2^{1/2} b^2 + 3^{1/2} (1/b)^{1/2} \pi^{1/2} (a+b \arcsin(cx))^{1/2} \sin(3a/b) \operatorname{FresnelS}(2^{1/2}/\pi^{1/2} 3^{1/2}/(1/b)^{1/2} (a+b \arcsin(cx))^{1/2}/b) + 2^{1/2} b^2 - 27 (1/b)^{1/2} \pi^{1/2} (a+b \arcsin(cx))^{1/2} \cos(a/b) \operatorname{FresnelC}(2^{1/2}/\pi^{1/2}/(1/b)^{1/2} (a+b \arcsin(cx))^{1/2}/b) + 2^{1/2} b^2 - 27 (1/b)^{1/2} \pi^{1/2} (a+b \arcsin(cx))^{1/2} \sin(a/b) \operatorname{FresnelS}(2^{1/2}/\pi^{1/2}/(1/b)^{1/2} (a+b \arcsin(cx))^{1/2}/b) + 2^{1/2} b^2 + 36 \arcsin(cx)^2 \sin((a+b \arcsin(cx))/b - a/b) b^2 - 12 \arcsin(cx)^2 \sin(3(a+b \arcsin(cx))/b - 3a/b) b^2 + 72 \arcsin(cx) \sin((a+b \arcsin(cx))/b - a/b) a b + 54 \arcsin(cx) \cos((a+b \arcsin(cx))/b - a/b) b^2 - 24 \arcsin(cx) \sin(3(a+b \arcsin(cx))/b - 3a/b) a b - 6 \arcsin(cx) \cos(3(a+b \arcsin(cx))/b - 3a/b) b^2 + 36 \sin((a+b \arcsin(cx))/b - a/b) a^2 + 54 \cos((a+b \arcsin(cx))/b - a/b) a b - 12 \sin(3(a+b \arcsin(cx))/b - 3a/b) a^2 - 6 \cos(3(a+b \arcsin(cx))/b - 3a/b) a b)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (b \arcsin(cx) + a)^{\frac{3}{2}} x^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(a+b*arcsin(c*x))^(3/2),x, algorithm="maxima")`

[Out] `integrate((b*arcsin(c*x) + a)^(3/2)*x^2, x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(a+b*arcsin(c*x))^(3/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 (a + b \operatorname{asin}(cx))^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*(a+b*asin(c*x))**(3/2),x)`

[Out] `Integral(x**2*(a + b*asin(c*x))**(3/2), x)`

Giac [C] time = 3.49969, size = 1740, normalized size = 5.56

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^(3/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/16*I*\sqrt{2}*\sqrt{\pi}*a*b^3*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)} \\ & /((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c^3) + 3/32*\sqrt{2}*\sqrt{\pi}*b^4* \\ & \operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{\operatorname{abs}(b)}/b \\ & *e^{(I*a/b)}/((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c^3) + 1/16*I*\sqrt{2}*\sqrt{\pi}*a*b^3*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)}/((-I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c^3) + 3/32*\sqrt{2}*\sqrt{\pi}*b^4* \\ & \operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{\operatorname{abs}(b)}/b \\ & *e^{(-I*a/b)}/((-I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c^3) + 1/24*I*\sqrt{\pi}*a*b^{(5/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{b} \\ & - 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{b}/\operatorname{abs}(b)*e^{(3*I*a/b)}/((\sqrt{6}*b^2 + I*\sqrt{6}*b^3/\operatorname{abs}(b))*c^3) - 1/48*\sqrt{\pi}*b^{(7/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{b} \\ & - 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{b}/\operatorname{abs}(b)*e^{(3*I*a/b)}/((\sqrt{6}*b^2 + I*\sqrt{6}*b^3/\operatorname{abs}(b))*c^3) + 1/16*I*\sqrt{2}*\sqrt{\pi}*a*b^2*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)}/((I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c^3) - 1/16*I*\sqrt{2}*\sqrt{\pi}*a*b^2*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)}/((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c^3) - 1/24*I*\sqrt{\pi}*a*b^{(5/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{b} \\ & + 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{b}/\operatorname{abs}(b)*e^{(-3*I*a/b)}/((\sqrt{6}*b^2 - I*\sqrt{6}*b^3/\operatorname{abs}(b))*c^3) - 1/48*\sqrt{\pi}*b^{(7/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{b} \\ & + 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{b}/\operatorname{abs}(b)*e^{(-3*I*a/b)}/((\sqrt{6}*b^2 - I*\sqrt{6}*b^3/\operatorname{abs}(b))*c^3) - 1/24*I*\sqrt{\pi}*a*b^{(3/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a)/\sqrt{b} \\ & - 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x)} + a*\sqrt{b}/\operatorname{abs}(b)*e^{(-3*I*a/b)}/((\sqrt{6}*b - I*\sqrt{6}*b^2/\operatorname{abs}(b))*c^3) + 1/24*I*\sqrt{b*\arcsin(c*x)} + a*b*\arcsin(c*x)*e^{(3*I*\arcsin(c*x))}/c^3 \\ & - 1/8*I*\sqrt{b*\arcsin(c*x)} + a*b*\arcsin(c*x)*e^{(I*\arcsin(c*x))}/c^3 + 1/8*I*\sqrt{b*\arcsin(c*x)} + a*b*\arcsin(c*x)*e^{(-I*\arcsin(c*x))}/c^3 \\ & - 1/24*I*\sqrt{b*\arcsin(c*x)} + a*b*\arcsin(c*x)*e^{(-3*I*\arcsin(c*x))}/c^3 + 1/24*I*\sqrt{b*\arcsin(c*x)} + a*a*e^{(3*I*\arcsin(c*x))}/c^3 \\ & - 1/48*\sqrt{b*\arcsin(c*x)} + a*b*e^{(3*I*\arcsin(c*x))}/c^3 - 1/8*I*\sqrt{b*\arcsin(c*x)} + a*a*e^{(I*\arcsin(c*x))}/c^3 + 3/16*\sqrt{b*\arcsin(c*x)} + a*b*e^{(I*\arcsin(c*x))}/c^3 \\ & + 1/8*I*\sqrt{b*\arcsin(c*x)} + a*a*e^{(-I*\arcsin(c*x))}/c^3 + 3/16*\sqrt{b*\arcsin(c*x)} + a*b*e^{(-I*\arcsin(c*x))}/c^3 - 1/24*I*\sqrt{b*\arcsin(c*x)} + a*a*e^{(-3*I*\arcsin(c*x))}/c^3 \\ & - 1/48*\sqrt{b*\arcsin(c*x)} + a*b*e^{(-3*I*\arcsin(c*x))}/c^3 \end{aligned}$$

3.179 $\int x \left(a + b \sin^{-1}(cx) \right)^{3/2} dx$

Optimal. Leaf size=172

$$\frac{3\sqrt{\pi}b^{3/2} \sin\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{32c^2} - \frac{3\sqrt{\pi}b^{3/2} \cos\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{32c^2} + \frac{3bx\sqrt{1-c^2x^2}\sqrt{a+b\sin^{-1}(cx)}}{8c} - \frac{(a + b\sin^{-1}(cx))^{3/2}}{4c^2} + \frac{x^2(a + b\sin^{-1}(cx))^{3/2}}{2} - \frac{(3b^{3/2}\sqrt{\pi} \cos\left(\frac{2a}{b}\right) \text{FresnelS}\left[\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right])}{32c^2} + \frac{(3b^{3/2}\sqrt{\pi} \text{FresnelC}\left[\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right]) \sin\left(\frac{2a}{b}\right)}{32c^2}$$

[Out] (3*b*x*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(8*c) - (a + b*ArcSin[c*x])^(3/2)/(4*c^2) + (x^2*(a + b*ArcSin[c*x])^(3/2))/2 - (3*b^(3/2)*Sqrt[Pi]*Cos[(2*a)/b]*FresnelS[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])])/(32*c^2) + (3*b^(3/2)*Sqrt[Pi]*FresnelC[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])])*Sin[(2*a)/b]/(32*c^2)

Rubi [A] time = 0.524971, antiderivative size = 172, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 11, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.786$, Rules used = {4629, 4707, 4641, 4635, 4406, 12, 3306, 3305, 3351, 3304, 3352}

$$\frac{3\sqrt{\pi}b^{3/2} \sin\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{32c^2} - \frac{3\sqrt{\pi}b^{3/2} \cos\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{32c^2} + \frac{3bx\sqrt{1-c^2x^2}\sqrt{a+b\sin^{-1}(cx)}}{8c} - \frac{(a + b\sin^{-1}(cx))^{3/2}}{4c^2} + \frac{x^2(a + b\sin^{-1}(cx))^{3/2}}{2} - \frac{(3b^{3/2}\sqrt{\pi} \cos\left(\frac{2a}{b}\right) \text{FresnelS}\left[\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right])}{32c^2} + \frac{(3b^{3/2}\sqrt{\pi} \text{FresnelC}\left[\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right]) \sin\left(\frac{2a}{b}\right)}{32c^2}$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*ArcSin[c*x])^(3/2), x]

[Out] (3*b*x*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(8*c) - (a + b*ArcSin[c*x])^(3/2)/(4*c^2) + (x^2*(a + b*ArcSin[c*x])^(3/2))/2 - (3*b^(3/2)*Sqrt[Pi]*Cos[(2*a)/b]*FresnelS[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])])/(32*c^2) + (3*b^(3/2)*Sqrt[Pi]*FresnelC[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])])*Sin[(2*a)/b]/(32*c^2)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((f_.)*(x_)^(m_)))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[((f*x)^(m - 2)*(a + b*ArcSin[c*x])^n)/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
\int x (a + b \sin^{-1}(cx))^{3/2} dx &= \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{1}{4} (3bc) \int \frac{x^2 \sqrt{a + b \sin^{-1}(cx)}}{\sqrt{1 - c^2 x^2}} dx \\
&= \frac{3bx\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{8c} + \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{1}{16} (3b^2) \int \frac{x}{\sqrt{a + b \sin^{-1}(cx)}} dx \\
&= \frac{3bx\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{8c} - \frac{(a + b \sin^{-1}(cx))^{3/2}}{4c^2} + \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{(3b^2) \operatorname{Si}(\sqrt{a + b \sin^{-1}(cx)})}{16c} \\
&= \frac{3bx\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{8c} - \frac{(a + b \sin^{-1}(cx))^{3/2}}{4c^2} + \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{(3b^2) \operatorname{Si}(\sqrt{a + b \sin^{-1}(cx)})}{16c} \\
&= \frac{3bx\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{8c} - \frac{(a + b \sin^{-1}(cx))^{3/2}}{4c^2} + \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{(3b^2) \operatorname{Si}(\sqrt{a + b \sin^{-1}(cx)})}{16c} \\
&= \frac{3bx\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{8c} - \frac{(a + b \sin^{-1}(cx))^{3/2}}{4c^2} + \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{(3b^2 \cos^{-1}(\sqrt{a + b \sin^{-1}(cx)}))}{16c} \\
&= \frac{3bx\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{8c} - \frac{(a + b \sin^{-1}(cx))^{3/2}}{4c^2} + \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{(3b \cos^{-1}(\sqrt{a + b \sin^{-1}(cx)}))}{16c} \\
&= \frac{3bx\sqrt{1 - c^2 x^2} \sqrt{a + b \sin^{-1}(cx)}}{8c} - \frac{(a + b \sin^{-1}(cx))^{3/2}}{4c^2} + \frac{1}{2} x^2 (a + b \sin^{-1}(cx))^{3/2} - \frac{3b^{3/2} \sqrt{\pi} \operatorname{Si}(\sqrt{a + b \sin^{-1}(cx)})}{16c}
\end{aligned}$$

Mathematica [C] time = 0.0585441, size = 126, normalized size = 0.73

$$\frac{b^2 e^{-\frac{2ia}{b}} \left(\sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{5}{2}, -\frac{2i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{4ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{5}{2}, \frac{2i(a+b \sin^{-1}(cx))}{b}\right) \right)}{16\sqrt{2}c^2 \sqrt{a + b \sin^{-1}(cx)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*(a + b*ArcSin[c*x])^(3/2), x]

[Out] (b^2*(Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[5/2, ((-2*I)*(a + b*ArcSin[c*x]))/b] + E^(((4*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[5/2, ((2*I)*(a + b*ArcSin[c*x]))/b]))/(16*Sqrt[2]*c^2*E^(((2*I)*a)/b)*Sqrt[a + b*ArcSin[c*x]])

Maple [A] time = 0.092, size = 267, normalized size = 1.6

$$-\frac{1}{32c^2} \left(3\sqrt{b^{-1}}\sqrt{\pi}\sqrt{a + b \arcsin(cx)} \cos\left(2\frac{a}{b}\right) \operatorname{FresnelS}\left(2\frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}}\sqrt{\pi b}}\right) b^2 - 3\sqrt{b^{-1}}\sqrt{\pi}\sqrt{a + b \arcsin(cx)} \sin\left(2\frac{a}{b}\right) \operatorname{FresnelC}\left(2\frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}}\sqrt{\pi b}}\right) b^2 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a+b*arcsin(c*x))^(3/2), x)

[Out] -1/32/c^2*(3*(1/b)^(1/2)*Pi^(1/2)*(a+b*arcsin(c*x))^(1/2)*cos(2*a/b)*FresnelS(2/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*b^2-3*(1/b)^(1/2)*Pi^(1/2)*(a+b*arcsin(c*x))^(1/2)*sin(2*a/b)*FresnelC(2/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*b^2)

$$\frac{1}{2}*(a+b*\arcsin(c*x))^{(1/2)}*\sin(2*a/b)*\text{FresnelC}(2/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*b^2+8*\arcsin(c*x)^2*\cos(2*(a+b*\arcsin(c*x))/b-2*a/b)*b^2+16*\arcsin(c*x)*\cos(2*(a+b*\arcsin(c*x))/b-2*a/b)*a*b-6*\arcsin(c*x)*\sin(2*(a+b*\arcsin(c*x))/b-2*a/b)*b^2+8*\cos(2*(a+b*\arcsin(c*x))/b-2*a/b)*a^2-6*\sin(2*(a+b*\arcsin(c*x))/b-2*a/b)*a*b)/(a+b*\arcsin(c*x))^{(1/2)}$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (b \arcsin(cx) + a)^{\frac{3}{2}} x dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^(3/2),x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(3/2)*x, x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x (a + b \arcsin(cx))^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*asin(c*x))**(3/2),x)

[Out] Integral(x*(a + b*asin(c*x))**(3/2), x)

Giac [C] time = 2.22962, size = 757, normalized size = 4.4

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*(a+b*arcsin(c*x))^(3/2),x, algorithm="giac")

[Out] $\frac{1}{16}\sqrt{\pi} * a * b^{(5/2)} * \text{erf}(-\sqrt{b * \arcsin(c * x) + a} / \sqrt{b}) - I * \sqrt{b * \arcsin(c * x) + a} * \sqrt{b} / \text{abs}(b) * e^{(2 * I * a / b)} / ((b^2 + I * b^3 / \text{abs}(b)) * c^2) + 3 / 64 * I * \sqrt{\pi} * b^{(7/2)} * \text{erf}(-\sqrt{b * \arcsin(c * x) + a} / \sqrt{b}) - I * \sqrt{b * \arcsin(c * x) + a} * \sqrt{b} / \text{abs}(b) * e^{(2 * I * a / b)} / ((b^2 + I * b^3 / \text{abs}(b)) * c^2) + 1 / 16 * \text{sqr}$

$$\begin{aligned}
& t(\pi) * a * b^{(5/2)} * \operatorname{erf}(-\sqrt{b * \arcsin(c * x) + a} / \sqrt{b} + I * \sqrt{b * \arcsin(c * x) + a} * \sqrt{b} / \operatorname{abs}(b)) * e^{(-2 * I * a / b) / ((b^2 - I * b^3 / \operatorname{abs}(b)) * c^2)} - 3 / 64 * I * \sqrt{\pi} * \\
& (\pi) * b^{(7/2)} * \operatorname{erf}(-\sqrt{b * \arcsin(c * x) + a} / \sqrt{b} + I * \sqrt{b * \arcsin(c * x) + a} * \sqrt{b} / \operatorname{abs}(b)) * e^{(-2 * I * a / b) / ((b^2 - I * b^3 / \operatorname{abs}(b)) * c^2)} - 1 / 16 * \sqrt{\pi} * \\
& a * b^{(3/2)} * \operatorname{erf}(-\sqrt{b * \arcsin(c * x) + a} / \sqrt{b} - I * \sqrt{b * \arcsin(c * x) + a} * \sqrt{b} / \operatorname{abs}(b)) * e^{(2 * I * a / b) / ((b + I * b^2 / \operatorname{abs}(b)) * c^2)} - 1 / 16 * \sqrt{\pi} * a * b^{(3 / 2)} * \\
& \operatorname{erf}(-\sqrt{b * \arcsin(c * x) + a} / \sqrt{b} + I * \sqrt{b * \arcsin(c * x) + a} * \sqrt{b} / \operatorname{abs}(b)) * e^{(-2 * I * a / b) / ((b - I * b^2 / \operatorname{abs}(b)) * c^2)} - 1 / 8 * \sqrt{b * \arcsin(c * x) + a} * \\
& b * \arcsin(c * x) * e^{(2 * I * \arcsin(c * x)) / c^2} - 1 / 8 * \sqrt{b * \arcsin(c * x) + a} * b * \arcsin(c * x) * e^{(-2 * I * \arcsin(c * x)) / c^2} - 1 / 8 * \sqrt{b * \arcsin(c * x) + a} * a * e^{(2 * I * a \arcsin(c * x)) / c^2} - 3 / 32 * I * \sqrt{b * \arcsin(c * x) + a} * b * e^{(2 * I * \arcsin(c * x)) / c^2} \\
& - 1 / 8 * \sqrt{b * \arcsin(c * x) + a} * a * e^{(-2 * I * \arcsin(c * x)) / c^2} + 3 / 32 * I * \sqrt{b * \arcsin(c * x) + a} * b * e^{(-2 * I * \arcsin(c * x)) / c^2}
\end{aligned}$$

3.180 $\int (a + b \sin^{-1}(cx))^{3/2} dx$

Optimal. Leaf size=159

$$\frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\cos\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{2c} - \frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\sin\left(\frac{a}{b}\right)S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{2c} + \frac{3b\sqrt{1-c^2x^2}\sqrt{a+b\sin^{-1}(cx)}}{2c}$$

[Out] (3*b*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(2*c) + x*(a + b*ArcSin[c*x])^(3/2) - (3*b^(3/2)*Sqrt[Pi/2]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(2*c) - (3*b^(3/2)*Sqrt[Pi/2]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(2*c)

Rubi [A] time = 0.280982, antiderivative size = 159, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4619, 4677, 4623, 3306, 3305, 3351, 3304, 3352}

$$\frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\cos\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{2c} - \frac{3\sqrt{\frac{\pi}{2}}b^{3/2}\sin\left(\frac{a}{b}\right)S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{2c} + \frac{3b\sqrt{1-c^2x^2}\sqrt{a+b\sin^{-1}(cx)}}{2c}$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^(3/2), x]

[Out] (3*b*Sqrt[1 - c^2*x^2]*Sqrt[a + b*ArcSin[c*x]])/(2*c) + x*(a + b*ArcSin[c*x])^(3/2) - (3*b^(3/2)*Sqrt[Pi/2]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(2*c) - (3*b^(3/2)*Sqrt[Pi/2]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(2*c)

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.), x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x], x] /; FreeQ[{a, b, c, n}, x]

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d,

e, f, x && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int (a + b \sin^{-1}(cx))^{3/2} dx &= x(a + b \sin^{-1}(cx))^{3/2} - \frac{1}{2}(3bc) \int \frac{x\sqrt{a + b \sin^{-1}(cx)}}{\sqrt{1 - c^2x^2}} dx \\ &= \frac{3b\sqrt{1 - c^2x^2}\sqrt{a + b \sin^{-1}(cx)}}{2c} + x(a + b \sin^{-1}(cx))^{3/2} - \frac{1}{4}(3b^2) \int \frac{1}{\sqrt{a + b \sin^{-1}(cx)}} dx \\ &= \frac{3b\sqrt{1 - c^2x^2}\sqrt{a + b \sin^{-1}(cx)}}{2c} + x(a + b \sin^{-1}(cx))^{3/2} - \frac{(3b) \operatorname{Subst}\left(\int \frac{\cos\left(\frac{a-x}{b}\right)}{\sqrt{x}} dx, x, a + b \sin^{-1}(cx)\right)}{4c} \\ &= \frac{3b\sqrt{1 - c^2x^2}\sqrt{a + b \sin^{-1}(cx)}}{2c} + x(a + b \sin^{-1}(cx))^{3/2} - \frac{(3b \cos\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \frac{\cos\left(\frac{x}{b}\right)}{\sqrt{x}} dx, x, a + b \sin^{-1}(cx)\right)}{4c} \\ &= \frac{3b\sqrt{1 - c^2x^2}\sqrt{a + b \sin^{-1}(cx)}}{2c} + x(a + b \sin^{-1}(cx))^{3/2} - \frac{(3b \cos\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \cos\left(\frac{x^2}{b}\right) dx, x, a + b \sin^{-1}(cx)\right)}{2c} \\ &= \frac{3b\sqrt{1 - c^2x^2}\sqrt{a + b \sin^{-1}(cx)}}{2c} + x(a + b \sin^{-1}(cx))^{3/2} - \frac{3b^{3/2} \sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) C\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a + b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2c} \end{aligned}$$

Mathematica [C] time = 2.79561, size = 291, normalized size = 1.83

$$b \left(\frac{2ae^{-\frac{ia}{b}} \left(\sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{3}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{2ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{3}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) \right)}{\sqrt{a+b \sin^{-1}(cx)}} \right) + 2 \left(3\sqrt{1 - c^2x^2} + 2cx \sin^{-1}(cx) \right) \sqrt{a+b \sin^{-1}(cx)}$$

Warning: Unable to verify antiderivative.

[In] Integrate[(a + b*ArcSin[c*x])^(3/2), x]

[Out] (b*(2*Sqrt[a + b*ArcSin[c*x]]*(3*Sqrt[1 - c^2*x^2] + 2*c*x*ArcSin[c*x])) + (2*a*(Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[3/2, ((-I)*(a + b*ArcSin[c*x]))/b] + E^(((2*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[3/2, (I*(a + b*ArcSin[c*x]))/b]))/(E^((I*a)/b)*Sqrt[a + b*ArcSin[c*x]]) - Sqrt[b^(-1)]*Sqrt[2*Pi]*FresnelC[Sqrt[b^(-1)]*Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]]]*(3*b*Cos[a/b] + 2*a*Sin[a/b]) + Sqrt[b^(-1)]*Sqrt[2*Pi]*FresnelS[Sqrt[b^(-1)]*Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]]]*(2*a*Cos[a/b] - 3*b*Sin[a/b]))/(4*c)

Maple [B] time = 0.056, size = 270, normalized size = 1.7

$$\frac{1}{4c} \left(-3 \sqrt{b^{-1}} \sqrt{\pi} \sqrt{a + b \arcsin(cx)} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{2} \sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}} \sqrt{\pi b}}\right) \sqrt{2} b^2 - 3 \sqrt{b^{-1}} \sqrt{\pi} \sqrt{a + b \arcsin(cx)} \sin\left(\frac{a}{b}\right) \text{FresnelS}\left(\frac{\sqrt{2} \sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}} \sqrt{\pi b}}\right) \sqrt{2} b^2 \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(3/2), x)

[Out] 1/4/c/(a+b*arcsin(c*x))^(1/2)*(-3*(1/b)^(1/2)*Pi^(1/2)*(a+b*arcsin(c*x))^(1/2)*cos(a/b)*FresnelC(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*2^(1/2)*b^2-3*(1/b)^(1/2)*Pi^(1/2)*(a+b*arcsin(c*x))^(1/2)*sin(a/b)*FresnelS(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*2^(1/2)*b^2+4*arcsin(c*x)^2*sin((a+b*arcsin(c*x))/b-a/b)*b^2+8*arcsin(c*x)*sin((a+b*arcsin(c*x))/b-a/b)*a*b+6*arcsin(c*x)*cos((a+b*arcsin(c*x))/b-a/b)*b^2+4*sin((a+b*arcsin(c*x))/b-a/b)*a^2+6*cos((a+b*arcsin(c*x))/b-a/b)*a*b

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (b \arcsin(cx) + a)^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2), x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(3/2), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2), x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int (a + b \operatorname{asin}(cx))^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**(3/2),x)

[Out] Integral((a + b*asin(c*x))**(3/2), x)

Giac [C] time = 2.46893, size = 879, normalized size = 5.53

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/4*I*\sqrt{2}*\sqrt{\pi}*a*b^3*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a})/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)/((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c)} \\ & + 3/8*\sqrt{2}*\sqrt{\pi}*b^4*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a})/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)/((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c)} \\ & + 1/4*I*\sqrt{2}*\sqrt{\pi}*a*b^3*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a})/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)/((-I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c)} \\ & + 3/8*\sqrt{2}*\sqrt{\pi}*b^4*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a})/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)/((-I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c)} \\ & + 1/4*I*\sqrt{2}*\sqrt{\pi}*a*b^2*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a})/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)/((I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c)} \\ & - 1/4*I*\sqrt{2}*\sqrt{\pi}*a*b^2*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a})/\sqrt{\operatorname{abs}(b)} \\ & - 1/2*\sqrt{2}*\sqrt{b*\operatorname{arcsin}(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)/((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c)} \\ & - 1/2*I*\sqrt{b*\operatorname{arcsin}(c*x) + a}*b*\operatorname{arcsin}(c*x)*e^{(I*\operatorname{arcsin}(c*x))/c} \\ & + 1/2*I*\sqrt{b*\operatorname{arcsin}(c*x) + a}*b*\operatorname{arcsin}(c*x)*e^{(-I*\operatorname{arcsin}(c*x))/c} \\ & - 1/2*I*\sqrt{b*\operatorname{arcsin}(c*x) + a}*a*e^{(I*\operatorname{arcsin}(c*x))/c} \\ & + 3/4*\sqrt{b*\operatorname{arcsin}(c*x) + a}*b*e^{(I*\operatorname{arcsin}(c*x))/c} \\ & + 1/2*I*\sqrt{b*\operatorname{arcsin}(c*x) + a}*a*e^{(-I*\operatorname{arcsin}(c*x))/c} \\ & + 3/4*\sqrt{b*\operatorname{arcsin}(c*x) + a}*b*e^{(-I*\operatorname{arcsin}(c*x))/c} \end{aligned}$$

$$3.181 \quad \int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{(a+b \sin^{-1}(cx))^{3/2}}{x}, x \right)$$

[Out] Unintegrable[(a + b*ArcSin[c*x])^(3/2)/x, x]

Rubi [A] time = 0.0451535, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*ArcSin[c*x])^(3/2)/x,x]

[Out] Defer[Int] [(a + b*ArcSin[c*x])^(3/2)/x, x]

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x} dx = \int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x} dx$$

Mathematica [A] time = 2.90078, size = 0, normalized size = 0.

$$\int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*ArcSin[c*x])^(3/2)/x,x]

[Out] Integrate[(a + b*ArcSin[c*x])^(3/2)/x, x]

Maple [A] time = 0.11, size = 0, normalized size = 0.

$$\int \frac{1}{x} (a+b \arcsin(cx))^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(3/2)/x,x)

[Out] int((a+b*arcsin(c*x))^(3/2)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{3}{2}}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2)/x,x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(3/2)/x, x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2)/x,x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(a + b \arcsin(cx))^{\frac{3}{2}}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**(3/2)/x,x)

[Out] Integral((a + b*asin(c*x))**(3/2)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{3}{2}}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2)/x,x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)^(3/2)/x, x)

$$3.182 \quad \int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x^2} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{(a+b \sin^{-1}(cx))^{3/2}}{x^2}, x \right)$$

[Out] Unintegrable[(a + b*ArcSin[c*x])^(3/2)/x^2, x]

Rubi [A] time = 0.0420042, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*ArcSin[c*x])^(3/2)/x^2, x]

[Out] Defer[Int][(a + b*ArcSin[c*x])^(3/2)/x^2, x]

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x^2} dx = \int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x^2} dx$$

Mathematica [A] time = 10.1427, size = 0, normalized size = 0.

$$\int \frac{(a+b \sin^{-1}(cx))^{3/2}}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*ArcSin[c*x])^(3/2)/x^2, x]

[Out] Integrate[(a + b*ArcSin[c*x])^(3/2)/x^2, x]

Maple [A] time = 0.169, size = 0, normalized size = 0.

$$\int \frac{1}{x^2} (a+b \arcsin(cx))^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(3/2)/x^2, x)

[Out] int((a+b*arcsin(c*x))^(3/2)/x^2, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{3}{2}}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2)/x^2,x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(3/2)/x^2, x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2)/x^2,x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(a + b \arcsin(cx))^{\frac{3}{2}}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**(3/2)/x**2,x)

[Out] Integral((a + b*asin(c*x))**(3/2)/x**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{3}{2}}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(3/2)/x^2,x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)^(3/2)/x^2, x)

3.183 $\int x^2 \left(a + b \sin^{-1}(cx) \right)^{5/2} dx$

Optimal. Leaf size=358

$$\frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\sin\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{16c^3} + \frac{5\sqrt{\frac{\pi}{6}}b^{5/2}\sin\left(\frac{3a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{144c^3} + \frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\cos\left(\frac{a}{b}\right)}{16c^3}$$

[Out] $(-5*b^2*x*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(6*c^2) - (5*b^2*x^3*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/36 + (5*b*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^(3/2))/(9*c^3) + (5*b*x^2*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^(3/2))/(18*c) + (x^3*(a + b*\text{ArcSin}[c*x])^(5/2))/3 + (15*b^(5/2)*\text{Sqrt}[\text{Pi}/2]*\text{Cos}[a/b]*\text{FresnelS}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(16*c^3) - (5*b^(5/2)*\text{Sqrt}[\text{Pi}/6]*\text{Cos}[(3*a)/b]*\text{FresnelS}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(144*c^3) - (15*b^(5/2)*\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(16*c^3) + (5*b^(5/2)*\text{Sqrt}[\text{Pi}/6]*\text{FresnelC}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[(3*a)/b])/(144*c^3)$

Rubi [A] time = 1.40912, antiderivative size = 358, normalized size of antiderivative = 1., number of steps used = 24, number of rules used = 11, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.688$, Rules used = {4629, 4707, 4677, 4619, 4723, 3306, 3305, 3351, 3304, 3352, 3312}

$$\frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\sin\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{16c^3} + \frac{5\sqrt{\frac{\pi}{6}}b^{5/2}\sin\left(\frac{3a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{144c^3} + \frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\cos\left(\frac{a}{b}\right)}{16c^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*(a + b*\text{ArcSin}[c*x])^(5/2), x]$

[Out] $(-5*b^2*x*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(6*c^2) - (5*b^2*x^3*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/36 + (5*b*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^(3/2))/(9*c^3) + (5*b*x^2*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^(3/2))/(18*c) + (x^3*(a + b*\text{ArcSin}[c*x])^(5/2))/3 + (15*b^(5/2)*\text{Sqrt}[\text{Pi}/2]*\text{Cos}[a/b]*\text{FresnelS}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(16*c^3) - (5*b^(5/2)*\text{Sqrt}[\text{Pi}/6]*\text{Cos}[(3*a)/b]*\text{FresnelS}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(144*c^3) - (15*b^(5/2)*\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(16*c^3) + (5*b^(5/2)*\text{Sqrt}[\text{Pi}/6]*\text{FresnelC}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[(3*a)/b])/(144*c^3)$

Rule 4629

$\text{Int}[(a + \text{ArcSin}[c*x])^n*(b*x)^m, x] := \text{Simp}[(x^{m+1}*(a + b*\text{ArcSin}[c*x])^n)/(m+1), x] - \text{Dist}[(b*c^n)/(m+1), \text{Int}[x^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}]/\text{Sqrt}[1 - c^2*x^2], x] /;$ FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

$\text{Int}[(a + \text{ArcSin}[c*x])^n*(f*x)^m/\text{Sqrt}[d + e*x^2], x] := \text{Simp}[(f*(f*x)^{m-1}*\text{Sqrt}[d + e*x^2]*(a + b*\text{ArcSin}[c*x])^n)/(e*m), x] + (\text{Dist}[(f^2*(m-1))/(c^2*m), \text{Int}[(f*x)^{m-2}*(a + b*\text{ArcSin}[c*x])^n]/\text{Sqrt}[d + e*x^2], x] + \text{Dist}[(b*f*n*\text{Sqrt}[1 - c^2*x^2])/(c*m*\text{Sqrt}[d + e*x^2]), \text{Int}[(f*x)^{m-1}*(a + b*\text{ArcSin}[c*x])^{n-1}], x] /;$ FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0]

&& GtQ[m, 1] && IntegerQ[m]

Rule 4677

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*(x_)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Simp[((d + e*x^2)^(p + 1)*(a + b*ArcSin[c*x])^n)/(2*e*(p + 1)), x] + Dist[(b*n*d^IntPart[p]*(d + e*x^2)^FracPart[p])/(2*c*(p + 1)*(1 - c^2*x^2)^FracPart[p]), Int[(1 - c^2*x^2)^(p + 1/2)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4619

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.), x_Symbol] := Simp[x*(a + b*ArcSin[c*x])^n, x] - Dist[b*c*n, Int[(x*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4723

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*(x_)^(m_.)*((d_) + (e_.)*(x_)^2)^(p_.), x_Symbol] := Dist[d^p/c^(m + 1), Subst[Int[(a + b*x)^n*SIN[x]^m*Cos[x]^(2*p + 1), x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[SIN[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[SIN[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[SIN[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[SIN[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, SIN[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f}

, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rubi steps

$$\begin{aligned}
 \int x^2 (a + b \sin^{-1}(cx))^{5/2} dx &= \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{5/2} - \frac{1}{6} (5bc) \int \frac{x^3 (a + b \sin^{-1}(cx))^{3/2}}{\sqrt{1 - c^2 x^2}} dx \\
 &= \frac{5bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{18c} + \frac{1}{3} x^3 (a + b \sin^{-1}(cx))^{5/2} - \frac{1}{12} (5b^2) \int x^2 \sqrt{a + b \sin^{-1}(cx)} dx \\
 &= -\frac{5}{36} b^2 x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{5b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{9c^3} + \frac{5bx^2 \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{18c} \\
 &= -\frac{5b^2 x \sqrt{a + b \sin^{-1}(cx)}}{6c^2} - \frac{5}{36} b^2 x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{5b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{9c^3} \\
 &= -\frac{5b^2 x \sqrt{a + b \sin^{-1}(cx)}}{6c^2} - \frac{5}{36} b^2 x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{5b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{9c^3} \\
 &= -\frac{5b^2 x \sqrt{a + b \sin^{-1}(cx)}}{6c^2} - \frac{5}{36} b^2 x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{5b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{9c^3} \\
 &= -\frac{5b^2 x \sqrt{a + b \sin^{-1}(cx)}}{6c^2} - \frac{5}{36} b^2 x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{5b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{9c^3} \\
 &= -\frac{5b^2 x \sqrt{a + b \sin^{-1}(cx)}}{6c^2} - \frac{5}{36} b^2 x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{5b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{9c^3} \\
 &= -\frac{5b^2 x \sqrt{a + b \sin^{-1}(cx)}}{6c^2} - \frac{5}{36} b^2 x^3 \sqrt{a + b \sin^{-1}(cx)} + \frac{5b \sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{9c^3}
 \end{aligned}$$

Mathematica [C] time = 0.273454, size = 228, normalized size = 0.64

$$b^3 e^{-\frac{3ia}{b}} \left(-81 e^{\frac{2ia}{b}} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \Gamma\left(\frac{7}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) - 81 e^{\frac{4ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \Gamma\left(\frac{7}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) + \sqrt{3} \right)$$

$$648c^3 \sqrt{a + b \sin^{-1}(cx)}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2*(a + b*ArcSin[c*x])^(5/2),x]

[Out] (b^3*(-81*E^(((2*I)*a)/b)*Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[7/2, ((-I)*(a + b*ArcSin[c*x]))/b] - 81*E^(((4*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[7/2, (I*(a + b*ArcSin[c*x]))/b] + Sqrt[3]*(Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[7/2, ((-3*I)*(a + b*ArcSin[c*x]))/b] + E^(((6*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[7/2, ((3*I)*(a + b*ArcSin[c*x]))/b]))/(648*c^3*E^(((3*I)*a)/b)*Sqrt[a + b*ArcSin[c*x]])

Maple [B] time = 0.118, size = 792, normalized size = 2.2

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*(a+b*arcsin(c*x))^(5/2),x)`

[Out] $\frac{1}{864} \frac{1}{c^3} \frac{1}{(a+b \arcsin(cx))^{\frac{1}{2}}} \left(-5 \cdot 3^{\frac{1}{2}} \cdot \frac{1}{b}^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \cdot 2^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \cos\left(\frac{3a}{b}\right) \cdot \text{FresnelS}\left(\frac{2^{\frac{1}{2}}}{\pi^{\frac{1}{2}}}\right) \cdot 3^{\frac{1}{2}} \cdot \frac{1}{b}^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \frac{1}{b} \cdot b^3 + 5 \cdot 3^{\frac{1}{2}} \cdot \frac{1}{b}^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \cdot 2^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \sin\left(\frac{3a}{b}\right) \cdot \text{FresnelC}\left(\frac{2^{\frac{1}{2}}}{\pi^{\frac{1}{2}}}\right) \cdot 3^{\frac{1}{2}} \cdot \frac{1}{b}^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \frac{1}{b} \cdot b^3 + 405 \cdot \frac{1}{b}^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \cdot 2^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \cos\left(\frac{a}{b}\right) \cdot \text{FresnelS}\left(\frac{2^{\frac{1}{2}}}{\pi^{\frac{1}{2}}}\right) \cdot \frac{1}{b}^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \frac{1}{b} \cdot b^3 - 405 \cdot \frac{1}{b}^{\frac{1}{2}} \cdot \pi^{\frac{1}{2}} \cdot 2^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \sin\left(\frac{a}{b}\right) \cdot \text{FresnelC}\left(\frac{2^{\frac{1}{2}}}{\pi^{\frac{1}{2}}}\right) \cdot \frac{1}{b}^{\frac{1}{2}} \cdot (a+b \arcsin(cx))^{\frac{1}{2}} \cdot \frac{1}{b} \cdot b^3 + 216 \arcsin(cx)^3 \sin\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot b^3 - 72 \arcsin(cx)^3 \sin\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot b^3 + 648 \arcsin(cx)^2 \sin\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot a \cdot b^2 + 540 \arcsin(cx)^2 \cos\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot b^3 - 216 \arcsin(cx)^2 \sin\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot a \cdot b^2 - 60 \arcsin(cx)^2 \cos\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot b^3 + 648 \arcsin(cx) \sin\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot a^2 \cdot b - 810 \arcsin(cx) \sin\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot b^3 + 1080 \arcsin(cx) \cos\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot a \cdot b^2 - 216 \arcsin(cx) \sin\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot a^2 \cdot b + 30 \arcsin(cx) \sin\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot b^3 - 120 \arcsin(cx) \cos\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot a \cdot b^2 + 216 \sin\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot a^3 - 810 \sin\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot a \cdot b^2 + 540 \cos\left(\frac{a+b \arcsin(cx)}{b-a}\right) \cdot a^2 \cdot b - 72 \sin\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot a^3 + 30 \sin\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot a \cdot b^2 - 60 \cos\left(\frac{3(a+b \arcsin(cx))}{b-3a}\right) \cdot a^2 \cdot b \right)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (b \arcsin(cx) + a)^{\frac{5}{2}} x^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(a+b*arcsin(c*x))^(5/2),x, algorithm="maxima")`

[Out] `integrate((b*arcsin(c*x) + a)^(5/2)*x^2, x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*(a+b*arcsin(c*x))^(5/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*(a+b*asin(c*x))**(5/2),x)

[Out] Timed out

Giac [C] time = 5.10383, size = 3357, normalized size = 9.38

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*(a+b*arcsin(c*x))^(5/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/8*I*\sqrt{2}*\sqrt{\pi}*a^2*b^3*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/ \\ & \sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)} / \\ & ((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c^3) + 3/16*\sqrt{2}*\sqrt{\pi}*a*b^4* \\ & \operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)} / ((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2* \\ & \sqrt{\operatorname{abs}(b)})*c^3) + 1/8*I*\sqrt{2}*\sqrt{\pi}*a^2*b^3*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{ \\ & \operatorname{abs}(b)}/b*e^{(-I*a/b)} / ((-I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c^3) + 3/16 \\ & *\sqrt{2}*\sqrt{\pi}*a*b^4*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(\\ & b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)} / ((-I*b \\ & ^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c^3) + 1/12*I*\sqrt{\pi}*a^2*b^{(5/2)}*\operatorname{erf} \\ & (-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{b} - 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(\\ & c*x) + a}*\sqrt{b}/\operatorname{abs}(b))*e^{(3*I*a/b)} / ((\sqrt{6}*b^2 + I*\sqrt{6}*b^3/\operatorname{abs}(b)) \\ & *c^3) - 1/24*\sqrt{\pi}*a*b^{(7/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{ \\ & b} - 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{b}/\operatorname{abs}(b))*e^{(3*I*a/b)} / (\\ & (\sqrt{6}*b^2 + I*\sqrt{6}*b^3/\operatorname{abs}(b))*c^3) + 1/8*I*\sqrt{2}*\sqrt{\pi}*a^2*b^2* \\ & \operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)} / ((I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{ \\ & \operatorname{abs}(b)})*c^3) - 3/16*\sqrt{2}*\sqrt{\pi}*a*b^3*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsi \\ & n(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b) \\ & }/b*e^{(I*a/b)} / ((I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c^3) - 15/64*I*\sqrt{2} \\ & *\sqrt{\pi}*b^4*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2 \\ & *\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(I*a/b)} / ((I*b^2/\sqrt{\operatorname{abs}(\\ & b)} + b*\sqrt{\operatorname{abs}(b)})*c^3) - 1/8*I*\sqrt{2}*\sqrt{\pi}*a^2*b^2*\operatorname{erf}(1/2*I*\sqrt{2} \\ & *\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + \\ & a}*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)} / ((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c^3) \\ & - 3/16*\sqrt{2}*\sqrt{\pi}*a*b^3*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{ \\ & \operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)} / \\ & ((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c^3) + 15/64*I*\sqrt{2}*\sqrt{\pi}*b^4 \\ & *\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b*e^{(-I*a/b)} / ((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{ \\ & \operatorname{abs}(b)})*c^3) - 1/12*I*\sqrt{\pi}*a^2*b^{(5/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcs \\ & in(c*x) + a})/\sqrt{b} + 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{b}/\operatorname{abs}(b) \\ &)*e^{(-3*I*a/b)} / ((\sqrt{6}*b^2 - I*\sqrt{6}*b^3/\operatorname{abs}(b))*c^3) - 1/24*\sqrt{\pi}*a \\ & *b^{(7/2)}*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{b} + 1/2*I*\sqrt{6}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{b}/\operatorname{abs}(b))*e^{(-3*I*a/b)} / ((\sqrt{6}*b^2 - I*\sqrt{6} \\ & *b^3/\operatorname{abs}(b))*c^3) + 1/24*I*\sqrt{b*\arcsin(c*x) + a}*b^2*\arcsin(c*x)^2*e^{(3 \\ & *I*\arcsin(c*x))}/c^3 - 1/8*I*\sqrt{b*\arcsin(c*x) + a}*b^2*\arcsin(c*x)^2*e^{(I* \\ & \arcsin(c*x))}/c^3 + 1/8*I*\sqrt{b*\arcsin(c*x) + a}*b^2*\arcsin(c*x)^2*e^{(-I*ar \\ & csin(c*x))}/c^3 - 1/24*I*\sqrt{b*\arcsin(c*x) + a}*b^2*\arcsin(c*x)^2*e^{(-3*I*a \\ & rcsin(c*x))}/c^3 - 1/24*I*\sqrt{\pi}*a^2*b^2*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c* \\ & x) + a})/\sqrt{b} - 1/2*I*\sqrt{6}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{b}/\operatorname{abs}(b))*e^{ \\ & (3*I*a/b)} / ((\sqrt{6}*b^{(3/2)} + I*\sqrt{6}*b^{(5/2)}/\operatorname{abs}(b))*c^3) + 1/24*I*\sqrt{\pi} \\ & *a^2*b^2*\operatorname{erf}(-1/2*\sqrt{6}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{b} + 1/2*I*\sqrt{6} \\ & *\sqrt{b*\arcsin(c*x) + a}*\sqrt{b}/\operatorname{abs}(b))*e^{(-3*I*a/b)} / ((\sqrt{6}*b^{(3/2)} - I \end{aligned}$$

$$\begin{aligned}
& \sqrt{6} * b^{(5/2)} / \text{abs}(b) * c^3 - 1/24 * I * \text{sqrt}(\pi) * a^2 * b^{(3/2)} * \text{erf}(-1/2 * \text{sqrt}(6) \\
&) * \text{sqrt}(b * \arcsin(c * x) + a) / \text{sqrt}(b) - 1/2 * I * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) * \text{sqrt} \\
& (b) / \text{abs}(b) * e^{(3 * I * a / b)} / ((\text{sqrt}(6) * b + I * \text{sqrt}(6) * b^2 / \text{abs}(b)) * c^3) + 1/24 * \\
& \text{sqrt}(\pi) * a * b^{(5/2)} * \text{erf}(-1/2 * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) / \text{sqrt}(b) - 1/2 * I \\
& * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) * \text{sqrt}(b) / \text{abs}(b)) * e^{(3 * I * a / b)} / ((\text{sqrt}(6) * b + \\
& I * \text{sqrt}(6) * b^2 / \text{abs}(b)) * c^3) + 5/288 * I * \text{sqrt}(\pi) * b^{(7/2)} * \text{erf}(-1/2 * \text{sqrt}(6) * \text{sqrt} \\
& (b * \arcsin(c * x) + a) / \text{sqrt}(b) - 1/2 * I * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) * \text{sqrt}(b) \\
& / \text{abs}(b)) * e^{(3 * I * a / b)} / ((\text{sqrt}(6) * b + I * \text{sqrt}(6) * b^2 / \text{abs}(b)) * c^3) + 1/24 * I * \text{sqrt} \\
& (\pi) * a^2 * b^{(3/2)} * \text{erf}(-1/2 * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) / \text{sqrt}(b) + 1/2 * I * \text{sqrt} \\
& (6) * \text{sqrt}(b * \arcsin(c * x) + a) * \text{sqrt}(b) / \text{abs}(b)) * e^{(-3 * I * a / b)} / ((\text{sqrt}(6) * b - I * \text{sqrt} \\
& (6) * b^2 / \text{abs}(b)) * c^3) + 1/24 * \text{sqrt}(\pi) * a * b^{(5/2)} * \text{erf}(-1/2 * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) / \text{sqrt}(b) + 1/2 * I * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) * \text{sqrt}(b) / \text{abs}(b)) * e^{(-3 * I * a / b)} / ((\text{sqrt}(6) * b - I * \text{sqrt}(6) * b^2 / \text{abs}(b)) * c^3) - 5/288 * I * \text{sqrt}(\pi) * b^{(7/2)} * \text{erf}(-1/2 * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) / \text{sqrt}(b) + 1/2 * I * \text{sqrt}(6) * \text{sqrt}(b * \arcsin(c * x) + a) * \text{sqrt}(b) / \text{abs}(b)) * e^{(-3 * I * a / b)} / ((\text{sqrt}(6) * b - I * \text{sqrt}(6) * b^2 / \text{abs}(b)) * c^3) + 1/12 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * \arcsin(c * x) * e^{(3 * I * \arcsin(c * x))} / c^3 - 5/144 * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * \arcsin(c * x) * e^{(3 * I * \arcsin(c * x))} / c^3 - 1/4 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * \arcsin(c * x) * e^{(I * \arcsin(c * x))} / c^3 + 5/16 * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * \arcsin(c * x) * e^{(I * \arcsin(c * x))} / c^3 + 1/4 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * \arcsin(c * x) * e^{(-I * \arcsin(c * x))} / c^3 + 5/16 * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * \arcsin(c * x) * e^{(-I * \arcsin(c * x))} / c^3 - 1/12 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * \arcsin(c * x) * e^{(-3 * I * \arcsin(c * x))} / c^3 - 5/144 * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * \arcsin(c * x) * e^{(-3 * I * \arcsin(c * x))} / c^3 + 1/24 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a^2 * e^{(3 * I * \arcsin(c * x))} / c^3 - 5/144 * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * e^{(3 * I * \arcsin(c * x))} / c^3 - 5/288 * I * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * e^{(3 * I * \arcsin(c * x))} / c^3 - 1/8 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a^2 * e^{(I * \arcsin(c * x))} / c^3 + 5/16 * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * e^{(I * \arcsin(c * x))} / c^3 + 15/32 * I * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * e^{(I * \arcsin(c * x))} / c^3 + 1/8 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a^2 * e^{(-I * \arcsin(c * x))} / c^3 + 5/16 * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * e^{(-I * \arcsin(c * x))} / c^3 - 15/32 * I * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * e^{(-I * \arcsin(c * x))} / c^3 - 1/24 * I * \text{sqrt}(b * \arcsin(c * x) + a) * a^2 * e^{(-3 * I * \arcsin(c * x))} / c^3 - 5/144 * \text{sqrt}(b * \arcsin(c * x) + a) * a * b * e^{(-3 * I * \arcsin(c * x))} / c^3 + 5/288 * I * \text{sqrt}(b * \arcsin(c * x) + a) * b^2 * e^{(-3 * I * \arcsin(c * x))} / c^3
\end{aligned}$$

3.184 $\int x \left(a + b \sin^{-1}(cx) \right)^{5/2} dx$

Optimal. Leaf size=216

$$\frac{15\sqrt{\pi}b^{5/2} \cos\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{128c^2} - \frac{15\sqrt{\pi}b^{5/2} \sin\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{128c^2} + \frac{15b^2\sqrt{a+b\sin^{-1}(cx)}}{64c^2} - \frac{15}{32}b^2$$

[Out] (15*b^2*Sqrt[a + b*ArcSin[c*x]])/(64*c^2) - (15*b^2*x^2*Sqrt[a + b*ArcSin[c*x]])/32 + (5*b*x*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(3/2))/(8*c) - (a + b*ArcSin[c*x])^(5/2)/(4*c^2) + (x^2*(a + b*ArcSin[c*x])^(5/2))/2 - (15*b^(5/2)*Sqrt[Pi]*Cos[(2*a)/b]*FresnelC[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])])/(128*c^2) - (15*b^(5/2)*Sqrt[Pi]*FresnelS[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])]*Sin[(2*a)/b])/(128*c^2)

Rubi [A] time = 0.742519, antiderivative size = 216, normalized size of antiderivative = 1., number of steps used = 12, number of rules used = 10, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.714$, Rules used = {4629, 4707, 4641, 4723, 3312, 3306, 3305, 3351, 3304, 3352}

$$\frac{15\sqrt{\pi}b^{5/2} \cos\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{128c^2} - \frac{15\sqrt{\pi}b^{5/2} \sin\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{128c^2} + \frac{15b^2\sqrt{a+b\sin^{-1}(cx)}}{64c^2} - \frac{15}{32}b^2$$

Antiderivative was successfully verified.

[In] Int[x*(a + b*ArcSin[c*x])^(5/2), x]

[Out] (15*b^2*Sqrt[a + b*ArcSin[c*x]])/(64*c^2) - (15*b^2*x^2*Sqrt[a + b*ArcSin[c*x]])/32 + (5*b*x*Sqrt[1 - c^2*x^2]*(a + b*ArcSin[c*x])^(3/2))/(8*c) - (a + b*ArcSin[c*x])^(5/2)/(4*c^2) + (x^2*(a + b*ArcSin[c*x])^(5/2))/2 - (15*b^(5/2)*Sqrt[Pi]*Cos[(2*a)/b]*FresnelC[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])])/(128*c^2) - (15*b^(5/2)*Sqrt[Pi]*FresnelS[(2*Sqrt[a + b*ArcSin[c*x]])/(Sqrt[b]*Sqrt[Pi])]*Sin[(2*a)/b])/(128*c^2)

Rule 4629

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Simp[(x^(m + 1)*(a + b*ArcSin[c*x])^n)/(m + 1), x] - Dist[(b*c*n)/(m + 1), Int[(x^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c}, x] && IGtQ[m, 0] && GtQ[n, 0]

Rule 4707

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((f_.)*(x_)^(m_.))/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] := Simp[(f*(f*x)^(m - 1)*Sqrt[d + e*x^2]*(a + b*ArcSin[c*x])^n)/(e*m), x] + (Dist[(f^2*(m - 1))/(c^2*m), Int[(f*x)^(m - 2)*(a + b*ArcSin[c*x])^n]/Sqrt[d + e*x^2], x], x] + Dist[(b*f*n*Sqrt[1 - c^2*x^2])/(c*m*Sqrt[d + e*x^2]), Int[(f*x)^(m - 1)*(a + b*ArcSin[c*x])^(n - 1), x], x] /; FreeQ[{a, b, c, d, e, f}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && GtQ[m, 1] && IntegerQ[m]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)/Sqrt[(d_.) + (e_.)*(x_)^2], x_Symbol] := Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; Fre

$\text{Eq}\{a, b, c, d, e, n\}, x\} \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{GtQ}[d, 0] \ \&\& \ \text{NeQ}[n, -1]$

Rule 4723

$\text{Int}[(a + \text{ArcSin}[c \cdot x] \cdot b)^n \cdot x^m \cdot (d + e \cdot x)^2 \cdot p, x_{\text{Symbol}}] \rightarrow \text{Dist}[d^p/c^{m+1}, \text{Subst}[\text{Int}[(a + b \cdot x)^n \cdot \text{Sin}[x]^m \cdot \text{Cos}[x]^{2p+1}, x], x, \text{ArcSin}[c \cdot x]], x] /;$ $\text{FreeQ}\{a, b, c, d, e, n\}, x\} \ \&\& \ \text{EqQ}[c^2*d + e, 0] \ \&\& \ \text{IntegerQ}[2*p] \ \&\& \ \text{GtQ}[p, -1] \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ (\text{IntegerQ}[p] \ || \ \text{GtQ}[d, 0])$

Rule 3312

$\text{Int}[(c + d \cdot x)^m \cdot \sin[e + f \cdot x]^n, x_{\text{Symbol}}] \rightarrow \text{Int}[\text{ExpandTrigReduce}[(c + d \cdot x)^m, \text{Sin}[e + f \cdot x]^n, x], x] /;$ $\text{FreeQ}\{c, d, e, f, m\}, x\} \ \&\& \ \text{IGtQ}[n, 1] \ \&\& \ (\text{!RationalQ}[m] \ || \ (\text{GeQ}[m, -1] \ \&\& \ \text{LtQ}[m, 1]))$

Rule 3306

$\text{Int}[\sin[e + f \cdot x] / \sqrt{c + d \cdot x}, x_{\text{Symbol}}] \rightarrow \text{Dist}[\text{Cos}[(d \cdot e - c \cdot f) / d], \text{Int}[\text{Sin}[c \cdot f / d + f \cdot x] / \sqrt{c + d \cdot x}, x], x] + \text{Dist}[\text{Sin}[(d \cdot e - c \cdot f) / d], \text{Int}[\text{Cos}[c \cdot f / d + f \cdot x] / \sqrt{c + d \cdot x}, x], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x\} \ \&\& \ \text{ComplexFreeQ}[f] \ \&\& \ \text{NeQ}[d \cdot e - c \cdot f, 0]$

Rule 3305

$\text{Int}[\sin[e + f \cdot x] / \sqrt{c + d \cdot x}, x_{\text{Symbol}}] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[f \cdot x^2 / d], x], x, \sqrt{c + d \cdot x}], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x\} \ \&\& \ \text{ComplexFreeQ}[f] \ \&\& \ \text{EqQ}[d \cdot e - c \cdot f, 0]$

Rule 3351

$\text{Int}[\text{Sin}[d \cdot (e + f \cdot x)^2], x_{\text{Symbol}}] \rightarrow \text{Simp}[(\sqrt{\text{Pi}/2} \cdot \text{FresnelS}[\sqrt{2/\text{Pi}} \cdot \text{Rt}[d, 2] \cdot (e + f \cdot x)]) / (f \cdot \text{Rt}[d, 2]), x] /;$ $\text{FreeQ}\{d, e, f\}, x\}$

Rule 3304

$\text{Int}[\sin[\text{Pi}/2 + e + f \cdot x] / \sqrt{c + d \cdot x}, x_{\text{Symbol}}] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Cos}[f \cdot x^2 / d], x], x, \sqrt{c + d \cdot x}], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x\} \ \&\& \ \text{ComplexFreeQ}[f] \ \&\& \ \text{EqQ}[d \cdot e - c \cdot f, 0]$

Rule 3352

$\text{Int}[\text{Cos}[d \cdot (e + f \cdot x)^2], x_{\text{Symbol}}] \rightarrow \text{Simp}[(\sqrt{\text{Pi}/2} \cdot \text{FresnelC}[\sqrt{2/\text{Pi}} \cdot \text{Rt}[d, 2] \cdot (e + f \cdot x)]) / (f \cdot \text{Rt}[d, 2]), x] /;$ $\text{FreeQ}\{d, e, f\}, x\}$

Rubi steps

$$\begin{aligned}
\int x(a + b \sin^{-1}(cx))^{5/2} dx &= \frac{1}{2}x^2(a + b \sin^{-1}(cx))^{5/2} - \frac{1}{4}(5bc) \int \frac{x^2(a + b \sin^{-1}(cx))^{3/2}}{\sqrt{1 - c^2x^2}} dx \\
&= \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} + \frac{1}{2}x^2(a + b \sin^{-1}(cx))^{5/2} - \frac{1}{16}(15b^2) \int x\sqrt{a + b \sin^{-1}(cx)} dx \\
&= -\frac{15}{32}b^2x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} - \frac{(a + b \sin^{-1}(cx))^{5/2}}{4c^2} + \dots \\
&= -\frac{15}{32}b^2x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} - \frac{(a + b \sin^{-1}(cx))^{5/2}}{4c^2} + \dots \\
&= -\frac{15}{32}b^2x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} - \frac{(a + b \sin^{-1}(cx))^{5/2}}{4c^2} + \dots \\
&= \frac{15b^2\sqrt{a + b \sin^{-1}(cx)}}{64c^2} - \frac{15}{32}b^2x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} - \dots \\
&= \frac{15b^2\sqrt{a + b \sin^{-1}(cx)}}{64c^2} - \frac{15}{32}b^2x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} - \dots \\
&= \frac{15b^2\sqrt{a + b \sin^{-1}(cx)}}{64c^2} - \frac{15}{32}b^2x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} - \dots \\
&= \frac{15b^2\sqrt{a + b \sin^{-1}(cx)}}{64c^2} - \frac{15}{32}b^2x^2\sqrt{a + b \sin^{-1}(cx)} + \frac{5bx\sqrt{1 - c^2x^2}(a + b \sin^{-1}(cx))^{3/2}}{8c} - \dots
\end{aligned}$$

Mathematica [C] time = 0.0945766, size = 141, normalized size = 0.65

$$\frac{e^{-\frac{2ia}{b}}(a + b \sin^{-1}(cx))^{5/2} \left(\sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{7}{2}, -\frac{2i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{4ia}{b}} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{7}{2}, \frac{2i(a+b \sin^{-1}(cx))}{b}\right) \right)}{32\sqrt{2}c^2 \left(\frac{(a+b \sin^{-1}(cx))^2}{b^2} \right)^{3/2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*(a + b*ArcSin[c*x])^(5/2), x]

[Out] ((a + b*ArcSin[c*x])^(5/2)*(Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[7/2, ((-2*I)*(a + b*ArcSin[c*x]))/b] + E^(((4*I)*a)/b)*Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[7/2, ((2*I)*(a + b*ArcSin[c*x]))/b]))/(32*Sqrt[2]*c^2*E^(((2*I)*a)/b)*((a + b*ArcSin[c*x])^2/b^2)^(3/2))

Maple [B] time = 0.068, size = 394, normalized size = 1.8

$$-\frac{1}{128c^2} \left(15\sqrt{b^{-1}}\sqrt{\pi}\sqrt{a + b \arcsin(cx)} \cos\left(2\frac{a}{b}\right) \text{FresnelC}\left(2\frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}}\sqrt{\pi}b}\right) b^3 + 15\sqrt{b^{-1}}\sqrt{\pi}\sqrt{a + b \arcsin(cx)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*(a+b*arcsin(c*x))^(5/2), x)

```
[Out] -1/128/c^2*(15*(1/b)^(1/2)*Pi^(1/2)*(a+b*arcsin(c*x))^(1/2)*cos(2*a/b)*FresnelC(2/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*b^3+15*(1/b)^(1/2)*Pi^(1/2)*(a+b*arcsin(c*x))^(1/2)*sin(2*a/b)*FresnelS(2/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*b^3+32*arcsin(c*x)^3*cos(2*(a+b*arcsin(c*x))/b-2*a/b)*b^3+96*arcsin(c*x)^2*cos(2*(a+b*arcsin(c*x))/b-2*a/b)*a*b^2-40*arcsin(c*x)^2*sin(2*(a+b*arcsin(c*x))/b-2*a/b)*b^3+96*arcsin(c*x)*cos(2*(a+b*arcsin(c*x))/b-2*a/b)*a^2*b-30*arcsin(c*x)*cos(2*(a+b*arcsin(c*x))/b-2*a/b)*b^3-80*arcsin(c*x)*sin(2*(a+b*arcsin(c*x))/b-2*a/b)*a*b^2+32*cos(2*(a+b*arcsin(c*x))/b-2*a/b)*a^3-30*cos(2*(a+b*arcsin(c*x))/b-2*a/b)*a*b^2-40*sin(2*(a+b*arcsin(c*x))/b-2*a/b)*a^2*b)/(a+b*arcsin(c*x))^(1/2)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (b \arcsin(cx) + a)^{\frac{5}{2}} x dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(a+b*arcsin(c*x))^(5/2),x, algorithm="maxima")
```

```
[Out] integrate((b*arcsin(c*x) + a)^(5/2)*x, x)
```

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(a+b*arcsin(c*x))^(5/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(a+b*asin(c*x))**(5/2),x)
```

```
[Out] Timed out
```

Giac [C] time = 2.79751, size = 1570, normalized size = 7.27

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*(a+b*arcsin(c*x))^(5/2),x, algorithm="giac")
```

```
[Out] 1/8*sqrt(pi)*a^2*b^(5/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/((b^2 + I*b^3/abs(b))*c^2) + 3/32*I*sqrt(pi)*a*b^(7/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/((b^2 + I*b^3/abs(b))*c^2) + 1/8*sqrt(pi)*a^2*b^(5/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/((b^2 - I*b^3/abs(b))*c^2) - 3/32*I*sqrt(pi)*a*b^(7/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/((b^2 - I*b^3/abs(b))*c^2) - 1/8*sqrt(b*arcsin(c*x) + a)*b^2*arcsin(c*x)^2*e^(2*I*arcsin(c*x))/c^2 - 1/8*sqrt(b*arcsin(c*x) + a)*b^2*arcsin(c*x)^2*e^(-2*I*arcsin(c*x))/c^2 - 1/16*sqrt(pi)*a^2*b^2*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/((b^(3/2) + I*b^(5/2)/abs(b))*c^2) - 1/16*sqrt(pi)*a^2*b^2*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/((b^(3/2) - I*b^(5/2)/abs(b))*c^2) - 1/16*sqrt(pi)*a^2*b^(3/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/((b + I*b^2/abs(b))*c^2) - 3/32*I*sqrt(pi)*a*b^(5/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/((b + I*b^2/abs(b))*c^2) + 15/256*sqrt(pi)*b^(7/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/((b + I*b^2/abs(b))*c^2) - 1/16*sqrt(pi)*a^2*b^(3/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/((b - I*b^2/abs(b))*c^2) + 3/32*I*sqrt(pi)*a*b^(5/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/((b - I*b^2/abs(b))*c^2) + 15/256*sqrt(pi)*b^(7/2)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/((b - I*b^2/abs(b))*c^2) - 1/4*sqrt(b*arcsin(c*x) + a)*a*b*arcsin(c*x)*e^(2*I*arcsin(c*x))/c^2 - 5/32*I*sqrt(b*arcsin(c*x) + a)*b^2*arcsin(c*x)*e^(2*I*arcsin(c*x))/c^2 - 1/4*sqrt(b*arcsin(c*x) + a)*a*b*arcsin(c*x)*e^(-2*I*arcsin(c*x))/c^2 + 5/32*I*sqrt(b*arcsin(c*x) + a)*b^2*arcsin(c*x)*e^(-2*I*arcsin(c*x))/c^2 - 1/8*sqrt(b*arcsin(c*x) + a)*a^2*e^(2*I*arcsin(c*x))/c^2 - 5/32*I*sqrt(b*arcsin(c*x) + a)*a*b*e^(2*I*arcsin(c*x))/c^2 + 15/128*sqrt(b*arcsin(c*x) + a)*b^2*e^(2*I*arcsin(c*x))/c^2 - 1/8*sqrt(b*arcsin(c*x) + a)*a^2*e^(-2*I*arcsin(c*x))/c^2 + 5/32*I*sqrt(b*arcsin(c*x) + a)*a*b*e^(-2*I*arcsin(c*x))/c^2 + 15/128*sqrt(b*arcsin(c*x) + a)*b^2*e^(-2*I*arcsin(c*x))/c^2
```

3.185 $\int (a + b \sin^{-1}(cx))^{5/2} dx$

Optimal. Leaf size=179

$$\frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\sin\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c} + \frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\cos\left(\frac{a}{b}\right)\text{S}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c} - \frac{15}{4}b^2x\sqrt{a+b\sin^{-1}(cx)} + \frac{5b^2}{4}\sqrt{a+b\sin^{-1}(cx)}$$

[Out] $(-15*b^2*x*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/4 + (5*b*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(3/2)})/(2*c) + x*(a + b*\text{ArcSin}[c*x])^{(5/2)} + (15*b^{(5/2)}*\text{Sqrt}[\text{Pi}/2]*\text{Cos}[a/b]*\text{FresnelS}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(4*c) - (15*b^{(5/2)}*\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(4*c)$

Rubi [A] time = 0.50197, antiderivative size = 179, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4619, 4677, 4723, 3306, 3305, 3351, 3304, 3352}

$$\frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\sin\left(\frac{a}{b}\right)\text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c} + \frac{15\sqrt{\frac{\pi}{2}}b^{5/2}\cos\left(\frac{a}{b}\right)\text{S}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b\sin^{-1}(cx)}}{\sqrt{b}}\right)}{4c} - \frac{15}{4}b^2x\sqrt{a+b\sin^{-1}(cx)} + \frac{5b^2}{4}\sqrt{a+b\sin^{-1}(cx)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*\text{ArcSin}[c*x])^{(5/2)}, x]$

[Out] $(-15*b^2*x*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/4 + (5*b*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(3/2)})/(2*c) + x*(a + b*\text{ArcSin}[c*x])^{(5/2)} + (15*b^{(5/2)}*\text{Sqrt}[\text{Pi}/2]*\text{Cos}[a/b]*\text{FresnelS}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(4*c) - (15*b^{(5/2)}*\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(4*c)$

Rule 4619

$\text{Int}[(a + \text{ArcSin}[c*x])^n, x] \rightarrow \text{Simp}[x*(a + b*\text{ArcSin}[c*x])^n, x] - \text{Dist}[b*c*n, \text{Int}[(x*(a + b*\text{ArcSin}[c*x])^{(n-1)})/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c}, x] && GtQ[n, 0]

Rule 4677

$\text{Int}[(a + \text{ArcSin}[c*x])^n*(d + e*x^2)^p, x] \rightarrow \text{Simp}[(d + e*x^2)^{p+1}*(a + b*\text{ArcSin}[c*x])^n/(2*e*(p+1)), x] + \text{Dist}[(b*n*d*\text{IntPart}[p]*(d + e*x^2)^{\text{FracPart}[p]}]/(2*c*(p+1)*(1 - c^2*x^2)^{\text{FracPart}[p]}), \text{Int}[(1 - c^2*x^2)^{p+1/2}*(a + b*\text{ArcSin}[c*x])^{(n-1)}, x], x] /;$ FreeQ[{a, b, c, d, e, p}, x] && EqQ[c^2*d + e, 0] && GtQ[n, 0] && NeQ[p, -1]

Rule 4723

$\text{Int}[(a + \text{ArcSin}[c*x])^n*(d + e*x^2)^m, x] \rightarrow \text{Dist}[d^p/c^{(m+1)}, \text{Subst}[\text{Int}[(a + b*x)^n*\text{Sin}[x]^m*\text{Cos}[x]^{(2*p+1)}, x], x, \text{ArcSin}[c*x]], x] /;$ FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && IntegerQ[2*p] && GtQ[p, -1] && IGtQ[m, 0] && (IntegerQ[p] || GtQ[d, 0])

Rule 3306

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos
[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d
*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d,
e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d
, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}
, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^(2)], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := D
ist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d
, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^(2)], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned}
\int (a + b \sin^{-1}(cx))^{5/2} dx &= x (a + b \sin^{-1}(cx))^{5/2} - \frac{1}{2}(5bc) \int \frac{x (a + b \sin^{-1}(cx))^{3/2}}{\sqrt{1 - c^2 x^2}} dx \\
&= \frac{5b\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{2c} + x (a + b \sin^{-1}(cx))^{5/2} - \frac{1}{4}(15b^2) \int \sqrt{a + b \sin^{-1}(cx)} dx \\
&= -\frac{15}{4}b^2 x \sqrt{a + b \sin^{-1}(cx)} + \frac{5b\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{2c} + x (a + b \sin^{-1}(cx))^{5/2} + \frac{1}{8}(15b^2) \int \sqrt{a + b \sin^{-1}(cx)} dx \\
&= -\frac{15}{4}b^2 x \sqrt{a + b \sin^{-1}(cx)} + \frac{5b\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{2c} + x (a + b \sin^{-1}(cx))^{5/2} + \frac{1}{8}(15b^2) \int \sqrt{a + b \sin^{-1}(cx)} dx \\
&= -\frac{15}{4}b^2 x \sqrt{a + b \sin^{-1}(cx)} + \frac{5b\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{2c} + x (a + b \sin^{-1}(cx))^{5/2} + \frac{1}{8}(15b^2) \int \sqrt{a + b \sin^{-1}(cx)} dx \\
&= -\frac{15}{4}b^2 x \sqrt{a + b \sin^{-1}(cx)} + \frac{5b\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{2c} + x (a + b \sin^{-1}(cx))^{5/2} + \frac{1}{8}(15b^2) \int \sqrt{a + b \sin^{-1}(cx)} dx \\
&= -\frac{15}{4}b^2 x \sqrt{a + b \sin^{-1}(cx)} + \frac{5b\sqrt{1 - c^2 x^2} (a + b \sin^{-1}(cx))^{3/2}}{2c} + x (a + b \sin^{-1}(cx))^{5/2} + \frac{15}{8}b^2 \sqrt{a + b \sin^{-1}(cx)}
\end{aligned}$$

Mathematica [C] time = 2.89902, size = 379, normalized size = 2.12

$$e^{-\frac{ia}{b}} \left(2b \left(2a^2 \sqrt{-\frac{i(a+b\sin^{-1}(cx))}{b}} \Gamma\left(\frac{3}{2}, -\frac{i(a+b\sin^{-1}(cx))}{b}\right) + 2a^2 e^{\frac{2ia}{b}} \sqrt{\frac{i(a+b\sin^{-1}(cx))}{b}} \Gamma\left(\frac{3}{2}, \frac{i(a+b\sin^{-1}(cx))}{b}\right) + e^{\frac{ia}{b}} (a + \dots \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[(a + b*ArcSin[c*x])^(5/2), x]

[Out] ((I*(4*a^2 + 15*b^2)*(-1 + E^(((2*I)*a)/b))*Sqrt[Pi/2]*Sqrt[a + b*ArcSin[c*x]]*FresnelC[Sqrt[b^(-1)]*Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]]])/Sqrt[b^(-1)] + ((4*a^2 + 15*b^2)*(1 + E^(((2*I)*a)/b))*Sqrt[Pi/2]*Sqrt[a + b*ArcSin[c*x]]*FresnelS[Sqrt[b^(-1)]*Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]]])/Sqrt[b^(-1)] + 2*b*(E^((I*a)/b)*(a + b*ArcSin[c*x])*(-15*b*c*x + 10*a*Sqrt[1 - c^2*x^2] + 2*(4*a*c*x + 5*b*Sqrt[1 - c^2*x^2])*ArcSin[c*x] + 4*b*c*x*ArcSin[c*x]^2 + 2*a^2*Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[3/2, ((-I)*(a + b*ArcSin[c*x]))/b] + 2*a^2*E^(((2*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[3/2, (I*(a + b*ArcSin[c*x]))/b]))/(8*c*E^((I*a)/b)*Sqrt[a + b*ArcSin[c*x]])

Maple [B] time = 0.067, size = 393, normalized size = 2.2

$$\frac{1}{8c} \left(15 \sqrt{b^{-1}} \sqrt{\pi} \sqrt{2} \sqrt{a + b \arcsin(cx)} \cos\left(\frac{a}{b}\right) \text{FresnelS}\left(\frac{\sqrt{2}\sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}}\sqrt{\pi}b}\right) b^3 - 15 \sqrt{b^{-1}} \sqrt{\pi} \sqrt{2} \sqrt{a + b \arcsin(cx)} \sin\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{2}\sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}}\sqrt{\pi}b}\right) b^3 + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(5/2), x)

[Out] 1/8/c/(a+b*arcsin(c*x))^(1/2)*(15*(1/b)^(1/2)*Pi^(1/2)*2^(1/2)*(a+b*arcsin(c*x))^(1/2)*cos(a/b)*FresnelS(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*b^3-15*(1/b)^(1/2)*Pi^(1/2)*2^(1/2)*(a+b*arcsin(c*x))^(1/2)*sin(a/b)*FresnelC(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*b^3+8*arcsin(c*x)^3*sin((a+b*arcsin(c*x))/b-a/b)*b^3+24*arcsin(c*x)^2*sin((a+b*arcsin(c*x))/b-a/b)*a*b^2+20*arcsin(c*x)^2*cos((a+b*arcsin(c*x))/b-a/b)*b^3+24*arcsin(c*x)*sin((a+b*arcsin(c*x))/b-a/b)*a^2*b-30*arcsin(c*x)*sin((a+b*arcsin(c*x))/b-a/b)*b^3+40*arcsin(c*x)*cos((a+b*arcsin(c*x))/b-a/b)*a*b^2+8*sin((a+b*arcsin(c*x))/b-a/b)*a^3-30*sin((a+b*arcsin(c*x))/b-a/b)*a*b^2+20*cos((a+b*arcsin(c*x))/b-a/b)*a^2*b

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (b \arcsin(cx) + a)^{\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2), x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(5/2), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**(5/2),x)

[Out] Timed out

Giac [C] time = 3.19333, size = 1578, normalized size = 8.82

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2),x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/2*I*\sqrt{2}*\sqrt{\pi}*a^2*b^3*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/ \\ & \sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(I*a/b)} / \\ & (((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c) + 3/4*\sqrt{2}*\sqrt{\pi}*a*b^4* \\ & \operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(I*a/b)} / ((I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{ \\ & \operatorname{abs}(b)})*c) + 1/2*I*\sqrt{2}*\sqrt{\pi}*a^2*b^3*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/ \\ & \sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(-I*a/b)} / \\ & ((-I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{\operatorname{abs}(b)})*c) + 3/4*\sqrt{2}*\sqrt{\pi}*a*b^4* \\ & \operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(-I*a/b)} / ((-I*b^3/\sqrt{\operatorname{abs}(b)} + b^2*\sqrt{ \\ & \operatorname{abs}(b)})*c) + 1/2*I*\sqrt{2}*\sqrt{\pi}*a^2*b^2*\operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/ \\ & \sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(I*a/b)} / \\ & (((I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c) - 15/16*I*\sqrt{2}*\sqrt{\pi}*b^4* \\ & \operatorname{erf}(-1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(I*a/b)} / ((I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{ \\ & \operatorname{abs}(b)})*c) - 1/2*I*\sqrt{2}*\sqrt{\pi}*a^2*b^2*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/ \\ & \sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(-I*a/b)} / \\ & ((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c) - 3/4*\sqrt{2}*\sqrt{\pi}*a*b^3* \\ & \operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/\sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{ \\ & b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(-I*a/b)} / ((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{ \\ & \operatorname{abs}(b)})*c) + 15/16*I*\sqrt{2}*\sqrt{\pi}*b^4*\operatorname{erf}(1/2*I*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a})/ \\ & \sqrt{\operatorname{abs}(b)} - 1/2*\sqrt{2}*\sqrt{b*\arcsin(c*x) + a}*\sqrt{\operatorname{abs}(b)}/b)*e^{(-I*a/b)} / \\ & ((-I*b^2/\sqrt{\operatorname{abs}(b)} + b*\sqrt{\operatorname{abs}(b)})*c) - 1/2*I* \end{aligned}$$

$$\begin{aligned}
& \sqrt{b \arcsin(cx) + a} b^2 \arcsin(cx)^2 e^{(I \arcsin(cx))} / c + 1/2 I \sqrt{b \arcsin(cx) + a} b^2 \arcsin(cx)^2 e^{(-I \arcsin(cx))} / c - I \sqrt{b \arcsin(cx) + a} a b \arcsin(cx) e^{(I \arcsin(cx))} / c + 5/4 \sqrt{b \arcsin(cx) + a} b^2 \arcsin(cx) e^{(I \arcsin(cx))} / c + I \sqrt{b \arcsin(cx) + a} a b \arcsin(cx) e^{(-I \arcsin(cx))} / c + 5/4 \sqrt{b \arcsin(cx) + a} b^2 \arcsin(cx) e^{(-I \arcsin(cx))} / c - 1/2 I \sqrt{b \arcsin(cx) + a} a^2 e^{(I \arcsin(cx))} / c + 5/4 \sqrt{b \arcsin(cx) + a} a b e^{(I \arcsin(cx))} / c + 15/8 I \sqrt{b \arcsin(cx) + a} b^2 e^{(I \arcsin(cx))} / c + 1/2 I \sqrt{b \arcsin(cx) + a} a^2 e^{(-I \arcsin(cx))} / c + 5/4 \sqrt{b \arcsin(cx) + a} a b e^{(-I \arcsin(cx))} / c - 15/8 I \sqrt{b \arcsin(cx) + a} b^2 e^{(-I \arcsin(cx))} / c
\end{aligned}$$

$$3.186 \quad \int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{(a+b \sin^{-1}(cx))^{5/2}}{x}, x \right)$$

[Out] Unintegrable[(a + b*ArcSin[c*x])^(5/2)/x, x]

Rubi [A] time = 0.0441739, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*ArcSin[c*x])^(5/2)/x,x]

[Out] Defer[Int] [(a + b*ArcSin[c*x])^(5/2)/x, x]

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x} dx = \int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x} dx$$

Mathematica [A] time = 3.05952, size = 0, normalized size = 0.

$$\int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*ArcSin[c*x])^(5/2)/x,x]

[Out] Integrate[(a + b*ArcSin[c*x])^(5/2)/x, x]

Maple [A] time = 0.101, size = 0, normalized size = 0.

$$\int \frac{1}{x} (a+b \arcsin(cx))^{\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(5/2)/x,x)

[Out] int((a+b*arcsin(c*x))^(5/2)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{5}{2}}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2)/x,x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(5/2)/x, x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2)/x,x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**(5/2)/x,x)

[Out] Timed out

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{5}{2}}}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2)/x,x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)^(5/2)/x, x)

$$3.187 \quad \int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x^2} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{(a+b \sin^{-1}(cx))^{5/2}}{x^2}, x \right)$$

[Out] Unintegrable[(a + b*ArcSin[c*x])^(5/2)/x^2, x]

Rubi [A] time = 0.0433305, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*ArcSin[c*x])^(5/2)/x^2, x]

[Out] Defer[Int][(a + b*ArcSin[c*x])^(5/2)/x^2, x]

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x^2} dx = \int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x^2} dx$$

Mathematica [A] time = 10.2156, size = 0, normalized size = 0.

$$\int \frac{(a+b \sin^{-1}(cx))^{5/2}}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*ArcSin[c*x])^(5/2)/x^2, x]

[Out] Integrate[(a + b*ArcSin[c*x])^(5/2)/x^2, x]

Maple [A] time = 0.161, size = 0, normalized size = 0.

$$\int \frac{1}{x^2} (a+b \arcsin(cx))^{\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^(5/2)/x^2, x)

[Out] int((a+b*arcsin(c*x))^(5/2)/x^2, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{5}{2}}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2)/x^2,x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(5/2)/x^2, x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2)/x^2,x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**(5/2)/x**2,x)

[Out] Timed out

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^{\frac{5}{2}}}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^(5/2)/x^2,x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)^(5/2)/x^2, x)

$$3.188 \quad \int \frac{x^2}{\sqrt{a+b \sin^{-1}(cx)}} dx$$

Optimal. Leaf size=223

$$\frac{\sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}} - \frac{\sqrt{\frac{\pi}{6}} \cos\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}} + \frac{\sqrt{\frac{\pi}{2}} \sin\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}}$$

```
[Out] (Sqrt[Pi/2]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]
)/(2*Sqrt[b]*c^3) - (Sqrt[Pi/6]*Cos[(3*a)/b]*FresnelC[(Sqrt[6/Pi]*Sqrt[a +
b*ArcSin[c*x]])/Sqrt[b]])/(2*Sqrt[b]*c^3) + (Sqrt[Pi/2]*FresnelS[(Sqrt[2/Pi
]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(2*Sqrt[b]*c^3) - (Sqrt[Pi/6]
*FresnelS[(Sqrt[6/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[(3*a)/b])/(2*Sq
rt[b]*c^3)
```

Rubi [A] time = 0.420864, antiderivative size = 223, normalized size of antiderivative = 1., number of steps used = 13, number of rules used = 7, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.438$, Rules used = {4635, 4406, 3306, 3305, 3351, 3304, 3352}

$$\frac{\sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}} - \frac{\sqrt{\frac{\pi}{6}} \cos\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}} + \frac{\sqrt{\frac{\pi}{2}} \sin\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}}$$

Antiderivative was successfully verified.

```
[In] Int[x^2/Sqrt[a + b*ArcSin[c*x]], x]
```

```
[Out] (Sqrt[Pi/2]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]
)/(2*Sqrt[b]*c^3) - (Sqrt[Pi/6]*Cos[(3*a)/b]*FresnelC[(Sqrt[6/Pi]*Sqrt[a +
b*ArcSin[c*x]])/Sqrt[b]])/(2*Sqrt[b]*c^3) + (Sqrt[Pi/2]*FresnelS[(Sqrt[2/Pi
]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(2*Sqrt[b]*c^3) - (Sqrt[Pi/6]
*FresnelS[(Sqrt[6/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[(3*a)/b])/(2*Sq
rt[b]*c^3)
```

Rule 4635

```
Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^(n_.)*(x_)^(m_.), x_Symbol] := Dist[1
/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x]
/; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x
]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 3306

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos
[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d
*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d,
e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]
```

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d
, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}
, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_)^2)], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := D
ist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d
, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_)^2)], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]]/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{x^2}{\sqrt{a + b \sin^{-1}(cx)}} dx &= \frac{\text{Subst} \left(\int \frac{\cos(x) \sin^2(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx) \right)}{c^3} \\ &= \frac{\text{Subst} \left(\int \left(\frac{\cos(x)}{4\sqrt{a+bx}} - \frac{\cos(3x)}{4\sqrt{a+bx}} \right) dx, x, \sin^{-1}(cx) \right)}{c^3} \\ &= \frac{\text{Subst} \left(\int \frac{\cos(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx) \right)}{4c^3} - \frac{\text{Subst} \left(\int \frac{\cos(3x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx) \right)}{4c^3} \\ &= \frac{\cos\left(\frac{a}{b}\right) \text{Subst} \left(\int \frac{\cos\left(\frac{a}{b}+x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx) \right)}{4c^3} - \frac{\cos\left(\frac{3a}{b}\right) \text{Subst} \left(\int \frac{\cos\left(\frac{3a}{b}+3x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx) \right)}{4c^3} + \dots \\ &= \frac{\cos\left(\frac{a}{b}\right) \text{Subst} \left(\int \cos\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)} \right)}{2bc^3} - \frac{\cos\left(\frac{3a}{b}\right) \text{Subst} \left(\int \cos\left(\frac{3x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)} \right)}{2bc^3} \\ &= \frac{\sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) C\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}} - \frac{\sqrt{\frac{\pi}{6}} \cos\left(\frac{3a}{b}\right) C\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}} + \frac{\sqrt{\frac{\pi}{2}} S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{2\sqrt{bc^3}} \end{aligned}$$

Mathematica [C] time = 0.266476, size = 228, normalized size = 1.02

$$\frac{i e^{-\frac{3ia}{b}} \left(3 e^{\frac{2ia}{b}} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{1}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) - 3 e^{\frac{4ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{1}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) + \sqrt{3} \left(e^{\frac{6ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \right) \right)}{24c^3 \sqrt{a + b \sin^{-1}(cx)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2/Sqrt[a + b*ArcSin[c*x]], x]

[Out] ((-I/24)*(3*E^(((2*I)*a)/b)*Sqrt[(-I)*(a + b*ArcSin[c*x])/b]*Gamma[1/2, (-I)*(a + b*ArcSin[c*x])/b] - 3*E^(((4*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x])

$$\frac{1}{b} \Gamma\left[\frac{1}{2}, \frac{(I(a + b \operatorname{ArcSin}[c*x]))}{b} + \sqrt{3} * (-\sqrt{((-I)*(a + b \operatorname{ArcSin}[c*x]))})}{b} \Gamma\left[\frac{1}{2}, \frac{((-3*I)*(a + b \operatorname{ArcSin}[c*x]))}{b}\right] + E^{((6*I)*a)/b} \sqrt{\frac{(I*(a + b \operatorname{ArcSin}[c*x]))}{b} \Gamma\left[\frac{1}{2}, \frac{((3*I)*(a + b \operatorname{ArcSin}[c*x]))}{b}\right]}\right]}{c^3 E^{((3*I)*a)/b} \sqrt{a + b \operatorname{ArcSin}[c*x]}}$$

Maple [A] time = 0.058, size = 168, normalized size = 0.8

$$\frac{\sqrt{2}\sqrt{\pi}}{12c^3} \sqrt{b^{-1}} \left(-\cos\left(3\frac{a}{b}\right) \operatorname{FresnelC}\left(\frac{\sqrt{2}\sqrt{3}}{\sqrt{\pi}b} \sqrt{a + b \arcsin(cx)} \frac{1}{\sqrt{b^{-1}}}\right) \sqrt{3} - \sin\left(3\frac{a}{b}\right) \operatorname{FresnelS}\left(\frac{\sqrt{2}\sqrt{3}}{\sqrt{\pi}b} \sqrt{a + b \arcsin(cx)}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a+b*arcsin(c*x))^(1/2),x)

[Out] 1/12/c^3*(1/b)^(1/2)*Pi^(1/2)*2^(1/2)*(-cos(3*a/b)*FresnelC(2^(1/2)/Pi^(1/2)*3^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*3^(1/2)-sin(3*a/b)*FresnelS(2^(1/2)/Pi^(1/2)*3^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*3^(1/2)+3*cos(a/b)*FresnelC(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)+3*sin(a/b)*FresnelS(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\sqrt{b \arcsin(cx) + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")

[Out] integrate(x^2/sqrt(b*arcsin(c*x) + a), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{\sqrt{a + b \arcsin(cx)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(a+b*asin(c*x))**(1/2),x)

[Out] Integral(x**2/sqrt(a + b*asin(c*x)), x)

Giac [C] time = 2.27106, size = 428, normalized size = 1.92

$$\frac{\sqrt{\pi} \operatorname{erf}\left(-\frac{\sqrt{6}\sqrt{b\arcsin(cx)+a}}{2\sqrt{b}} - \frac{i\sqrt{6}\sqrt{b\arcsin(cx)+a}\sqrt{b}}{2|b|}\right) e^{\left(\frac{3ia}{b}\right)}}{4\left(\sqrt{6}\sqrt{b} + \frac{i\sqrt{6}b^{\frac{3}{2}}}{|b|}\right) c^3} - \frac{\sqrt{\pi} \operatorname{erf}\left(-\frac{i\sqrt{2}\sqrt{b\arcsin(cx)+a}}{2\sqrt{|b|}} - \frac{\sqrt{2}\sqrt{b\arcsin(cx)+a}\sqrt{|b|}}{2b}\right) e^{\left(\frac{ia}{b}\right)}}{4c^3\left(\frac{i\sqrt{2}b}{\sqrt{|b|}} + \sqrt{2}\sqrt{|b|}\right)} - \sqrt{\pi} \operatorname{erf}\left(\frac{ia}{b}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^(1/2),x, algorithm="giac")

[Out] $\frac{1}{4}\sqrt{\pi}\operatorname{erf}\left(-\frac{1}{2}\sqrt{6}\sqrt{b\arcsin(c*x)+a}/\sqrt{b}\right) - \frac{1}{2}I\sqrt{6}\sqrt{b\arcsin(c*x)+a}\sqrt{b}/\operatorname{abs}(b) e^{(3Ia/b)/((\sqrt{6}\sqrt{b} + I\sqrt{6}b^{(3/2)}/\operatorname{abs}(b))c^3)} - \frac{1}{4}\sqrt{\pi}\operatorname{erf}\left(-\frac{1}{2}I\sqrt{2}\sqrt{b\arcsin(c*x)+a}/\sqrt{\operatorname{abs}(b)}\right) - \frac{1}{2}\sqrt{2}\sqrt{b\arcsin(c*x)+a}\sqrt{\operatorname{abs}(b)}/b e^{(Ia/b)/(c^3(I\sqrt{2}b/\sqrt{\operatorname{abs}(b)} + \sqrt{2}\sqrt{\operatorname{abs}(b)}))} - \frac{1}{4}\sqrt{\pi}\operatorname{erf}\left(\frac{1}{2}I\sqrt{2}\sqrt{b\arcsin(c*x)+a}/\sqrt{\operatorname{abs}(b)}\right) - \frac{1}{2}\sqrt{2}\sqrt{b\arcsin(c*x)+a}\sqrt{\operatorname{abs}(b)}/b e^{(-Ia/b)/(c^3(-I\sqrt{2}b/\sqrt{\operatorname{abs}(b)} + \sqrt{2}\sqrt{\operatorname{abs}(b)}))} + \frac{1}{4}\sqrt{\pi}\operatorname{erf}\left(-\frac{1}{2}\sqrt{6}\sqrt{b\arcsin(c*x)+a}/\sqrt{b}\right) + \frac{1}{2}I\sqrt{6}\sqrt{b\arcsin(c*x)+a}\sqrt{b}/\operatorname{abs}(b) e^{(-3Ia/b)/((\sqrt{6}\sqrt{b} - I\sqrt{6}b^{(3/2)}/\operatorname{abs}(b))c^3)}$

$$3.189 \quad \int \frac{x}{\sqrt{a+b \sin^{-1}(cx)}} dx$$

Optimal. Leaf size=99

$$\frac{\sqrt{\pi} \cos\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{2\sqrt{bc^2}} - \frac{\sqrt{\pi} \sin\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{2\sqrt{bc^2}}$$

[Out] (Sqrt[Pi]*Cos[(2*a)/b]*FresnelS[(2*Sqrt[a + b*ArcSin[c*x]])]/(Sqrt[b]*Sqrt[Pi]))/(2*Sqrt[b]*c^2) - (Sqrt[Pi]*FresnelC[(2*Sqrt[a + b*ArcSin[c*x]])]/(Sqrt[b]*Sqrt[Pi]))*Sin[(2*a)/b]/(2*Sqrt[b]*c^2)

Rubi [A] time = 0.17644, antiderivative size = 99, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 8, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.571$, Rules used = {4635, 4406, 12, 3306, 3305, 3351, 3304, 3352}

$$\frac{\sqrt{\pi} \cos\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{2\sqrt{bc^2}} - \frac{\sqrt{\pi} \sin\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{2\sqrt{bc^2}}$$

Antiderivative was successfully verified.

[In] Int[x/Sqrt[a + b*ArcSin[c*x]],x]

[Out] (Sqrt[Pi]*Cos[(2*a)/b]*FresnelS[(2*Sqrt[a + b*ArcSin[c*x]])]/(Sqrt[b]*Sqrt[Pi]))/(2*Sqrt[b]*c^2) - (Sqrt[Pi]*FresnelC[(2*Sqrt[a + b*ArcSin[c*x]])]/(Sqrt[b]*Sqrt[Pi]))*Sin[(2*a)/b]/(2*Sqrt[b]*c^2)

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d
, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}
, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := D
ist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d
, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{x}{\sqrt{a + b \sin^{-1}(cx)}} dx &= \frac{\text{Subst}\left(\int \frac{\cos(x) \sin(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{c^2} \\ &= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{2\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{c^2} \\ &= \frac{\text{Subst}\left(\int \frac{\sin(2x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2c^2} \\ &= \frac{\cos\left(\frac{2a}{b}\right) \text{Subst}\left(\int \frac{\sin\left(\frac{2a}{b}+2x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2c^2} - \frac{\sin\left(\frac{2a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{2a}{b}+2x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2c^2} \\ &= \frac{\cos\left(\frac{2a}{b}\right) \text{Subst}\left(\int \sin\left(\frac{2x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{bc^2} - \frac{\sin\left(\frac{2a}{b}\right) \text{Subst}\left(\int \cos\left(\frac{2x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{bc^2} \\ &= \frac{\sqrt{\pi} \cos\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{2\sqrt{bc^2}} - \frac{\sqrt{\pi} C\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right) \sin\left(\frac{2a}{b}\right)}{2\sqrt{bc^2}} \end{aligned}$$

Mathematica [C] time = 0.0610222, size = 123, normalized size = 1.24

$$\frac{e^{-\frac{2ia}{b}} \left(\sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{1}{2}, -\frac{2i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{4ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{1}{2}, \frac{2i(a+b \sin^{-1}(cx))}{b}\right) \right)}{4\sqrt{2}c^2 \sqrt{a + b \sin^{-1}(cx)}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[x/Sqrt[a + b*ArcSin[c*x]], x]
```

```
[Out] -(Sqrt[(-I)*(a + b*ArcSin[c*x])]/b)*Gamma[1/2, ((-2*I)*(a + b*ArcSin[c*x])
)/b] + E^(((4*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[1/2, ((2*I)*(a
+ b*ArcSin[c*x]))/b]/(4*Sqrt[2]*c^2*E^(((2*I)*a)/b)*Sqrt[a + b*ArcSin[c*x
```

]])

Maple [A] time = 0.038, size = 80, normalized size = 0.8

$$-\frac{\sqrt{\pi}}{2c^2}\sqrt{b^{-1}}\left(\sin\left(2\frac{a}{b}\right)\text{FresnelC}\left(2\frac{\sqrt{a+b\arcsin(cx)}}{\sqrt{\pi}\sqrt{b^{-1}b}}\right)-\cos\left(2\frac{a}{b}\right)\text{FresnelS}\left(2\frac{\sqrt{a+b\arcsin(cx)}}{\sqrt{\pi}\sqrt{b^{-1}b}}\right)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x/(a+b*arcsin(c*x))^(1/2),x)

[Out] $-1/2*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(\sin(2*a/b)*\text{FresnelC}(2/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)-\cos(2*a/b)*\text{FresnelS}(2/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b))/c^2$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\sqrt{b \arcsin(cx) + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")

[Out] integrate(x/sqrt(b*arcsin(c*x) + a), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{\sqrt{a + b \arcsin(cx)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*asin(c*x))**(1/2),x)

[Out] Integral(x/sqrt(a + b*asin(c*x)), x)

Giac [C] time = 1.99215, size = 178, normalized size = 1.8

$$\frac{i\sqrt{\pi} \operatorname{erf}\left(-\frac{\sqrt{b}\arcsin(cx)+a}{\sqrt{b}} + \frac{i\sqrt{b}\arcsin(cx)+a\sqrt{b}}{|b|}\right) e^{\left(-\frac{2ia}{b}\right)}}{4c^2\left(\sqrt{b} - \frac{ib^{\frac{3}{2}}}{|b|}\right)} - \frac{i\sqrt{\pi} \operatorname{erf}\left(-\frac{\sqrt{b}\arcsin(cx)+a}{\sqrt{b}} - \frac{i\sqrt{b}\arcsin(cx)+a\sqrt{b}}{|b|}\right) e^{\left(\frac{2ia}{b}\right)}}{4\sqrt{b}c^2\left(\frac{ib}{|b|} + 1\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x/(a+b*arcsin(c*x))^(1/2),x, algorithm="giac")

[Out] 1/4*I*sqrt(pi)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) + I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(-2*I*a/b)/(c^2*(sqrt(b) - I*b^(3/2)/abs(b))) - 1/4*I*sqrt(pi)*erf(-sqrt(b*arcsin(c*x) + a)/sqrt(b) - I*sqrt(b*arcsin(c*x) + a)*sqrt(b)/abs(b))*e^(2*I*a/b)/(sqrt(b)*c^2*(I*b/abs(b) + 1))

$$3.190 \quad \int \frac{1}{\sqrt{a+b \sin^{-1}(cx)}} dx$$

Optimal. Leaf size=101

$$\frac{\sqrt{2\pi} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{\sqrt{bc}} + \frac{\sqrt{2\pi} \sin\left(\frac{a}{b}\right) \text{S}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{\sqrt{bc}}$$

[Out] (Sqrt[2*Pi]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(Sqrt[b]*c) + (Sqrt[2*Pi]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(Sqrt[b]*c)

Rubi [A] time = 0.0909293, antiderivative size = 101, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {4623, 3306, 3305, 3351, 3304, 3352}

$$\frac{\sqrt{2\pi} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{\sqrt{bc}} + \frac{\sqrt{2\pi} \sin\left(\frac{a}{b}\right) \text{S}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{\sqrt{bc}}$$

Antiderivative was successfully verified.

[In] Int[1/Sqrt[a + b*ArcSin[c*x]],x]

[Out] (Sqrt[2*Pi]*Cos[a/b]*FresnelC[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]])/(Sqrt[b]*c) + (Sqrt[2*Pi]*FresnelS[(Sqrt[2/Pi]*Sqrt[a + b*ArcSin[c*x]])/Sqrt[b]]*Sin[a/b])/(Sqrt[b]*c)

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.)^ (n_), x_Symbol] :> Dist[1/(b*c), Subst[Int[x^n * Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] :> Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := D
ist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d
, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^(2)], x_Symbol] := Simp[(Sqrt[Pi/2]*Fresne
lC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)]/(f*Rt[d, 2])), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\int \frac{1}{\sqrt{a + b \sin^{-1}(cx)}} dx = \frac{\text{Subst}\left(\int \frac{\cos\left(\frac{a-x}{b}\right)}{\sqrt{x}} dx, x, a + b \sin^{-1}(cx)\right)}{bc}$$

$$= \frac{\cos\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\cos\left(\frac{x}{b}\right)}{\sqrt{x}} dx, x, a + b \sin^{-1}(cx)\right)}{bc} + \frac{\sin\left(\frac{a}{b}\right) \text{Subst}\left(\int \frac{\sin\left(\frac{x}{b}\right)}{\sqrt{x}} dx, x, a + b \sin^{-1}(cx)\right)}{bc}$$

$$= \frac{(2 \cos\left(\frac{a}{b}\right)) \text{Subst}\left(\int \cos\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{bc} + \frac{(2 \sin\left(\frac{a}{b}\right)) \text{Subst}\left(\int \sin\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{bc}$$

$$= \frac{\sqrt{2\pi} \cos\left(\frac{a}{b}\right) C\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a + b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{\sqrt{bc}} + \frac{\sqrt{2\pi} S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a + b \sin^{-1}(cx)}}{\sqrt{b}}\right) \sin\left(\frac{a}{b}\right)}{\sqrt{bc}}$$

Mathematica [C] time = 0.0873759, size = 121, normalized size = 1.2

$$\frac{ie^{-\frac{ia}{b}} \left(e^{\frac{2ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{1}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) - \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{1}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) \right)}{2c\sqrt{a + b \sin^{-1}(cx)}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[1/Sqrt[a + b*ArcSin[c*x]],x]
```

```
[Out] ((I/2)*(-(Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[1/2, ((-I)*(a + b*ArcSin
[c*x]))/b]) + E^(((2*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[1/2, (I
*(a + b*ArcSin[c*x]))/b]))/(c*E^((I*a)/b)*Sqrt[a + b*ArcSin[c*x]])
```

Maple [A] time = 0.029, size = 83, normalized size = 0.8

$$\frac{\sqrt{2}\sqrt{\pi}}{c} \sqrt{b^{-1}} \left(\cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{2}}{\sqrt{\pi b}} \sqrt{a + b \arcsin(cx)} \frac{1}{\sqrt{b^{-1}}}\right) + \sin\left(\frac{a}{b}\right) \text{FresnelS}\left(\frac{\sqrt{2}}{\sqrt{\pi b}} \sqrt{a + b \arcsin(cx)} \frac{1}{\sqrt{b^{-1}}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(1/(a+b*arcsin(c*x))^(1/2),x)
```

```
[Out] 2^(1/2)*Pi^(1/2)*(1/b)^(1/2)*(cos(a/b)*FresnelC(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)
)*(a+b*arcsin(c*x))^(1/2)/b)+sin(a/b)*FresnelS(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)
```


$*(a+b*\arcsin(c*x))^{(1/2)/b})/c$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{b \arcsin(cx) + a}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")

[Out] integrate(1/sqrt(b*arcsin(c*x) + a), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{a + b \arcsin(cx)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*asin(c*x))**(1/2),x)

[Out] Integral(1/sqrt(a + b*asin(c*x)), x)

Giac [C] time = 1.9122, size = 215, normalized size = 2.13

$$\frac{\sqrt{\pi} \operatorname{erf}\left(-\frac{i\sqrt{2}\sqrt{b \arcsin(cx)+a}}{2\sqrt{|b|}} - \frac{\sqrt{2}\sqrt{b \arcsin(cx)+a}\sqrt{|b|}}{2b}\right) e^{\left(\frac{ia}{b}\right)}}{c\left(\frac{i\sqrt{2}b}{\sqrt{|b|}} + \sqrt{2}\sqrt{|b|}\right)} - \frac{\sqrt{\pi} \operatorname{erf}\left(\frac{i\sqrt{2}\sqrt{b \arcsin(cx)+a}}{2\sqrt{|b|}} - \frac{\sqrt{2}\sqrt{b \arcsin(cx)+a}\sqrt{|b|}}{2b}\right) e^{\left(-\frac{ia}{b}\right)}}{c\left(-\frac{i\sqrt{2}b}{\sqrt{|b|}} + \sqrt{2}\sqrt{|b|}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^(1/2),x, algorithm="giac")

[Out] -sqrt(pi)*erf(-1/2*I*sqrt(2)*sqrt(b*arcsin(c*x) + a)/sqrt(abs(b)) - 1/2*sqrt(2)*sqrt(b*arcsin(c*x) + a)*sqrt(abs(b))/b)*e^(I*a/b)/(c*(I*sqrt(2)*b/sqrt(abs(b)) + sqrt(2)*sqrt(abs(b)))) - sqrt(pi)*erf(1/2*I*sqrt(2)*sqrt(b*arcsin(c*x) + a)/sqrt(abs(b)) - 1/2*sqrt(2)*sqrt(b*arcsin(c*x) + a)*sqrt(abs(b))/b)*e^(-I*a/b)/(c*(-I*sqrt(2)*b/sqrt(abs(b)) + sqrt(2)*sqrt(abs(b))))

$$3.191 \quad \int \frac{1}{x\sqrt{a+b\sin^{-1}(cx)}} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable}\left(\frac{1}{x\sqrt{a+b\sin^{-1}(cx)}}, x\right)$$

[Out] Unintegrable[1/(x*Sqrt[a + b*ArcSin[c*x]]), x]

Rubi [A] time = 0.0373151, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0$., Rules used = {}

$$\int \frac{1}{x\sqrt{a+b\sin^{-1}(cx)}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*Sqrt[a + b*ArcSin[c*x]]), x]

[Out] Defer[Int][1/(x*Sqrt[a + b*ArcSin[c*x]]), x]

Rubi steps

$$\int \frac{1}{x\sqrt{a+b\sin^{-1}(cx)}} dx = \int \frac{1}{x\sqrt{a+b\sin^{-1}(cx)}} dx$$

Mathematica [A] time = 2.86607, size = 0, normalized size = 0.

$$\int \frac{1}{x\sqrt{a+b\sin^{-1}(cx)}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*Sqrt[a + b*ArcSin[c*x]]), x]

[Out] Integrate[1/(x*Sqrt[a + b*ArcSin[c*x]]), x]

Maple [A] time = 0.082, size = 0, normalized size = 0.

$$\int \frac{1}{x\sqrt{a+b\arcsin(cx)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(a+b*arcsin(c*x))^(1/2), x)

[Out] `int(1/x/(a+b*arcsin(c*x))^(1/2),x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{b \arcsin(cx) + ax}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")`

[Out] `integrate(1/(sqrt(b*arcsin(c*x) + a)*x), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x\sqrt{a + b \arcsin(cx)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*asin(c*x))**(1/2),x)`

[Out] `Integral(1/(x*sqrt(a + b*asin(c*x))), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{b \arcsin(cx) + ax}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(1/2),x, algorithm="giac")`

[Out] `integrate(1/(sqrt(b*arcsin(c*x) + a)*x), x)`

$$3.192 \quad \int \frac{1}{x^2 \sqrt{a+b \sin^{-1}(cx)}} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{1}{x^2 \sqrt{a+b \sin^{-1}(cx)}}, x \right)$$

[Out] Unintegrable[1/(x^2*Sqrt[a + b*ArcSin[c*x]]), x]

Rubi [A] time = 0.0368645, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0$., Rules used = {}

$$\int \frac{1}{x^2 \sqrt{a+b \sin^{-1}(cx)}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*Sqrt[a + b*ArcSin[c*x]]),x]

[Out] Defer[Int][1/(x^2*Sqrt[a + b*ArcSin[c*x]]), x]

Rubi steps

$$\int \frac{1}{x^2 \sqrt{a+b \sin^{-1}(cx)}} dx = \int \frac{1}{x^2 \sqrt{a+b \sin^{-1}(cx)}} dx$$

Mathematica [A] time = 11.6302, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sqrt{a+b \sin^{-1}(cx)}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*Sqrt[a + b*ArcSin[c*x]]),x]

[Out] Integrate[1/(x^2*Sqrt[a + b*ArcSin[c*x]]), x]

Maple [A] time = 0.137, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sqrt{a+b \arcsin(cx)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(a+b*arcsin(c*x))^(1/2),x)

[Out] `int(1/x^2/(a+b*arcsin(c*x))^(1/2),x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{b \arcsin(cx) + ax^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(1/2),x, algorithm="maxima")`

[Out] `integrate(1/(sqrt(b*arcsin(c*x) + a)*x^2), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(1/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 \sqrt{a + b \arcsin(cx)}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(a+b*asin(c*x))**(1/2),x)`

[Out] `Integral(1/(x**2*sqrt(a + b*asin(c*x))), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{b \arcsin(cx) + ax^2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(1/2),x, algorithm="giac")`

[Out] `integrate(1/(sqrt(b*arcsin(c*x) + a)*x^2), x)`

$$3.193 \quad \int \frac{x^2}{(a+b \sin^{-1}(cx))^{3/2}} dx$$

Optimal. Leaf size=250

$$\frac{\sqrt{\frac{\pi}{2}} \sin\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3} - \frac{\sqrt{\frac{3\pi}{2}} \sin\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3} - \frac{\sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3}$$

[Out] $(-2*x^2*\text{Sqrt}[1 - c^2*x^2])/(b*c*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) - (\text{Sqrt}[\text{Pi}/2]*\text{Cos}[a/b]*\text{FresnelS}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(b^{3/2}*c^3) + (\text{Sqrt}[(3*\text{Pi})/2]*\text{Cos}[(3*a)/b]*\text{FresnelS}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(b^{3/2}*c^3) + (\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(b^{3/2}*c^3) - (\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelC}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[(3*a)/b])/(b^{3/2}*c^3)$

Rubi [A] time = 0.418084, antiderivative size = 250, normalized size of antiderivative = 1., number of steps used = 12, number of rules used = 6, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {4631, 3306, 3305, 3351, 3304, 3352}

$$\frac{\sqrt{\frac{\pi}{2}} \sin\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3} - \frac{\sqrt{\frac{3\pi}{2}} \sin\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3} - \frac{\sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2/(a + b*\text{ArcSin}[c*x])^{3/2}, x]$

[Out] $(-2*x^2*\text{Sqrt}[1 - c^2*x^2])/(b*c*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) - (\text{Sqrt}[\text{Pi}/2]*\text{Cos}[a/b]*\text{FresnelS}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(b^{3/2}*c^3) + (\text{Sqrt}[(3*\text{Pi})/2]*\text{Cos}[(3*a)/b]*\text{FresnelS}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(b^{3/2}*c^3) + (\text{Sqrt}[\text{Pi}/2]*\text{FresnelC}[(\text{Sqrt}[2/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(b^{3/2}*c^3) - (\text{Sqrt}[(3*\text{Pi})/2]*\text{FresnelC}[(\text{Sqrt}[6/\text{Pi}]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[(3*a)/b])/(b^{3/2}*c^3)$

Rule 4631

$\text{Int}[(a + \text{ArcSin}(c*x))^{n+1} * (b*x)^m, x_Symbol] \rightarrow \text{Simp}[x^m * \text{Sqrt}[1 - c^2*x^2] * (a + b*\text{ArcSin}[c*x])^{n+1} / (b*c*(n+1)), x] - \text{Dist}[1/(b*c^{m+1}*(n+1)), \text{Subst}[\text{Int}[\text{ExpandTrigReduce}[(a + b*x)^{n+1}, \text{Sin}[x]^{m-1}*(m - (m+1)*\text{Sin}[x]^2), x], x], x, \text{ArcSin}[c*x]], x] /;$ $\text{FreeQ}\{a, b, c\}, x \ \&\& \ \text{IGtQ}[m, 0] \ \&\& \ \text{GeQ}[n, -2] \ \&\& \ \text{LtQ}[n, -1]$

Rule 3306

$\text{Int}[\sin(e + f*x)/\text{Sqrt}(c + d*x), x_Symbol] \rightarrow \text{Dist}[\text{Cos}[(d*e - c*f)/d], \text{Int}[\text{Sin}(c*f/d + f*x)/\text{Sqrt}(c + d*x), x], x] + \text{Dist}[\text{Sin}[(d*e - c*f)/d], \text{Int}[\text{Cos}(c*f/d + f*x)/\text{Sqrt}(c + d*x), x], x] /;$ $\text{FreeQ}\{c, d, e, f\}, x \ \&\& \ \text{ComplexFreeQ}[f] \ \&\& \ \text{NeQ}[d*e - c*f, 0]$

Rule 3305

$\text{Int}[\sin(e + f*x)/\text{Sqrt}(c + d*x), x_Symbol] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}(f*x^2)/d], x], x, \text{Sqrt}(c + d*x)] /;$ $\text{FreeQ}\{c, d, e, f\}$

, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))²], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x²)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))²], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int \frac{x^2}{(a + b \sin^{-1}(cx))^{3/2}} dx &= -\frac{2x^2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} + \frac{2 \operatorname{Subst}\left(\int \left(-\frac{\sin(x)}{4\sqrt{a+bx}} + \frac{3\sin(3x)}{4\sqrt{a+bx}}\right) dx, x, \sin^{-1}(cx)\right)}{bc^3} \\ &= -\frac{2x^2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{\operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2bc^3} + \frac{3 \operatorname{Subst}\left(\int \frac{\sin(3x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2bc^3} \\ &= -\frac{2x^2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Subst}\left(\int \frac{\sin\left(\frac{a}{b}+x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2bc^3} + \frac{\left(3 \cos\left(\frac{3a}{b}\right)\right) \operatorname{Subst}\left(\int \frac{\sin(3x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{2bc^3} \\ &= -\frac{2x^2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{\cos\left(\frac{a}{b}\right) \operatorname{Subst}\left(\int \sin\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{b^2c^3} + \frac{\left(3 \cos\left(\frac{3a}{b}\right)\right) \operatorname{Subst}\left(\int \sin\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{b^2c^3} \\ &= -\frac{2x^2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{\sqrt{\frac{\pi}{2}} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3} + \frac{\sqrt{\frac{3\pi}{2}} \cos\left(\frac{3a}{b}\right) S\left(\frac{\sqrt{\frac{6}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c^3} \end{aligned}$$

Mathematica [C] time = 0.443021, size = 343, normalized size = 1.37

$$e^{-\frac{3i(a+b \sin^{-1}(cx))}{b}} \left(e^{\frac{2ia}{b}+3i \sin^{-1}(cx)} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{1}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{4ia}{b}+3i \sin^{-1}(cx)} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{1}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) \right)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x²/(a + b*ArcSin[c*x])^(3/2), x]

[Out] (E^{((3*I)*a)/b} - E^{((3*I)*a)/b + (2*I)*ArcSin[c*x]) - E^{((3*I)*a)/b + (4*I)*ArcSin[c*x]) + E^{((3*I)*(a + 2*b*ArcSin[c*x]))/b} + E^{((2*I)*a)/b + (3*I)*ArcSin[c*x])*Sqrt[(-I)*(a + b*ArcSin[c*x])/b]*Gamma[1/2, (-I)*(a + b*ArcSin[c*x])/b] + E^{((4*I)*a)/b + (3*I)*ArcSin[c*x])*Sqrt[(I*(a + b*ArcSin[c*x]))/b]}}}}

$c\sin[cx])/b]*\text{Gamma}[1/2, (I*(a + b*\text{ArcSin}[cx]))/b] - \text{Sqrt}[3]*E^{((3*I)*\text{ArcSin}[cx])}*\text{Sqrt}[((-I)*(a + b*\text{ArcSin}[cx]))/b]*\text{Gamma}[1/2, ((-3*I)*(a + b*\text{ArcSin}[cx]))/b] - \text{Sqrt}[3]*E^{((3*I)*((2*a)/b + \text{ArcSin}[cx]))}*\text{Sqrt}[(I*(a + b*\text{ArcSin}[cx]))/b]*\text{Gamma}[1/2, ((3*I)*(a + b*\text{ArcSin}[cx]))/b]/(4*b*c^3*E^{((3*I)*(a + b*\text{ArcSin}[cx]))/b})*\text{Sqrt}[a + b*\text{ArcSin}[cx]]]$

Maple [A] time = 0.066, size = 295, normalized size = 1.2

$$-\frac{1}{2bc^3} \left(-\sqrt{3}\sqrt{b^{-1}}\sqrt{\pi}\sqrt{2}\sqrt{a + b \arcsin(cx)} \cos\left(3\frac{a}{b}\right) \text{FresnelS}\left(\frac{\sqrt{2}\sqrt{3}}{\sqrt{\pi}b}\sqrt{a + b \arcsin(cx)}\frac{1}{\sqrt{b^{-1}}}\right) + \sqrt{3}\sqrt{b^{-1}}\sqrt{\pi}\sqrt{2}\sqrt{a + b \arcsin(cx)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2/(a+b*arcsin(c*x))^(3/2),x)

[Out] $-1/2/c^3/b/(a+b*\arcsin(cx))^{1/2}*(-3^{1/2}*(1/b)^{1/2}*\text{Pi}^{1/2}*2^{1/2}*(a+b*\arcsin(cx))^{1/2}*\cos(3*a/b)*\text{FresnelS}(2^{1/2}/\text{Pi}^{1/2}*3^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)+3^{1/2}*(1/b)^{1/2}*\text{Pi}^{1/2}*2^{1/2}*(a+b*\arcsin(cx))^{1/2}*\sin(3*a/b)*\text{FresnelC}(2^{1/2}/\text{Pi}^{1/2}*3^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)+(1/b)^{1/2}*\text{Pi}^{1/2}*2^{1/2}*(a+b*\arcsin(cx))^{1/2}*\cos(a/b)*\text{FresnelS}(2^{1/2}/\text{Pi}^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)-(1/b)^{1/2}*\text{Pi}^{1/2}*2^{1/2}*(a+b*\arcsin(cx))^{1/2}*\sin(a/b)*\text{FresnelC}(2^{1/2}/\text{Pi}^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)+\cos((a+b*\arcsin(cx))/b-a/b)-\cos(3*(a+b*\arcsin(cx))/b-3*a/b)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(b \arcsin(cx) + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^(3/2),x, algorithm="maxima")

[Out] integrate(x^2/(b*arcsin(c*x) + a)^(3/2), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(a + b \arcsin(cx))^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(a+b*asin(c*x))**(3/2), x)

[Out] Integral(x**2/(a + b*asin(c*x))**(3/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(b \arcsin(cx) + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^(3/2), x, algorithm="giac")

[Out] integrate(x^2/(b*arcsin(c*x) + a)^(3/2), x)

$$3.194 \quad \int \frac{x}{(a+b \sin^{-1}(cx))^{3/2}} dx$$

Optimal. Leaf size=130

$$\frac{2\sqrt{\pi} \cos\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{b^{3/2}c^2} + \frac{2\sqrt{\pi} \sin\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{b^{3/2}c^2} - \frac{2x\sqrt{1-c^2x^2}}{bc\sqrt{a+b \sin^{-1}(cx)}}$$

[Out] $(-2*x*\text{Sqrt}[1 - c^2*x^2])/(b*c*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) + (2*\text{Sqrt}[\text{Pi}]*\text{Cos}[(2*a)/b]*\text{FresnelC}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}]))/(b^{(3/2)}*c^2) + (2*\text{Sqrt}[\text{Pi}]*\text{FresnelS}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}])]*\text{Sin}[(2*a)/b])/(b^{(3/2)}*c^2)$

Rubi [A] time = 0.162871, antiderivative size = 130, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.429$, Rules used = {4631, 3306, 3305, 3351, 3304, 3352}

$$\frac{2\sqrt{\pi} \cos\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{b^{3/2}c^2} + \frac{2\sqrt{\pi} \sin\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{b^{3/2}c^2} - \frac{2x\sqrt{1-c^2x^2}}{bc\sqrt{a+b \sin^{-1}(cx)}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x/(a + b*\text{ArcSin}[c*x])^{(3/2)}, x]$

[Out] $(-2*x*\text{Sqrt}[1 - c^2*x^2])/(b*c*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) + (2*\text{Sqrt}[\text{Pi}]*\text{Cos}[(2*a)/b]*\text{FresnelC}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}]))/(b^{(3/2)}*c^2) + (2*\text{Sqrt}[\text{Pi}]*\text{FresnelS}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}])]*\text{Sin}[(2*a)/b])/(b^{(3/2)}*c^2)$

Rule 4631

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + x)^n*(x)^m, x_Symbol] \rightarrow \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{n+1})/(b*c*(n+1)), x] - \text{Dist}[1/(b*c^{m+1}*(n+1)), \text{Subst}[\text{Int}[\text{ExpandTrigReduce}[(a + b*x)^{n+1}, \text{Sin}[x]^{m-1}*(m - (m+1)*\text{Sin}[x]^2), x], x], x, \text{ArcSin}[c*x]], x] /; \text{FreeQ}\{a, b, c\}, x \&\& \text{IGtQ}[m, 0] \&\& \text{GeQ}[n, -2] \&\& \text{LtQ}[n, -1]$

Rule 3306

$\text{Int}[\sin[(e + f*x)]/\text{Sqrt}[c + d*x], x_Symbol] \rightarrow \text{Dist}[\text{Cos}[(d*e - c*f)/d], \text{Int}[\text{Sin}[(c*f)/d + f*x]/\text{Sqrt}[c + d*x], x], x] + \text{Dist}[\text{Sin}[(d*e - c*f)/d], \text{Int}[\text{Cos}[(c*f)/d + f*x]/\text{Sqrt}[c + d*x], x], x] /; \text{FreeQ}\{c, d, e, f\}, x \&\& \text{ComplexFreeQ}[f] \&\& \text{NeQ}[d*e - c*f, 0]$

Rule 3305

$\text{Int}[\sin[(e + f*x)]/\text{Sqrt}[c + d*x], x_Symbol] \rightarrow \text{Dist}[2/d, \text{Subst}[\text{Int}[\text{Sin}[f*x^2]/d], x], x, \text{Sqrt}[c + d*x], x] /; \text{FreeQ}\{c, d, e, f\}, x \&\& \text{ComplexFreeQ}[f] \&\& \text{EqQ}[d*e - c*f, 0]$

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))²], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x²)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))²], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned} \int \frac{x}{(a + b \sin^{-1}(cx))^{3/2}} dx &= -\frac{2x\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} + \frac{2 \operatorname{Subst}\left(\int \frac{\cos(2x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{bc^2} \\ &= -\frac{2x\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} + \frac{\left(2 \cos\left(\frac{2a}{b}\right)\right) \operatorname{Subst}\left(\int \frac{\cos\left(\frac{2a}{b}+2x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{bc^2} + \frac{\left(2 \sin\left(\frac{2a}{b}\right)\right)}{bc^2} \\ &= -\frac{2x\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} + \frac{\left(4 \cos\left(\frac{2a}{b}\right)\right) \operatorname{Subst}\left(\int \cos\left(\frac{2x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{b^2c^2} + \frac{\left(4 \sin\left(\frac{2a}{b}\right)\right)}{b^2c^2} \\ &= -\frac{2x\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} + \frac{2\sqrt{\pi} \cos\left(\frac{2a}{b}\right) C\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{b^{3/2}c^2} + \frac{2\sqrt{\pi} S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right) \sin\left(\frac{2a}{b}\right)}{b^{3/2}c^2} \end{aligned}$$

Mathematica [C] time = 0.145312, size = 155, normalized size = 1.19

$$\frac{ie^{-\frac{2ia}{b}} \left(-\sqrt{2} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{1}{2}, -\frac{2i(a+b \sin^{-1}(cx))}{b}\right) + \sqrt{2} e^{\frac{4ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{1}{2}, \frac{2i(a+b \sin^{-1}(cx))}{b}\right) + 2ie^{\frac{2ia}{b}} \right)}{2bc^2 \sqrt{a + b \sin^{-1}(cx)}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x/(a + b*ArcSin[c*x])^(3/2), x]

[Out] ((I/2)*(-(Sqrt[2]*Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[1/2, ((-2*I)*(a + b*ArcSin[c*x]))/b]) + Sqrt[2]*E^(((4*I)*a)/b)*Sqrt[(I*(a + b*ArcSin[c*x]))/b]*Gamma[1/2, ((2*I)*(a + b*ArcSin[c*x]))/b] + (2*I)*E^(((2*I)*a)/b)*Sin[2*ArcSin[c*x]])/(b*c^2*E^(((2*I)*a)/b)*Sqrt[a + b*ArcSin[c*x]])

Maple [A] time = 0.045, size = 143, normalized size = 1.1

$$-\frac{1}{bc^2} \left(-2\sqrt{b^{-1}\sqrt{\pi}\sqrt{a + b \arcsin(cx)}} \cos\left(2\frac{a}{b}\right) \operatorname{FresnelC}\left(2\frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}\sqrt{\pi}b}}\right) - 2\sqrt{b^{-1}\sqrt{\pi}\sqrt{a + b \arcsin(cx)}} \sin\left(2\frac{a}{b}\right) \operatorname{FresnelS}\left(2\frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{b^{-1}\sqrt{\pi}b}}\right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a+b*arcsin(c*x))^(3/2),x)`

[Out] $-1/c^2/b/(a+b*\arcsin(c*x))^{1/2}*(-2*(1/b)^{1/2}*Pi^{1/2}*(a+b*\arcsin(c*x))^{1/2}*\cos(2*a/b)*FresnelC(2/Pi^{1/2})/(1/b)^{1/2}*(a+b*\arcsin(c*x))^{1/2}/b)-2*(1/b)^{1/2}*Pi^{1/2}*(a+b*\arcsin(c*x))^{1/2}*\sin(2*a/b)*FresnelS(2/Pi^{1/2})/(1/b)^{1/2}*(a+b*\arcsin(c*x))^{1/2}/b)+\sin(2*(a+b*\arcsin(c*x))/b-2*a/b)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(b \arcsin(cx) + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(a+b*arcsin(c*x))^(3/2),x, algorithm="maxima")`

[Out] `integrate(x/(b*arcsin(c*x) + a)^(3/2), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(a+b*arcsin(c*x))^(3/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(a + b \arcsin(cx))^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(a+b*asin(c*x))**(3/2),x)`

[Out] `Integral(x/(a + b*asin(c*x))**(3/2), x)`

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(b \arcsin(cx) + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x/(a+b*arcsin(c*x))^(3/2),x, algorithm="giac")
```

```
[Out] integrate(x/(b*arcsin(c*x) + a)^(3/2), x)
```

$$3.195 \quad \int \frac{1}{(a+b \sin^{-1}(cx))^{3/2}} dx$$

Optimal. Leaf size=137

$$\frac{2\sqrt{2\pi} \sin\left(\frac{a}{b}\right) \operatorname{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c} - \frac{2\sqrt{2\pi} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c} - \frac{2\sqrt{1-c^2x^2}}{bc\sqrt{a+b \sin^{-1}(cx)}}$$

[Out] $(-2*\sqrt{1-c^2*x^2})/(b*c*\sqrt{a+b*\operatorname{ArcSin}[c*x]}) - (2*\sqrt{2*\pi}*\cos[a/b]*\operatorname{FresnelS}[(\sqrt{2/\pi}*\sqrt{a+b*\operatorname{ArcSin}[c*x]})/\sqrt{b}])/(b^{(3/2)*c}) + (2*\sqrt{2*\pi}*\operatorname{FresnelC}[(\sqrt{2/\pi}*\sqrt{a+b*\operatorname{ArcSin}[c*x]})/\sqrt{b}]*\sin[a/b])/(b^{(3/2)*c})$

Rubi [A] time = 0.29426, antiderivative size = 137, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.583$, Rules used = {4621, 4723, 3306, 3305, 3351, 3304, 3352}

$$\frac{2\sqrt{2\pi} \sin\left(\frac{a}{b}\right) \operatorname{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c} - \frac{2\sqrt{2\pi} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c} - \frac{2\sqrt{1-c^2x^2}}{bc\sqrt{a+b \sin^{-1}(cx)}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a+b*\operatorname{ArcSin}[c*x])^{(-3/2)}, x]$

[Out] $(-2*\sqrt{1-c^2*x^2})/(b*c*\sqrt{a+b*\operatorname{ArcSin}[c*x]}) - (2*\sqrt{2*\pi}*\cos[a/b]*\operatorname{FresnelS}[(\sqrt{2/\pi}*\sqrt{a+b*\operatorname{ArcSin}[c*x]})/\sqrt{b}])/(b^{(3/2)*c}) + (2*\sqrt{2*\pi}*\operatorname{FresnelC}[(\sqrt{2/\pi}*\sqrt{a+b*\operatorname{ArcSin}[c*x]})/\sqrt{b}]*\sin[a/b])/(b^{(3/2)*c})$

Rule 4621

$\operatorname{Int}[(a + \operatorname{ArcSin}(c*x))^{n+1}, x] := \operatorname{Simp}[(\sqrt{1-c^2x^2}*(a+b*\operatorname{ArcSin}[c*x])^{n+1})/(b*c*(n+1)), x] + \operatorname{Dist}[c/(b*(n+1)), \operatorname{Int}[(x*(a+b*\operatorname{ArcSin}[c*x])^{n+1})/\sqrt{1-c^2x^2}, x], x] /;$ $\operatorname{FreeQ}\{a, b, c\}, x \&\& \operatorname{LtQ}[n, -1]$

Rule 4723

$\operatorname{Int}[(a + \operatorname{ArcSin}(c*x))^n * (d + e*x)^m, x] := \operatorname{Dist}[d^p/c^{m+1}, \operatorname{Subst}[\operatorname{Int}[(a+b*x)^n * \sin[x]^m * \cos[x]^{2p+1}, x], x, \operatorname{ArcSin}[c*x]], x] /;$ $\operatorname{FreeQ}\{a, b, c, d, e, n\}, x \&\& \operatorname{EqQ}[c^2*d + e, 0] \&\& \operatorname{IntegerQ}[2*p] \&\& \operatorname{GtQ}[p, -1] \&\& \operatorname{IGtQ}[m, 0] \&\& (\operatorname{IntegerQ}[p] \mid \mid \operatorname{GtQ}[d, 0])$

Rule 3306

$\operatorname{Int}[\sin(e*x + f*x)/\sqrt{c + d*x}, x] := \operatorname{Dist}[\cos[(d*e - c*f)/d], \operatorname{Int}[\sin[(c*f)/d + f*x]/\sqrt{c + d*x}, x], x] + \operatorname{Dist}[\sin[(d*e - c*f)/d], \operatorname{Int}[\cos[(c*f)/d + f*x]/\sqrt{c + d*x}, x], x] /;$ $\operatorname{FreeQ}\{c, d, e, f\}, x \&\& \operatorname{ComplexFreeQ}[f] \&\& \operatorname{NeQ}[d*e - c*f, 0]$

Rule 3305

```
Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d,
Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f},
x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3351

```
Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^-2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rule 3304

```
Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d,
Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]
```

Rule 3352

```
Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^-2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]
```

Rubi steps

$$\begin{aligned} \int \frac{1}{(a + b \sin^{-1}(cx))^{3/2}} dx &= -\frac{2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{(2c) \int \frac{x}{\sqrt{1-c^2x^2}\sqrt{a+b \sin^{-1}(cx)}} dx}{b} \\ &= -\frac{2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{2 \operatorname{Subst}\left(\int \frac{\sin(x)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{bc} \\ &= -\frac{2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{(2 \cos\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \frac{\sin\left(\frac{a}{b}+x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{bc} + \frac{(2 \sin\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \frac{\cos\left(\frac{a}{b}+x\right)}{\sqrt{a+bx}} dx, x, \sin^{-1}(cx)\right)}{bc} \\ &= -\frac{2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{(4 \cos\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \sin\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{b^2c} + \frac{(4 \sin\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \cos\left(\frac{x^2}{b}\right) dx, x, \sqrt{a + b \sin^{-1}(cx)}\right)}{b^2c} \\ &= -\frac{2\sqrt{1-c^2x^2}}{bc\sqrt{a + b \sin^{-1}(cx)}} - \frac{2\sqrt{2\pi} \cos\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c} + \frac{2\sqrt{2\pi} C\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{3/2}c} \operatorname{Si}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right) \end{aligned}$$

Mathematica [C] time = 0.297999, size = 167, normalized size = 1.22

$$\frac{e^{-\frac{i(a+b \sin^{-1}(cx))}{b}} \left(e^{i \sin^{-1}(cx)} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{1}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) + e^{\frac{ia}{b}} \left(e^{\frac{i(a+b \sin^{-1}(cx))}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}} \operatorname{Gamma}\left(\frac{1}{2}, \frac{i(a+b \sin^{-1}(cx))}{b}\right) \right) \right)}{bc\sqrt{a + b \sin^{-1}(cx)}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[(a + b*ArcSin[c*x])^(-3/2), x]
```

```
[Out] (E^(I*ArcSin[c*x])*Sqrt[((-I)*(a + b*ArcSin[c*x]))/b]*Gamma[1/2, ((-I)*(a + b*ArcSin[c*x]))/b] + E^((I*a)/b)*(-1 - E^((2*I)*ArcSin[c*x]) + E^((I*(a +
```

$b \cdot \text{ArcSin}[c \cdot x]) / b) \cdot \text{Sqrt}[(I \cdot (a + b \cdot \text{ArcSin}[c \cdot x])) / b] \cdot \text{Gamma}[1/2, (I \cdot (a + b \cdot \text{ArcSin}[c \cdot x])) / b]) / (b \cdot c \cdot E^{(I \cdot (a + b \cdot \text{ArcSin}[c \cdot x])) / b}) \cdot \text{Sqrt}[a + b \cdot \text{ArcSin}[c \cdot x]]]$

Maple [A] time = 0.042, size = 149, normalized size = 1.1

$$-2 \frac{1}{bc\sqrt{a+b\arcsin(cx)}} \left(\sqrt{b^{-1}} \sqrt{\pi} \sqrt{2} \sqrt{a+b\arcsin(cx)} \cos\left(\frac{a}{b}\right) \text{FresnelS}\left(\frac{\sqrt{2}\sqrt{a+b\arcsin(cx)}}{\sqrt{b^{-1}}\sqrt{\pi}b}\right) - \sqrt{b^{-1}} \sqrt{\pi} \sqrt{2} \sqrt{a+b\arcsin(cx)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a+b*arcsin(c*x))^(3/2),x)

[Out] $-2/c/b * ((1/b)^{(1/2)} * \pi^{(1/2)} * 2^{(1/2)} * (a+b*\arcsin(c*x))^{(1/2)} * \cos(a/b) * \text{FresnelS}(2^{(1/2)}/\pi^{(1/2)}/(1/b)^{(1/2)} * (a+b*\arcsin(c*x))^{(1/2)}/b) - (1/b)^{(1/2)} * \pi^{(1/2)} * 2^{(1/2)} * (a+b*\arcsin(c*x))^{(1/2)} * \sin(a/b) * \text{FresnelC}(2^{(1/2)}/\pi^{(1/2)}/(1/b)^{(1/2)} * (a+b*\arcsin(c*x))^{(1/2)}/b) + \cos((a+b*\arcsin(c*x))/b - a/b)) / (a+b*\arcsin(c*x))^{(1/2)}$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^(3/2),x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(-3/2), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^(3/2),x, algorithm="fricas")

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(a + b \arcsin(cx))^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*asin(c*x))**(3/2),x)


```
[Out] Integral((a + b*asin(c*x))**(-3/2), x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a+b*arcsin(c*x))^(3/2),x, algorithm="giac")
```

```
[Out] integrate((b*arcsin(c*x) + a)^(-3/2), x)
```

$$3.196 \quad \int \frac{1}{x(a+b \sin^{-1}(cx))^{3/2}} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{1}{x(a+b \sin^{-1}(cx))^{3/2}}, x \right)$$

[Out] Unintegrable[1/(x*(a + b*ArcSin[c*x])^(3/2)), x]

Rubi [A] time = 0.0442315, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*(a + b*ArcSin[c*x])^(3/2)),x]

[Out] Defer[Int][1/(x*(a + b*ArcSin[c*x])^(3/2)), x]

Rubi steps

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^{3/2}} dx = \int \frac{1}{x(a+b \sin^{-1}(cx))^{3/2}} dx$$

Mathematica [A] time = 3.4583, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*(a + b*ArcSin[c*x])^(3/2)),x]

[Out] Integrate[1/(x*(a + b*ArcSin[c*x])^(3/2)), x]

Maple [A] time = 0.079, size = 0, normalized size = 0.

$$\int \frac{1}{x} (a + b \arcsin(cx))^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(a+b*arcsin(c*x))^(3/2),x)

[Out] `int(1/x/(a+b*arcsin(c*x))^(3/2),x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{3}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(3/2),x, algorithm="maxima")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(3/2)*x), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(3/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x(a + b \arcsin(cx))^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*asin(c*x))**(3/2),x)`

[Out] `Integral(1/(x*(a + b*asin(c*x))**(3/2)), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{3}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(3/2),x, algorithm="giac")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(3/2)*x), x)`

$$3.197 \quad \int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{3/2}} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{1}{x^2 (a + b \sin^{-1}(cx))^{3/2}}, x \right)$$

[Out] Unintegrable[1/(x^2*(a + b*ArcSin[c*x])^(3/2)), x]

Rubi [A] time = 0.0428374, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*(a + b*ArcSin[c*x])^(3/2)),x]

[Out] Defer[Int][1/(x^2*(a + b*ArcSin[c*x])^(3/2)), x]

Rubi steps

$$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{3/2}} dx = \int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{3/2}} dx$$

Mathematica [A] time = 11.4046, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{3/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*(a + b*ArcSin[c*x])^(3/2)),x]

[Out] Integrate[1/(x^2*(a + b*ArcSin[c*x])^(3/2)), x]

Maple [A] time = 0.158, size = 0, normalized size = 0.

$$\int \frac{1}{x^2} (a + b \arcsin(cx))^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(a+b*arcsin(c*x))^(3/2),x)

[Out] `int(1/x^2/(a+b*arcsin(c*x))^(3/2),x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{3}{2}} x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(3/2),x, algorithm="maxima")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(3/2)*x^2), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(3/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (a + b \arcsin(cx))^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(a+b*asin(c*x))**(3/2),x)`

[Out] `Integral(1/(x**2*(a + b*asin(c*x))**(3/2)), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{3}{2}} x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(3/2),x, algorithm="giac")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(3/2)*x^2), x)`

$$3.198 \quad \int \frac{x^2}{(a+b \sin^{-1}(cx))^{5/2}} dx$$

Optimal. Leaf size=291

$$\frac{\sqrt{2\pi} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c^3} + \frac{\sqrt{6\pi} \cos\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{5/2}c^3} - \frac{\sqrt{2\pi} \sin\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c^3}$$

[Out] $(-2*x^2*\text{Sqrt}[1 - c^2*x^2])/(3*b*c*(a + b*\text{ArcSin}[c*x])^{(3/2)}) - (8*x)/(3*b^2*c^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) + (4*x^3)/(b^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) - (\text{Sqrt}[2*Pi]*\text{Cos}[a/b]*\text{FresnelC}[(\text{Sqrt}[2/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(3*b^{(5/2)}*c^3) + (\text{Sqrt}[6*Pi]*\text{Cos}[(3*a)/b]*\text{FresnelC}[(\text{Sqrt}[6/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(b^{(5/2)}*c^3) - (\text{Sqrt}[2*Pi]*\text{FresnelS}[(\text{Sqrt}[2/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(3*b^{(5/2)}*c^3) + (\text{Sqrt}[6*Pi]*\text{FresnelS}[(\text{Sqrt}[6/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[(3*a)/b])/(b^{(5/2)}*c^3)$

Rubi [A] time = 1.00719, antiderivative size = 291, normalized size of antiderivative = 1., number of steps used = 22, number of rules used = 10, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {4633, 4719, 4635, 4406, 3306, 3305, 3351, 3304, 3352, 4623}

$$\frac{\sqrt{2\pi} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c^3} + \frac{\sqrt{6\pi} \cos\left(\frac{3a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{6}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{b^{5/2}c^3} - \frac{\sqrt{2\pi} \sin\left(\frac{a}{b}\right) S\left(\frac{\sqrt{\frac{2}{\pi}} \sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2/(a + b*\text{ArcSin}[c*x])^{(5/2)}, x]$

[Out] $(-2*x^2*\text{Sqrt}[1 - c^2*x^2])/(3*b*c*(a + b*\text{ArcSin}[c*x])^{(3/2)}) - (8*x)/(3*b^2*c^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) + (4*x^3)/(b^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) - (\text{Sqrt}[2*Pi]*\text{Cos}[a/b]*\text{FresnelC}[(\text{Sqrt}[2/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(3*b^{(5/2)}*c^3) + (\text{Sqrt}[6*Pi]*\text{Cos}[(3*a)/b]*\text{FresnelC}[(\text{Sqrt}[6/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]])/(b^{(5/2)}*c^3) - (\text{Sqrt}[2*Pi]*\text{FresnelS}[(\text{Sqrt}[2/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[a/b])/(3*b^{(5/2)}*c^3) + (\text{Sqrt}[6*Pi]*\text{FresnelS}[(\text{Sqrt}[6/Pi]*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/\text{Sqrt}[b]]*\text{Sin}[(3*a)/b])/(b^{(5/2)}*c^3)$

Rule 4633

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + x)^n*(x)^m, x_Symbol] \rightarrow \text{Simp}[(x^m*\text{Sqrt}[1 - c^2*x^2]*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*(n+1)), x] + (\text{Dist}[(c*(m+1))/(b*(n+1)), \text{Int}[(x^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x] - \text{Dist}[m/(b*c*(n+1)), \text{Int}[(x^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)})/\text{Sqrt}[1 - c^2*x^2], x], x]) /; \text{FreeQ}\{a, b, c\}, x \&\& \text{IGtQ}[m, 0] \&\& \text{LtQ}[n, -2]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + x)^n*((f + x)^m)/\text{Sqrt}[d + (e + x)^2], x_Symbol] \rightarrow \text{Simp}[(f*x)^m*(a + b*\text{ArcSin}[c*x])^{(n+1)})/(b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m)/(b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{(m-1)}*(a + b*\text{ArcSin}[c*x])^{(n+1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x \&$

& EqQ[c^2*d + e, 0] && LtQ[n, -1] && GtQ[d, 0]

Rule 4635

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_*(x_)^(m_.), x_Symbol] := Dist[1/c^(m + 1), Subst[Int[(a + b*x)^n*Sin[x]^m*Cos[x], x], x, ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 4623

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^n_, x_Symbol] := Dist[1/(b*c), Subst[Int[x^n*Cos[a/b - x/b], x], x, a + b*ArcSin[c*x]], x] /; FreeQ[{a, b, c, n}, x]

Rubi steps

$$\begin{aligned}
\int \frac{x^2}{(a + b \sin^{-1}(cx))^{5/2}} dx &= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} + \frac{4 \int \frac{x}{\sqrt{1-c^2x^2}(a+b \sin^{-1}(cx))^{3/2}} dx}{3bc} - \frac{(2c) \int \frac{x^3}{\sqrt{1-c^2x^2}(a+b \sin^{-1}(cx))^{3/2}} dx}{b} \\
&= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{8x}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{4x^3}{b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{12 \int \frac{x^2}{\sqrt{a+b \sin^{-1}(cx)}} dx}{b^2} \\
&= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{8x}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{4x^3}{b^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8 \text{Subst}\left(\int \frac{\cos(\frac{x}{b})}{\sqrt{a+b \sin^{-1}(cx)}} dx\right)}{b^2} \\
&= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{8x}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{4x^3}{b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{12 \text{Subst}\left(\int \frac{\cos(\frac{x}{b})}{4\sqrt{a+b \sin^{-1}(cx)}} dx\right)}{b^2} \\
&= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{8x}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{4x^3}{b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{3 \text{Subst}\left(\int \frac{\cos(\frac{x}{b})}{\sqrt{a+b \sin^{-1}(cx)}} dx\right)}{b^2} \\
&= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{8x}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{4x^3}{b^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8\sqrt{2\pi} \cos\left(\frac{a}{b}\right) C}{3b^2} \\
&= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{8x}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{4x^3}{b^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8\sqrt{2\pi} \cos\left(\frac{a}{b}\right) C}{3b^2} \\
&= -\frac{2x^2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{8x}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{4x^3}{b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{\sqrt{2\pi} \cos\left(\frac{a}{b}\right) C}{3b^5}
\end{aligned}$$

Mathematica [C] time = 1.85544, size = 370, normalized size = 1.27

$$-2be^{-\frac{ia}{b}} \left(-\frac{i(a+b \sin^{-1}(cx))}{b}\right)^{3/2} \text{Gamma}\left(\frac{1}{2}, -\frac{i(a+b \sin^{-1}(cx))}{b}\right) + 6\sqrt{3}be^{-\frac{3ia}{b}} \left(-\frac{i(a+b \sin^{-1}(cx))}{b}\right)^{3/2} \text{Gamma}\left(\frac{1}{2}, -\frac{3i(a+b \sin^{-1}(cx))}{b}\right) +$$

Warning: Unable to verify antiderivative.

[In] Integrate[x^2/(a + b*ArcSin[c*x])^(5/2), x]

[Out] (((-6*I)*a)/E^((3*I)*ArcSin[c*x]) + (b*(1 - (6*I)*ArcSin[c*x]))/E^((3*I)*ArcSin[c*x]) + E^((3*I)*ArcSin[c*x])*((6*I)*a + b + (6*I)*b*ArcSin[c*x]) - I*E^(I*ArcSin[c*x])*(2*a - I*b + 2*b*ArcSin[c*x]) - (2*b*(((I)*a + b*ArcSin[c*x]))/b)^(3/2)*Gamma[1/2, ((-I)*(a + b*ArcSin[c*x]))/b])/E^((I*a)/b) + (I*(2*a + I*b + 2*b*ArcSin[c*x]) + (2*I)*b*E^(((I)*(a + b*ArcSin[c*x]))/b))*((I*(a + b*ArcSin[c*x]))/b)^(3/2)*Gamma[1/2, (I*(a + b*ArcSin[c*x]))/b])/E^(I*ArcSin[c*x]) + (6*Sqrt[3]*b*(((I)*a + b*ArcSin[c*x]))/b)^(3/2)*Gamma[1/2, ((-3*I)*(a + b*ArcSin[c*x]))/b])/E^(((3*I)*a)/b) + 6*Sqrt[3]*b*E^(((3*I)*a)/b)*((I*(a + b*ArcSin[c*x]))/b)^(3/2)*Gamma[1/2, ((3*I)*(a + b*ArcSin[c*x]))/b))/(12*b^2*c^3*(a + b*ArcSin[c*x])^(3/2))

Maple [B] time = 0.088, size = 660, normalized size = 2.3

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] $\int x^2/(a+b*\arcsin(cx))^{5/2}, x$

[Out] $\frac{1}{6}c^3/b^2*(6*\arcsin(cx)*(a+b*\arcsin(cx))^{1/2}*\cos(3a/b)*\text{FresnelC}(2^{1/2}/\text{Pi}^{1/2}*3^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*3^{1/2}*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*b+6*\arcsin(cx)*(a+b*\arcsin(cx))^{1/2}*\sin(3a/b)*\text{FresnelS}(2^{1/2}/\text{Pi}^{1/2}*3^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*3^{1/2}*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*b-2*\arcsin(cx)*(a+b*\arcsin(cx))^{1/2}*\cos(a/b)*\text{FresnelC}(2^{1/2}/\text{Pi}^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*b-2*\arcsin(cx)*(a+b*\arcsin(cx))^{1/2}*\sin(a/b)*\text{FresnelS}(2^{1/2}/\text{Pi}^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*b+6*(a+b*\arcsin(cx))^{1/2}*\cos(3a/b)*\text{FresnelC}(2^{1/2}/\text{Pi}^{1/2}*3^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*3^{1/2}*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*a+6*(a+b*\arcsin(cx))^{1/2}*\sin(3a/b)*\text{FresnelS}(2^{1/2}/\text{Pi}^{1/2}*3^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*3^{1/2}*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*a-2*(a+b*\arcsin(cx))^{1/2}*\cos(a/b)*\text{FresnelC}(2^{1/2}/\text{Pi}^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*a-2*(a+b*\arcsin(cx))^{1/2}*\sin(a/b)*\text{FresnelS}(2^{1/2}/\text{Pi}^{1/2}/(1/b)^{1/2}*(a+b*\arcsin(cx))^{1/2}/b)*(1/b)^{(1/2)*2^{1/2}}*\text{Pi}^{1/2}*a+2*\arcsin(cx)*\sin((a+b*\arcsin(cx))/b-a/b)*b-6*\arcsin(cx)*\sin(3*(a+b*\arcsin(cx))/b-3a/b)*b-\cos((a+b*\arcsin(cx))/b-a/b)*b+2*\sin((a+b*\arcsin(cx))/b-a/b)*a+\cos(3*(a+b*\arcsin(cx))/b-3a/b)*b-6*\sin(3*(a+b*\arcsin(cx))/b-3a/b)*a)/(a+b*\arcsin(cx))^{3/2}$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(b \arcsin(cx) + a)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\int x^2/(a+b*\arcsin(cx))^{5/2}, x, \text{algorithm}="maxima"$

[Out] $\int x^2/(b*\arcsin(cx) + a)^{5/2}, x$

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] $\int x^2/(a+b*\arcsin(cx))^{5/2}, x, \text{algorithm}="fricas"$

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(a + b \operatorname{asin}(cx))^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2/(a+b*asin(c*x))**(5/2),x)

[Out] Integral(x**2/(a + b*asin(c*x))**(5/2), x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x^2}{(b \operatorname{arcsin}(cx) + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2/(a+b*arcsin(c*x))^(5/2),x, algorithm="giac")

[Out] integrate(x^2/(b*arcsin(c*x) + a)^(5/2), x)

$$3.199 \quad \int \frac{x}{(a+b \sin^{-1}(cx))^{5/2}} dx$$

Optimal. Leaf size=180

$$\frac{8\sqrt{\pi} \sin\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{3b^{5/2}c^2} - \frac{8\sqrt{\pi} \cos\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{3b^{5/2}c^2} - \frac{4}{3b^2c^2\sqrt{a+b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a+b \sin^{-1}(cx)}}$$

[Out] $(-2*x*\text{Sqrt}[1 - c^2*x^2])/(3*b*c*(a + b*\text{ArcSin}[c*x])^{(3/2)}) - 4/(3*b^2*c^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) + (8*x^2)/(3*b^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) - (8*\text{Sqrt}[\text{Pi}]*\text{Cos}[(2*a)/b]*\text{FresnelS}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}]]))/(3*b^{(5/2)}*c^2) + (8*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}])]*\text{Sin}[(2*a)/b])/(3*b^{(5/2)}*c^2)$

Rubi [A] time = 0.506164, antiderivative size = 180, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 11, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.786$, Rules used = {4633, 4719, 4635, 4406, 12, 3306, 3305, 3351, 3304, 3352, 4641}

$$\frac{8\sqrt{\pi} \sin\left(\frac{2a}{b}\right) \text{FresnelC}\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{\pi}\sqrt{b}}\right)}{3b^{5/2}c^2} - \frac{8\sqrt{\pi} \cos\left(\frac{2a}{b}\right) S\left(\frac{2\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}\sqrt{\pi}}\right)}{3b^{5/2}c^2} - \frac{4}{3b^2c^2\sqrt{a+b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a+b \sin^{-1}(cx)}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x/(a + b*\text{ArcSin}[c*x])^{(5/2)}, x]$

[Out] $(-2*x*\text{Sqrt}[1 - c^2*x^2])/(3*b*c*(a + b*\text{ArcSin}[c*x])^{(3/2)}) - 4/(3*b^2*c^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) + (8*x^2)/(3*b^2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]]) - (8*\text{Sqrt}[\text{Pi}]*\text{Cos}[(2*a)/b]*\text{FresnelS}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}]]))/(3*b^{(5/2)}*c^2) + (8*\text{Sqrt}[\text{Pi}]*\text{FresnelC}[(2*\text{Sqrt}[a + b*\text{ArcSin}[c*x]])/(\text{Sqrt}[b]*\text{Sqrt}[\text{Pi}])]*\text{Sin}[(2*a)/b])/(3*b^{(5/2)}*c^2)$

Rule 4633

$\text{Int}[(a + \text{ArcSin}[c*x])^n * (x^m) * (b)^n, x_Symbol] := \text{Simp}[(x^m * \text{Sqrt}[1 - c^2*x^2] * (a + b*\text{ArcSin}[c*x])^{(n+1)}) / (b*c*(n+1)), x] + (\text{Dist}[(c*(m+1)) / (b*(n+1)), \text{Int}[(x^{(m+1)} * (a + b*\text{ArcSin}[c*x])^{(n+1)}) / \text{Sqrt}[1 - c^2*x^2], x], x] - \text{Dist}[m / (b*c*(n+1)), \text{Int}[(x^{(m-1)} * (a + b*\text{ArcSin}[c*x])^{(n+1)}) / \text{Sqrt}[1 - c^2*x^2], x], x]) /; \text{FreeQ}\{a, b, c\}, x \&\& \text{IGtQ}[m, 0] \&\& \text{LtQ}[n, -2]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c*x])^n * (f*x)^m * (d + e*x^2), x_Symbol] := \text{Simp}[(f*x)^m * (a + b*\text{ArcSin}[c*x])^{(n+1)}) / (b*c*\text{Sqrt}[d]*(n+1)), x] - \text{Dist}[(f*m) / (b*c*\text{Sqrt}[d]*(n+1)), \text{Int}[(f*x)^{(m-1)} * (a + b*\text{ArcSin}[c*x])^{(n+1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, m\}, x \&\& \text{EqQ}[c^2*d + e, 0] \&\& \text{LtQ}[n, -1] \&\& \text{GtQ}[d, 0]$

Rule 4635

$\text{Int}[(a + \text{ArcSin}[c*x])^n * (x^m), x_Symbol] := \text{Dist}[1/c^{(m+1)}, \text{Subst}[\text{Int}[(a + b*x)^n * \text{Sin}[x]^m * \text{Cos}[x], x], x, \text{ArcSin}[c*x]], x]$

;/; FreeQ[{a, b, c, n}, x] && IGtQ[m, 0]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3306

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] :> Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_)]/Sqrt[(c_.) + (d_.)*(x_)], x_Symbol] :> Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_))^2], x_Symbol] :> Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 4641

Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[(a + b*ArcSin[c*x])^(n + 1)/(b*c*Sqrt[d]*(n + 1)), x] /; FreeQ[{a, b, c, d, e, n}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && NeQ[n, -1]

Rubi steps

$$\begin{aligned}
\int \frac{x}{(a + b \sin^{-1}(cx))^{5/2}} dx &= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} + \frac{2 \int \frac{1}{\sqrt{1-c^2x^2}(a+b \sin^{-1}(cx))^{3/2}} dx}{3bc} - \frac{(4c) \int \frac{x^2}{\sqrt{1-c^2x^2}(a+b \sin^{-1}(cx))^{3/2}} dx}{3b} \\
&= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{4}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{16 \int \frac{x}{\sqrt{a+b \sin^{-1}(cx)}} dx}{3b^2} \\
&= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{4}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{16 \text{Subst}\left(\int \frac{x}{\sqrt{a+b \sin^{-1}(cx)}} dx\right)}{3b^2} \\
&= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{4}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{16 \text{Subst}\left(\int \frac{x}{\sqrt{a+b \sin^{-1}(cx)}} dx\right)}{3b^2} \\
&= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{4}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{8 \text{Subst}\left(\int \frac{x}{\sqrt{a+b \sin^{-1}(cx)}} dx\right)}{3b^2} \\
&= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{4}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{8 \cos\left(\frac{2a}{b}\right)}{3b^2} \\
&= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{4}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{16 \cos\left(\frac{2a}{b}\right)}{3b^2} \\
&= -\frac{2x\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{4}{3b^2c^2\sqrt{a + b \sin^{-1}(cx)}} + \frac{8x^2}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{8\sqrt{\pi} \cos\left(\frac{2a}{b}\right)}{3b^2}
\end{aligned}$$

Mathematica [C] time = 1.23093, size = 173, normalized size = 0.96

$$\frac{b \sin\left(2 \sin^{-1}(cx)\right) + 2\left(a + b \sin^{-1}(cx)\right) \left(-\sqrt{2} e^{-\frac{2ia}{b}} \sqrt{-\frac{i(a+b \sin^{-1}(cx))}{b}} \text{Gamma}\left(\frac{1}{2}, -\frac{2i(a+b \sin^{-1}(cx))}{b}\right) - \sqrt{2} e^{\frac{2ia}{b}} \sqrt{\frac{i(a+b \sin^{-1}(cx))}{b}}\right)}{3b^2c^2(a + b \sin^{-1}(cx))^{3/2}}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x/(a + b*ArcSin[c*x])^(5/2), x]

[Out] $-(2*(a + b*ArcSin[c*x])*(E^{((-2*I)*ArcSin[c*x])} + E^{((2*I)*ArcSin[c*x])}) - (\text{Sqrt}[2]*\text{Sqrt}[\frac{((-I)*(a + b*ArcSin[c*x])}{b})*\text{Gamma}[1/2, \frac{((-2*I)*(a + b*ArcSin[c*x])}{b})}{E^{((2*I)*a)/b} - \text{Sqrt}[2]*E^{((2*I)*a)/b}*\text{Sqrt}[\frac{(I*(a + b*ArcSin[c*x])}{b})*\text{Gamma}[1/2, \frac{(2*I)*(a + b*ArcSin[c*x])}{b}] + b*\text{Sin}[2*ArcSin[c*x]]])}{(3*b^2*c^2*(a + b*ArcSin[c*x])^{(3/2)})}$

Maple [B] time = 0.059, size = 311, normalized size = 1.7

$$-\frac{1}{3b^2c^2} \left(8 \arcsin(cx) \sqrt{\pi} \sqrt{b^{-1}} \sqrt{a + b \arcsin(cx)} \cos\left(2 \frac{a}{b}\right) \text{FresnelS}\left(2 \frac{\sqrt{a + b \arcsin(cx)}}{\sqrt{\pi} \sqrt{b^{-1}} b}\right) b - 8 \arcsin(cx) \sqrt{\pi} \sqrt{b} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x/(a+b*arcsin(c*x))^(5/2),x)`

[Out]
$$-1/3/c^2/b^2*(8*\arcsin(c*x)*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\cos(2*a/b)*\text{FresnelS}(2/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*b-8*\arcsin(c*x)*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\sin(2*a/b)*\text{FresnelC}(2/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*b+8*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\cos(2*a/b)*\text{FresnelS}(2/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*a-8*\text{Pi}^{(1/2)}*(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}*\sin(2*a/b)*\text{FresnelC}(2/\text{Pi}^{(1/2)}/(1/b)^{(1/2)}*(a+b*\arcsin(c*x))^{(1/2)}/b)*a+4*\arcsin(c*x)*\cos(2*(a+b*\arcsin(c*x))/b-2*a/b)*b+\sin(2*(a+b*\arcsin(c*x))/b-2*a/b)*b+4*\cos(2*(a+b*\arcsin(c*x))/b-2*a/b)*a)/(a+b*\arcsin(c*x))^{(3/2)}$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(b \arcsin(cx) + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(a+b*arcsin(c*x))^(5/2),x, algorithm="maxima")`

[Out] `integrate(x/(b*arcsin(c*x) + a)^(5/2), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(a+b*arcsin(c*x))^(5/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(a + b \arcsin(cx))^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x/(a+b*asin(c*x))**(5/2),x)`

[Out] `Integral(x/(a + b*asin(c*x))**(5/2), x)`

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{x}{(b \arcsin(cx) + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x/(a+b*arcsin(c*x))^(5/2),x, algorithm="giac")
```

```
[Out] integrate(x/(b*arcsin(c*x) + a)^(5/2), x)
```

$$3.200 \quad \int \frac{1}{(a+b \sin^{-1}(cx))^{5/2}} dx$$

Optimal. Leaf size=163

$$\frac{4\sqrt{2\pi} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c} - \frac{4\sqrt{2\pi} \sin\left(\frac{a}{b}\right) \text{S}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c} + \frac{4x}{3b^2\sqrt{a+b \sin^{-1}(cx)}} - \frac{2\sqrt{1-c^2}}{3bc(a+b \sin^{-1}(cx))}$$

[Out] $(-2\sqrt{1-c^2x^2})/(3bc(a+b\text{ArcSin}[cx])^{3/2}) + (4x)/(3b^2\sqrt{a+b\text{ArcSin}[cx]}) - (4\sqrt{2\pi}\cos[a/b]\text{FresnelC}[(\sqrt{2/\pi}\sqrt{a+b\text{ArcSin}[cx]})/\sqrt{b}])/(3b^{5/2}c) - (4\sqrt{2\pi}\sin[a/b]\text{FresnelS}[(\sqrt{2/\pi}\sqrt{a+b\text{ArcSin}[cx]})/\sqrt{b}])/(3b^{5/2}c)$

Rubi [A] time = 0.275994, antiderivative size = 163, normalized size of antiderivative = 1., number of steps used = 8, number of rules used = 8, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {4621, 4719, 4623, 3306, 3305, 3351, 3304, 3352}

$$\frac{4\sqrt{2\pi} \cos\left(\frac{a}{b}\right) \text{FresnelC}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c} - \frac{4\sqrt{2\pi} \sin\left(\frac{a}{b}\right) \text{S}\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c} + \frac{4x}{3b^2\sqrt{a+b \sin^{-1}(cx)}} - \frac{2\sqrt{1-c^2}}{3bc(a+b \sin^{-1}(cx))}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b\text{ArcSin}[cx])^{-5/2}, x]$

[Out] $(-2\sqrt{1-c^2x^2})/(3bc(a+b\text{ArcSin}[cx])^{3/2}) + (4x)/(3b^2\sqrt{a+b\text{ArcSin}[cx]}) - (4\sqrt{2\pi}\cos[a/b]\text{FresnelC}[(\sqrt{2/\pi}\sqrt{a+b\text{ArcSin}[cx]})/\sqrt{b}])/(3b^{5/2}c) - (4\sqrt{2\pi}\sin[a/b]\text{FresnelS}[(\sqrt{2/\pi}\sqrt{a+b\text{ArcSin}[cx]})/\sqrt{b}])/(3b^{5/2}c)$

Rule 4621

$\text{Int}[(a + \text{ArcSin}[c(x)](b))^{(n)}, x_Symbol] \rightarrow \text{Simp}[(\sqrt{1-c^2x^2}(a+b\text{ArcSin}[cx])^{(n+1)})/(bc(n+1)), x] + \text{Dist}[c/(b(n+1)), \text{Int}[(x(a+b\text{ArcSin}[cx])^{(n+1)})/\sqrt{1-c^2x^2}, x], x] /;$ $\text{FreeQ}\{a, b, c\}, x \&\& \text{LtQ}[n, -1]$

Rule 4719

$\text{Int}[(a + \text{ArcSin}[c(x)](b))^{(n)}(f(x))^m/\sqrt{d+e(x)^2}, x_Symbol] \rightarrow \text{Simp}[(f(x))^m(a+b\text{ArcSin}[cx])^{(n+1)})/(bc\sqrt{d+e(x)^2}(n+1)), x] - \text{Dist}[(f(x))^m/(bc\sqrt{d+e(x)^2}(n+1)), \text{Int}[(f(x))^{(m-1)}(a+b\text{ArcSin}[cx])^{(n+1)}, x], x] /;$ $\text{FreeQ}\{a, b, c, d, e, f, m\}, x \&\& \text{EqQ}[c^2d+e, 0] \&\& \text{LtQ}[n, -1] \&\& \text{GtQ}[d, 0]$

Rule 4623

$\text{Int}[(a + \text{ArcSin}[c(x)](b))^{(n)}, x_Symbol] \rightarrow \text{Dist}[1/(bc), \text{Subst}[\text{Int}[x^n\cos[a/b-x/b], x], x, a+b\text{ArcSin}[cx]], x] /;$ $\text{FreeQ}\{a, b, c, n\}, x$

Rule 3306

Int[sin[(e_.) + (f_.)*(x_.)]/Sqrt[(c_.) + (d_.)*(x_.)], x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/Sqrt[c + d*x], x], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && NeQ[d*e - c*f, 0]

Rule 3305

Int[sin[(e_.) + (f_.)*(x_.)]/Sqrt[(c_.) + (d_.)*(x_.)], x_Symbol] := Dist[2/d, Subst[Int[Sin[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3351

Int[Sin[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelS[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rule 3304

Int[sin[Pi/2 + (e_.) + (f_.)*(x_.)]/Sqrt[(c_.) + (d_.)*(x_.)], x_Symbol] := Dist[2/d, Subst[Int[Cos[(f*x^2)/d], x], x, Sqrt[c + d*x]], x] /; FreeQ[{c, d, e, f}, x] && ComplexFreeQ[f] && EqQ[d*e - c*f, 0]

Rule 3352

Int[Cos[(d_.)*((e_.) + (f_.)*(x_.))^2], x_Symbol] := Simp[(Sqrt[Pi/2]*FresnelC[Sqrt[2/Pi]*Rt[d, 2]*(e + f*x)])/(f*Rt[d, 2]), x] /; FreeQ[{d, e, f}, x]

Rubi steps

$$\begin{aligned}
 \int \frac{1}{(a + b \sin^{-1}(cx))^{5/2}} dx &= -\frac{2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} - \frac{(2c) \int \frac{x}{\sqrt{1-c^2x^2}(a+b \sin^{-1}(cx))^{3/2}} dx}{3b} \\
 &= -\frac{2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} + \frac{4x}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{4 \int \frac{1}{\sqrt{a+b \sin^{-1}(cx)}} dx}{3b^2} \\
 &= -\frac{2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} + \frac{4x}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{4 \operatorname{Subst}\left(\int \frac{\cos\left(\frac{a}{b} - \frac{x}{b}\right)}{\sqrt{x}} dx, x, a + b \sin^{-1}(cx)\right)}{3b^3c} \\
 &= -\frac{2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} + \frac{4x}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{(4 \cos\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \frac{\cos\left(\frac{x}{b}\right)}{\sqrt{x}} dx, x, a + b \sin^{-1}(cx)\right)}{3b^3c} \\
 &= -\frac{2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} + \frac{4x}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{(8 \cos\left(\frac{a}{b}\right)) \operatorname{Subst}\left(\int \cos\left(\frac{x^2}{b}\right) dx, x, a + b \sin^{-1}(cx)\right)}{3b^3c} \\
 &= -\frac{2\sqrt{1-c^2x^2}}{3bc(a + b \sin^{-1}(cx))^{3/2}} + \frac{4x}{3b^2\sqrt{a + b \sin^{-1}(cx)}} - \frac{4\sqrt{2\pi} \cos\left(\frac{a}{b}\right) C\left(\frac{\sqrt{\frac{2}{\pi}}\sqrt{a+b \sin^{-1}(cx)}}{\sqrt{b}}\right)}{3b^{5/2}c}
 \end{aligned}$$

Mathematica [C] time = 0.851546, size = 214, normalized size = 1.31

$$e^{-\frac{i(a+b\sin^{-1}(cx))}{b}} \left(-2be^{i\sin^{-1}(cx)} \left(-\frac{i(a+b\sin^{-1}(cx))}{b} \right)^{3/2} \Gamma\left(\frac{1}{2}, -\frac{i(a+b\sin^{-1}(cx))}{b}\right) - ie^{\frac{ia}{b}} \left(-2ibe^{\frac{i(a+b\sin^{-1}(cx))}{b}} \left(\frac{i(a+b\sin^{-1}(cx))}{b} \right)^{3/2} \Gamma\left(\frac{1}{2}, \frac{i(a+b\sin^{-1}(cx))}{b}\right) \right) \right)$$

$$3b^2c(a+b\sin^{-1}(cx))$$

Warning: Unable to verify antiderivative.

[In] Integrate[(a + b*ArcSin[c*x])^(-5/2), x]

[Out] (-2*b*E^(I*ArcSin[c*x])*((-I)*(a + b*ArcSin[c*x]))/b)^(3/2)*Gamma[1/2, ((-I)*(a + b*ArcSin[c*x]))/b] - I*E^((I*a)/b)*(2*a*(-1 + E^((2*I)*ArcSin[c*x])) + b*(-I - 2*ArcSin[c*x] + E^((2*I)*ArcSin[c*x]))*(-I + 2*ArcSin[c*x])) - (2*I)*b*E^((I*(a + b*ArcSin[c*x]))/b)*((I*(a + b*ArcSin[c*x]))/b)^(3/2)*Gamma[1/2, (I*(a + b*ArcSin[c*x]))/b]/(3*b^2*c*E^((I*(a + b*ArcSin[c*x]))/b)*(a + b*ArcSin[c*x])^(3/2))

Maple [B] time = 0.053, size = 325, normalized size = 2.

$$\frac{2}{3b^2c} \left(-2 \arcsin(cx) \sqrt{a + b \arcsin(cx)} \cos\left(\frac{a}{b}\right) \operatorname{FresnelC}\left(\frac{\sqrt{2}\sqrt{a + b \arcsin(cx)}}{\sqrt{\pi}\sqrt{b-1}b}\right) \sqrt{b-1}\sqrt{2}\sqrt{\pi}b - 2 \arcsin(cx) \sqrt{a + b \arcsin(cx)} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(a+b*arcsin(c*x))^(5/2), x)

[Out] 2/3/c/b^2*(-2*arcsin(c*x)*(a+b*arcsin(c*x))^(1/2)*cos(a/b)*FresnelC(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*(1/b)^(1/2)*2^(1/2)*Pi^(1/2)*b-2*arcsin(c*x)*(a+b*arcsin(c*x))^(1/2)*sin(a/b)*FresnelS(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*(1/b)^(1/2)*2^(1/2)*Pi^(1/2)*b-2*(a+b*arcsin(c*x))^(1/2)*cos(a/b)*FresnelC(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*(1/b)^(1/2)*2^(1/2)*Pi^(1/2)*a-2*(a+b*arcsin(c*x))^(1/2)*sin(a/b)*FresnelS(2^(1/2)/Pi^(1/2)/(1/b)^(1/2)*(a+b*arcsin(c*x))^(1/2)/b)*(1/b)^(1/2)*2^(1/2)*Pi^(1/2)*a+2*arcsin(c*x)*sin((a+b*arcsin(c*x))/b-a/b)*b-cos((a+b*arcsin(c*x))/b-a/b)*b+2*sin((a+b*arcsin(c*x))/b-a/b)*a)/(a+b*arcsin(c*x))^(3/2)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{5/2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(a+b*arcsin(c*x))^(5/2), x, algorithm="maxima")

[Out] integrate((b*arcsin(c*x) + a)^(-5/2), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a+b*arcsin(c*x))^(5/2),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(a + b \operatorname{asin}(cx))^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a+b*asin(c*x))**(5/2),x)
```

```
[Out] Integral((a + b*asin(c*x))**(-5/2), x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \operatorname{arcsin}(cx) + a)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(a+b*arcsin(c*x))^(5/2),x, algorithm="giac")
```

```
[Out] integrate((b*arcsin(c*x) + a)^(-5/2), x)
```

$$3.201 \quad \int \frac{1}{x(a+b \sin^{-1}(cx))^{5/2}} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{1}{x(a+b \sin^{-1}(cx))^{5/2}}, x \right)$$

[Out] Unintegrable[1/(x*(a + b*ArcSin[c*x])^(5/2)), x]

Rubi [A] time = 0.0452953, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^{5/2}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x*(a + b*ArcSin[c*x])^(5/2)),x]

[Out] Defer[Int][1/(x*(a + b*ArcSin[c*x])^(5/2)), x]

Rubi steps

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^{5/2}} dx = \int \frac{1}{x(a+b \sin^{-1}(cx))^{5/2}} dx$$

Mathematica [A] time = 3.61281, size = 0, normalized size = 0.

$$\int \frac{1}{x(a+b \sin^{-1}(cx))^{5/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x*(a + b*ArcSin[c*x])^(5/2)),x]

[Out] Integrate[1/(x*(a + b*ArcSin[c*x])^(5/2)), x]

Maple [A] time = 0.073, size = 0, normalized size = 0.

$$\int \frac{1}{x} (a + b \arcsin(cx))^{-\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x/(a+b*arcsin(c*x))^(5/2),x)

[Out] `int(1/x/(a+b*arcsin(c*x))^(5/2),x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{5}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(5/2),x, algorithm="maxima")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(5/2)*x), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(5/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{x(a + b \arcsin(cx))^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*asin(c*x))**(5/2),x)`

[Out] `Integral(1/(x*(a + b*asin(c*x))**(5/2)), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{5}{2}} x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x/(a+b*arcsin(c*x))^(5/2),x, algorithm="giac")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(5/2)*x), x)`

$$3.202 \quad \int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{5/2}} dx$$

Optimal. Leaf size=18

$$\text{Unintegrable} \left(\frac{1}{x^2 (a + b \sin^{-1}(cx))^{5/2}}, x \right)$$

[Out] Unintegrable[1/(x^2*(a + b*ArcSin[c*x])^(5/2)), x]

Rubi [A] time = 0.0451862, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{5/2}} dx$$

Verification is Not applicable to the result.

[In] Int[1/(x^2*(a + b*ArcSin[c*x])^(5/2)),x]

[Out] Defer[Int][1/(x^2*(a + b*ArcSin[c*x])^(5/2)), x]

Rubi steps

$$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{5/2}} dx = \int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{5/2}} dx$$

Mathematica [A] time = 11.4478, size = 0, normalized size = 0.

$$\int \frac{1}{x^2 (a + b \sin^{-1}(cx))^{5/2}} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(x^2*(a + b*ArcSin[c*x])^(5/2)),x]

[Out] Integrate[1/(x^2*(a + b*ArcSin[c*x])^(5/2)), x]

Maple [A] time = 0.161, size = 0, normalized size = 0.

$$\int \frac{1}{x^2} (a + b \arcsin(cx))^{-\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/x^2/(a+b*arcsin(c*x))^(5/2),x)

[Out] `int(1/x^2/(a+b*arcsin(c*x))^(5/2),x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{5}{2}} x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(5/2),x, algorithm="maxima")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(5/2)*x^2), x)`

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(5/2),x, algorithm="fricas")`

[Out] Exception raised: UnboundLocalError

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x**2/(a+b*asin(c*x))**(5/2),x)`

[Out] Timed out

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(b \arcsin(cx) + a)^{\frac{5}{2}} x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/x^2/(a+b*arcsin(c*x))^(5/2),x, algorithm="giac")`

[Out] `integrate(1/((b*arcsin(c*x) + a)^(5/2)*x^2), x)`

3.203 $\int (dx)^{5/2} (a + b \sin^{-1}(cx)) dx$

Optimal. Leaf size=120

$$\frac{20bd^{5/2}\text{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right), -1\right)}{147c^{7/2}} + \frac{2(dx)^{7/2}(a + b\sin^{-1}(cx))}{7d} + \frac{20bd^2\sqrt{1-c^2x^2}\sqrt{dx}}{147c^3} + \frac{4b\sqrt{1-c^2x^2}(dx)^{5/2}}{49c}$$

[Out] $(20*b*d^2*\text{Sqrt}[d*x]*\text{Sqrt}[1 - c^2*x^2])/(147*c^3) + (4*b*(d*x)^{(5/2)}*\text{Sqrt}[1 - c^2*x^2])/(49*c) + (2*(d*x)^{(7/2)}*(a + b*\text{ArcSin}[c*x]))/(7*d) - (20*b*d^{(5/2)}*\text{EllipticF}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/(147*c^{(7/2)})$

Rubi [A] time = 0.075921, antiderivative size = 120, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4627, 321, 329, 221}

$$\frac{2(dx)^{7/2}(a + b\sin^{-1}(cx))}{7d} + \frac{20bd^2\sqrt{1-c^2x^2}\sqrt{dx}}{147c^3} - \frac{20bd^{5/2}F\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{147c^{7/2}} + \frac{4b\sqrt{1-c^2x^2}(dx)^{5/2}}{49c}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x]), x]$

[Out] $(20*b*d^2*\text{Sqrt}[d*x]*\text{Sqrt}[1 - c^2*x^2])/(147*c^3) + (4*b*(d*x)^{(5/2)}*\text{Sqrt}[1 - c^2*x^2])/(49*c) + (2*(d*x)^{(7/2)}*(a + b*\text{ArcSin}[c*x]))/(7*d) - (20*b*d^{(5/2)}*\text{EllipticF}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/(147*c^{(7/2)})$

Rule 4627

$\text{Int}[(a_.) + \text{ArcSin}[c_.*(x_.)]*(b_.)]^{(n_.)}*((d_.)*(x_.))^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{(m+1)}*(a + b*\text{ArcSin}[c*x])^{(n-1)}/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 321

$\text{Int}[(c_.)*(x_.))^{(m_.)}*((a_.) + (b_.)*(x_.)^{(n_.)})^{(p_.)}, x_Symbol] \rightarrow \text{Simp}[(c^{(n-1)}*(c*x)^{(m-n+1)}*(a + b*x^n)^{(p+1)})/(b*(m+n*p+1)), x] - \text{Dist}[(a*c^n*(m-n+1))/(b*(m+n*p+1)), \text{Int}[(c*x)^{(m-n)}*(a + b*x^n)^p, x], x] /;$ FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n-1] && NeQ[m+n*p+1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 329

$\text{Int}[(c_.)*(x_.))^{(m_.)}*((a_.) + (b_.)*(x_.)^{(n_.)})^{(p_.)}, x_Symbol] \rightarrow \text{With}[\{k = \text{Denominator}[m]\}, \text{Dist}[k/c, \text{Subst}[\text{Int}[x^{(k*(m+1)-1)}*(a + (b*x^{(k*n)})/c^n)^p, x], x, (c*x)^{(1/k)}], x]] /;$ FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && FractionQ[m] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 221

$\text{Int}[1/\text{Sqrt}[(a_.) + (b_.)*(x_.)^4], x_Symbol] \rightarrow \text{Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /;$ FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rubi steps

$$\begin{aligned}
\int (dx)^{5/2} (a + b \sin^{-1}(cx)) dx &= \frac{2(dx)^{7/2} (a + b \sin^{-1}(cx))}{7d} - \frac{(2bc) \int \frac{(dx)^{7/2}}{\sqrt{1-c^2x^2}} dx}{7d} \\
&= \frac{4b(dx)^{5/2} \sqrt{1-c^2x^2}}{49c} + \frac{2(dx)^{7/2} (a + b \sin^{-1}(cx))}{7d} - \frac{(10bd) \int \frac{(dx)^{3/2}}{\sqrt{1-c^2x^2}} dx}{49c} \\
&= \frac{20bd^2 \sqrt{dx} \sqrt{1-c^2x^2}}{147c^3} + \frac{4b(dx)^{5/2} \sqrt{1-c^2x^2}}{49c} + \frac{2(dx)^{7/2} (a + b \sin^{-1}(cx))}{7d} - \frac{(10bd^3) \int \frac{(dx)^{1/2}}{\sqrt{1-c^2x^2}} dx}{147c^3} \\
&= \frac{20bd^2 \sqrt{dx} \sqrt{1-c^2x^2}}{147c^3} + \frac{4b(dx)^{5/2} \sqrt{1-c^2x^2}}{49c} + \frac{2(dx)^{7/2} (a + b \sin^{-1}(cx))}{7d} - \frac{(20bd^2) \int \frac{(dx)^{1/2}}{\sqrt{1-c^2x^2}} dx}{147c^3} \\
&= \frac{20bd^2 \sqrt{dx} \sqrt{1-c^2x^2}}{147c^3} + \frac{4b(dx)^{5/2} \sqrt{1-c^2x^2}}{49c} + \frac{2(dx)^{7/2} (a + b \sin^{-1}(cx))}{7d} - \frac{20bd^{5/2} F\left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, c^2x^2\right)}{147c^3}
\end{aligned}$$

Mathematica [C] time = 0.0394848, size = 100, normalized size = 0.83

$$\frac{2d^2 \sqrt{dx} \left(-10b \operatorname{Hypergeometric2F1} \left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, c^2x^2 \right) + 21ac^3x^3 + 6bc^2x^2 \sqrt{1-c^2x^2} + 10b \sqrt{1-c^2x^2} + 21bc^3x^3 \sin^{-1}(cx) \right)}{147c^3}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^(5/2)*(a + b*ArcSin[c*x]),x]

[Out] (2*d^2*Sqrt[d*x]*(21*a*c^3*x^3 + 10*b*Sqrt[1 - c^2*x^2] + 6*b*c^2*x^2*Sqrt[1 - c^2*x^2] + 21*b*c^3*x^3*ArcSin[c*x] - 10*b*Hypergeometric2F1[1/4, 1/2, 5/4, c^2*x^2]))/(147*c^3)

Maple [A] time = 0.036, size = 144, normalized size = 1.2

$$2 \frac{1}{d} \left(\frac{1}{7} (dx)^{7/2} a + b \left(\frac{1}{7} (dx)^{7/2} \arcsin(cx) - \frac{2}{7} \frac{c}{d} \left(-\frac{1}{7} \frac{d^2 (dx)^{5/2} \sqrt{-c^2x^2 + 1}}{c^2} - \frac{5 d^4 \sqrt{dx} \sqrt{-c^2x^2 + 1}}{21 c^4} + \frac{5 d^4 \sqrt{-cx}}{21 c^4 \sqrt{-c^2x^2 + 1}} \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(5/2)*(a+b*arcsin(c*x)),x)

[Out] 2/d*(1/7*(d*x)^(7/2)*a+b*(1/7*(d*x)^(7/2)*arcsin(c*x)-2/7*c/d*(-1/7/c^2*d^2*(d*x)^(5/2)*(-c^2*x^2+1)^(1/2)-5/21/c^4*d^4*(d*x)^(1/2)*(-c^2*x^2+1)^(1/2)+5/21/c^4*d^4/(c/d)^(1/2)*(-c*x+1)^(1/2)*(c*x+1)^(1/2)/(-c^2*x^2+1)^(1/2)*EllipticF((d*x)^(1/2)*(c/d)^(1/2),I)))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(5/2)*(a+b*arcsin(c*x)),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\left(bd^2x^2 \arcsin(cx) + ad^2x^2\right)\sqrt{dx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(5/2)*(a+b*arcsin(c*x)),x, algorithm="fricas")
```

```
[Out] integral((b*d^2*x^2*arcsin(c*x) + a*d^2*x^2)*sqrt(d*x), x)
```

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)**(5/2)*(a+b*asin(c*x)),x)
```

```
[Out] Timed out
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int (dx)^{\frac{5}{2}} (b \arcsin(cx) + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(5/2)*(a+b*arcsin(c*x)),x, algorithm="giac")
```

```
[Out] integrate((d*x)^(5/2)*(b*arcsin(c*x) + a), x)
```

3.204 $\int (dx)^{3/2} (a + b \sin^{-1}(cx)) dx$

Optimal. Leaf size=124

$$\frac{12bd^{3/2}\text{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right), -1\right)}{25c^{5/2}} + \frac{2(dx)^{5/2}(a + b \sin^{-1}(cx))}{5d} - \frac{12bd^{3/2}E\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right)\middle| -1\right)}{25c^{5/2}} + \frac{4b\sqrt{1-c^2x^2}(dx)^{3/2}}{25c}$$

[Out] (4*b*(d*x)^(3/2)*Sqrt[1 - c^2*x^2])/(25*c) + (2*(d*x)^(5/2)*(a + b*ArcSin[c*x]))/(5*d) - (12*b*d^(3/2)*EllipticE[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(25*c^(5/2)) + (12*b*d^(3/2)*EllipticF[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(25*c^(5/2))

Rubi [A] time = 0.0984692, antiderivative size = 124, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.438, Rules used = {4627, 321, 329, 307, 221, 1199, 424}

$$\frac{2(dx)^{5/2}(a + b \sin^{-1}(cx))}{5d} + \frac{12bd^{3/2}F\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right)\middle| -1\right)}{25c^{5/2}} - \frac{12bd^{3/2}E\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right)\middle| -1\right)}{25c^{5/2}} + \frac{4b\sqrt{1-c^2x^2}(dx)^{3/2}}{25c}$$

Antiderivative was successfully verified.

[In] Int[(d*x)^(3/2)*(a + b*ArcSin[c*x]), x]

[Out] (4*b*(d*x)^(3/2)*Sqrt[1 - c^2*x^2])/(25*c) + (2*(d*x)^(5/2)*(a + b*ArcSin[c*x]))/(5*d) - (12*b*d^(3/2)*EllipticE[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(25*c^(5/2)) + (12*b*d^(3/2)*EllipticF[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(25*c^(5/2))

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 321

Int[((c_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(c^(n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), Int[(c*x)^(m - n)*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n - 1] && NeQ[m + n*p + 1, 0] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 329

Int[((c_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> With[{k = Denominator[m]}, Dist[k/c, Subst[Int[x^(k*(m + 1) - 1)*(a + (b*x^(k*n)))/c^n]^p, x], x, (c*x)^(1/k)], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && FractionQ[m] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 307

Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] :> With[{q = Rt[-(b/a), 2]}, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S

`qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]`

Rule 221

`Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]`

Rule 1199

`Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sqrt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]`

Rule 424

`Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]`

Rubi steps

$$\begin{aligned}
 \int (dx)^{3/2} (a + b \sin^{-1}(cx)) dx &= \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))}{5d} - \frac{(2bc) \int \frac{(dx)^{5/2}}{\sqrt{1-c^2x^2}} dx}{5d} \\
 &= \frac{4b(dx)^{3/2} \sqrt{1-c^2x^2}}{25c} + \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))}{5d} - \frac{(6bd) \int \frac{\sqrt{dx}}{\sqrt{1-c^2x^2}} dx}{25c} \\
 &= \frac{4b(dx)^{3/2} \sqrt{1-c^2x^2}}{25c} + \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))}{5d} - \frac{(12b) \text{Subst} \left(\int \frac{x^2}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{25c} \\
 &= \frac{4b(dx)^{3/2} \sqrt{1-c^2x^2}}{25c} + \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))}{5d} + \frac{(12bd) \text{Subst} \left(\int \frac{1}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{25c^2} \\
 &= \frac{4b(dx)^{3/2} \sqrt{1-c^2x^2}}{25c} + \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))}{5d} + \frac{12bd^{3/2} F \left(\sin^{-1} \left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}} \right) \middle| -1 \right)}{25c^{5/2}} - \frac{(12bd)}{25c^2} \\
 &= \frac{4b(dx)^{3/2} \sqrt{1-c^2x^2}}{25c} + \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))}{5d} - \frac{12bd^{3/2} E \left(\sin^{-1} \left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}} \right) \middle| -1 \right)}{25c^{5/2}} + \frac{12bd}{25c^2}
 \end{aligned}$$

Mathematica [C] time = 0.0248279, size = 66, normalized size = 0.53

$$\frac{2(dx)^{3/2} \left(-2b \text{Hypergeometric2F1} \left(\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, c^2x^2 \right) + 5acx + 2b\sqrt{1-c^2x^2} + 5bcx \sin^{-1}(cx) \right)}{25c}$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^(3/2)*(a + b*ArcSin[c*x]),x]

[Out] (2*(d*x)^(3/2)*(5*a*c*x + 2*b*Sqrt[1 - c^2*x^2] + 5*b*c*x*ArcSin[c*x] - 2*b*Hypergeometric2F1[1/2, 3/4, 7/4, c^2*x^2]))/(25*c)

Maple [A] time = 0.01, size = 138, normalized size = 1.1

$$2 \frac{1}{d} \left(\frac{1}{5} (dx)^{5/2} a + b \left(\frac{1}{5} (dx)^{5/2} \arcsin(cx) - \frac{2}{5} \frac{c}{d} \left(-\frac{1}{5} \frac{d^2 (dx)^{3/2} \sqrt{-c^2 x^2 + 1}}{c^2} - \frac{3}{5} \frac{d^3 \sqrt{-cx+1} \sqrt{cx+1}}{c^3 \sqrt{-c^2 x^2 + 1}} \right) \right) \right) \left(\text{EllipticF} \left(\frac{(dx)^{1/2}}{c} \sqrt{c^2 x^2 + 1}, I \right) - \text{EllipticE} \left(\frac{(dx)^{1/2}}{c} \sqrt{c^2 x^2 + 1}, I \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(3/2)*(a+b*arcsin(c*x)),x)

[Out] 2/d*(1/5*(d*x)^(5/2)*a+b*(1/5*(d*x)^(5/2)*arcsin(c*x)-2/5*c/d*(-1/5/c^2*d^2*(d*x)^(3/2)*(-c^2*x^2+1)^(1/2)-3/5/c^3*d^3/(c/d)^(1/2)*(-c*x+1)^(1/2)*(c*x+1)^(1/2)/(-c^2*x^2+1)^(1/2)*(EllipticF((d*x)^(1/2)*(c/d)^(1/2),I)-EllipticE((d*x)^(1/2)*(c/d)^(1/2),I))))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(3/2)*(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left((bdx \arcsin(cx) + adx) \sqrt{dx}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(3/2)*(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral((b*d*x*arcsin(c*x) + a*d*x)*sqrt(d*x), x)

Sympy [A] time = 163.098, size = 82, normalized size = 0.66

$$a \left(\begin{cases} 0 & \text{for } d = 0 \\ \frac{2(dx)^{5/2}}{5d} & \text{otherwise} \end{cases} \right) - bc \left(\begin{cases} 0 & \text{for } d = 0 \\ \frac{d^{3/2} x^{7/2} \Gamma(\frac{7}{4}) {}_2F_1 \left(\frac{1}{2}, \frac{7}{4} \middle| \frac{11}{4} \right) c^2 x^2 e^{2i\pi}}{5\Gamma(\frac{11}{4})} & \text{otherwise} \end{cases} \right) + b \left(\begin{cases} 0 & \text{for } d = 0 \\ \frac{2(dx)^{5/2}}{5d} & \text{otherwise} \end{cases} \right) \arcsin(cx)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**(3/2)*(a+b*asin(c*x)),x)

[Out] a*Piecewise((0, Eq(d, 0)), (2*(d*x)**(5/2)/(5*d), True)) - b*c*Piecewise((0, Eq(d, 0)), (d**(3/2)*x**(7/2)*gamma(7/4)*hyper((1/2, 7/4), (11/4,), c**2*

```
x**2*exp_polar(2*I*pi)/(5*gamma(11/4)), True)) + b*Piecewise((0, Eq(d, 0))
, (2*(d*x)**(5/2)/(5*d), True))*asin(c*x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int (dx)^{\frac{3}{2}} (b \arcsin(cx) + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(3/2)*(a+b*arcsin(c*x)),x, algorithm="giac")
```

```
[Out] integrate((d*x)^(3/2)*(b*arcsin(c*x) + a), x)
```

3.205 $\int \sqrt{dx} (a + b \sin^{-1}(cx)) dx$

Optimal. Leaf size=88

$$\frac{4b\sqrt{d}\text{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right), -1\right)}{9c^{3/2}} + \frac{2(dx)^{3/2}(a + b\sin^{-1}(cx))}{3d} + \frac{4b\sqrt{1-c^2x^2}\sqrt{dx}}{9c}$$

```
[Out] (4*b*Sqrt[d*x]*Sqrt[1 - c^2*x^2])/(9*c) + (2*(d*x)^(3/2)*(a + b*ArcSin[c*x])
)/(3*d) - (4*b*Sqrt[d]*EllipticF[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])
/(9*c^(3/2))
```

Rubi [A] time = 0.044585, antiderivative size = 88, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {4627, 321, 329, 221}

$$\frac{2(dx)^{3/2}(a + b\sin^{-1}(cx))}{3d} + \frac{4b\sqrt{1-c^2x^2}\sqrt{dx}}{9c} - \frac{4b\sqrt{d}F\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right)\middle| -1\right)}{9c^{3/2}}$$

Antiderivative was successfully verified.

```
[In] Int[Sqrt[d*x]*(a + b*ArcSin[c*x]),x]
```

```
[Out] (4*b*Sqrt[d*x]*Sqrt[1 - c^2*x^2])/(9*c) + (2*(d*x)^(3/2)*(a + b*ArcSin[c*x])
)/(3*d) - (4*b*Sqrt[d]*EllipticF[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])
/(9*c^(3/2))
```

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 321

```
Int[((c_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[(c^(
n - 1)*(c*x)^(m - n + 1)*(a + b*x^n)^(p + 1))/(b*(m + n*p + 1)), x] - Dist[
(a*c^n*(m - n + 1))/(b*(m + n*p + 1)), Int[(c*x)^(m - n)*(a + b*x^n)^p, x],
x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && GtQ[m, n - 1] && NeQ[m + n*p
+ 1, 0] && IntBinomialQ[a, b, c, n, m, p, x]
```

Rule 329

```
Int[((c_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> With[{k =
Denominator[m]}, Dist[k/c, Subst[Int[x^(k*(m + 1) - 1)*(a + (b*x^(k*n)))/c^
n]^p, x], x, (c*x)^(1/k)], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && F
ractionQ[m] && IntBinomialQ[a, b, c, n, m, p, x]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] :> Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \sqrt{dx} (a + b \sin^{-1}(cx)) dx &= \frac{2(dx)^{3/2} (a + b \sin^{-1}(cx))}{3d} - \frac{(2bc) \int \frac{(dx)^{3/2}}{\sqrt{1-c^2x^2}} dx}{3d} \\
&= \frac{4b\sqrt{dx}\sqrt{1-c^2x^2}}{9c} + \frac{2(dx)^{3/2} (a + b \sin^{-1}(cx))}{3d} - \frac{(2bd) \int \frac{1}{\sqrt{dx}\sqrt{1-c^2x^2}} dx}{9c} \\
&= \frac{4b\sqrt{dx}\sqrt{1-c^2x^2}}{9c} + \frac{2(dx)^{3/2} (a + b \sin^{-1}(cx))}{3d} - \frac{(4b) \text{Subst} \left(\int \frac{1}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{9c} \\
&= \frac{4b\sqrt{dx}\sqrt{1-c^2x^2}}{9c} + \frac{2(dx)^{3/2} (a + b \sin^{-1}(cx))}{3d} - \frac{4b\sqrt{d}F \left(\sin^{-1} \left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}} \right) \middle| -1 \right)}{9c^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.0172088, size = 66, normalized size = 0.75

$$\frac{2\sqrt{dx} \left(-2b \text{Hypergeometric2F1} \left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, c^2x^2 \right) + 3acx + 2b\sqrt{1-c^2x^2} + 3bcx \sin^{-1}(cx) \right)}{9c}$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[d*x]*(a + b*ArcSin[c*x]),x]

[Out] (2*Sqrt[d*x]*(3*a*c*x + 2*b*Sqrt[1 - c^2*x^2] + 3*b*c*x*ArcSin[c*x] - 2*b*Hypergeometric2F1[1/4, 1/2, 5/4, c^2*x^2]))/(9*c)

Maple [A] time = 0.008, size = 119, normalized size = 1.4

$$2 \frac{1}{d} \left(\frac{1}{3} (dx)^{3/2} a + b \left(\frac{1}{3} (dx)^{3/2} \arcsin(cx) - \frac{2}{3} \frac{c}{d} \left(-\frac{1}{3} \frac{d^2 \sqrt{dx} \sqrt{-c^2x^2 + 1}}{c^2} + \frac{1}{3} \frac{d^2 \sqrt{-cx + 1} \sqrt{cx + 1}}{c^2 \sqrt{-c^2x^2 + 1}} \text{EllipticF} \left(\sqrt{dx}, \dots \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(1/2)*(a+b*arcsin(c*x)),x)

[Out] 2/d*(1/3*(d*x)^(3/2)*a+b*(1/3*(d*x)^(3/2)*arcsin(c*x)-2/3*c/d*(-1/3/c^2*d^2*(d*x)^(1/2)*(-c^2*x^2+1)^(1/2)+1/3/c^2*d^2/(c/d)^(1/2)*(-c*x+1)^(1/2)*(c*x+1)^(1/2)/(-c^2*x^2+1)^(1/2)*EllipticF((d*x)^(1/2)*(c/d)^(1/2),I)))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\sqrt{dx}(b \arcsin(cx) + a), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(sqrt(d*x)*(b*arcsin(c*x) + a), x)

Sympy [A] time = 4.41945, size = 76, normalized size = 0.86

$$\frac{2a(dx)^{\frac{3}{2}}}{3d} - \frac{bc(dx)^{\frac{5}{2}}\Gamma\left(\frac{5}{4}\right) {}_2F_1\left(\frac{1}{2}, \frac{5}{4} \middle| \frac{9}{4}; c^2x^2e^{2i\pi}\right)}{3d^2\Gamma\left(\frac{9}{4}\right)} + \frac{2b(dx)^{\frac{3}{2}}\text{asin}(cx)}{3d}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**(1/2)*(a+b*asin(c*x)),x)

[Out] 2*a*(d*x)**(3/2)/(3*d) - b*c*(d*x)**(5/2)*gamma(5/4)*hyper((1/2, 5/4), (9/4,), c**2*x**2*exp_polar(2*I*pi))/(3*d**2*gamma(9/4)) + 2*b*(d*x)**(3/2)*asin(c*x)/(3*d)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{dx}(b \arcsin(cx) + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] integrate(sqrt(d*x)*(b*arcsin(c*x) + a), x)

$$3.206 \quad \int \frac{a+b \sin^{-1}(cx)}{\sqrt{dx}} dx$$

Optimal. Leaf size=89

$$\frac{4b \operatorname{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right), -1\right)}{\sqrt{c}\sqrt{d}} + \frac{2\sqrt{dx}(a+b \sin^{-1}(cx))}{d} - \frac{4bE\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{\sqrt{c}\sqrt{d}}$$

[Out] (2*Sqrt[d*x]*(a + b*ArcSin[c*x]))/d - (4*b*EllipticE[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(Sqrt[c]*Sqrt[d]) + (4*b*EllipticF[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(Sqrt[c]*Sqrt[d])

Rubi [A] time = 0.0780528, antiderivative size = 89, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 6, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {4627, 329, 307, 221, 1199, 424}

$$\frac{2\sqrt{dx}(a+b \sin^{-1}(cx))}{d} + \frac{4bF\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{\sqrt{c}\sqrt{d}} - \frac{4bE\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{\sqrt{c}\sqrt{d}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])/Sqrt[d*x], x]

[Out] (2*Sqrt[d*x]*(a + b*ArcSin[c*x]))/d - (4*b*EllipticE[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(Sqrt[c]*Sqrt[d]) + (4*b*EllipticF[ArcSin[(Sqrt[c]*Sqrt[d*x])/Sqrt[d]], -1])/(Sqrt[c]*Sqrt[d])

Rule 4627

```
Int[((a_.) + ArcSin[(c_.)*(x_)]*(b_.))^(n_.)*((d_.)*(x_))^(m_.), x_Symbol]
:= Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)
)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2
*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]
```

Rule 329

```
Int[((c_.)*(x_))^(m_)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := With[{k =
Denominator[m]}, Dist[k/c, Subst[Int[x^(k*(m + 1) - 1)*(a + (b*x^(k*n)))/c^
n]^(p), x], x, (c*x)^(1/k)], x] /; FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && F
ractionQ[m] && IntBinomialQ[a, b, c, n, m, p, x]
```

Rule 307

```
Int[(x_)^2/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := With[{q = Rt[-(b/a), 2]}
, -Dist[q^(-1), Int[1/Sqrt[a + b*x^4], x], x] + Dist[1/q, Int[(1 + q*x^2)/S
qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]
```

Rule 221

```
Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b,
4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[
b/a] && GtQ[a, 0]
```

Rule 1199

```
Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sq
rt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c,
d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]
```

Rule 424

```
Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[
(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c
), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{a + b \sin^{-1}(cx)}{\sqrt{dx}} dx &= \frac{2\sqrt{dx}(a + b \sin^{-1}(cx))}{d} - \frac{(2bc) \int \frac{\sqrt{dx}}{\sqrt{1-c^2x^2}} dx}{d} \\
&= \frac{2\sqrt{dx}(a + b \sin^{-1}(cx))}{d} - \frac{(4bc) \operatorname{Subst} \left(\int \frac{x^2}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{d^2} \\
&= \frac{2\sqrt{dx}(a + b \sin^{-1}(cx))}{d} + \frac{(4b) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{d} - \frac{(4b) \operatorname{Subst} \left(\int \frac{1+\frac{cx^2}{d}}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{d} \\
&= \frac{2\sqrt{dx}(a + b \sin^{-1}(cx))}{d} + \frac{4bF \left(\sin^{-1} \left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}} \right) \middle| -1 \right)}{\sqrt{c}\sqrt{d}} - \frac{(4b) \operatorname{Subst} \left(\int \frac{\sqrt{1+\frac{cx^2}{d}}}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{d} \\
&= \frac{2\sqrt{dx}(a + b \sin^{-1}(cx))}{d} - \frac{4bE \left(\sin^{-1} \left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}} \right) \middle| -1 \right)}{\sqrt{c}\sqrt{d}} + \frac{4bF \left(\sin^{-1} \left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}} \right) \middle| -1 \right)}{\sqrt{c}\sqrt{d}}
\end{aligned}$$

Mathematica [C] time = 0.0146566, size = 45, normalized size = 0.51

$$\frac{2x \left(3(a + b \sin^{-1}(cx)) - 2bcx \operatorname{Hypergeometric2F1} \left(\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, c^2x^2 \right) \right)}{3\sqrt{dx}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(a + b*ArcSin[c*x])/Sqrt[d*x], x]
```

```
[Out] (2*x*(3*(a + b*ArcSin[c*x]) - 2*b*c*x*Hypergeometric2F1[1/2, 3/4, 7/4, c^2*x^2]))/(3*Sqrt[d*x])
```

Maple [A] time = 0.009, size = 98, normalized size = 1.1

$$\frac{2}{d} \left(a\sqrt{dx} + b \left(\sqrt{dx} \arcsin(cx) + 2 \frac{\sqrt{-cx+1}\sqrt{cx+1}}{\sqrt{-c^2x^2+1}} \left(\operatorname{EllipticF} \left(\sqrt{dx}\sqrt{\frac{c}{d}}, i \right) - \operatorname{EllipticE} \left(\sqrt{dx}\sqrt{\frac{c}{d}}, i \right) \right) \frac{1}{\sqrt{\frac{c}{d}}} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((a+b*arcsin(c*x))/(d*x)^(1/2),x)
```

```
[Out] 2/d*(a*(d*x)^(1/2)+b*((d*x)^(1/2)*arcsin(c*x)+2/(c/d)^(1/2)*(-c*x+1)^(1/2)*
(c*x+1)^(1/2)/(-c^2*x^2+1)^(1/2)*(EllipticF((d*x)^(1/2)*(c/d)^(1/2),I)-Elli
pticE((d*x)^(1/2)*(c/d)^(1/2),I)))
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))/(d*x)^(1/2),x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{dx}(b \arcsin(cx) + a)}{dx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))/(d*x)^(1/2),x, algorithm="fricas")
```

```
[Out] integral(sqrt(d*x)*(b*arcsin(c*x) + a)/(d*x), x)
```

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*asin(c*x))/(d*x)**(1/2),x)
```

```
[Out] Exception raised: TypeError
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{b \arcsin(cx) + a}{\sqrt{dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))/(d*x)^(1/2),x, algorithm="giac")
```

```
[Out] integrate((b*arcsin(c*x) + a)/sqrt(d*x), x)
```

$$3.207 \quad \int \frac{a+b \sin^{-1}(cx)}{(dx)^{3/2}} dx$$

Optimal. Leaf size=55

$$\frac{4b\sqrt{c}\text{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right), -1\right)}{d^{3/2}} - \frac{2(a+b \sin^{-1}(cx))}{d\sqrt{dx}}$$

[Out] $(-2*(a + b*\text{ArcSin}[c*x]))/(d*\text{Sqrt}[d*x]) + (4*b*\text{Sqrt}[c]*\text{EllipticF}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/d^{(3/2)}$

Rubi [A] time = 0.0377391, antiderivative size = 55, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.188$, Rules used = {4627, 329, 221}

$$\frac{4b\sqrt{c}F\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{d^{3/2}} - \frac{2(a+b \sin^{-1}(cx))}{d\sqrt{dx}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*\text{ArcSin}[c*x])/(d*x)^{(3/2)}, x]$

[Out] $(-2*(a + b*\text{ArcSin}[c*x]))/(d*\text{Sqrt}[d*x]) + (4*b*\text{Sqrt}[c]*\text{EllipticF}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/d^{(3/2)}$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(d*x)^m, x_Symbol] \rightarrow \text{Simp}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}/\text{Sqrt}[1 - c^2*x^2], x], x] /; \text{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{NeQ}[m, -1]$

Rule 329

$\text{Int}[(c*x)^m*(a + b*x^n)^p, x_Symbol] \rightarrow \text{With}\{k = \text{Denominator}[m]\}, \text{Dist}[k/c, \text{Subst}[\text{Int}[x^{k*(m+1)-1}*(a + (b*x^{k*n}))^p/c^n], x, (c*x)^{1/k}], x] /; \text{FreeQ}\{a, b, c, p\}, x \ \&\& \ \text{IGtQ}[n, 0] \ \&\& \ \text{FractionQ}[m] \ \&\& \ \text{IntBinomialQ}[a, b, c, n, m, p, x]$

Rule 221

$\text{Int}[1/\text{Sqrt}[(a + b*x^4)], x_Symbol] \rightarrow \text{Simp}[\text{EllipticF}[\text{ArcSin}[(\text{Rt}[-b, 4]*x)/\text{Rt}[a, 4]], -1]/(\text{Rt}[a, 4]*\text{Rt}[-b, 4]), x] /; \text{FreeQ}\{a, b\}, x \ \&\& \ \text{NegQ}[b/a] \ \&\& \ \text{GtQ}[a, 0]$

Rubi steps

$$\begin{aligned}
\int \frac{a + b \sin^{-1}(cx)}{(dx)^{3/2}} dx &= -\frac{2(a + b \sin^{-1}(cx))}{d\sqrt{dx}} + \frac{(2bc) \int \frac{1}{\sqrt{dx}\sqrt{1-c^2x^2}} dx}{d} \\
&= -\frac{2(a + b \sin^{-1}(cx))}{d\sqrt{dx}} + \frac{(4bc) \operatorname{Subst} \left(\int \frac{1}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx} \right)}{d^2} \\
&= -\frac{2(a + b \sin^{-1}(cx))}{d\sqrt{dx}} + \frac{4b\sqrt{c}F \left(\sin^{-1} \left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}} \right) \middle| -1 \right)}{d^{3/2}}
\end{aligned}$$

Mathematica [C] time = 0.0134947, size = 40, normalized size = 0.73

$$-\frac{2x \left(-2bcx \operatorname{Hypergeometric2F1} \left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, c^2x^2 \right) + a + b \sin^{-1}(cx) \right)}{(dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])/(d*x)^(3/2), x]

[Out] (-2*x*(a + b*ArcSin[c*x] - 2*b*c*x*Hypergeometric2F1[1/4, 1/2, 5/4, c^2*x^2]))/(d*x)^(3/2)

Maple [A] time = 0.009, size = 85, normalized size = 1.6

$$2 \frac{1}{d} \left(-\frac{a}{\sqrt{dx}} + b \left(-\frac{\arcsin(cx)}{\sqrt{dx}} + 2 \frac{c\sqrt{-cx+1}\sqrt{cx+1}}{d\sqrt{-c^2x^2+1}} \operatorname{EllipticF} \left(\sqrt{dx} \sqrt{\frac{c}{d}}, i \right) \frac{1}{\sqrt{\frac{c}{d}}} \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))/(d*x)^(3/2), x)

[Out] 2/d*(-a/(d*x)^(1/2)+b*(-1/(d*x)^(1/2)*arcsin(c*x)+2*c/d/(c/d)^(1/2)*(-c*x+1)^(1/2)*(c*x+1)^(1/2)/(-c^2*x^2+1)^(1/2)*EllipticF((d*x)^(1/2)*(c/d)^(1/2), I)))

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/(d*x)^(3/2), x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{dx}(b \arcsin(cx) + a)}{d^2x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/(d*x)^(3/2),x, algorithm="fricas")

[Out] integral(sqrt(d*x)*(b*arcsin(c*x) + a)/(d^2*x^2), x)

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))/(d*x)**(3/2),x)

[Out] Exception raised: TypeError

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{b \arcsin(cx) + a}{(dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))/(d*x)^(3/2),x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)/(d*x)^(3/2), x)

$$3.208 \quad \int \frac{a+b \sin^{-1}(cx)}{(dx)^{5/2}} dx$$

Optimal. Leaf size=125

$$\frac{4bc^{3/2}\text{EllipticF}\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right), -1\right)}{3d^{5/2}} - \frac{2(a+b \sin^{-1}(cx))}{3d(dx)^{3/2}} - \frac{4bc\sqrt{1-c^2x^2}}{3d^2\sqrt{dx}} - \frac{4bc^{3/2}E\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right)\right) - 1}{3d^{5/2}}$$

[Out] $(-4*b*c*\text{Sqrt}[1 - c^2*x^2])/(3*d^2*\text{Sqrt}[d*x]) - (2*(a + b*\text{ArcSin}[c*x]))/(3*d*(d*x)^{(3/2)}) - (4*b*c^{(3/2)}*\text{EllipticE}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/(3*d^{(5/2)}) + (4*b*c^{(3/2)}*\text{EllipticF}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/(3*d^{(5/2)})$

Rubi [A] time = 0.0968909, antiderivative size = 125, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 7, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.438$, Rules used = {4627, 325, 329, 307, 221, 1199, 424}

$$-\frac{2(a+b \sin^{-1}(cx))}{3d(dx)^{3/2}} - \frac{4bc\sqrt{1-c^2x^2}}{3d^2\sqrt{dx}} + \frac{4bc^{3/2}F\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right)\right) - 1}{3d^{5/2}} - \frac{4bc^{3/2}E\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right)\right) - 1}{3d^{5/2}}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(a + b*\text{ArcSin}[c*x])/(d*x)^{(5/2)}, x]$

[Out] $(-4*b*c*\text{Sqrt}[1 - c^2*x^2])/(3*d^2*\text{Sqrt}[d*x]) - (2*(a + b*\text{ArcSin}[c*x]))/(3*d*(d*x)^{(3/2)}) - (4*b*c^{(3/2)}*\text{EllipticE}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/(3*d^{(5/2)}) + (4*b*c^{(3/2)}*\text{EllipticF}[\text{ArcSin}[(\text{Sqrt}[c]*\text{Sqrt}[d*x])/\text{Sqrt}[d]], -1])/(3*d^{(5/2)})$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b*x)^n*(d*x)^m, x_Symbol] \rightarrow \text{Simp}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c^n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 325

$\text{Int}[(c*x)^m*(a + b*x^n)^p, x_Symbol] \rightarrow \text{Simp}[(c*x)^{m+1}*(a + b*x^n)^{p+1}/(a*c*(m+1)), x] - \text{Dist}[(b*(m+n*(p+1)+1))/(a*c^n*(m+1)), \text{Int}[(c*x)^{m+n}*(a + b*x^n)^p, x], x] /;$ FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && LtQ[m, -1] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 329

$\text{Int}[(c*x)^m*(a + b*x^n)^p, x_Symbol] \rightarrow \text{With}[\{k = \text{Denominator}[m]\}, \text{Dist}[k/c, \text{Subst}[\text{Int}[x^{k*(m+1)-1}*(a + (b*x^{k*n}))^p/c^n], x], (c*x)^{1/k}], x] /;$ FreeQ[{a, b, c, p}, x] && IGtQ[n, 0] && FractionQ[m] && IntBinomialQ[a, b, c, n, m, p, x]

Rule 307

$\text{Int}[x^2/\text{Sqrt}[a + b*x^4], x_Symbol] \rightarrow \text{With}[\{q = \text{Rt}[-(b/a), 2]\}, -\text{Dist}[q^{-1}, \text{Int}[1/\text{Sqrt}[a + b*x^4], x], x] + \text{Dist}[1/q, \text{Int}[(1 + q*x^2)/\text{Sqrt}[a + b*x^4], x], x] /;$

qrt[a + b*x^4], x], x]] /; FreeQ[{a, b}, x] && NegQ[b/a]

Rule 221

Int[1/Sqrt[(a_) + (b_.)*(x_)^4], x_Symbol] := Simp[EllipticF[ArcSin[(Rt[-b, 4]*x)/Rt[a, 4]], -1]/(Rt[a, 4]*Rt[-b, 4]), x] /; FreeQ[{a, b}, x] && NegQ[b/a] && GtQ[a, 0]

Rule 1199

Int[((d_) + (e_.)*(x_)^2)/Sqrt[(a_) + (c_.)*(x_)^4], x_Symbol] := Dist[d/Sqrt[a], Int[Sqrt[1 + (e*x^2)/d]/Sqrt[1 - (e*x^2)/d], x], x] /; FreeQ[{a, c, d, e}, x] && NegQ[c/a] && EqQ[c*d^2 + a*e^2, 0] && GtQ[a, 0]

Rule 424

Int[Sqrt[(a_) + (b_.)*(x_)^2]/Sqrt[(c_) + (d_.)*(x_)^2], x_Symbol] := Simp[(Sqrt[a]*EllipticE[ArcSin[Rt[-(d/c), 2]*x], (b*c)/(a*d)])/(Sqrt[c]*Rt[-(d/c), 2]), x] /; FreeQ[{a, b, c, d}, x] && NegQ[d/c] && GtQ[c, 0] && GtQ[a, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{a + b \sin^{-1}(cx)}{(dx)^{5/2}} dx &= -\frac{2(a + b \sin^{-1}(cx))}{3d(dx)^{3/2}} + \frac{(2bc) \int \frac{1}{(dx)^{3/2} \sqrt{1-c^2x^2}} dx}{3d} \\
 &= -\frac{4bc\sqrt{1-c^2x^2}}{3d^2\sqrt{dx}} - \frac{2(a + b \sin^{-1}(cx))}{3d(dx)^{3/2}} - \frac{(2bc^3) \int \frac{\sqrt{dx}}{\sqrt{1-c^2x^2}} dx}{3d^3} \\
 &= -\frac{4bc\sqrt{1-c^2x^2}}{3d^2\sqrt{dx}} - \frac{2(a + b \sin^{-1}(cx))}{3d(dx)^{3/2}} - \frac{(4bc^3) \text{Subst}\left(\int \frac{x^2}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx}\right)}{3d^4} \\
 &= -\frac{4bc\sqrt{1-c^2x^2}}{3d^2\sqrt{dx}} - \frac{2(a + b \sin^{-1}(cx))}{3d(dx)^{3/2}} + \frac{(4bc^2) \text{Subst}\left(\int \frac{1}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx}\right)}{3d^3} - \frac{(4bc^2) \text{Subst}\left(\int \frac{\sqrt{1+\frac{c^2x^4}{d^2}}}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx}\right)}{3d^3} \\
 &= -\frac{4bc\sqrt{1-c^2x^2}}{3d^2\sqrt{dx}} - \frac{2(a + b \sin^{-1}(cx))}{3d(dx)^{3/2}} + \frac{4bc^{3/2} F\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{3d^{5/2}} - \frac{(4bc^2) \text{Subst}\left(\int \frac{\sqrt{1+\frac{c^2x^4}{d^2}}}{\sqrt{1-\frac{c^2x^4}{d^2}}} dx, x, \sqrt{dx}\right)}{3d^3} \\
 &= -\frac{4bc\sqrt{1-c^2x^2}}{3d^2\sqrt{dx}} - \frac{2(a + b \sin^{-1}(cx))}{3d(dx)^{3/2}} - \frac{4bc^{3/2} E\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{3d^{5/2}} + \frac{4bc^{3/2} F\left(\sin^{-1}\left(\frac{\sqrt{c}\sqrt{dx}}{\sqrt{d}}\right) \middle| -1\right)}{3d^{5/2}}
 \end{aligned}$$

Mathematica [C] time = 0.015386, size = 42, normalized size = 0.34

$$\frac{2x \left(2bcx \text{Hypergeometric2F1}\left(-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, c^2x^2\right) + a + b \sin^{-1}(cx) \right)}{3(dx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])/(d*x)^(5/2), x]

[Out] $(-2*x*(a + b*\text{ArcSin}[c*x] + 2*b*c*x*\text{Hypergeometric2F1}[-1/4, 1/2, 3/4, c^2*x^2]))/(3*(d*x)^(5/2))$

Maple [A] time = 0.013, size = 129, normalized size = 1.

$$2 \frac{1}{d} \left(-\frac{1}{3} \frac{a}{(dx)^{3/2}} + b \left(-\frac{1}{3} \frac{\arcsin(cx)}{(dx)^{3/2}} + 2/3 \frac{c}{d} \left(-\frac{\sqrt{-c^2x^2+1}}{\sqrt{dx}} + \frac{c\sqrt{-cx+1}\sqrt{cx+1}}{d\sqrt{-c^2x^2+1}} \left(\text{EllipticF} \left(\sqrt{dx} \sqrt{\frac{c}{d}}, i \right) - \text{EllipticE} \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*arcsin(c*x))/(d*x)^(5/2),x)`

[Out] $2/d*(-1/3*a/(d*x)^(3/2)+b*(-1/3/(d*x)^(3/2)*\arcsin(c*x)+2/3*c/d*(-(-c^2*x^2+1)^(1/2)/(d*x)^(1/2)+c/d/(c/d)^(1/2)*(-c*x+1)^(1/2)*(c*x+1)^(1/2)/(-c^2*x^2+1)^(1/2)*(EllipticF((d*x)^(1/2)*(c/d)^(1/2),I)-EllipticE((d*x)^(1/2)*(c/d)^(1/2),I))))$

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))/(d*x)^(5/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{\sqrt{dx}(b \arcsin(cx) + a)}{d^3x^3}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))/(d*x)^(5/2),x, algorithm="fricas")`

[Out] `integral(sqrt(d*x)*(b*arcsin(c*x) + a)/(d^3*x^3), x)`

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))/(d*x)**(5/2),x)`

[Out] Exception raised: TypeError

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{b \arcsin(cx) + a}{(dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))/(d*x)^(5/2),x, algorithm="giac")
```

```
[Out] integrate((b*arcsin(c*x) + a)/(d*x)^(5/2), x)
```

3.209 $\int (dx)^{5/2} (a + b \sin^{-1}(cx))^2 dx$

Optimal. Leaf size=109

$$\frac{16b^2c^2(dx)^{11/2}\text{HypergeometricPFQ}\left(\left\{1, \frac{11}{4}, \frac{11}{4}\right\}, \left\{\frac{13}{4}, \frac{15}{4}\right\}, c^2x^2\right)}{693d^3} - \frac{8bc(dx)^{9/2}\text{Hypergeometric2F1}\left(\frac{1}{2}, \frac{9}{4}, \frac{13}{4}, c^2x^2\right)(a + b \sin^{-1}(cx))}{63d^2}$$

[Out] $(2*(d*x)^{(7/2)}*(a + b*\text{ArcSin}[c*x])^2)/(7*d) - (8*b*c*(d*x)^{(9/2)}*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/2, 9/4, 13/4, c^2*x^2])/(63*d^2) + (16*b^2*c^2*(d*x)^{(11/2)}*\text{HypergeometricPFQ}[\{1, 11/4, 11/4\}, \{13/4, 15/4\}, c^2*x^2])/(693*d^3)$

Rubi [A] time = 0.140792, antiderivative size = 109, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4627, 4711}

$$\frac{16b^2c^2(dx)^{11/2} {}_3F_2\left(1, \frac{11}{4}, \frac{11}{4}; \frac{13}{4}, \frac{15}{4}; c^2x^2\right)}{693d^3} - \frac{8bc(dx)^{9/2} {}_2F_1\left(\frac{1}{2}, \frac{9}{4}; \frac{13}{4}; c^2x^2\right)(a + b \sin^{-1}(cx))}{63d^2} + \frac{2(dx)^{7/2}(a + b \sin^{-1}(cx))^2}{7d}$$

Antiderivative was successfully verified.

[In] Int[(d*x)^(5/2)*(a + b*ArcSin[c*x])^2,x]

[Out] $(2*(d*x)^{(7/2)}*(a + b*\text{ArcSin}[c*x])^2)/(7*d) - (8*b*c*(d*x)^{(9/2)}*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/2, 9/4, 13/4, c^2*x^2])/(63*d^2) + (16*b^2*c^2*(d*x)^{(11/2)}*\text{HypergeometricPFQ}[\{1, 11/4, 11/4\}, \{13/4, 15/4\}, c^2*x^2])/(693*d^3)$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((d_.)*(x_.))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4711

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))*((f_.)*(x_.))^(m_.))/Sqrt[(d_.) + (e_.)*(x_.)^2], x_Symbol] :> Simp[((f*x)^(m + 1)*(a + b*ArcSin[c*x])*Hypergeometric2F1[1/2, (1 + m)/2, (3 + m)/2, c^2*x^2])/(Sqrt[d]*f*(m + 1)), x] - Simp[(b*c*(f*x)^(m + 2)*HypergeometricPFQ[{1, 1 + m/2, 1 + m/2}, {3/2 + m/2, 2 + m/2}, c^2*x^2])/(Sqrt[d]*f^2*(m + 1)*(m + 2)), x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int (dx)^{5/2} (a + b \sin^{-1}(cx))^2 dx &= \frac{2(dx)^{7/2} (a + b \sin^{-1}(cx))^2}{7d} - \frac{(4bc) \int \frac{(dx)^{7/2} (a + b \sin^{-1}(cx))}{\sqrt{1 - c^2x^2}} dx}{7d} \\ &= \frac{2(dx)^{7/2} (a + b \sin^{-1}(cx))^2}{7d} - \frac{8bc(dx)^{9/2} (a + b \sin^{-1}(cx)) {}_2F_1\left(\frac{1}{2}, \frac{9}{4}; \frac{13}{4}; c^2x^2\right)}{63d^2} + \frac{16b^2c^2(dx)^{11/2} {}_3F_2\left(1, \frac{11}{4}, \frac{11}{4}; \frac{13}{4}, \frac{15}{4}; c^2x^2\right)}{693d^3} \end{aligned}$$

Mathematica [A] time = 0.0609168, size = 90, normalized size = 0.83

$$\frac{2}{693}x(dx)^{5/2} \left(8b^2c^2x^2 \text{HypergeometricPFQ} \left(\left\{ 1, \frac{11}{4}, \frac{11}{4} \right\}, \left\{ \frac{13}{4}, \frac{15}{4} \right\}, c^2x^2 \right) + 11(a + b \sin^{-1}(cx)) \left(9(a + b \sin^{-1}(cx)) \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^(5/2)*(a + b*ArcSin[c*x])^2,x]

[Out] (2*x*(d*x)^(5/2)*(11*(a + b*ArcSin[c*x])*(9*(a + b*ArcSin[c*x]) - 4*b*c*x*Hypergeometric2F1[1/2, 9/4, 13/4, c^2*x^2]) + 8*b^2*c^2*x^2*HypergeometricPFQ[{1, 11/4, 11/4}, {13/4, 15/4}, c^2*x^2]))/693

Maple [F] time = 0.158, size = 0, normalized size = 0.

$$\int (dx)^{\frac{5}{2}} (a + b \arcsin(cx))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(5/2)*(a+b*arcsin(c*x))^2,x)

[Out] int((d*x)^(5/2)*(a+b*arcsin(c*x))^2,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(5/2)*(a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left((b^2d^2x^2 \arcsin(cx))^2 + 2abd^2x^2 \arcsin(cx) + a^2d^2x^2 \right) \sqrt{dx}, x$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(5/2)*(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] integral((b^2*d^2*x^2*arcsin(c*x)^2 + 2*a*b*d^2*x^2*arcsin(c*x) + a^2*d^2*x^2)*sqrt(d*x), x)

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**(5/2)*(a+b*asin(c*x))**2,x)

[Out] Timed out

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int (dx)^{\frac{5}{2}} (b \arcsin(cx) + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(5/2)*(a+b*arcsin(c*x))^2,x, algorithm="giac")

[Out] integrate((d*x)^(5/2)*(b*arcsin(c*x) + a)^2, x)

3.210 $\int (dx)^{3/2} (a + b \sin^{-1}(cx))^2 dx$

Optimal. Leaf size=109

$$\frac{16b^2c^2(dx)^{9/2}\text{HypergeometricPFQ}\left(\left\{1, \frac{9}{4}, \frac{9}{4}\right\}, \left\{\frac{11}{4}, \frac{13}{4}\right\}, c^2x^2\right)}{315d^3} - \frac{8bc(dx)^{7/2}\text{Hypergeometric2F1}\left(\frac{1}{2}, \frac{7}{4}, \frac{11}{4}, c^2x^2\right)(a + b \sin^{-1}(cx))}{35d^2}$$

[Out] $(2*(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])^2)/(5*d) - (8*b*c*(d*x)^{(7/2)}*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/2, 7/4, 11/4, c^2*x^2])/(35*d^2) + (16*b^2*c^2*(d*x)^{(9/2)}*\text{HypergeometricPFQ}[\{1, 9/4, 9/4\}, \{11/4, 13/4\}, c^2*x^2])/(315*d^3)$

Rubi [A] time = 0.141035, antiderivative size = 109, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4627, 4711}

$$\frac{16b^2c^2(dx)^{9/2} {}_3F_2\left(1, \frac{9}{4}, \frac{9}{4}; \frac{11}{4}, \frac{13}{4}; c^2x^2\right)}{315d^3} - \frac{8bc(dx)^{7/2} {}_2F_1\left(\frac{1}{2}, \frac{7}{4}; \frac{11}{4}; c^2x^2\right)(a + b \sin^{-1}(cx))}{35d^2} + \frac{2(dx)^{5/2}(a + b \sin^{-1}(cx))^2}{5d}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^2, x]$

[Out] $(2*(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])^2)/(5*d) - (8*b*c*(d*x)^{(7/2)}*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/2, 7/4, 11/4, c^2*x^2])/(35*d^2) + (16*b^2*c^2*(d*x)^{(9/2)}*\text{HypergeometricPFQ}[\{1, 9/4, 9/4\}, \{11/4, 13/4\}, c^2*x^2])/(315*d^3)$

Rule 4627

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + (d*x)^m)^n, x]$
 $\text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^n/(d*(m+1)), x] - \text{Dist}[(b*c*n)/(d*(m+1)), \text{Int}[(d*x)^{m+1}*(a + b*\text{ArcSin}[c*x])^{n-1}/\text{Sqrt}[1 - c^2*x^2], x], x] /;$ FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4711

$\text{Int}[(a + \text{ArcSin}[c*x])*(b + (f*x)^m)^n/\text{Sqrt}[d + e*(x)^2], x]$
 $\text{Simp}[(f*x)^{m+1}*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/2, (1+m)/2, (3+m)/2, c^2*x^2]/(\text{Sqrt}[d]*f*(m+1)), x] - \text{Simp}[(b*c*(f*x)^{m+2}*\text{HypergeometricPFQ}[\{1, 1+m/2, 1+m/2\}, \{3/2+m/2, 2+m/2\}, c^2*x^2])]/(\text{Sqrt}[d]*f^2*(m+1)*(m+2)), x] /;$ FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int (dx)^{3/2} (a + b \sin^{-1}(cx))^2 dx &= \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))^2}{5d} - \frac{(4bc) \int \frac{(dx)^{5/2} (a + b \sin^{-1}(cx))}{\sqrt{1-c^2x^2}} dx}{5d} \\ &= \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))^2}{5d} - \frac{8bc(dx)^{7/2} (a + b \sin^{-1}(cx)) {}_2F_1\left(\frac{1}{2}, \frac{7}{4}; \frac{11}{4}; c^2x^2\right)}{35d^2} + \frac{16b^2c^2(dx)^{9/2} {}_3F_2\left(1, \frac{9}{4}, \frac{9}{4}; \frac{11}{4}, \frac{13}{4}; c^2x^2\right)}{315d^3} \end{aligned}$$

Mathematica [A] time = 0.0560194, size = 90, normalized size = 0.83

$$\frac{2}{315}x(dx)^{3/2}\left(8b^2c^2x^2\text{HypergeometricPFQ}\left(\left\{1, \frac{9}{4}, \frac{9}{4}\right\}, \left\{\frac{11}{4}, \frac{13}{4}\right\}, c^2x^2\right) + 9(a + b\sin^{-1}(cx))\left(7(a + b\sin^{-1}(cx)) - 4bc\right)\right)$$

Antiderivative was successfully verified.

[In] Integrate[(d*x)^(3/2)*(a + b*ArcSin[c*x])^2,x]

[Out] (2*x*(d*x)^(3/2)*(9*(a + b*ArcSin[c*x])*(7*(a + b*ArcSin[c*x]) - 4*b*c*x*Hypergeometric2F1[1/2, 7/4, 11/4, c^2*x^2]) + 8*b^2*c^2*x^2*HypergeometricPFQ[{1, 9/4, 9/4}, {11/4, 13/4}, c^2*x^2]))/315

Maple [F] time = 0.143, size = 0, normalized size = 0.

$$\int (dx)^{\frac{3}{2}} (a + b \arcsin(cx))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(3/2)*(a+b*arcsin(c*x))^2,x)

[Out] int((d*x)^(3/2)*(a+b*arcsin(c*x))^2,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(3/2)*(a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\left(b^2dx \arcsin(cx)^2 + 2abdx \arcsin(cx) + a^2dx\right)\sqrt{dx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(3/2)*(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] integral((b^2*d*x*arcsin(c*x)^2 + 2*a*b*d*x*arcsin(c*x) + a^2*d*x)*sqrt(d*x), x)

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)**(3/2)*(a+b*asin(c*x))**2,x)
```

```
[Out] Timed out
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int (dx)^{\frac{3}{2}} (b \arcsin(cx) + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(3/2)*(a+b*arcsin(c*x))^2,x, algorithm="giac")
```

```
[Out] integrate((d*x)^(3/2)*(b*arcsin(c*x) + a)^2, x)
```

3.211 $\int \sqrt{dx} (a + b \sin^{-1}(cx))^2 dx$

Optimal. Leaf size=109

$$\frac{16b^2c^2(dx)^{7/2}\text{HypergeometricPFQ}\left(\left\{1, \frac{7}{4}, \frac{7}{4}\right\}, \left\{\frac{9}{4}, \frac{11}{4}\right\}, c^2x^2\right)}{105d^3} - \frac{8bc(dx)^{5/2}\text{Hypergeometric2F1}\left(\frac{1}{2}, \frac{5}{4}, \frac{9}{4}, c^2x^2\right)(a + b \sin^{-1}(cx))}{15d^2}$$

[Out] $(2*(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^2)/(3*d) - (8*b*c*(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/2, 5/4, 9/4, c^2*x^2])/(15*d^2) + (16*b^2*c^2*(d*x)^{(7/2)}*\text{HypergeometricPFQ}[\{1, 7/4, 7/4\}, \{9/4, 11/4\}, c^2*x^2])/(105*d^3)$

Rubi [A] time = 0.142631, antiderivative size = 109, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4627, 4711}

$$\frac{16b^2c^2(dx)^{7/2} {}_3F_2\left(1, \frac{7}{4}, \frac{7}{4}; \frac{9}{4}, \frac{11}{4}; c^2x^2\right)}{105d^3} - \frac{8bc(dx)^{5/2} {}_2F_1\left(\frac{1}{2}, \frac{5}{4}; \frac{9}{4}; c^2x^2\right)(a + b \sin^{-1}(cx))}{15d^2} + \frac{2(dx)^{3/2}(a + b \sin^{-1}(cx))^2}{3d}$$

Antiderivative was successfully verified.

[In] Int[Sqrt[d*x]*(a + b*ArcSin[c*x])^2,x]

[Out] $(2*(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^2)/(3*d) - (8*b*c*(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/2, 5/4, 9/4, c^2*x^2])/(15*d^2) + (16*b^2*c^2*(d*x)^{(7/2)}*\text{HypergeometricPFQ}[\{1, 7/4, 7/4\}, \{9/4, 11/4\}, c^2*x^2])/(105*d^3)$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((d_.)*(x_.))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4711

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))*((f_.)*(x_.))^(m_.))/Sqrt[(d_.) + (e_.)*(x_.)^2], x_Symbol] :> Simp[((f*x)^(m + 1)*(a + b*ArcSin[c*x])*Hypergeometric2F1[1/2, (1 + m)/2, (3 + m)/2, c^2*x^2])/(Sqrt[d]*f*(m + 1)), x] - Simp[(b*c*(f*x)^(m + 2)*HypergeometricPFQ[{1, 1 + m/2, 1 + m/2}, {3/2 + m/2, 2 + m/2}, c^2*x^2])/(Sqrt[d]*f^2*(m + 1)*(m + 2)), x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \sqrt{dx} (a + b \sin^{-1}(cx))^2 dx &= \frac{2(dx)^{3/2}(a + b \sin^{-1}(cx))^2}{3d} - \frac{(4bc) \int \frac{(dx)^{3/2}(a + b \sin^{-1}(cx))}{\sqrt{1 - c^2x^2}} dx}{3d} \\ &= \frac{2(dx)^{3/2}(a + b \sin^{-1}(cx))^2}{3d} - \frac{8bc(dx)^{5/2}(a + b \sin^{-1}(cx)) {}_2F_1\left(\frac{1}{2}, \frac{5}{4}; \frac{9}{4}; c^2x^2\right)}{15d^2} + \frac{16b^2c^2(dx)^{7/2} {}_3F_2\left(1, \frac{7}{4}, \frac{7}{4}; \frac{9}{4}, \frac{11}{4}; c^2x^2\right)}{105d^3} \end{aligned}$$

Mathematica [A] time = 0.0519041, size = 90, normalized size = 0.83

$$\frac{2}{105}x\sqrt{dx}\left(8b^2c^2x^2\text{HypergeometricPFQ}\left(\left\{1, \frac{7}{4}, \frac{7}{4}\right\}, \left\{\frac{9}{4}, \frac{11}{4}\right\}, c^2x^2\right) + 7(a + b\sin^{-1}(cx))\left(5(a + b\sin^{-1}(cx)) - 4bc\right)\right)$$

Antiderivative was successfully verified.

[In] Integrate[Sqrt[d*x]*(a + b*ArcSin[c*x])^2,x]

[Out] (2*x*Sqrt[d*x]*(7*(a + b*ArcSin[c*x])*(5*(a + b*ArcSin[c*x]) - 4*b*c*x*Hypergeometric2F1[1/2, 5/4, 9/4, c^2*x^2]) + 8*b^2*c^2*x^2*HypergeometricPFQ[{1, 7/4, 7/4}, {9/4, 11/4}, c^2*x^2]))/105

Maple [F] time = 0.184, size = 0, normalized size = 0.

$$\int \sqrt{dx} (a + b \arcsin(cx))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(1/2)*(a+b*arcsin(c*x))^2,x)

[Out] int((d*x)^(1/2)*(a+b*arcsin(c*x))^2,x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x))^2,x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\left(b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2\right)\sqrt{dx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x))^2,x, algorithm="fricas")

[Out] integral((b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2)*sqrt(d*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{dx} (a + b \arcsin(cx))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)**(1/2)*(a+b*asin(c*x))**2,x)
```

```
[Out] Integral(sqrt(d*x)*(a + b*asin(c*x))**2, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{dx}(b \arcsin(cx) + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x))^2,x, algorithm="giac")
```

```
[Out] integrate(sqrt(d*x)*(b*arcsin(c*x) + a)^2, x)
```

$$3.212 \quad \int \frac{(a+b \sin^{-1}(cx))^2}{\sqrt{dx}} dx$$

Optimal. Leaf size=107

$$\frac{16b^2c^2(dx)^{5/2}\text{HypergeometricPFQ}\left(\left\{1, \frac{5}{4}, \frac{5}{4}\right\}, \left\{\frac{7}{4}, \frac{9}{4}\right\}, c^2x^2\right)}{15d^3} - \frac{8bc(dx)^{3/2}\text{Hypergeometric2F1}\left(\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, c^2x^2\right)(a+b \sin^{-1}(cx))^2}{3d^2}$$

[Out] (2*Sqrt[d*x]*(a + b*ArcSin[c*x])^2)/d - (8*b*c*(d*x)^(3/2)*(a + b*ArcSin[c*x])*Hypergeometric2F1[1/2, 3/4, 7/4, c^2*x^2])/(3*d^2) + (16*b^2*c^2*(d*x)^(5/2)*HypergeometricPFQ[{1, 5/4, 5/4}, {7/4, 9/4}, c^2*x^2])/(15*d^3)

Rubi [A] time = 0.130082, antiderivative size = 107, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4627, 4711}

$$\frac{16b^2c^2(dx)^{5/2} {}_3F_2\left(1, \frac{5}{4}, \frac{5}{4}; \frac{7}{4}, \frac{9}{4}; c^2x^2\right)}{15d^3} - \frac{8bc(dx)^{3/2} {}_2F_1\left(\frac{1}{2}, \frac{3}{4}; \frac{7}{4}; c^2x^2\right)(a+b \sin^{-1}(cx))^2}{3d^2} + \frac{2\sqrt{dx}(a+b \sin^{-1}(cx))^2}{d}$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^2/Sqrt[d*x], x]

[Out] (2*Sqrt[d*x]*(a + b*ArcSin[c*x])^2)/d - (8*b*c*(d*x)^(3/2)*(a + b*ArcSin[c*x])*Hypergeometric2F1[1/2, 3/4, 7/4, c^2*x^2])/(3*d^2) + (16*b^2*c^2*(d*x)^(5/2)*HypergeometricPFQ[{1, 5/4, 5/4}, {7/4, 9/4}, c^2*x^2])/(15*d^3)

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_)])*(b_.))^n_.*(d_.)*(x_)^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4711

Int[(((a_.) + ArcSin[(c_.)*(x_)])*(b_.))*((f_.)*(x_)^(m_))/Sqrt[(d_) + (e_.)*(x_)^2], x_Symbol] :> Simp[((f*x)^(m + 1)*(a + b*ArcSin[c*x])*Hypergeometric2F1[1/2, (1 + m)/2, (3 + m)/2, c^2*x^2])/(Sqrt[d]*f*(m + 1)), x] - Simp[(b*c*(f*x)^(m + 2)*HypergeometricPFQ[{1, 1 + m/2, 1 + m/2}, {3/2 + m/2, 2 + m/2}, c^2*x^2])/(Sqrt[d]*f^2*(m + 1)*(m + 2)), x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \frac{(a+b \sin^{-1}(cx))^2}{\sqrt{dx}} dx &= \frac{2\sqrt{dx}(a+b \sin^{-1}(cx))^2}{d} - \frac{(4bc) \int \frac{\sqrt{dx}(a+b \sin^{-1}(cx))}{\sqrt{1-c^2x^2}} dx}{d} \\ &= \frac{2\sqrt{dx}(a+b \sin^{-1}(cx))^2}{d} - \frac{8bc(dx)^{3/2}(a+b \sin^{-1}(cx)) {}_2F_1\left(\frac{1}{2}, \frac{3}{4}; \frac{7}{4}; c^2x^2\right)}{3d^2} + \frac{16b^2c^2(dx)^{5/2}}{15d^3} \end{aligned}$$

Mathematica [A] time = 0.0492373, size = 90, normalized size = 0.84

$$\frac{2x \left(8b^2c^2x^2 \text{HypergeometricPFQ} \left(\left\{ 1, \frac{5}{4}, \frac{5}{4} \right\}, \left\{ \frac{7}{4}, \frac{9}{4} \right\}, c^2x^2 \right) + 5(a + b \sin^{-1}(cx)) \left(3(a + b \sin^{-1}(cx)) - 4bcx \text{Hypergeometric} \right. \right.}{15\sqrt{dx}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])^2/Sqrt[d*x],x]

[Out] (2*x*(5*(a + b*ArcSin[c*x])*(3*(a + b*ArcSin[c*x]) - 4*b*c*x*Hypergeometric 2F1[1/2, 3/4, 7/4, c^2*x^2]) + 8*b^2*c^2*x^2*HypergeometricPFQ[{1, 5/4, 5/4 }, {7/4, 9/4}, c^2*x^2]))/(15*Sqrt[d*x])

Maple [F] time = 0.358, size = 0, normalized size = 0.

$$\int (a + b \arcsin(cx))^2 \frac{1}{\sqrt{dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^2/(d*x)^(1/2),x)

[Out] int((a+b*arcsin(c*x))^2/(d*x)^(1/2),x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(1/2),x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{(b^2 \arcsin(cx))^2 + 2ab \arcsin(cx) + a^2}{dx} \sqrt{dx}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(1/2),x, algorithm="fricas")

[Out] integral((b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2)*sqrt(d*x)/(d*x), x)

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*asin(c*x))**2/(d*x)**(1/2),x)
```

```
[Out] Exception raised: TypeError
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^2}{\sqrt{dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(1/2),x, algorithm="giac")
```

```
[Out] integrate((b*arcsin(c*x) + a)^2/sqrt(d*x), x)
```

$$3.213 \quad \int \frac{(a+b \sin^{-1}(cx))^2}{(dx)^{3/2}} dx$$

Optimal. Leaf size=105

$$\frac{16b^2c^2(dx)^{3/2}\text{HypergeometricPFQ}\left(\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, c^2x^2\right)}{3d^3} + \frac{8bc\sqrt{dx}\text{Hypergeometric2F1}\left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, c^2x^2\right)(a+b \sin^{-1}(cx))}{d^2}$$

[Out] $(-2*(a + b*\text{ArcSin}[c*x])^2)/(d*\text{Sqrt}[d*x]) + (8*b*c*\text{Sqrt}[d*x]*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/4, 1/2, 5/4, c^2*x^2])/d^2 - (16*b^2*c^2*(d*x)^(3/2)*\text{HypergeometricPFQ}[\{3/4, 3/4, 1\}, \{5/4, 7/4\}, c^2*x^2])/(3*d^3)$

Rubi [A] time = 0.134948, antiderivative size = 105, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4627, 4711}

$$\frac{16b^2c^2(dx)^{3/2} {}_3F_2\left(\frac{3}{4}, \frac{3}{4}, 1; \frac{5}{4}, \frac{7}{4}; c^2x^2\right)}{3d^3} + \frac{8bc\sqrt{dx} {}_2F_1\left(\frac{1}{4}, \frac{1}{2}; \frac{5}{4}; c^2x^2\right)(a+b \sin^{-1}(cx))}{d^2} - \frac{2(a+b \sin^{-1}(cx))^2}{d\sqrt{dx}}$$

Antiderivative was successfully verified.

[In] Int[(a + b*ArcSin[c*x])^2/(d*x)^(3/2), x]

[Out] $(-2*(a + b*\text{ArcSin}[c*x])^2)/(d*\text{Sqrt}[d*x]) + (8*b*c*\text{Sqrt}[d*x]*(a + b*\text{ArcSin}[c*x])*\text{Hypergeometric2F1}[1/4, 1/2, 5/4, c^2*x^2])/d^2 - (16*b^2*c^2*(d*x)^(3/2)*\text{HypergeometricPFQ}[\{3/4, 3/4, 1\}, \{5/4, 7/4\}, c^2*x^2])/(3*d^3)$

Rule 4627

Int[((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))^(n_.)*((d_.)*(x_.))^(m_.), x_Symbol] :> Simp[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^n)/(d*(m + 1)), x] - Dist[(b*c*n)/(d*(m + 1)), Int[((d*x)^(m + 1)*(a + b*ArcSin[c*x])^(n - 1))/Sqrt[1 - c^2*x^2], x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && NeQ[m, -1]

Rule 4711

Int[(((a_.) + ArcSin[(c_.)*(x_.)]*(b_.))*((f_.)*(x_.))^(m_.))/Sqrt[(d_.) + (e_.)*(x_.)^2], x_Symbol] :> Simp[((f*x)^(m + 1)*(a + b*ArcSin[c*x])*Hypergeometric2F1[1/2, (1 + m)/2, (3 + m)/2, c^2*x^2])/(Sqrt[d]*f*(m + 1)), x] - Simp[(b*c*(f*x)^(m + 2)*HypergeometricPFQ[{1, 1 + m/2, 1 + m/2}, {3/2 + m/2, 2 + m/2}, c^2*x^2])/(Sqrt[d]*f^2*(m + 1)*(m + 2)), x] /; FreeQ[{a, b, c, d, e, f, m}, x] && EqQ[c^2*d + e, 0] && GtQ[d, 0] && !IntegerQ[m]

Rubi steps

$$\begin{aligned} \int \frac{(a+b \sin^{-1}(cx))^2}{(dx)^{3/2}} dx &= -\frac{2(a+b \sin^{-1}(cx))^2}{d\sqrt{dx}} + \frac{(4bc) \int \frac{a+b \sin^{-1}(cx)}{\sqrt{dx}\sqrt{1-c^2x^2}} dx}{d} \\ &= -\frac{2(a+b \sin^{-1}(cx))^2}{d\sqrt{dx}} + \frac{8bc\sqrt{dx}(a+b \sin^{-1}(cx)) {}_2F_1\left(\frac{1}{4}, \frac{1}{2}; \frac{5}{4}; c^2x^2\right)}{d^2} - \frac{16b^2c^2(dx)^{3/2} {}_3F_2\left(\frac{3}{4}, \frac{3}{4}\right)}{3d^3} \end{aligned}$$

Mathematica [A] time = 0.0471097, size = 87, normalized size = 0.83

$$\frac{2x \left(8b^2c^2x^2 \text{HypergeometricPFQ} \left(\left\{ \frac{3}{4}, \frac{3}{4}, 1 \right\}, \left\{ \frac{5}{4}, \frac{7}{4} \right\}, c^2x^2 \right) + 3(a + b \sin^{-1}(cx)) \left(-4bcx \text{Hypergeometric2F1} \left(\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, c^2x^2 \right) + 8b^2c^2x^2 \text{HypergeometricPFQ} \left[\left\{ \frac{3}{4}, \frac{3}{4}, 1 \right\}, \left\{ \frac{5}{4}, \frac{7}{4} \right\}, c^2x^2 \right] \right) \right)}{3(dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])^2/(d*x)^(3/2), x]

[Out] (-2*x*(3*(a + b*ArcSin[c*x])*(a + b*ArcSin[c*x] - 4*b*c*x*Hypergeometric2F1[1/4, 1/2, 5/4, c^2*x^2]) + 8*b^2*c^2*x^2*HypergeometricPFQ[{3/4, 3/4, 1}, {5/4, 7/4}, c^2*x^2]))/(3*(d*x)^(3/2))

Maple [F] time = 0.154, size = 0, normalized size = 0.

$$\int (a + b \arcsin(cx))^2 (dx)^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^2/(d*x)^(3/2), x)

[Out] int((a+b*arcsin(c*x))^2/(d*x)^(3/2), x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(3/2), x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{(b^2 \arcsin(cx))^2 + 2ab \arcsin(cx) + a^2}{d^2x^2} \sqrt{dx}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(3/2), x, algorithm="fricas")

[Out] integral((b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2)*sqrt(d*x)/(d^2*x^2), x)

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**2/(d*x)**(3/2),x)`

[Out] Exception raised: TypeError

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^2}{(dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^2/(d*x)^(3/2),x, algorithm="giac")`

[Out] `integrate((b*arcsin(c*x) + a)^2/(d*x)^(3/2), x)`

$$3.214 \quad \int \frac{(a+b \sin^{-1}(cx))^2}{(dx)^{5/2}} dx$$

Optimal. Leaf size=109

$$\frac{16b^2c^2\sqrt{dx}\operatorname{HypergeometricPFQ}\left(\left\{\frac{1}{4}, \frac{1}{4}, 1\right\}, \left\{\frac{3}{4}, \frac{5}{4}\right\}, c^2x^2\right)}{3d^3} - \frac{8bc\operatorname{Hypergeometric2F1}\left(-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, c^2x^2\right)(a+b \sin^{-1}(cx))}{3d^2\sqrt{dx}}$$

[Out] $(-2*(a + b*\operatorname{ArcSin}[c*x])^2)/(3*d*(d*x)^{(3/2)}) - (8*b*c*(a + b*\operatorname{ArcSin}[c*x])*$
 $\operatorname{Hypergeometric2F1}[-1/4, 1/2, 3/4, c^2*x^2])/(3*d^2*\operatorname{Sqrt}[d*x]) + (16*b^2*c^2*$
 $\operatorname{Sqrt}[d*x]*\operatorname{HypergeometricPFQ}[\{1/4, 1/4, 1\}, \{3/4, 5/4\}, c^2*x^2])/(3*d^3)$

Rubi [A] time = 0.14545, antiderivative size = 109, normalized size of antiderivative = 1., number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {4627, 4711}

$$\frac{16b^2c^2\sqrt{dx}{}_3F_2\left(\frac{1}{4}, \frac{1}{4}, 1; \frac{3}{4}, \frac{5}{4}; c^2x^2\right)}{3d^3} - \frac{8bc{}_2F_1\left(-\frac{1}{4}, \frac{1}{2}; \frac{3}{4}; c^2x^2\right)(a+b \sin^{-1}(cx))}{3d^2\sqrt{dx}} - \frac{2(a+b \sin^{-1}(cx))^2}{3d(dx)^{3/2}}$$

Antiderivative was successfully verified.

[In] $\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])^2/(d*x)^{(5/2)}, x]$

[Out] $(-2*(a + b*\operatorname{ArcSin}[c*x])^2)/(3*d*(d*x)^{(3/2)}) - (8*b*c*(a + b*\operatorname{ArcSin}[c*x])*$
 $\operatorname{Hypergeometric2F1}[-1/4, 1/2, 3/4, c^2*x^2])/(3*d^2*\operatorname{Sqrt}[d*x]) + (16*b^2*c^2*$
 $\operatorname{Sqrt}[d*x]*\operatorname{HypergeometricPFQ}[\{1/4, 1/4, 1\}, \{3/4, 5/4\}, c^2*x^2])/(3*d^3)$

Rule 4627

$\operatorname{Int}[(a + \operatorname{ArcSin}[c*x])^n*(d*x)^m, x]$
 $\rightarrow \operatorname{Simp}[(d*x)^{m+1}*(a + b*\operatorname{ArcSin}[c*x])^n/(d*(m+1)), x] - \operatorname{Dist}[(b*c*n)/(d*(m+1)), \operatorname{Int}[(d*x)^{m+1}*(a + b*\operatorname{ArcSin}[c*x])^{n-1}/\operatorname{Sqrt}[1 - c^2*x^2], x], x] /;$
 $\operatorname{FreeQ}\{a, b, c, d, m\}, x \ \&\& \ \operatorname{IGtQ}[n, 0] \ \&\& \ \operatorname{NeQ}[m, -1]$

Rule 4711

$\operatorname{Int}[(a + \operatorname{ArcSin}[c*x])^n*(d*x)^m, x]$
 $\rightarrow \operatorname{Simp}[(f*x)^{m+1}*(a + b*\operatorname{ArcSin}[c*x])*$
 $\operatorname{Hypergeometric2F1}[1/2, (1+m)/2, (3+m)/2, c^2*x^2]/(\operatorname{Sqrt}[d]*f*(m+1)), x] - \operatorname{Simp}[(b*c*(f*x)^{m+2}*$
 $\operatorname{HypergeometricPFQ}[\{1, 1+m/2, 1+m/2\}, \{3/2+m/2, 2+m/2\}, c^2*x^2]/(\operatorname{Sqrt}[d]*f^2*(m+1)*(m+2)), x] /;$
 $\operatorname{FreeQ}\{a, b, c, d, e, f, m\}, x \ \&\& \ \operatorname{EqQ}[c^2*d + e, 0] \ \&\& \ \operatorname{GtQ}[d, 0] \ \&\& \ \operatorname{IntegerQ}[m]$

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^2}{(dx)^{5/2}} dx = -\frac{2(a+b \sin^{-1}(cx))^2}{3d(dx)^{3/2}} + \frac{(4bc) \int \frac{a+b \sin^{-1}(cx)}{(dx)^{3/2}\sqrt{1-c^2x^2}} dx}{3d}$$

$$= -\frac{2(a+b \sin^{-1}(cx))^2}{3d(dx)^{3/2}} - \frac{8bc(a+b \sin^{-1}(cx)){}_2F_1\left(-\frac{1}{4}, \frac{1}{2}; \frac{3}{4}; c^2x^2\right)}{3d^2\sqrt{dx}} + \frac{16b^2c^2\sqrt{dx}{}_3F_2\left(\frac{1}{4}, \frac{1}{4}, 1; \frac{3}{4}, \frac{5}{4}; c^2x^2\right)}{3d^3}$$

Mathematica [A] time = 0.0541036, size = 87, normalized size = 0.8

$$\frac{x \left(16b^2c^2x^2 \text{HypergeometricPFQ} \left(\left\{ \frac{1}{4}, \frac{1}{4}, 1 \right\}, \left\{ \frac{3}{4}, \frac{5}{4} \right\}, c^2x^2 \right) - 2(a + b \sin^{-1}(cx)) \left(4bcx \text{Hypergeometric2F1} \left(-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, c^2x^2 \right) \right) \right)}{3(dx)^{5/2}}$$

Antiderivative was successfully verified.

[In] Integrate[(a + b*ArcSin[c*x])^2/(d*x)^(5/2),x]

[Out] (x*(-2*(a + b*ArcSin[c*x])*(a + b*ArcSin[c*x] + 4*b*c*x*Hypergeometric2F1[-1/4, 1/2, 3/4, c^2*x^2]) + 16*b^2*c^2*x^2*HypergeometricPFQ[{1/4, 1/4, 1}, {3/4, 5/4}, c^2*x^2]))/(3*(d*x)^(5/2))

Maple [F] time = 0.144, size = 0, normalized size = 0.

$$\int (a + b \arcsin(cx))^2 (dx)^{-\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((a+b*arcsin(c*x))^2/(d*x)^(5/2),x)

[Out] int((a+b*arcsin(c*x))^2/(d*x)^(5/2),x)

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(5/2),x, algorithm="maxima")

[Out] Exception raised: ValueError

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{(b^2 \arcsin(cx))^2 + 2ab \arcsin(cx) + a^2}{d^3 x^3} \sqrt{dx}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(5/2),x, algorithm="fricas")

[Out] integral((b^2*arcsin(c*x)^2 + 2*a*b*arcsin(c*x) + a^2)*sqrt(d*x)/(d^3*x^3), x)

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*asin(c*x))**2/(d*x)**(5/2),x)

[Out] Exception raised: TypeError

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^2}{(dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((a+b*arcsin(c*x))^2/(d*x)^(5/2),x, algorithm="giac")

[Out] integrate((b*arcsin(c*x) + a)^2/(d*x)^(5/2), x)

3.215 $\int (dx)^{3/2} (a + b \sin^{-1}(cx))^3 dx$

Optimal. Leaf size=68

$$\frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))^3}{5d} - \frac{6bc \text{Unintegrable}\left(\frac{(dx)^{5/2}(a+b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}}, x\right)}{5d}$$

[Out] $(2*(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])^3)/(5*d) - (6*b*c*\text{Unintegrable}[\frac{(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])^2}{\text{Sqrt}[1 - c^2*x^2]}, x])/(5*d)$

Rubi [A] time = 0.169876, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int (dx)^{3/2} (a + b \sin^{-1}(cx))^3 dx$$

Verification is Not applicable to the result.

[In] $\text{Int}[(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^3, x]$

[Out] $(2*(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])^3)/(5*d) - (6*b*c*\text{Defer}[\text{Int}[\frac{(d*x)^{(5/2)}*(a + b*\text{ArcSin}[c*x])^2}{\text{Sqrt}[1 - c^2*x^2]}, x]])/(5*d)$

Rubi steps

$$\int (dx)^{3/2} (a + b \sin^{-1}(cx))^3 dx = \frac{2(dx)^{5/2} (a + b \sin^{-1}(cx))^3}{5d} - \frac{(6bc) \int \frac{(dx)^{5/2} (a + b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}} dx}{5d}$$

Mathematica [A] time = 36.3794, size = 0, normalized size = 0.

$$\int (dx)^{3/2} (a + b \sin^{-1}(cx))^3 dx$$

Verification is Not applicable to the result.

[In] $\text{Integrate}[(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^3, x]$

[Out] $\text{Integrate}[(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^3, x]$

Maple [A] time = 0.144, size = 0, normalized size = 0.

$$\int (dx)^{3/2} (a + b \arcsin(cx))^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{int}((d*x)^{(3/2)}*(a+b*\arcsin(c*x))^3, x)$

[Out] `int((d*x)^(3/2)*(a+b*arcsin(c*x))^3,x)`

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)^(3/2)*(a+b*arcsin(c*x))^3,x, algorithm="maxima")`

[Out] Exception raised: ValueError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\left(b^3 dx \arcsin(cx)^3 + 3 ab^2 dx \arcsin(cx)^2 + 3 a^2 b dx \arcsin(cx) + a^3 dx\right) \sqrt{dx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)^(3/2)*(a+b*arcsin(c*x))^3,x, algorithm="fricas")`

[Out] `integral((b^3*d*x*arcsin(c*x)^3 + 3*a*b^2*d*x*arcsin(c*x)^2 + 3*a^2*b*d*x*a
rcsin(c*x) + a^3*d*x)*sqrt(d*x), x)`

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)**(3/2)*(a+b*asin(c*x))**3,x)`

[Out] Timed out

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int (dx)^{\frac{3}{2}} (b \arcsin(cx) + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((d*x)^(3/2)*(a+b*arcsin(c*x))^3,x, algorithm="giac")`

[Out] `integrate((d*x)^(3/2)*(b*arcsin(c*x) + a)^3, x)`

3.216 $\int \sqrt{dx} (a + b \sin^{-1}(cx))^3 dx$

Optimal. Leaf size=66

$$\frac{2(dx)^{3/2} (a + b \sin^{-1}(cx))^3}{3d} - \frac{2bc \text{Unintegrable}\left(\frac{(dx)^{3/2} (a + b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}}, x\right)}{d}$$

[Out] $(2*(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^3)/(3*d) - (2*b*c*\text{Unintegrable}[((d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^2)/\text{Sqrt}[1 - c^2*x^2], x])/d$

Rubi [A] time = 0.167883, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \sqrt{dx} (a + b \sin^{-1}(cx))^3 dx$$

Verification is Not applicable to the result.

[In] `Int[Sqrt[d*x]*(a + b*ArcSin[c*x])^3,x]`

[Out] $(2*(d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^3)/(3*d) - (2*b*c*\text{Defer}[\text{Int}][((d*x)^{(3/2)}*(a + b*\text{ArcSin}[c*x])^2)/\text{Sqrt}[1 - c^2*x^2], x])/d$

Rubi steps

$$\int \sqrt{dx} (a + b \sin^{-1}(cx))^3 dx = \frac{2(dx)^{3/2} (a + b \sin^{-1}(cx))^3}{3d} - \frac{(2bc) \int \frac{(dx)^{3/2} (a + b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}} dx}{d}$$

Mathematica [F] time = 180.002, size = 0, normalized size = 0.

\$Aborted

Verification is Not applicable to the result.

[In] `Integrate[Sqrt[d*x]*(a + b*ArcSin[c*x])^3,x]`

[Out] \$Aborted

Maple [A] time = 0.142, size = 0, normalized size = 0.

$$\int \sqrt{dx} (a + b \arcsin(cx))^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((d*x)^(1/2)*(a+b*arcsin(c*x))^3,x)`


```
[Out] int((d*x)^(1/2)*(a+b*arcsin(c*x))^3,x)
```

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x))^3,x, algorithm="maxima")
```

```
[Out] Exception raised: ValueError
```

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\left(b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3\right)\sqrt{dx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x))^3,x, algorithm="fricas")
```

```
[Out] integral((b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) +
a^3)*sqrt(d*x), x)
```

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{dx} (a + b \arcsin(cx))^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)**(1/2)*(a+b*asin(c*x))**3,x)
```

```
[Out] Integral(sqrt(d*x)*(a + b*asin(c*x))**3, x)
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \sqrt{dx} (b \arcsin(cx) + a)^3 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x)^(1/2)*(a+b*arcsin(c*x))^3,x, algorithm="giac")
```

```
[Out] integrate(sqrt(d*x)*(b*arcsin(c*x) + a)^3, x)
```

$$3.217 \quad \int \frac{(a+b \sin^{-1}(cx))^3}{\sqrt{dx}} dx$$

Optimal. Leaf size=64

$$\frac{2\sqrt{dx}(a+b \sin^{-1}(cx))^3}{d} - \frac{6bc \text{Unintegrable}\left(\frac{\sqrt{dx}(a+b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}}, x\right)}{d}$$

[Out] (2*Sqrt[d*x]*(a + b*ArcSin[c*x])^3)/d - (6*b*c*Unintegrable[(Sqrt[d*x]*(a + b*ArcSin[c*x])^2)/Sqrt[1 - c^2*x^2], x])/d

Rubi [A] time = 0.160063, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(a+b \sin^{-1}(cx))^3}{\sqrt{dx}} dx$$

Verification is Not applicable to the result.

[In] Int[(a + b*ArcSin[c*x])^3/Sqrt[d*x], x]

[Out] (2*Sqrt[d*x]*(a + b*ArcSin[c*x])^3)/d - (6*b*c*Defer[Int] [(Sqrt[d*x]*(a + b*ArcSin[c*x])^2)/Sqrt[1 - c^2*x^2], x])/d

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^3}{\sqrt{dx}} dx = \frac{2\sqrt{dx}(a+b \sin^{-1}(cx))^3}{d} - \frac{(6bc) \int \frac{\sqrt{dx}(a+b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}} dx}{d}$$

Mathematica [A] time = 8.12599, size = 0, normalized size = 0.

$$\int \frac{(a+b \sin^{-1}(cx))^3}{\sqrt{dx}} dx$$

Verification is Not applicable to the result.

[In] Integrate[(a + b*ArcSin[c*x])^3/Sqrt[d*x], x]

[Out] Integrate[(a + b*ArcSin[c*x])^3/Sqrt[d*x], x]

Maple [A] time = 0.199, size = 0, normalized size = 0.

$$\int (a + b \arcsin(cx))^3 \frac{1}{\sqrt{dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*arcsin(c*x))^3/(d*x)^(1/2),x)`

[Out] `int((a+b*arcsin(c*x))^3/(d*x)^(1/2),x)`

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(1/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{(b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3)\sqrt{dx}}{dx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(1/2),x, algorithm="fricas")`

[Out] `integral((b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) + a^3)*sqrt(d*x)/(d*x), x)`

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**3/(d*x)**(1/2),x)`

[Out] Exception raised: TypeError

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^3}{\sqrt{dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(1/2),x, algorithm="giac")`

[Out] `integrate((b*arcsin(c*x) + a)^3/sqrt(d*x), x)`

$$3.218 \quad \int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{3/2}} dx$$

Optimal. Leaf size=64

$$\frac{6bc \operatorname{Unintegrable}\left(\frac{(a+b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}\sqrt{dx}}, x\right)}{d} - \frac{2(a+b \sin^{-1}(cx))^3}{d\sqrt{dx}}$$

[Out] $(-2*(a + b*\operatorname{ArcSin}[c*x])^3)/(d*\operatorname{Sqrt}[d*x]) + (6*b*c*\operatorname{Unintegrable}[(a + b*\operatorname{ArcSin}[c*x])^2/(\operatorname{Sqrt}[d*x]*\operatorname{Sqrt}[1 - c^2*x^2]), x])/d$

Rubi [A] time = 0.159132, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] $\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])^3/(d*x)^{(3/2)}, x]$

[Out] $(-2*(a + b*\operatorname{ArcSin}[c*x])^3)/(d*\operatorname{Sqrt}[d*x]) + (6*b*c*\operatorname{Defer}[\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])^2/(\operatorname{Sqrt}[d*x]*\operatorname{Sqrt}[1 - c^2*x^2]), x])/d$

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{3/2}} dx = -\frac{2(a+b \sin^{-1}(cx))^3}{d\sqrt{dx}} + \frac{(6bc) \int \frac{(a+b \sin^{-1}(cx))^2}{\sqrt{dx}\sqrt{1-c^2x^2}} dx}{d}$$

Mathematica [A] time = 7.57556, size = 0, normalized size = 0.

$$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{3/2}} dx$$

Verification is Not applicable to the result.

[In] $\operatorname{Integrate}[(a + b*\operatorname{ArcSin}[c*x])^3/(d*x)^{(3/2)}, x]$

[Out] $\operatorname{Integrate}[(a + b*\operatorname{ArcSin}[c*x])^3/(d*x)^{(3/2)}, x]$

Maple [A] time = 0.145, size = 0, normalized size = 0.

$$\int (a + b \arcsin(cx))^3 (dx)^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*arcsin(c*x))^3/(d*x)^(3/2),x)`

[Out] `int((a+b*arcsin(c*x))^3/(d*x)^(3/2),x)`

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(3/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{(b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3)\sqrt{dx}}{d^2x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(3/2),x, algorithm="fricas")`

[Out] `integral((b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) + a^3)*sqrt(d*x)/(d^2*x^2), x)`

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**3/(d*x)**(3/2),x)`

[Out] Exception raised: TypeError

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^3}{(dx)^{\frac{3}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(3/2),x, algorithm="giac")`

[Out] `integrate((b*arcsin(c*x) + a)^3/(d*x)^(3/2), x)`

$$3.219 \quad \int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{5/2}} dx$$

Optimal. Leaf size=66

$$\frac{2bc \operatorname{Unintegrable}\left(\frac{(a+b \sin^{-1}(cx))^2}{\sqrt{1-c^2x^2}(dx)^{3/2}}, x\right)}{d} - \frac{2(a+b \sin^{-1}(cx))^3}{3d(dx)^{3/2}}$$

[Out] $(-2*(a + b*\operatorname{ArcSin}[c*x])^3)/(3*d*(d*x)^(3/2)) + (2*b*c*\operatorname{Unintegrable}[(a + b*\operatorname{ArcSin}[c*x])^2/((d*x)^(3/2)*\operatorname{Sqrt}[1 - c^2*x^2]), x])/d$

Rubi [A] time = 0.173453, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{5/2}} dx$$

Verification is Not applicable to the result.

[In] $\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])^3/(d*x)^(5/2), x]$

[Out] $(-2*(a + b*\operatorname{ArcSin}[c*x])^3)/(3*d*(d*x)^(3/2)) + (2*b*c*\operatorname{Defer}[\operatorname{Int}[(a + b*\operatorname{ArcSin}[c*x])^2/((d*x)^(3/2)*\operatorname{Sqrt}[1 - c^2*x^2]), x])/d$

Rubi steps

$$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{5/2}} dx = -\frac{2(a+b \sin^{-1}(cx))^3}{3d(dx)^{3/2}} + \frac{(2bc) \int \frac{(a+b \sin^{-1}(cx))^2}{(dx)^{3/2}\sqrt{1-c^2x^2}} dx}{d}$$

Mathematica [A] time = 13.1286, size = 0, normalized size = 0.

$$\int \frac{(a+b \sin^{-1}(cx))^3}{(dx)^{5/2}} dx$$

Verification is Not applicable to the result.

[In] $\operatorname{Integrate}[(a + b*\operatorname{ArcSin}[c*x])^3/(d*x)^(5/2), x]$

[Out] $\operatorname{Integrate}[(a + b*\operatorname{ArcSin}[c*x])^3/(d*x)^(5/2), x]$

Maple [A] time = 0.139, size = 0, normalized size = 0.

$$\int (a + b \arcsin(cx))^3 (dx)^{-\frac{5}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int((a+b*arcsin(c*x))^3/(d*x)^(5/2),x)`

[Out] `int((a+b*arcsin(c*x))^3/(d*x)^(5/2),x)`

Maxima [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: ValueError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(5/2),x, algorithm="maxima")`

[Out] Exception raised: ValueError

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{(b^3 \arcsin(cx)^3 + 3ab^2 \arcsin(cx)^2 + 3a^2b \arcsin(cx) + a^3)\sqrt{dx}}{d^3x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(5/2),x, algorithm="fricas")`

[Out] `integral((b^3*arcsin(c*x)^3 + 3*a*b^2*arcsin(c*x)^2 + 3*a^2*b*arcsin(c*x) + a^3)*sqrt(d*x)/(d^3*x^3), x)`

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: TypeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*asin(c*x))**3/(d*x)**(5/2),x)`

[Out] Exception raised: TypeError

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(b \arcsin(cx) + a)^3}{(dx)^{\frac{5}{2}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((a+b*arcsin(c*x))^3/(d*x)^(5/2),x, algorithm="giac")`

[Out] `integrate((b*arcsin(c*x) + a)^3/(d*x)^(5/2), x)`

$$3.220 \quad \int \frac{(dx)^{3/2}}{a+b \sin^{-1}(cx)} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable}\left(\frac{(dx)^{3/2}}{a+b \sin^{-1}(cx)}, x\right)$$

[Out] Unintegrable[(d*x)^(3/2)/(a + b*ArcSin[c*x]), x]

Rubi [A] time = 0.0296614, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(dx)^{3/2}}{a+b \sin^{-1}(cx)} dx$$

Verification is Not applicable to the result.

[In] Int[(d*x)^(3/2)/(a + b*ArcSin[c*x]),x]

[Out] Defer[Int] [(d*x)^(3/2)/(a + b*ArcSin[c*x]), x]

Rubi steps

$$\int \frac{(dx)^{3/2}}{a+b \sin^{-1}(cx)} dx = \int \frac{(dx)^{3/2}}{a+b \sin^{-1}(cx)} dx$$

Mathematica [A] time = 2.67572, size = 0, normalized size = 0.

$$\int \frac{(dx)^{3/2}}{a+b \sin^{-1}(cx)} dx$$

Verification is Not applicable to the result.

[In] Integrate[(d*x)^(3/2)/(a + b*ArcSin[c*x]),x]

[Out] Integrate[(d*x)^(3/2)/(a + b*ArcSin[c*x]), x]

Maple [A] time = 0.093, size = 0, normalized size = 0.

$$\int \frac{1}{a+b \arcsin(cx)} (dx)^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(3/2)/(a+b*arcsin(c*x)),x)

[Out] int((d*x)^(3/2)/(a+b*arcsin(c*x)),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(dx)^{\frac{3}{2}}}{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(3/2)/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate((d*x)^(3/2)/(b*arcsin(c*x) + a), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{dx}dx}{b \arcsin(cx) + a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(3/2)/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(sqrt(d*x)*d*x/(b*arcsin(c*x) + a), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(dx)^{\frac{3}{2}}}{a + b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**(3/2)/(a+b*asin(c*x)),x)

[Out] Integral((d*x)**(3/2)/(a + b*asin(c*x)), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(dx)^{\frac{3}{2}}}{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(3/2)/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] integrate((d*x)^(3/2)/(b*arcsin(c*x) + a), x)

$$3.221 \quad \int \frac{\sqrt{dx}}{a+b \sin^{-1}(cx)} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable}\left(\frac{\sqrt{dx}}{a+b \sin^{-1}(cx)}, x\right)$$

[Out] Unintegrable[Sqrt[d*x]/(a + b*ArcSin[c*x]), x]

Rubi [A] time = 0.0260333, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sqrt{dx}}{a+b \sin^{-1}(cx)} dx$$

Verification is Not applicable to the result.

[In] Int[Sqrt[d*x]/(a + b*ArcSin[c*x]), x]

[Out] Defer[Int][Sqrt[d*x]/(a + b*ArcSin[c*x]), x]

Rubi steps

$$\int \frac{\sqrt{dx}}{a+b \sin^{-1}(cx)} dx = \int \frac{\sqrt{dx}}{a+b \sin^{-1}(cx)} dx$$

Mathematica [A] time = 2.56472, size = 0, normalized size = 0.

$$\int \frac{\sqrt{dx}}{a+b \sin^{-1}(cx)} dx$$

Verification is Not applicable to the result.

[In] Integrate[Sqrt[d*x]/(a + b*ArcSin[c*x]), x]

[Out] Integrate[Sqrt[d*x]/(a + b*ArcSin[c*x]), x]

Maple [A] time = 0.092, size = 0, normalized size = 0.

$$\int \frac{1}{a+b \arcsin(cx)} \sqrt{dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(1/2)/(a+b*arcsin(c*x)), x)

[Out] int((d*x)^(1/2)/(a+b*arcsin(c*x)), x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{dx}}{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate(sqrt(d*x)/(b*arcsin(c*x) + a), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{dx}}{b \arcsin(cx) + a}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(sqrt(d*x)/(b*arcsin(c*x) + a), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{dx}}{a + b \arcsin(cx)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)**(1/2)/(a+b*asin(c*x)),x)

[Out] Integral(sqrt(d*x)/(a + b*asin(c*x)), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{dx}}{b \arcsin(cx) + a} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x)^(1/2)/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] integrate(sqrt(d*x)/(b*arcsin(c*x) + a), x)

$$3.222 \quad \int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable} \left(\frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))}, x \right)$$

[Out] Unintegrable[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])), x]

Rubi [A] time = 0.0292444, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Int[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])),x]

[Out] Defer[Int][1/(Sqrt[d*x]*(a + b*ArcSin[c*x])), x]

Rubi steps

$$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))} dx = \int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))} dx$$

Mathematica [A] time = 0.769351, size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])),x]

[Out] Integrate[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])), x]

Maple [A] time = 0.1, size = 0, normalized size = 0.

$$\int \frac{1}{a+b \arcsin(cx)} \frac{1}{\sqrt{dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x)^(1/2)/(a+b*arcsin(c*x)),x)

[Out] int(1/(d*x)^(1/2)/(a+b*arcsin(c*x)),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{dx}(b \arcsin(cx) + a)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)^(1/2)/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate(1/(sqrt(d*x)*(b*arcsin(c*x) + a)), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{dx}}{bdx \arcsin(cx) + adx}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)^(1/2)/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(sqrt(d*x)/(b*d*x*arcsin(c*x) + a*d*x), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{dx}(a + b \arcsin(cx))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)**(1/2)/(a+b*asin(c*x)),x)

[Out] Integral(1/(sqrt(d*x)*(a + b*asin(c*x))), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{dx}(b \arcsin(cx) + a)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)^(1/2)/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] integrate(1/(sqrt(d*x)*(b*arcsin(c*x) + a)), x)

$$3.223 \quad \int \frac{1}{(dx)^{3/2}(a+b \sin^{-1}(cx))} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable} \left(\frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))}, x \right)$$

[Out] Unintegrable[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])), x]

Rubi [A] time = 0.0317726, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Int[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])),x]

[Out] Defer[Int][1/((d*x)^(3/2)*(a + b*ArcSin[c*x])), x]

Rubi steps

$$\int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))} dx = \int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))} dx$$

Mathematica [A] time = 3.84077, size = 0, normalized size = 0.

$$\int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])),x]

[Out] Integrate[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])), x]

Maple [A] time = 0.099, size = 0, normalized size = 0.

$$\int \frac{1}{a + b \arcsin(cx)} (dx)^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x)^(3/2)/(a+b*arcsin(c*x)),x)

[Out] int(1/(d*x)^(3/2)/(a+b*arcsin(c*x)),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(dx)^{\frac{3}{2}} (b \arcsin(cx) + a)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)^(3/2)/(a+b*arcsin(c*x)),x, algorithm="maxima")

[Out] integrate(1/((d*x)^(3/2)*(b*arcsin(c*x) + a)), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{dx}}{bd^2x^2 \arcsin(cx) + ad^2x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)^(3/2)/(a+b*arcsin(c*x)),x, algorithm="fricas")

[Out] integral(sqrt(d*x)/(b*d^2*x^2*arcsin(c*x) + a*d^2*x^2), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(dx)^{\frac{3}{2}} (a + b \arcsin(cx))} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)**(3/2)/(a+b*asin(c*x)),x)

[Out] Integral(1/((d*x)**(3/2)*(a + b*asin(c*x))), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(dx)^{\frac{3}{2}} (b \arcsin(cx) + a)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(1/(d*x)^(3/2)/(a+b*arcsin(c*x)),x, algorithm="giac")

[Out] integrate(1/((d*x)^(3/2)*(b*arcsin(c*x) + a)), x)

$$3.224 \quad \int \frac{(dx)^{3/2}}{(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable} \left(\frac{(dx)^{3/2}}{(a+b \sin^{-1}(cx))^2}, x \right)$$

[Out] Unintegrable[(d*x)^(3/2)/(a + b*ArcSin[c*x])^2, x]

Rubi [A] time = 0.0291117, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{(dx)^{3/2}}{(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[(d*x)^(3/2)/(a + b*ArcSin[c*x])^2,x]

[Out] Defer[Int] [(d*x)^(3/2)/(a + b*ArcSin[c*x])^2, x]

Rubi steps

$$\int \frac{(dx)^{3/2}}{(a+b \sin^{-1}(cx))^2} dx = \int \frac{(dx)^{3/2}}{(a+b \sin^{-1}(cx))^2} dx$$

Mathematica [A] time = 5.6831, size = 0, normalized size = 0.

$$\int \frac{(dx)^{3/2}}{(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(d*x)^(3/2)/(a + b*ArcSin[c*x])^2,x]

[Out] Integrate[(d*x)^(3/2)/(a + b*ArcSin[c*x])^2, x]

Maple [A] time = 0.098, size = 0, normalized size = 0.

$$\int \frac{1}{(a+b \arcsin(cx))^2} (dx)^{\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(3/2)/(a+b*arcsin(c*x))^2,x)

[Out] $\int (d*x)^{(3/2)/(a+b*\arcsin(c*x))^2, x)$

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{\sqrt{cx+1}\sqrt{-cx+1}d^{\frac{3}{2}}x^{\frac{3}{2}} - \frac{1}{2}(b^2c \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) + abc)\sqrt{d} \int \frac{(5c^2dx^2-3d)\sqrt{cx+1}\sqrt{-cx+1}\sqrt{x}}{abc^3x^2-abc+(b^2c^3x^2-b^2c)\arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})}}{b^2c \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) + abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)^{(3/2)/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="maxima")$

[Out] $-(\sqrt{cx+1}\sqrt{-cx+1}*d^{(3/2)}*x^{(3/2)} - (b^2*c*\arctan2(cx, \sqrt{cx+1}\sqrt{-cx+1}) + a*b*c)*\sqrt{d}*\text{integrate}(1/2*(5*c^2*d*x^2 - 3*d)*\sqrt{cx+1}\sqrt{-cx+1}\sqrt{x}/(a*b*c^3*x^2 - a*b*c + (b^2*c^3*x^2 - b^2*c)*\arctan2(cx, \sqrt{cx+1}\sqrt{-cx+1})), x))/(b^2*c*\arctan2(cx, \sqrt{cx+1}\sqrt{-cx+1}) + a*b*c)$

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{d}dx}{b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)^{(3/2)/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="fricas")$

[Out] $\text{integral}(\sqrt{d*x}*d*x/(b^2*\arcsin(c*x)^2 + 2*a*b*\arcsin(c*x) + a^2), x)$

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(dx)^{\frac{3}{2}}}{(a + b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)**(3/2)/(a+b*\arcsin(c*x))**2, x)$

[Out] $\text{Integral}((d*x)**(3/2)/(a + b*\arcsin(c*x))**2, x)$

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{(dx)^{\frac{3}{2}}}{(b \arcsin(cx) + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)^{(3/2)/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="giac")$

[Out] $\text{integrate}((d*x)^{(3/2)/(b*\arcsin(c*x) + a)^2, x)$

$$3.225 \quad \int \frac{\sqrt{dx}}{(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable} \left(\frac{\sqrt{dx}}{(a+b \sin^{-1}(cx))^2}, x \right)$$

[Out] Unintegrable[Sqrt[d*x]/(a + b*ArcSin[c*x])^2, x]

Rubi [A] time = 0.0256366, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sqrt{dx}}{(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[Sqrt[d*x]/(a + b*ArcSin[c*x])^2,x]

[Out] Defer[Int][Sqrt[d*x]/(a + b*ArcSin[c*x])^2, x]

Rubi steps

$$\int \frac{\sqrt{dx}}{(a+b \sin^{-1}(cx))^2} dx = \int \frac{\sqrt{dx}}{(a+b \sin^{-1}(cx))^2} dx$$

Mathematica [A] time = 4.8966, size = 0, normalized size = 0.

$$\int \frac{\sqrt{dx}}{(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[Sqrt[d*x]/(a + b*ArcSin[c*x])^2,x]

[Out] Integrate[Sqrt[d*x]/(a + b*ArcSin[c*x])^2, x]

Maple [A] time = 0.095, size = 0, normalized size = 0.

$$\int \frac{1}{(a+b \arcsin(cx))^2} \sqrt{dx} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((d*x)^(1/2)/(a+b*arcsin(c*x))^2,x)

[Out] $\int (d*x)^{(1/2)/(a+b*\arcsin(c*x))^2, x)$

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{\frac{1}{2} (b^2 c \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) + abc) \sqrt{d} \int \frac{(3c^2x^2-1)\sqrt{cx+1}\sqrt{-cx+1}\sqrt{x}}{abc^3x^3-abcx+(b^2c^3x^3-b^2cx) \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1})} dx - \sqrt{cx+1}\sqrt{-cx+1}\sqrt{d}}{b^2c \arctan(cx, \sqrt{cx+1}\sqrt{-cx+1}) + abc}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)^{(1/2)/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="maxima")$

[Out] $((b^2*c*\arctan2(c*x, \sqrt{c*x + 1})*\sqrt{-c*x + 1}) + a*b*c)*\sqrt{d}*\text{integrate}(1/2*(3*c^2*x^2 - 1)*\sqrt{c*x + 1}*\sqrt{-c*x + 1}*\sqrt{x}/(a*b*c^3*x^3 - a*b*c*x + (b^2*c^3*x^3 - b^2*c*x)*\arctan2(c*x, \sqrt{c*x + 1}*\sqrt{-c*x + 1})), x) - \sqrt{c*x + 1}*\sqrt{-c*x + 1}*\sqrt{d}*\sqrt{x})/(b^2*c*\arctan2(c*x, \sqrt{c*x + 1}*\sqrt{-c*x + 1}) + a*b*c)$

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sqrt{dx}}{b^2 \arcsin(cx)^2 + 2ab \arcsin(cx) + a^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)^{(1/2)/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="fricas")$

[Out] $\text{integral}(\sqrt{d*x}/(b^2*\arcsin(c*x)^2 + 2*a*b*\arcsin(c*x) + a^2), x)$

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{dx}}{(a + b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)**(1/2)/(a+b*\arcsin(c*x))**2, x)$

[Out] $\text{Integral}(\sqrt{d*x}/(a + b*\arcsin(c*x))**2, x)$

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sqrt{dx}}{(b \arcsin(cx) + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}((d*x)^{(1/2)/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="giac")$

[Out] $\text{integrate}(\sqrt{d*x}/(b*\arcsin(c*x) + a)^2, x)$

$$3.226 \quad \int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable}\left(\frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))^2}, x\right)$$

[Out] Unintegrable[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])^2), x]

Rubi [A] time = 0.0253785, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])^2), x]

[Out] Defer[Int][1/(Sqrt[d*x]*(a + b*ArcSin[c*x])^2), x]

Rubi steps

$$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))^2} dx = \int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))^2} dx$$

Mathematica [A] time = 8.37607, size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{dx}(a+b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])^2), x]

[Out] Integrate[1/(Sqrt[d*x]*(a + b*ArcSin[c*x])^2), x]

Maple [A] time = 0.102, size = 0, normalized size = 0.

$$\int \frac{1}{(a+b \arcsin(cx))^2} \frac{1}{\sqrt{dx}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x)^(1/2)/(a+b*arcsin(c*x))^2, x)

[Out] $\int (1/(d*x)^{(1/2)})/(a+b*\arcsin(c*x))^2, x$

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{\frac{1}{2} \left(b^2 c d x \arctan \left(c x, \sqrt{c x + 1} \sqrt{-c x + 1} \right) + a b c d x \right) \sqrt{d} \int \frac{(c^2 x^2 + 1) \sqrt{c x + 1} \sqrt{-c x + 1} \sqrt{x}}{a b c^3 d x^4 - a b c d x^2 + (b^2 c^3 d x^4 - b^2 c d x^2) \arctan \left(c x, \sqrt{c x + 1} \sqrt{-c x + 1} \right)} dx - \sqrt{c x + 1}}{b^2 c d x \arctan \left(c x, \sqrt{c x + 1} \sqrt{-c x + 1} \right) + a b c d x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(d*x)^{(1/2)})/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="maxima")$

[Out] $((b^2*c*d*x*\arctan2(c*x, \sqrt{c*x + 1})*\sqrt{-c*x + 1}) + a*b*c*d*x)*\sqrt{d} * \text{integrate}(1/2*(c^2*x^2 + 1)*\sqrt{c*x + 1}*\sqrt{-c*x + 1}*\sqrt{x}/(a*b*c^3*d*x^4 - a*b*c*d*x^2 + (b^2*c^3*d*x^4 - b^2*c*d*x^2)*\arctan2(c*x, \sqrt{c*x + 1})*\sqrt{-c*x + 1})), x) - \sqrt{c*x + 1}*\sqrt{-c*x + 1}*\sqrt{d}*\sqrt{x})/(b^2*c*d*x*\arctan2(c*x, \sqrt{c*x + 1})*\sqrt{-c*x + 1}) + a*b*c*d*x)$

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{\sqrt{dx}}{b^2 dx \arcsin(cx)^2 + 2 ab dx \arcsin(cx) + a^2 dx}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(d*x)^{(1/2)})/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="fricas")$

[Out] $\text{integral}(\sqrt{d*x}/(b^2*d*x*\arcsin(c*x)^2 + 2*a*b*d*x*\arcsin(c*x) + a^2*d*x), x)$

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{dx} (a + b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(d*x)**(1/2))/(a+b*\arcsin(c*x))**2, x)$

[Out] $\text{Integral}(1/(\sqrt{d*x}*(a + b*\arcsin(c*x))**2), x)$

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{\sqrt{dx} (b \arcsin(cx) + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] $\text{integrate}(1/(d*x)^{(1/2)})/(a+b*\arcsin(c*x))^2, x, \text{algorithm}="giac")$

[Out] $\text{integrate}(1/(\sqrt{d*x}*(b*\arcsin(c*x) + a)^2), x)$

$$3.227 \quad \int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))^2} dx$$

Optimal. Leaf size=20

$$\text{Unintegrable} \left(\frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))^2}, x \right)$$

[Out] Unintegrable[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])^2), x]

Rubi [A] time = 0.0279332, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Int[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])^2), x]

[Out] Defer[Int][1/((d*x)^(3/2)*(a + b*ArcSin[c*x])^2), x]

Rubi steps

$$\int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))^2} dx = \int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))^2} dx$$

Mathematica [A] time = 13.5607, size = 0, normalized size = 0.

$$\int \frac{1}{(dx)^{3/2} (a + b \sin^{-1}(cx))^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])^2), x]

[Out] Integrate[1/((d*x)^(3/2)*(a + b*ArcSin[c*x])^2), x]

Maple [A] time = 0.092, size = 0, normalized size = 0.

$$\int \frac{1}{(a + b \arcsin(cx))^2} (dx)^{-\frac{3}{2}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(1/(d*x)^(3/2)/(a+b*arcsin(c*x))^2,x)

[Out] $\int (1/(d*x)^{(3/2)})/(a+b*\arcsin(c*x))^2, x$

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\frac{\frac{1}{2} \left(b^2 c d^2 x^2 \arctan \left(c x, \sqrt{c x + 1} \sqrt{-c x + 1} \right) + a b c d^2 x^2 \right) \sqrt{d} \int \frac{(c^2 x^2 - 3) \sqrt{c x + 1} \sqrt{-c x + 1} \sqrt{x}}{a b c^3 d^2 x^5 - a b c d^2 x^3 + (b^2 c^3 d^2 x^5 - b^2 c d^2 x^3) \arctan \left(c x, \sqrt{c x + 1} \sqrt{-c x + 1} \right)} dx + b^2 c d^2 x^2 \arctan \left(c x, \sqrt{c x + 1} \sqrt{-c x + 1} \right) + a b c d^2 x^2}{b^2 c d^2 x^2 \arctan \left(c x, \sqrt{c x + 1} \sqrt{-c x + 1} \right) + a b c d^2 x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x)^(3/2)/(a+b*arcsin(c*x))^2,x, algorithm="maxima")`

[Out] $-\left((b^2 * c * d^2 * x^2 * \arctan2(c * x, \sqrt{c * x + 1} * \sqrt{-c * x + 1})) + a * b * c * d^2 * x^2 \right) * \sqrt{d} * \int \frac{1/2 * (c^2 * x^2 - 3) * \sqrt{c * x + 1} * \sqrt{-c * x + 1} * \sqrt{x}}{(a * b * c^3 * d^2 * x^5 - a * b * c * d^2 * x^3 + (b^2 * c^3 * d^2 * x^5 - b^2 * c * d^2 * x^3) * \arctan2(c * x, \sqrt{c * x + 1} * \sqrt{-c * x + 1}))}, x + \sqrt{c * x + 1} * \sqrt{-c * x + 1} * \sqrt{d} * \sqrt{x} / (b^2 * c * d^2 * x^2 * \arctan2(c * x, \sqrt{c * x + 1} * \sqrt{-c * x + 1})) + a * b * c * d^2 * x^2$

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral} \left(\frac{\sqrt{dx}}{b^2 d^2 x^2 \arcsin(cx)^2 + 2 a b d^2 x^2 \arcsin(cx) + a^2 d^2 x^2}, x \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x)^(3/2)/(a+b*arcsin(c*x))^2,x, algorithm="fricas")`

[Out] $\text{integral}(\sqrt{d*x}/(b^2*d^2*x^2*\arcsin(c*x)^2 + 2*a*b*d^2*x^2*\arcsin(c*x) + a^2*d^2*x^2), x)$

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(dx)^{\frac{3}{2}} (a + b \arcsin(cx))^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(1/(d*x)**(3/2)/(a+b*asin(c*x))**2,x)`

[Out] `Integral(1/((d*x)**(3/2)*(a + b*asin(c*x))**2), x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{1}{(dx)^{\frac{3}{2}} (b \arcsin(cx) + a)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(1/(d*x)^(3/2)/(a+b*arcsin(c*x))^2,x, algorithm="giac")
```

```
[Out] integrate(1/((d*x)^(3/2)*(b*arcsin(c*x) + a)^2), x)
```


Chapter 4

Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

4.0.1 Mathematica and Rubi grading function

```
1 (* Original version thanks to Albert Rich emailed on 03/21/2017 *)
2 (* ::Package:: *)
3
4 (* ::Subsection:: *)
5 (*GradeAntiderivative[result,optimal]*)
6
7
8 (* ::Text:: *)
9 (*If result and optimal are mathematical expressions, *)
10 (*      GradeAntiderivative[result,optimal] returns*)
11 (* "F" if the result fails to integrate an expression that*)
12 (*   is integrable*)
13 (* "C" if result involves higher level functions than necessary*)
14 (* "B" if result is more than twice the size of the optimal*)
15 (*   antiderivative*)
16 (* "A" if result can be considered optimal*)
17
18
19 GradeAntiderivative[result_,optimal_] :=
20   If[ExpnType[result]<=ExpnType[optimal],
21     If[FreeQ[result,Complex] || Not[FreeQ[optimal,Complex]],
22       If[LeafCount[result]<=2*LeafCount[optimal],
23         "A",
24         "B"],
25       "C"],
26     If[FreeQ[result,Integrate] && FreeQ[result,Int],
27       "C",
28       "F"]]
29
30
31 (* ::Text:: *)
32 (*The following summarizes the type number assigned an *)
33 (*expression based on the functions it involves*)
34 (*1 = rational function*)
35 (*2 = algebraic function*)
36 (*3 = elementary function*)
37 (*4 = special function*)
```

```

38 (*5 = hyperpergeometric function*)
39 (*6 = appell function*)
40 (*7 = rootsum function*)
41 (*8 = integrate function*)
42 (*9 = unknown function*)
43
44
45 ExpnType[expn_] :=
46   If[AtomQ[expn],
47     1,
48     If[ListQ[expn],
49       Max[Map[ExpnType,expn]],
50       If[Head[expn]===Power,
51         If[IntegerQ[expn[[2]]],
52           ExpnType[expn[[1]]],
53           If[Head[expn[[2]]]===Rational,
54             If[IntegerQ[expn[[1]]] || Head[expn[[1]]]===Rational,
55               1,
56               Max[ExpnType[expn[[1]],2]],
57             Max[ExpnType[expn[[1]],ExpnType[expn[[2]],3]],
58             If[Head[expn]===Plus || Head[expn]===Times,
59               Max[ExpnType[First[expn]],ExpnType[Rest[expn]]],
60             If[ElementaryFunctionQ[Head[expn]],
61               Max[3,ExpnType[expn[[1]]],
62             If[SpecialFunctionQ[Head[expn]],
63               Apply[Max,Append[Map[ExpnType,Apply[List,expn]],4]],
64             If[HypergeometricFunctionQ[Head[expn]],
65               Apply[Max,Append[Map[ExpnType,Apply[List,expn]],5]],
66             If[AppellFunctionQ[Head[expn]],
67               Apply[Max,Append[Map[ExpnType,Apply[List,expn]],6]],
68             If[Head[expn]===RootSum,
69               Apply[Max,Append[Map[ExpnType,Apply[List,expn]],7]],
70             If[Head[expn]===Integrate || Head[expn]===Int,
71               Apply[Max,Append[Map[ExpnType,Apply[List,expn]],8]],
72             9]]]]]]]]]]]
73
74
75 ElementaryFunctionQ[func_] :=
76   MemberQ[{
77     Exp,Log,
78     Sin,Cos,Tan,Cot,Sec,Csc,
79     ArcSin,ArcCos,ArcTan,ArcCot,ArcSec,ArcCsc,
80     Sinh,Cosh,Tanh,Coth,Sech,Csch,
81     ArcSinh,ArcCosh,ArcTanh,ArcCoth,ArcSech,ArcCsch
82   },func]
83
84
85 SpecialFunctionQ[func_] :=
86   MemberQ[{
87     Erf, Erfc, Erfi,
88     FresnelS, FresnelC,
89     ExpIntegralE, ExpIntegralEi, LogIntegral,
90     SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
91     Gamma, LogGamma, PolyGamma,
92     Zeta, PolyLog, ProductLog,
93     EllipticF, EllipticE, EllipticPi
94   },func]
95
96
97 HypergeometricFunctionQ[func_] :=
98   MemberQ[{Hypergeometric1F1,Hypergeometric2F1,HypergeometricPFQ},func]
99
100

```

```

101 AppellFunctionQ[func_] :=
102   MemberQ[{AppellF1},func]

```

4.0.2 Maple grading function

```

1 # File: GradeAntiderivative.mpl
2 # Original version thanks to Albert Rich emailed on 03/21/2017
3
4 #Nasser 03/22/2017 Use Maple leaf count instead since buildin
5 #Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
6 #Nasser 03/24/2017 corrected the check for complex result
7 #Nasser 10/27/2017 check for leafsize and do not call ExpnType()
8 # if leaf size is "too large". Set at 500,000
9 #Nasser 12/22/2019 Added debug flag, added 'dilog' to special functions
10 # see problem 156, file Apostol_Problems
11
12 GradeAntiderivative := proc(result,optimal)
13 local leaf_count_result, leaf_count_optimal,ExpnType_result,ExpnType_optimal,
14     debug:=false;
15
16     leaf_count_result:=leafcount(result);
17     #do NOT call ExpnType() if leaf size is too large. Recursion problem
18     if leaf_count_result > 500000 then
19         return "B";
20     fi;
21
22     leaf_count_optimal:=leafcount(optimal);
23
24     ExpnType_result:=ExpnType(result);
25     ExpnType_optimal:=ExpnType(optimal);
26
27     if debug then
28         print("ExpnType_result",ExpnType_result," ExpnType_optimal=",
29             ExpnType_optimal);
30     fi;
31
32 # If result and optimal are mathematical expressions,
33 # GradeAntiderivative[result,optimal] returns
34 # "F" if the result fails to integrate an expression that
35 # is integrable
36 # "C" if result involves higher level functions than necessary
37 # "B" if result is more than twice the size of the optimal
38 # antiderivative
39 # "A" if result can be considered optimal
40
41 #This check below actually is not needed, since I only
42 #call this grading only for passed integrals. i.e. I check
43 #for "F" before calling this. But no harm of keeping it here.
44 #just in case.
45
46 if not type(result,freeof('int')) then
47     return "F";
48 end if;
49
50 if ExpnType_result<=ExpnType_optimal then
51     if debug then
52         print("ExpnType_result<=ExpnType_optimal");
53     fi;
54     if is_contains_complex(result) then
55         if is_contains_complex(optimal) then
56             if debug then

```

```

57         print("both result and optimal complex");
58         fi;
59         #both result and optimal complex
60         if leaf_count_result<=2*leaf_count_optimal then
61             return "A";
62         else
63             return "B";
64         end if
65     else #result contains complex but optimal is not
66         if debug then
67             print("result contains complex but optimal is not");
68         fi;
69         return "C";
70     end if
71 else # result do not contain complex
72     # this assumes optimal do not as well
73     if debug then
74         print("result do not contain complex, this assumes optimal do
not as well");
75     fi;
76     if leaf_count_result<=2*leaf_count_optimal then
77         if debug then
78             print("leaf_count_result<=2*leaf_count_optimal");
79         fi;
80         return "A";
81     else
82         if debug then
83             print("leaf_count_result>2*leaf_count_optimal");
84         fi;
85         return "B";
86     end if
87 end if
88 else #ExpnType(result) > ExpnType(optimal)
89     if debug then
90         print("ExpnType(result) > ExpnType(optimal)");
91     fi;
92     return "C";
93 end if
94
95 end proc:
96
97 #
98 # is_contains_complex(result)
99 # takes expressions and returns true if it contains "I" else false
100 #
101 #Nasser 032417
102 is_contains_complex:= proc(expression)
103     return (has(expression,I));
104 end proc:
105
106 # The following summarizes the type number assigned an expression
107 # based on the functions it involves
108 # 1 = rational function
109 # 2 = algebraic function
110 # 3 = elementary function
111 # 4 = special function
112 # 5 = hyperpergeometric function
113 # 6 = appell function
114 # 7 = rootsum function
115 # 8 = integrate function
116 # 9 = unknown function
117
118 ExpnType := proc(expn)

```

```

119   if type(expn,'atomic') then
120     1
121   elif type(expn,'list') then
122     apply(max,map(ExpnType,expn))
123   elif type(expn,'sqrt') then
124     if type(op(1,expn),'rational') then
125       1
126     else
127       max(2,ExpnType(op(1,expn)))
128     end if
129   elif type(expn,'`^`') then
130     if type(op(2,expn),'integer') then
131       ExpnType(op(1,expn))
132     elif type(op(2,expn),'rational') then
133       if type(op(1,expn),'rational') then
134         1
135       else
136         max(2,ExpnType(op(1,expn)))
137       end if
138     else
139       max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
140     end if
141   elif type(expn,'`+`') or type(expn,'`*`') then
142     max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
143   elif ElementaryFunctionQ(op(0,expn)) then
144     max(3,ExpnType(op(1,expn)))
145   elif SpecialFunctionQ(op(0,expn)) then
146     max(4,apply(max,map(ExpnType,[op(expn)])))
147   elif HypergeometricFunctionQ(op(0,expn)) then
148     max(5,apply(max,map(ExpnType,[op(expn)])))
149   elif AppellFunctionQ(op(0,expn)) then
150     max(6,apply(max,map(ExpnType,[op(expn)])))
151   elif op(0,expn)='int' then
152     max(8,apply(max,map(ExpnType,[op(expn)]))) else
153     9
154   end if
155 end proc:
156
157
158 ElementaryFunctionQ := proc(func)
159   member(func,[
160     exp,log,ln,
161     sin,cos,tan,cot,sec,csc,
162     arcsin,arccos,arctan,arccot,arcsec,arccsc,
163     sinh,cosh,tanh,coth,sech,csch,
164     arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
165 end proc:
166
167 SpecialFunctionQ := proc(func)
168   member(func,[
169     erf,erfc,erfi,
170     FresnelS,FresnelC,
171     Ei,Ei,Li,Si,Ci,Shi,Chi,
172     GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
173     EllipticF,EllipticE,EllipticPi])
174 end proc:
175
176 HypergeometricFunctionQ := proc(func)
177   member(func,[Hypergeometric1F1,hypergeom,HypergeometricPFQ])
178 end proc:
179
180 AppellFunctionQ := proc(func)
181   member(func,[AppellF1])

```

```

182 end proc:
183
184 # u is a sum or product.  rest(u) returns all but the
185 # first term or factor of u.
186 rest := proc(u) local v;
187     if nops(u)=2 then
188         op(2,u)
189     else
190         apply(op(0,u),op(2..nops(u),u))
191     end if
192 end proc:
193
194 #leafcount(u) returns the number of nodes in u.
195 #Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
196 leafcount := proc(u)
197     MmaTranslator[Mma][LeafCount](u);
198 end proc:

```

4.0.3 Sympy grading function

```

1 #Dec 24, 2019. Nasser M. Abbasi:
2 #           Port of original Maple grading function by
3 #           Albert Rich to use with Sympy/Python
4 #Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
5 #           added 'exp_polar'
6 from sympy import *
7
8 def leaf_count(expr):
9     #sympy do not have leaf count function. This is approximation
10    return round(1.7*count_ops(expr))
11
12 def is_sqrt(expr):
13     if isinstance(expr,Pow):
14         if expr.args[1] == Rational(1,2):
15             return True
16         else:
17             return False
18     else:
19         return False
20
21 def is_elementary_function(func):
22     return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
23                    asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
24                    asinh,acosh,atanh,acoth,asech,acsch
25                    ]
26
27 def is_special_function(func):
28     return func in [ erf,erfc,erfi,
29                    fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
30                    gamma,loggamma,digamma,zeta,polylog,LambertW,
31                    elliptic_f,elliptic_e,elliptic_pi,exp_polar
32                    ]
33
34 def is_hypergeometric_function(func):
35     return func in [hyper]
36
37 def is_appell_function(func):
38     return func in [appellf1]
39
40 def is_atom(expn):
41     try:
42         if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
43             return True

```

```

44     else:
45         return False
46
47     except AttributeError as error:
48         return False
49
50 def expnType(expn):
51     debug=False
52     if debug:
53         print("expn=",expn,"type(expn)=",type(expn))
54
55     if is_atom(expn):
56         return 1
57     elif isinstance(expn,list):
58         return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
59     elif is_sqrt(expn):
60         if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
61             return 1
62         else:
63             return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
64     elif isinstance(expn,Pow): #type(expn,``^`)
65         if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
66             return expnType(expn.args[0]) #ExpnType(op(1,expn))
67         elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
68             if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
69                 return 1
70             else:
71                 return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn
72 )))
73     else:
74         return max(3,expnType(expn.args[0]),expnType(expn.args[1])) #max(3,
75 ExpnType(op(1,expn)),ExpnType(op(2,expn)))
76     elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,``+`) or
77 type(expn,``*`)
78     m1 = expnType(expn.args[0])
79     m2 = expnType(list(expn.args[1:]))
80     return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
81     elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
82     return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
83     elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
84     m1 = max(map(expnType, list(expn.args)))
85     return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))
86     elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,
87 expn))
88     m1 = max(map(expnType, list(expn.args)))
89     return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
90     elif is_appell_function(expn.func):
91     m1 = max(map(expnType, list(expn.args)))
92     return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
93     elif isinstance(expn,RootSum):
94     m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType
95 ,Apply[List,expn]],7]],
96     return max(7,m1)
97     elif str(expn).find("Integral") != -1:
98     m1 = max(map(expnType, list(expn.args)))
99     return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
100     else:
101     return 9
102
103 #main function
104 def grade_antiderivative(result,optimal):
105
106     leaf_count_result = leaf_count(result)

```

```

102 leaf_count_optimal = leaf_count(optimal)
103
104 expnType_result = expnType(result)
105 expnType_optimal = expnType(optimal)
106
107 if str(result).find("Integral") != -1:
108     return "F"
109
110 if expnType_result <= expnType_optimal:
111     if result.has(I):
112         if optimal.has(I): #both result and optimal complex
113             if leaf_count_result <= 2*leaf_count_optimal:
114                 return "A"
115             else:
116                 return "B"
117         else: #result contains complex but optimal is not
118             return "C"
119     else: # result do not contain complex, this assumes optimal do not as
well
120         if leaf_count_result <= 2*leaf_count_optimal:
121             return "A"
122         else:
123             return "B"
124     else:
125         return "C"

```

4.0.4 SageMath grading function

```

1 #Dec 24, 2019. Nasser: Ported original Maple grading function by
2 #     Albert Rich to use with Sagemath. This is used to
3 #     grade Fracas, Giac and Maxima results.
4 #Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
5 #     'arctan2','floor','abs','log_integral'
6
7 from sage.all import *
8 from sage.symbolic.operators import add_vararg, mul_vararg
9
10 def tree(expr):
11     debug=False;
12     if debug:
13         print ("Enter tree(expr), expr=",expr)
14         print ("expr.operator()=",expr.operator())
15         print ("expr.operands()=",expr.operands())
16         print ("map(tree, expr.operands()=",map(tree, expr.operands()))
17
18     if expr.operator() is None:
19         return expr
20     else:
21         return [expr.operator()+list(map(tree, expr.operands()))
22
23 def leaf_count(anti):
24     debug=False;
25
26     if debug: print ("Enter leaf_count, anti=", anti, " len(anti)=", len(anti))
27
28     if len(anti) == 0: #special check for optimal being 0 for some test cases.
29         if debug: print ("len(anti) == 0")
30         return 1
31     else:
32         if debug: print ("round(1.35*len(flatten(tree(anti))))=",round(1.35*len
(flatten(tree(anti))))
33         return round(1.35*len(flatten(tree(anti)))) #fudge factor
34             #since this estimate of leaf count is bit lower than

```



```

35         #what it should be compared to Mathematica's
36
37 def is_sqrt(expr):
38     debug=False;
39     if expr.operator() == operator.pow: #isinstance(expr,Pow):
40         if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
41             if debug: print ("expr is sqrt")
42             return True
43         else:
44             return False
45     else:
46         return False
47
48 def is_elementary_function(func):
49     debug = False
50
51     m = func.name() in ['exp','log','ln',
52         'sin','cos','tan','cot','sec','csc',
53         'arcsin','arccos','arctan','arccot','arcsec','arccsc',
54         'sinh','cosh','tanh','coth','sech','csch',
55         'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
56         'arctan2','floor','abs'
57     ]
58     if debug:
59         if m:
60             print ("func ", func , " is elementary_function")
61         else:
62             print ("func ", func , " is NOT elementary_function")
63
64
65     return m
66
67 def is_special_function(func):
68     debug = False
69
70     if debug: print ("type(func)=", type(func))
71
72     m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
73         'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','
74     sinh_integral'
75         'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
76         'polylog','lambert_w','elliptic_f','elliptic_e',
77         'elliptic_pi','exp_integral_e','log_integral']
78
79     if debug:
80         print ("m=",m)
81         if m:
82             print ("func ", func , " is special_function")
83         else:
84             print ("func ", func , " is NOT special_function")
85
86     return m
87
88
89 def is_hypergeometric_function(func):
90     return func.name() in ['hypergeometric','hypergeometric_M','
91     hypergeometric_U']
92
93 def is_appell_function(func):
94     return func.name() in ['hypergeometric'] #[appellf1] can't find this in
95     sagemath

```

```

95 def is_atom(expn):
96
97     #thanks to answer at https://ask.sagemath.org/question/49179/what-is-
sagemath-equivalent-to-atomic-type-in-maple/
98     try:
99         if expn.parent() is SR:
100             return expn.operator() is None
101         if expn.parent() in (ZZ, QQ, AA, QQbar):
102             return expn in expn.parent() # Should always return True
103         if hasattr(expn.parent(),"base_ring") and hasattr(expn.parent(),"gens")
:
104             return expn in expn.parent().base_ring() or expn in expn.parent().
gens()
105         return False
106
107     except AttributeError as error:
108         return False
109
110
111 def expnType(expn):
112     debug=False
113
114     if debug:
115         print(">>>>Enter expnType, expn=", expn)
116         print(">>>>is_atom(expn)=", is_atom(expn))
117
118     if is_atom(expn):
119         return 1
120     elif type(expn)==list: #isinstance(expn,list):
121         return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
122     elif is_sqrt(expn):
123         if type(expn.operands()[0])==Rational: #type(isinstance(expn.args[0],
Rational):
124             return 1
125         else:
126             return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.
args[0]))
127     elif expn.operator() == operator.pow: #isinstance(expn,Pow)
128         if type(expn.operands()[1])==Integer: #isinstance(expn.args[1],Integer
)
129             return expnType(expn.operands()[0]) #expnType(expn.args[0])
130         elif type(expn.operands()[1])==Rational: #isinstance(expn.args[1],
Rational)
131             if type(expn.operands()[0])==Rational: #isinstance(expn.args[0],
Rational)
132                 return 1
133             else:
134                 return max(2,expnType(expn.operands()[0])) #max(2,expnType(
expn.args[0]))
135         else:
136             return max(3,expnType(expn.operands()[0]),expnType(expn.operands()
[1])) #max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1]))
137     elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #
isinstance(expn,Add) or isinstance(expn,Mul)
138         m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
139         m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
140         return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn)))
141     elif is_elementary_function(expn.operator()): #is_elementary_function(expn
.func)
142         return max(3,expnType(expn.operands()[0]))
143     elif is_special_function(expn.operator()): #is_special_function(expn.func)
144         m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))

```

```

145     return max(4,m1)    #max(4,m1)
146     elif is_hypergeometric_function(expn.operator()): #
is_hypergeometric_function(expn.func)
147         m1 = max(map(expnType, expn.operands()))    #max(map(expnType, list(
expn.args)))
148         return max(5,m1)    #max(5,m1)
149     elif is_appell_function(expn.operator()):
150         m1 = max(map(expnType, expn.operands()))    #max(map(expnType, list(
expn.args)))
151         return max(6,m1)    #max(6,m1)
152     elif str(expn).find("Integral") != -1: #this will never happen, since it
153         #is checked before calling the grading function that is passed.
154         #but kept it here.
155         m1 = max(map(expnType, expn.operands()))    #max(map(expnType, list(
expn.args)))
156         return max(8,m1)    #max(5,apply(max,map(ExpnType,[op(expn)])))
157     else:
158         return 9
159
160 #main function
161 def grade_antiderivative(result,optimal):
162     debug = False;
163
164     if debug: print ("Enter grade_antiderivative for sagemath")
165
166     leaf_count_result = leaf_count(result)
167     leaf_count_optimal = leaf_count(optimal)
168
169     if debug: print ("leaf_count_result=", leaf_count_result, "
leaf_count_optimal=",leaf_count_optimal)
170
171
172     expnType_result = expnType(result)
173     expnType_optimal = expnType(optimal)
174
175     if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",
expnType_optimal)
176
177     if expnType_result <= expnType_optimal:
178         if result.has(I):
179             if optimal.has(I): #both result and optimal complex
180                 if leaf_count_result <= 2*leaf_count_optimal:
181                     return "A"
182                 else:
183                     return "B"
184             else: #result contains complex but optimal is not
185                 return "C"
186         else: # result do not contain complex, this assumes optimal do not as
well
187             if leaf_count_result <= 2*leaf_count_optimal:
188                 return "A"
189             else:
190                 return "B"
191     else:
192         return "C"

```